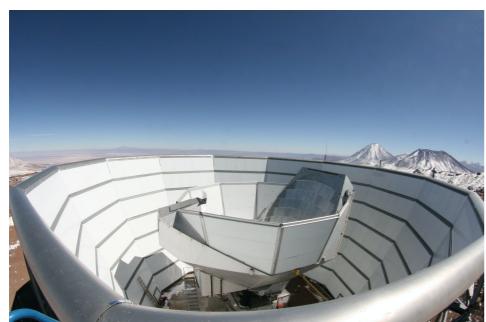


Astrophysics and Cosmology with the Sunyaev Zeldovich Effects

Boris Bolliet

*DAMTP
Cambridge University*



ACT cluster cosmology co-Leader
SO SZ working group co-Leader





ASPEN CENTER
FOR PHYSICS



2023 SUMMER PROGRAM

May 28 to September 17, 2023

Groups and Clusters of Galaxies at the Crossroad between Astrophysics and Cosmology

Aug 27 to Sept 17

Organizers:

Boris Boullet, Cambridge University

Stefano Borgani, University of Trieste

Stefano Ettori, European Southern Observatory

***Elena Pierpaoli**, University of Southern California

APPLICATION DEADLINE – JANUARY 31, 2023

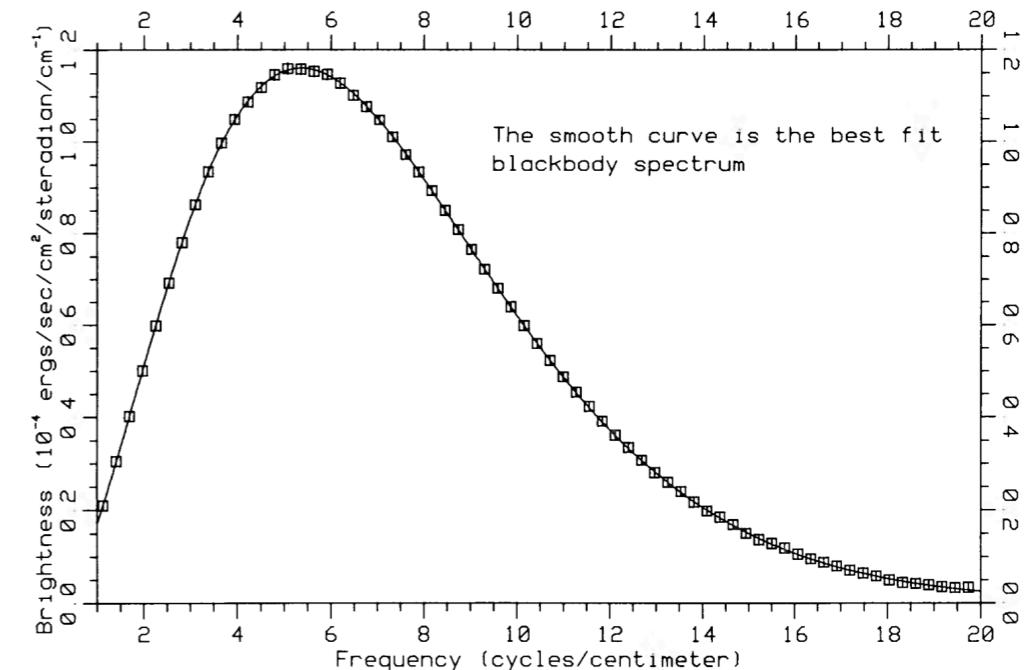


Accidental discovery of CMB in 1964 by
Penzias and Wilson (Nobel 1978)

- Ultimate confirmation of the **expanding universe** (Friedmann 1922, Lemaître 1927) and the **Big Bang** model
- Clearly **detectable** (a lucky fact!)
- Opens the door to **precision cosmology**

Young universe in **thermal equilibrium**

Radiation has a **black body** spectrum
and is isotropic

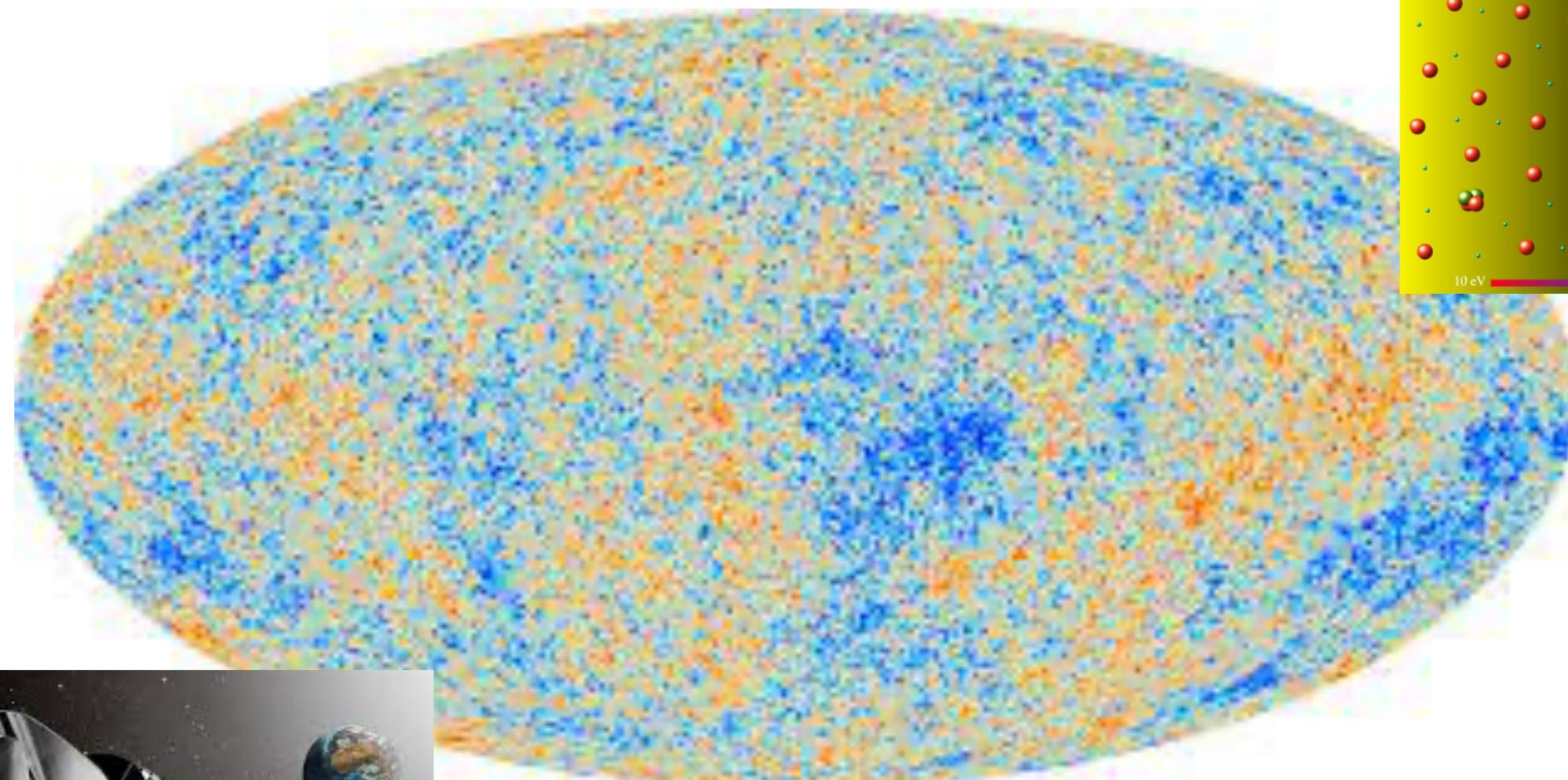


Measurement with COBE/FIRAS data
Mather et al 1990 (Nobel 2006)

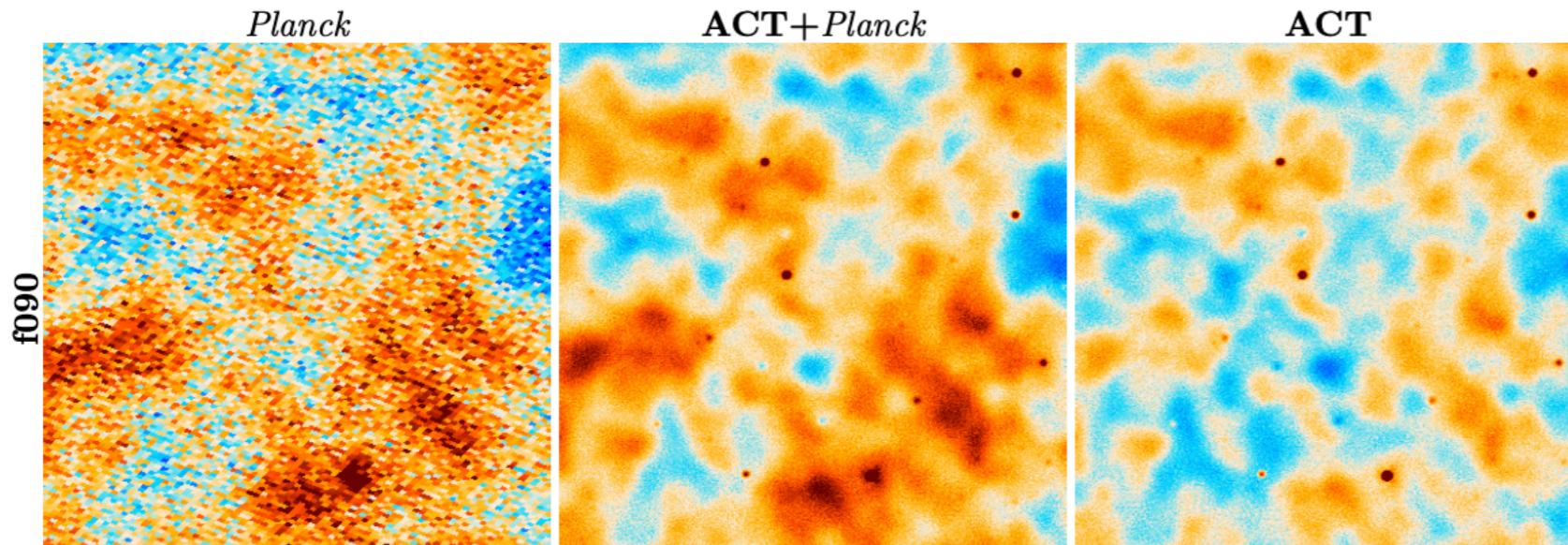
- Isotropic radiation ($\Delta T/T \sim 10^{-5}$)
- $\bar{T} = 2.7\text{K}$
- “Emitted” at redshift $z = 1100$ when the universe was 380 000 years old

When CMB is produced
universe becomes **neutral**

Hydrogen + Helium
Recombination



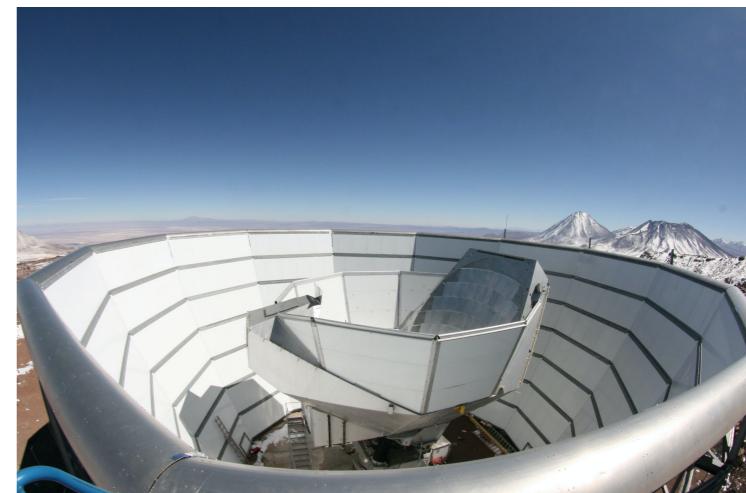
CMB seen from space by **Planck** space telescope



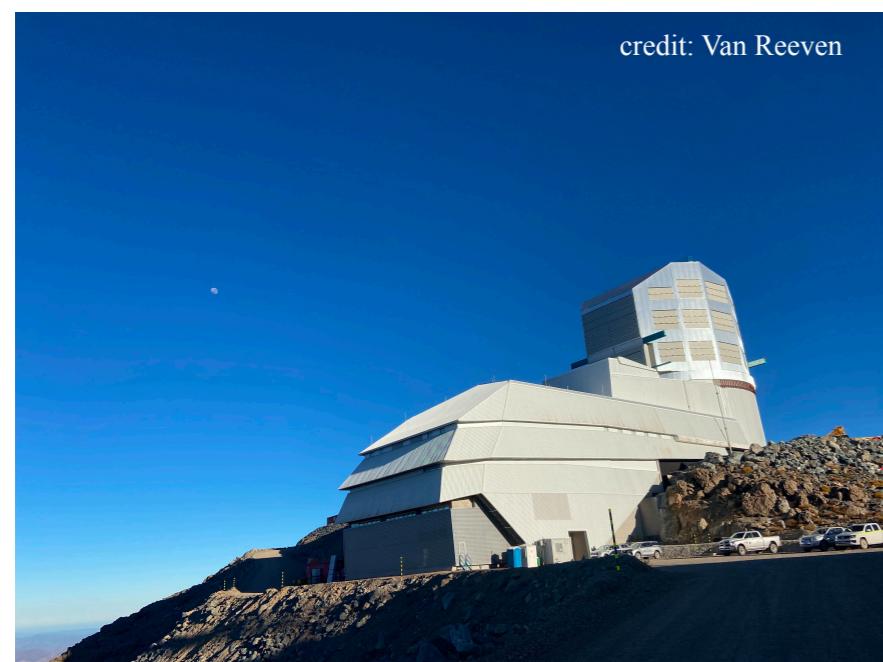
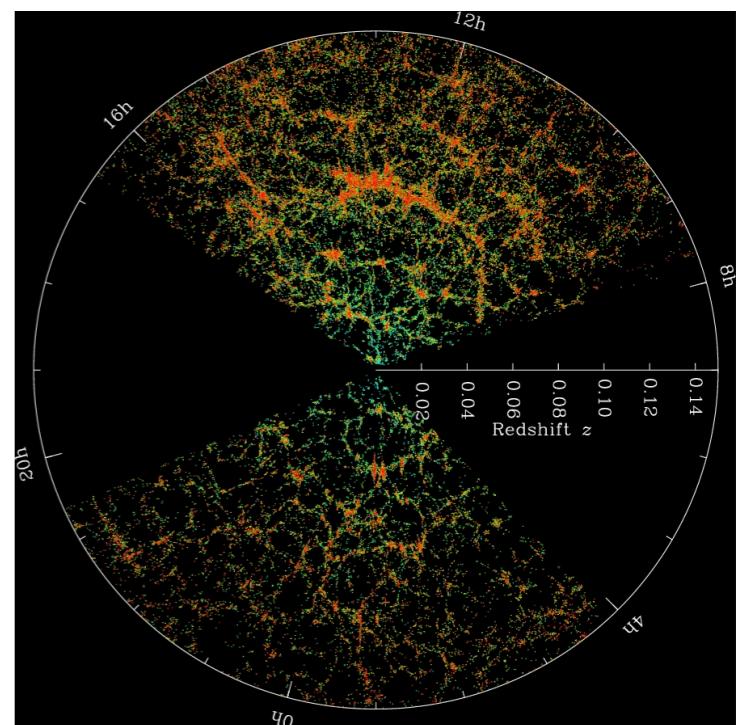
CMB anisotropy at 90 GHz with Planck and ACT

Naess et al 2020

High sensitivity
high resolution
large area CMB sky maps



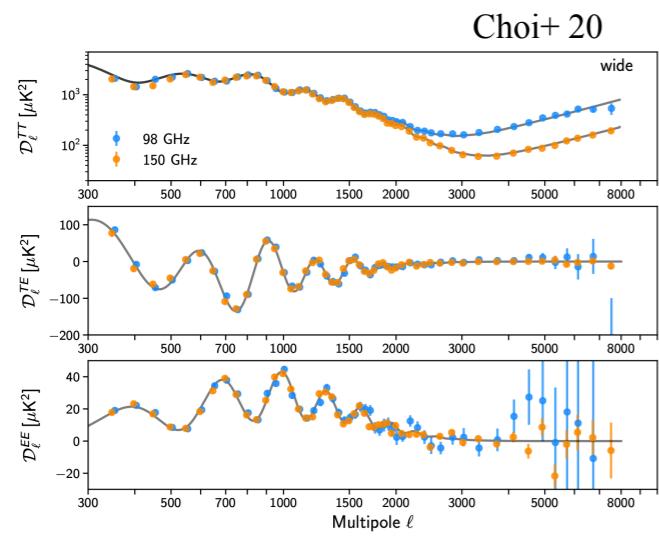
ACT (also SPT, Planck from sky)

Galaxy surveys
with 100's of millions objects

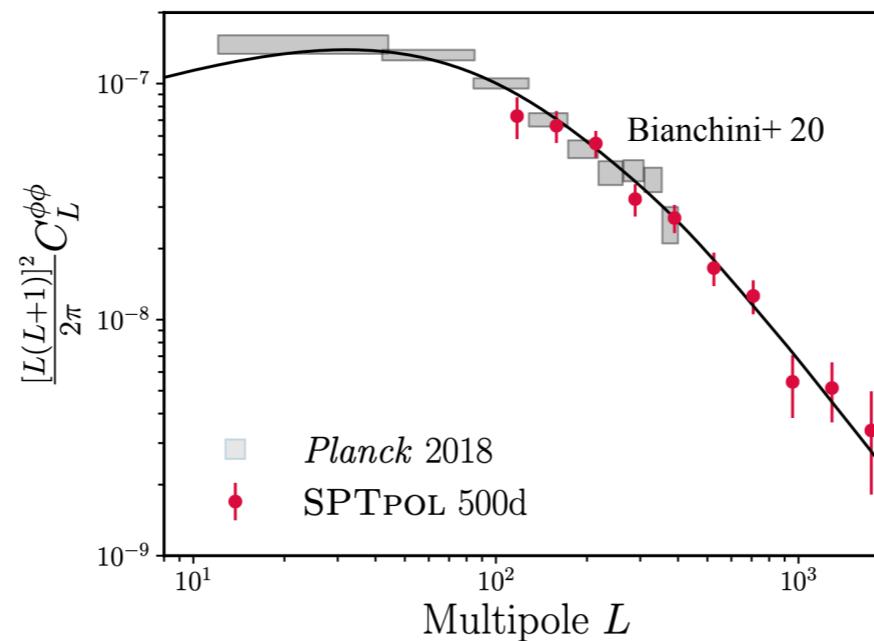
Rubin (also DES, unWISE, SDSS, DESI,...)

See <https://www.legacysurvey.org/viewer/>

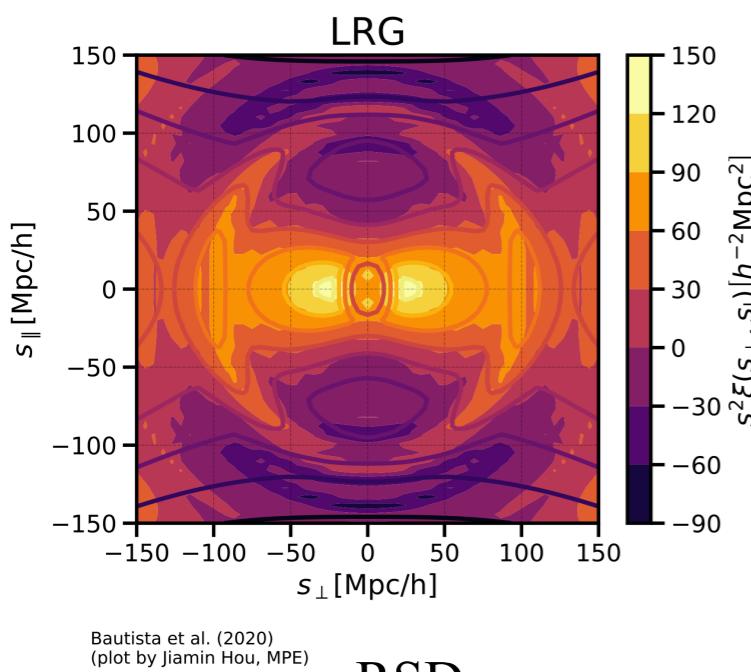
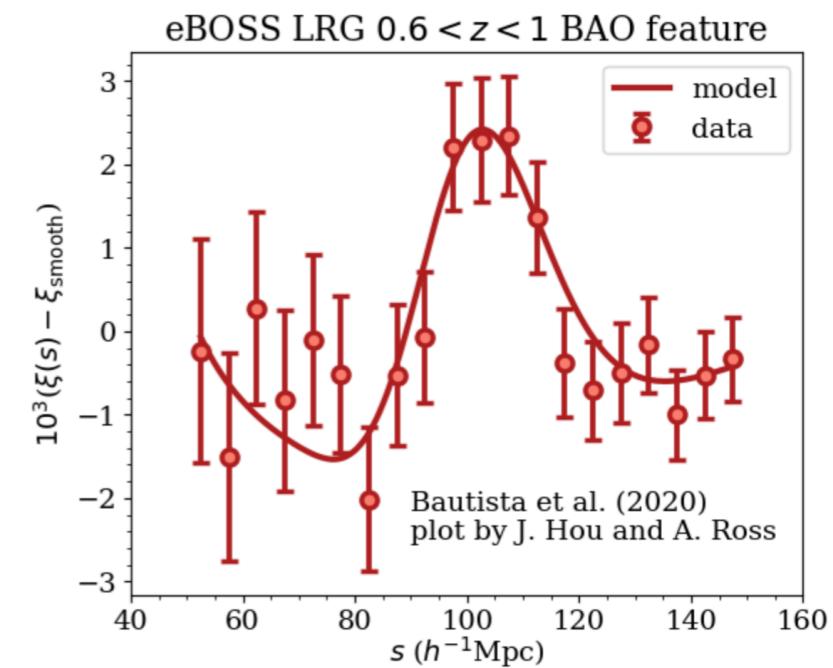
- Currently relies on a few observables



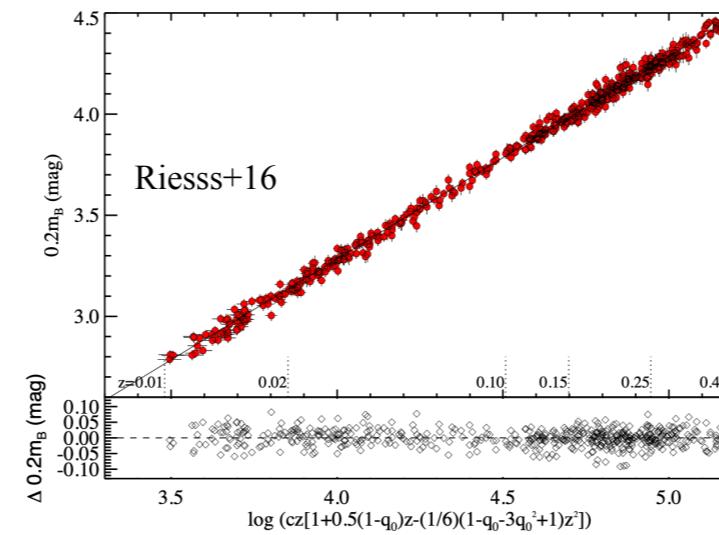
CMB Power Spectra
Temperature & Polarization



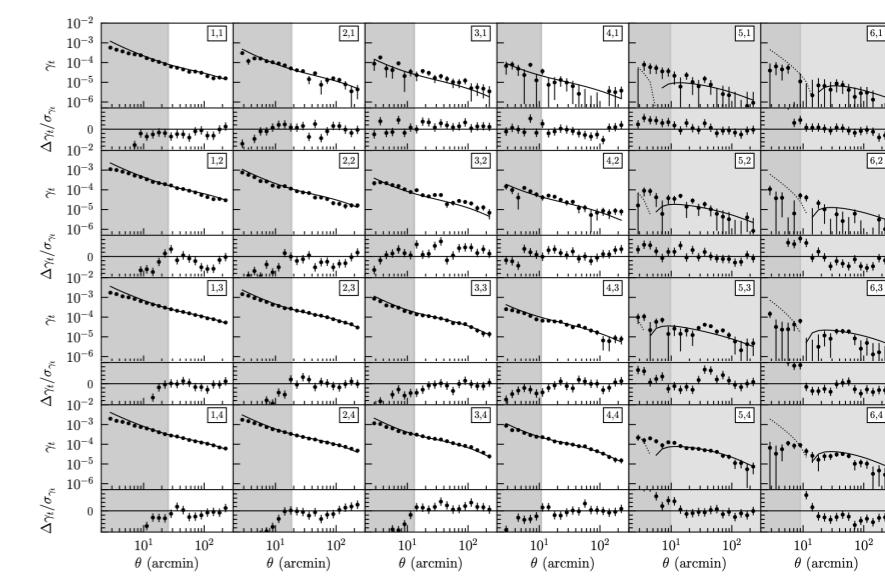
Lensing potential power spectrum
New ACT measurement coming!



RSD



SNIa



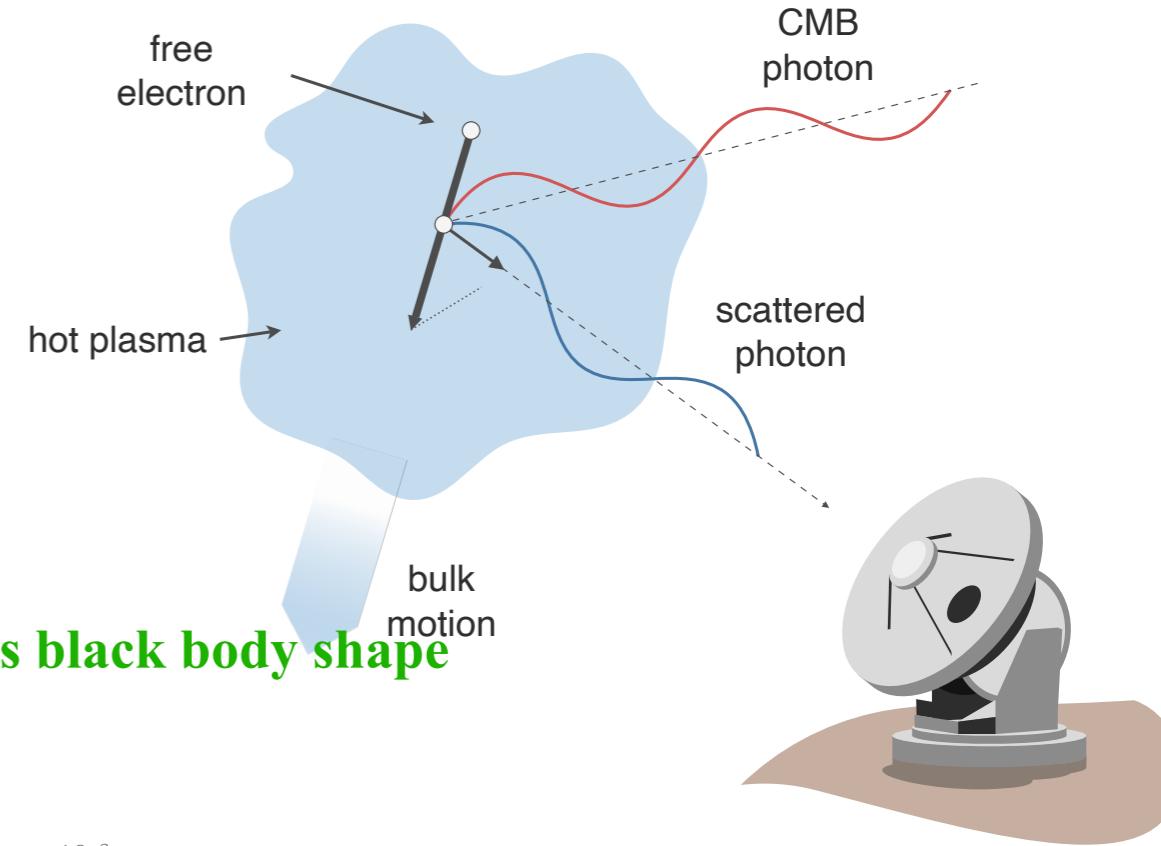
Galaxy lensing and clustering

- Only few years back, most of these probes weren't part of precision cosmology
- **SZ** (about to be) part of it.... **WHAT** is SZ? **WHY** is it important? And **HOW**?

WHAT?

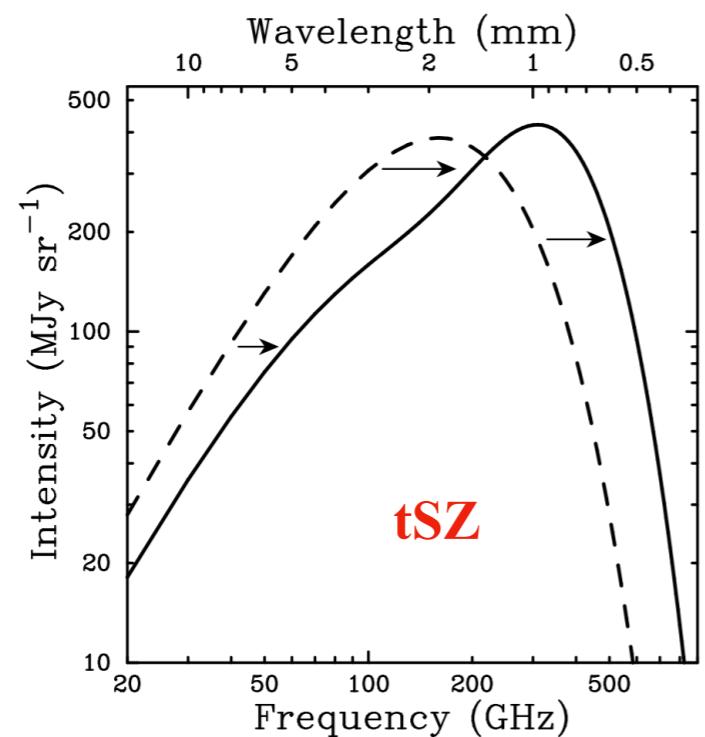
- SZ = **Compton scattering** between **CMB** and **electrons**

- Electrons are in the ionized plasma around galaxies
ICM: **intra cluster medium**
CGM: circum galactic medium



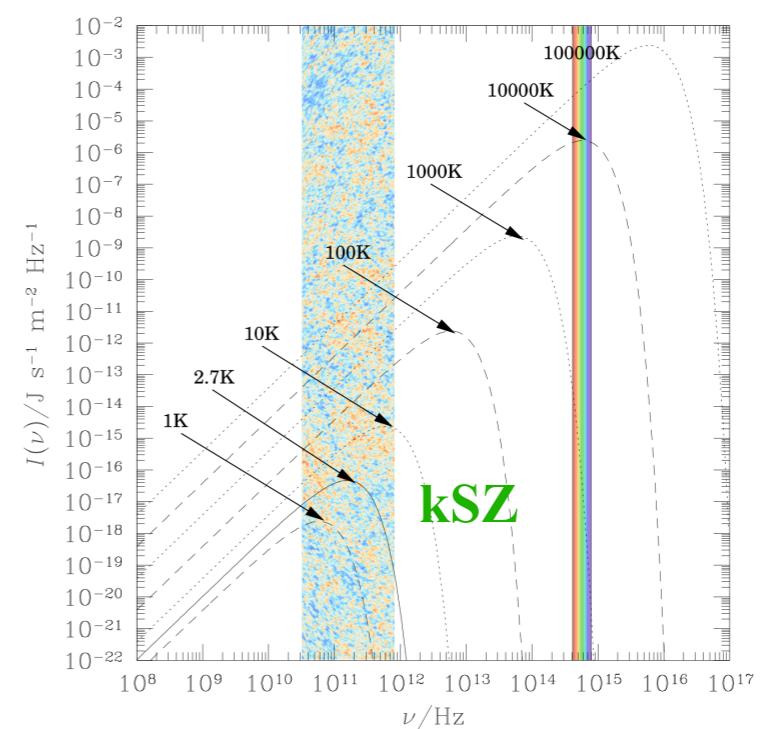
- **THERMAL “tSZ”** is **frequency dependent**

- **KINETIC “kSZ”** is Doppler boost of CMB spectrum, **preserves black body shape**



- **tSZ** effect direct probe of **gas pressure**

- **kSZ** effect direct probe of **gas momentum**
(i.e., **velocity** and **density**)
- ... some maths to understand this



- Both tSZ and kSZ are **redshift independent**, using CMB as a backlight

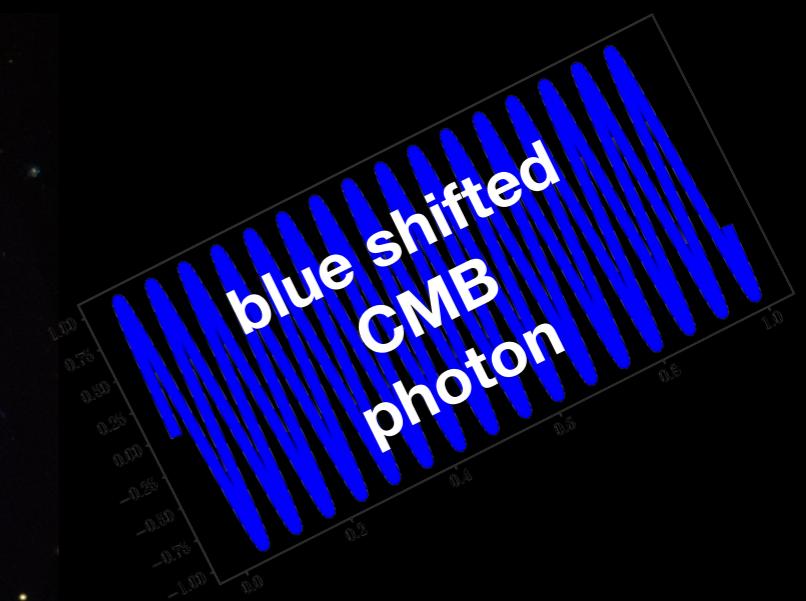
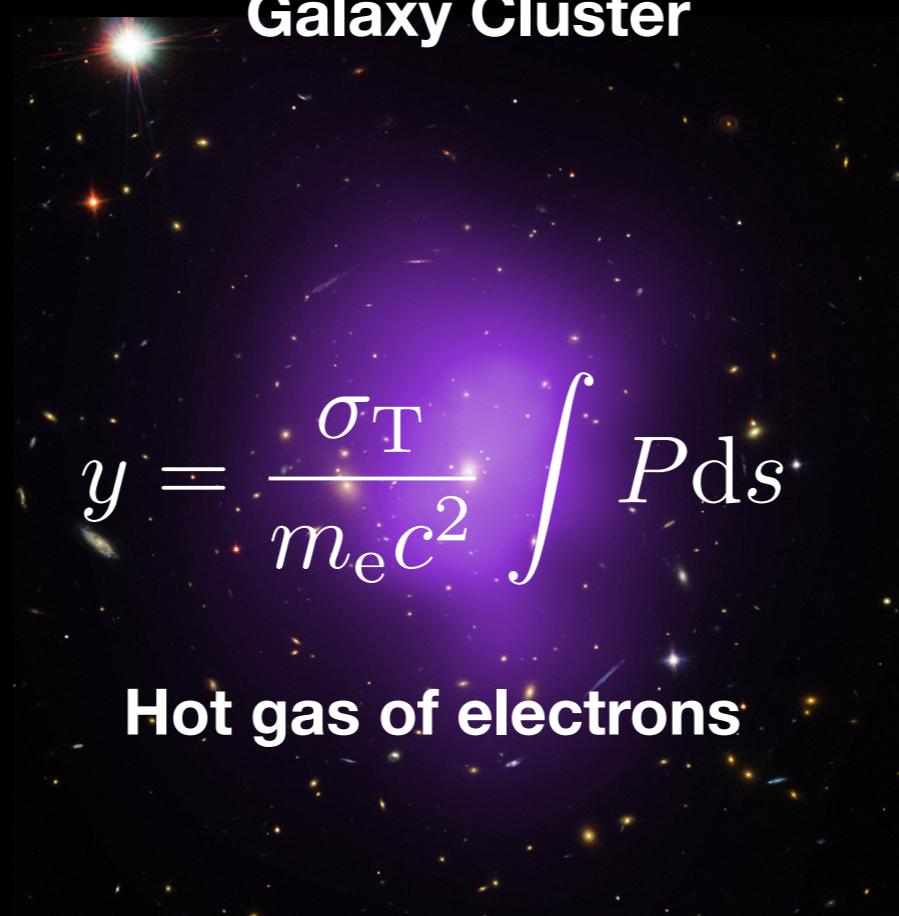
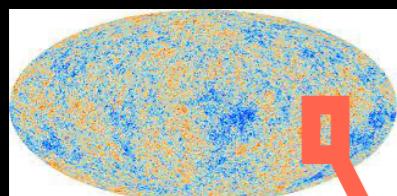
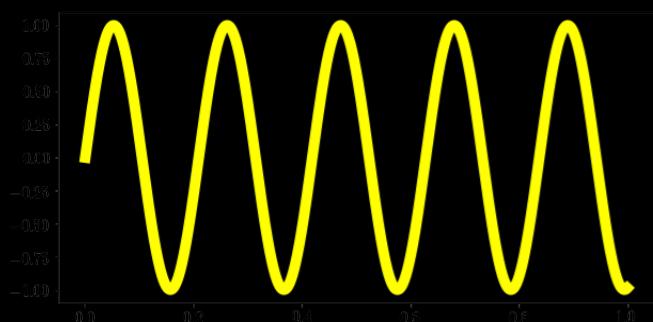


Sunyaev & Zeldovich
~1970

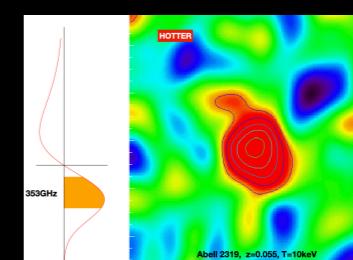
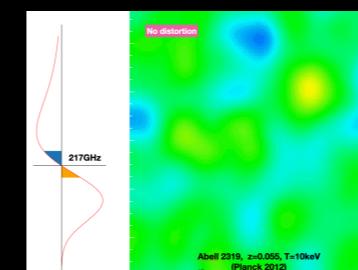
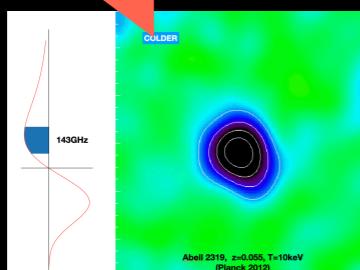
Inverse Compton Scattering

Electron gives energy to photon

CMB
photon

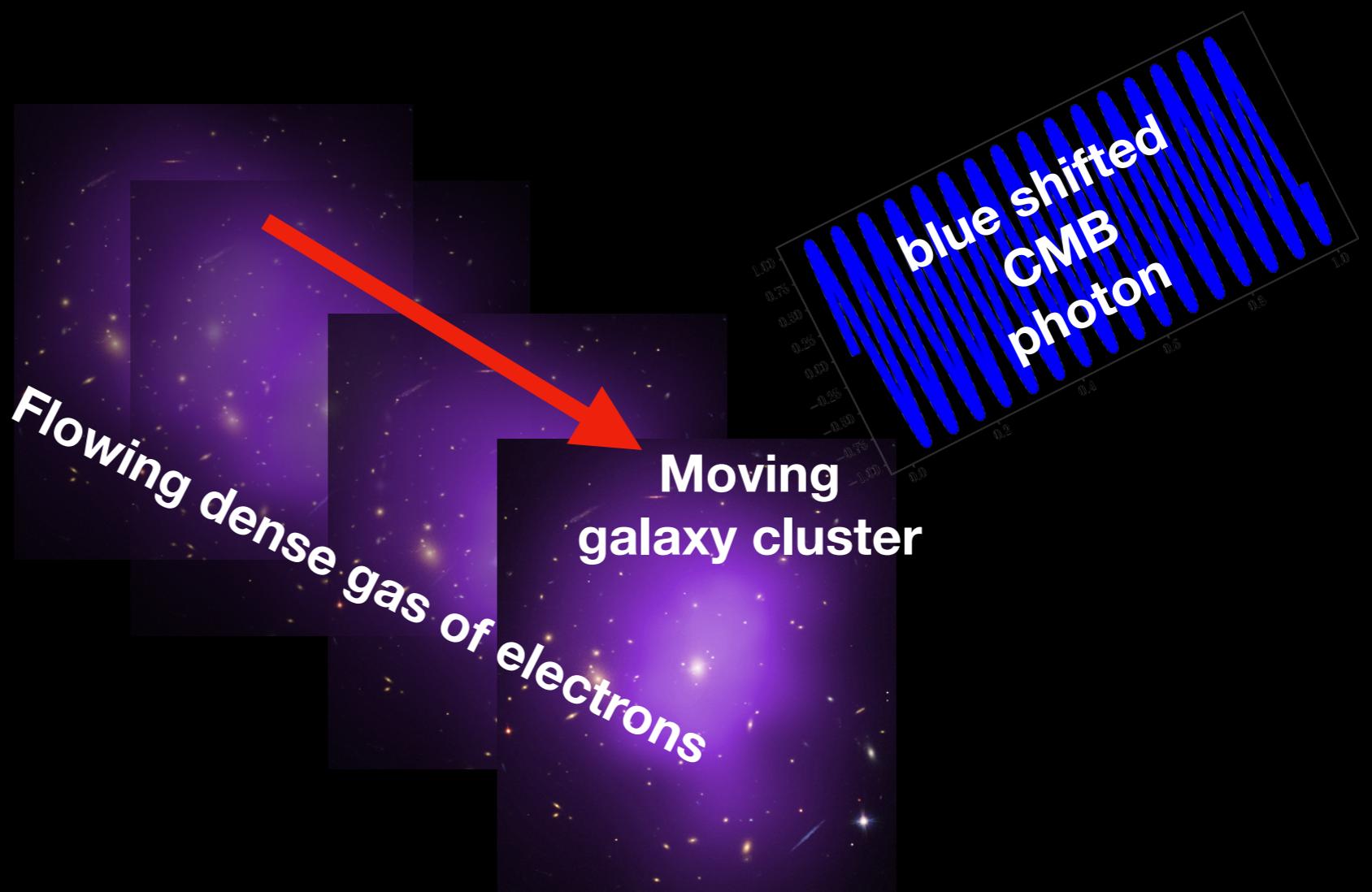
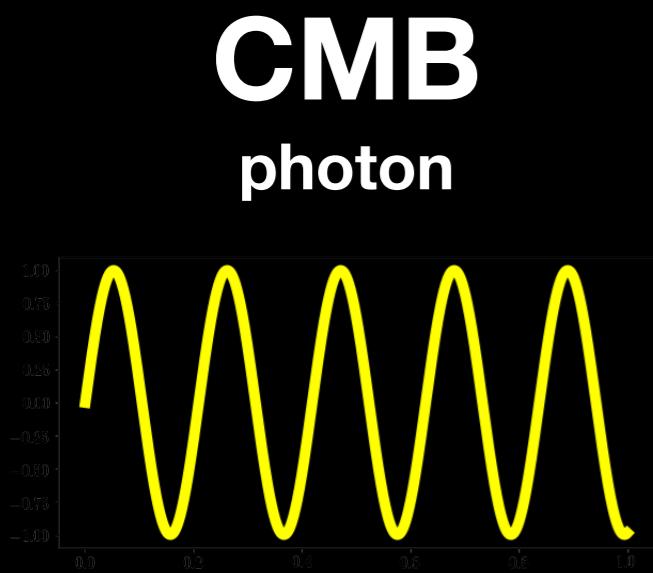


THERMAL SUNYAEV ZELODOVICH EFFECT



Doppler shift of photons due to electrons bulk motion

$$\Theta_{\text{kSZ}} \sim \int \sigma_T n_e \mathbf{v} \cdot \mathbf{n} dl$$



KINETIC SUNYAEV ZELDOVICH EFFECT

- Boltzmann equation in CMB frame with Compton scattering

$$\frac{\partial n(\omega)}{\partial t} = -2 \int \frac{d^3 p}{(2\pi)^3} d^3 p' d^3 k' W \{ n(\omega)[1 + n(\omega')]f(E) - n(\omega')[1 + n(\omega)]f(E') \},$$

Photon occupation number

Relativistic Maxwellian electron distribution

- Expand in powers of $\Delta x \equiv \frac{\omega' - \omega}{k_B T_e}$
- Expand in powers of β

$$f_C(E_C) = [e^{\{(E_C - m) - (\mu_C - m)\}/k_B T_e} + 1]^{-1}$$

$$\approx e^{-\{(E_C - m) - (\mu_C - m)\}/k_B T_e},$$

kSZ**tSZ**

Thermal-kinetic SZ effect

$$E_C = \gamma (E - \vec{\beta} \cdot \vec{p})$$

Velocity/Density

Temperature/Pressure

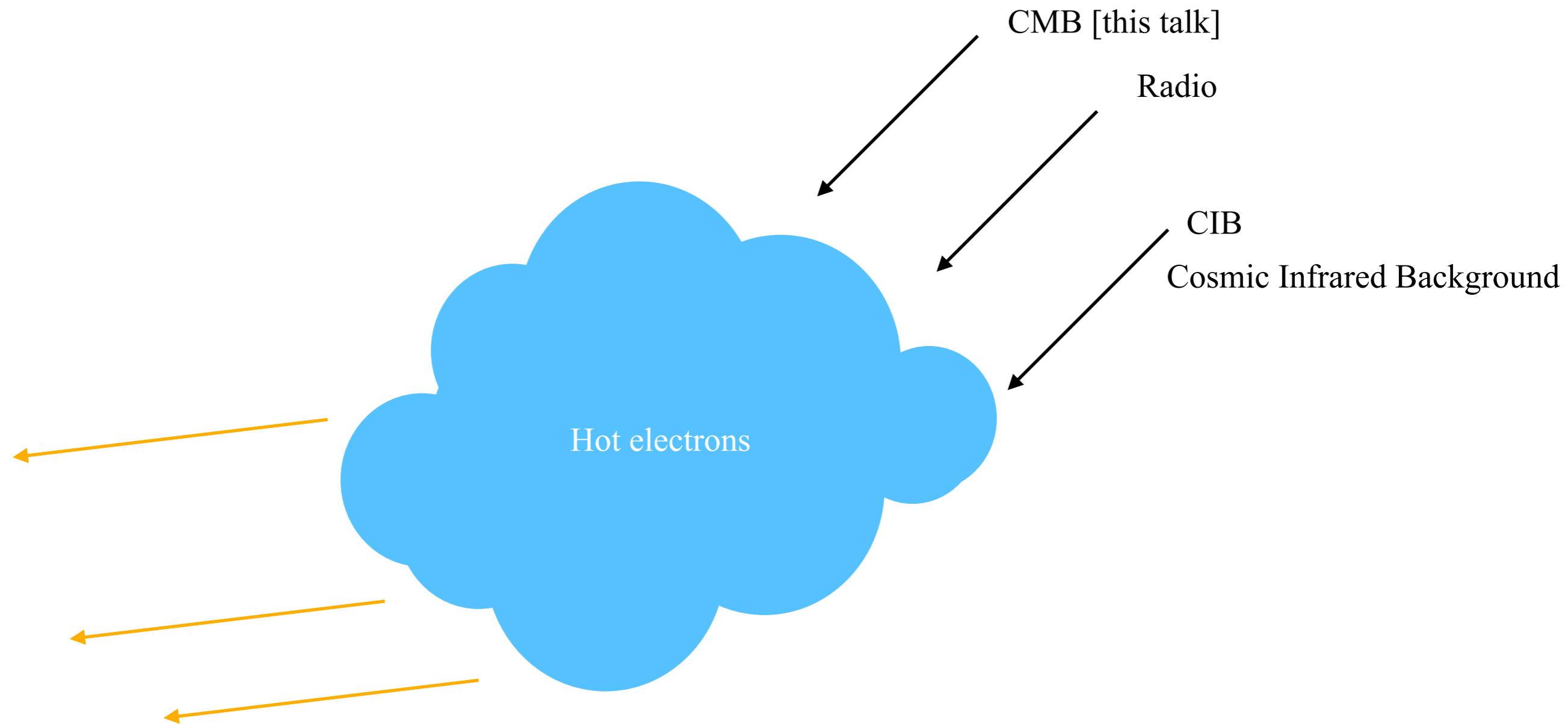
$$= \mathbf{v} \cdot \hat{\mathbf{n}} \mathcal{G} + \theta_e \mathcal{Y} + \mathbf{v} \cdot \hat{\mathbf{n}} \theta_e \left(\frac{2}{5} \mathcal{G} - \mathcal{Y}^{(2)} + \frac{7}{5} \mathcal{Y}^{(3)} \right) \\ + \theta_e^2 \left(-\frac{3}{10} \mathcal{Y}^{(2)} - \frac{21}{10} \mathcal{Y}^{(3)} + \frac{7}{10} \mathcal{Y}^{(4)} \right) + \mathbf{v} \cdot \hat{\mathbf{n}} \theta_e^2 \left(\frac{1}{5} \mathcal{G} - \frac{7}{10} \mathcal{Y}^{(3)} - \frac{33}{10} \mathcal{Y}^{(4)} + \frac{11}{10} \mathcal{Y}^{(5)} \right) + \mathcal{O}(v^2, \theta_e^3)$$

Relativistic (thermal) SZ effect

Relativistic thermal-kinetic SZ effect

See Coulton et al 2020

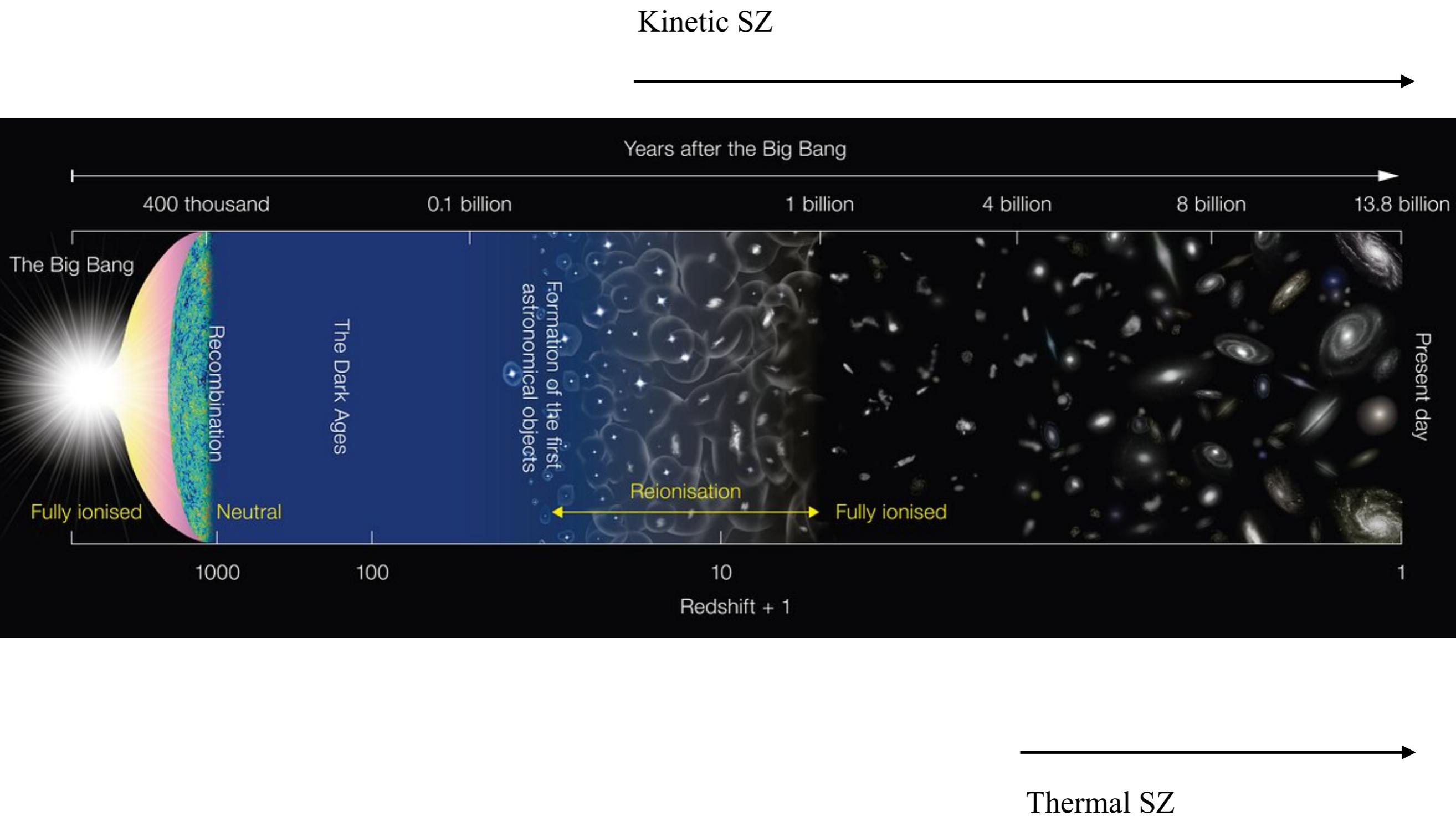
Hot electrons Inverse-Compton scatter photons irrespective of their nature



A certainly well-known fact.... which had not been studied in details until a year ago

Radio SZ: Holder & Chluba 2021

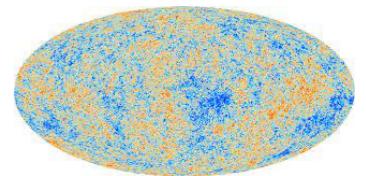
CIB SZ: Sabyr, Hill, Bolliet 2022



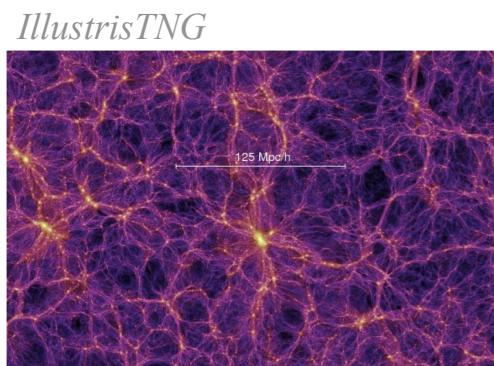
WHY?

$$\Omega_\Lambda \approx 0.7 \quad \Omega_m \approx 0.3$$

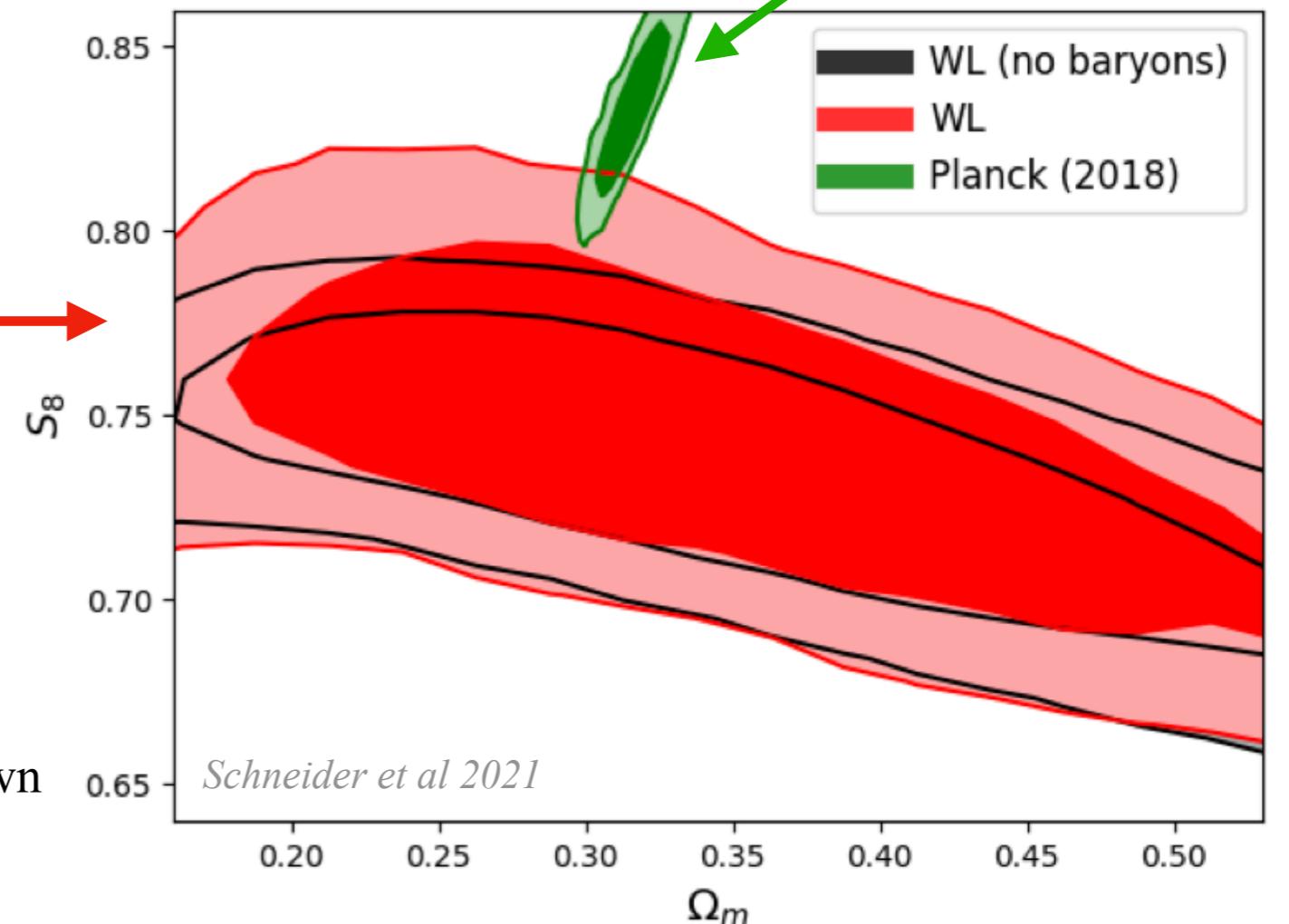
- Most of the universe is dark: dark energy (70%) dark matter (25% or 85% around galaxies)
- the **S8 tension** (matter clustering $P(k)$ at $2\text{-}3\sigma$) and Hubble tension (Age of the universe 4σ)



$$S_8 = \sigma_8 \Omega_m^{0.5}$$



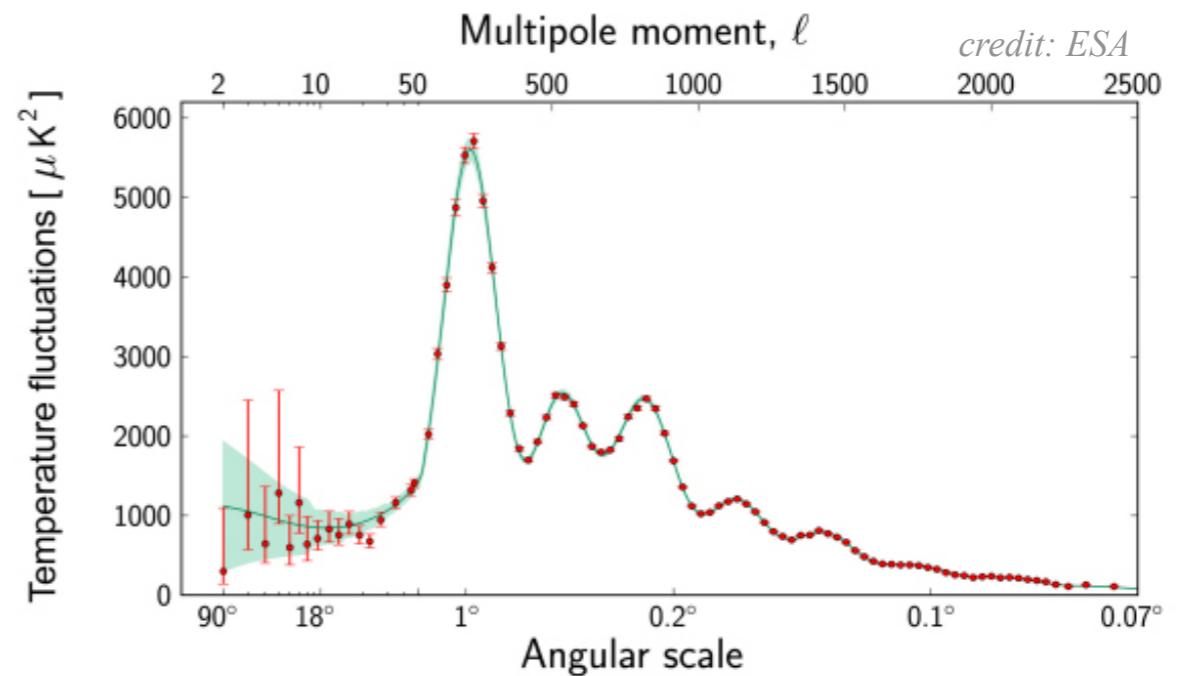
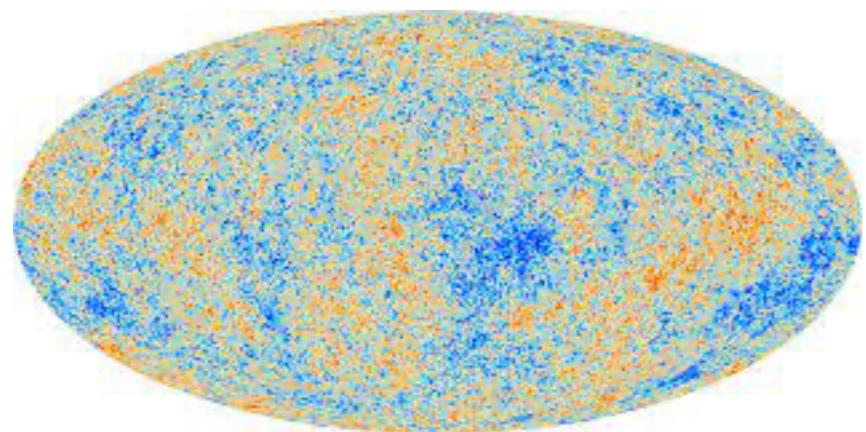
Low redshift probes
Weak Lensing
Clustering
and SZ
 $z \approx 0 - 3$



- Inflation/Big Bang
- **Galaxy formation and evolution** largely unknown
- **Baryonic effects** in precision cosmology

SZ can provide unique insight into these key questions

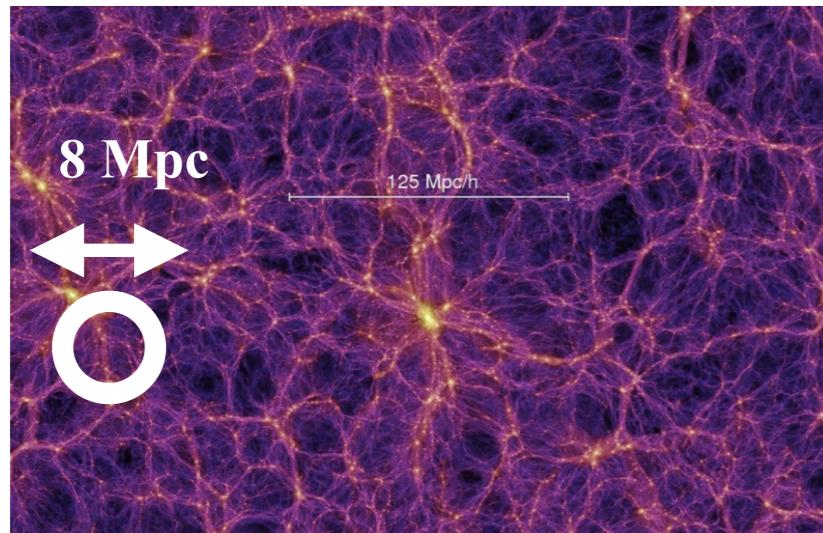
Analog to CMB power spectra



Matter power spectrum

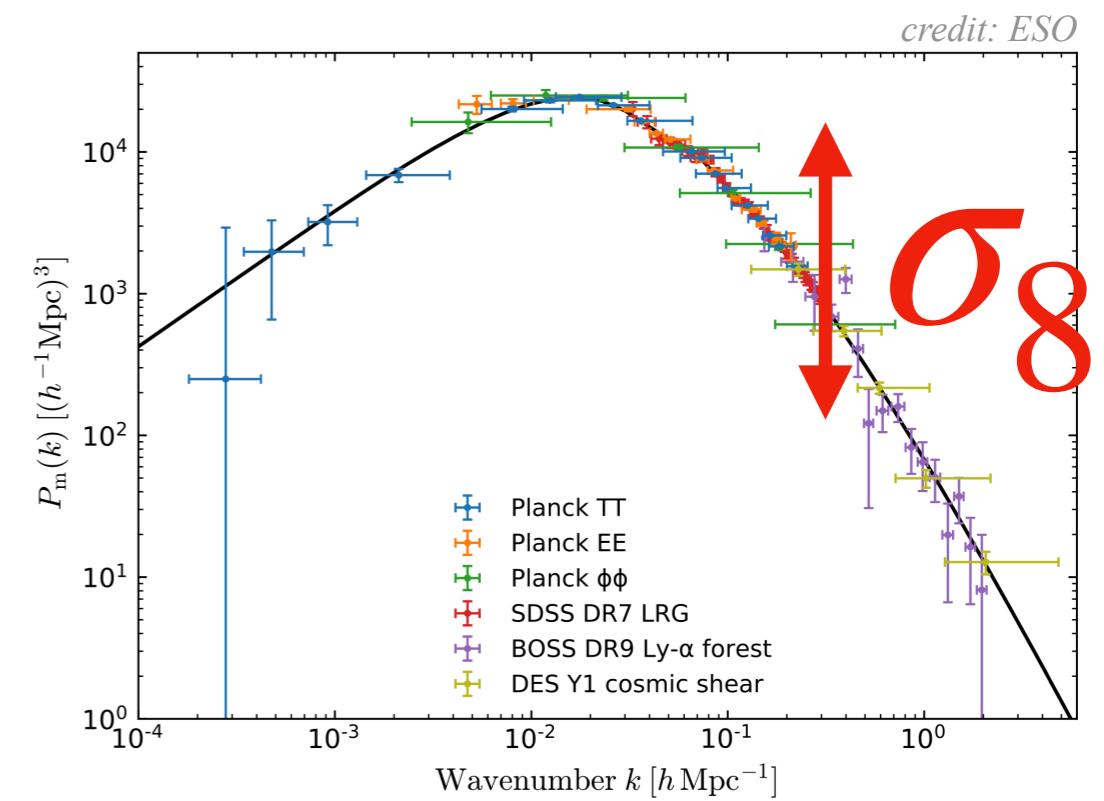
$$\xi(r) = \langle \delta(\mathbf{x})\delta(\mathbf{x}') \rangle = \frac{1}{V} \int d^3\mathbf{x} \delta(\mathbf{x})\delta(\mathbf{x} - \mathbf{r}).$$

$$\xi(r) = \int \frac{d^3 k}{(2\pi)^3} P(k) e^{i\mathbf{k}\cdot(\mathbf{x}-\mathbf{x}')}$$



$$(\sigma_8)^2 = \frac{1}{2\pi^2} \int d\log k W^2(kR) k^3 P(k)$$

$$0.1 h/\text{Mpc} \lesssim k \lesssim 1 h/\text{Mpc}$$



- S8 tension means **tension between Λ CDM (model) and data (observations)**

see 2203.06142

- Is it really a tension?

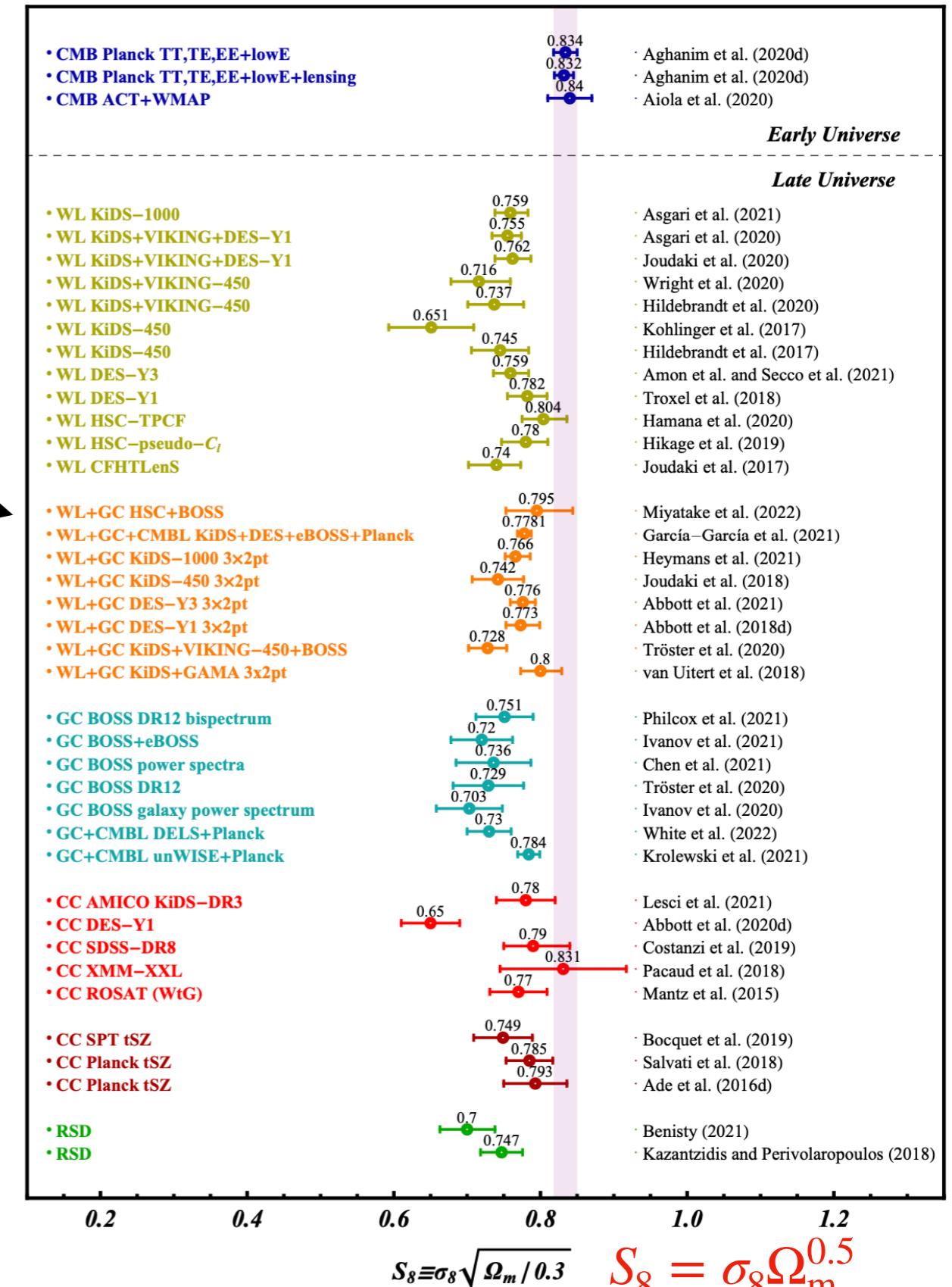
2-3 σ is not that much... but...

Tension is seen in many **different datasets**
using **different probes**, that are **independent**

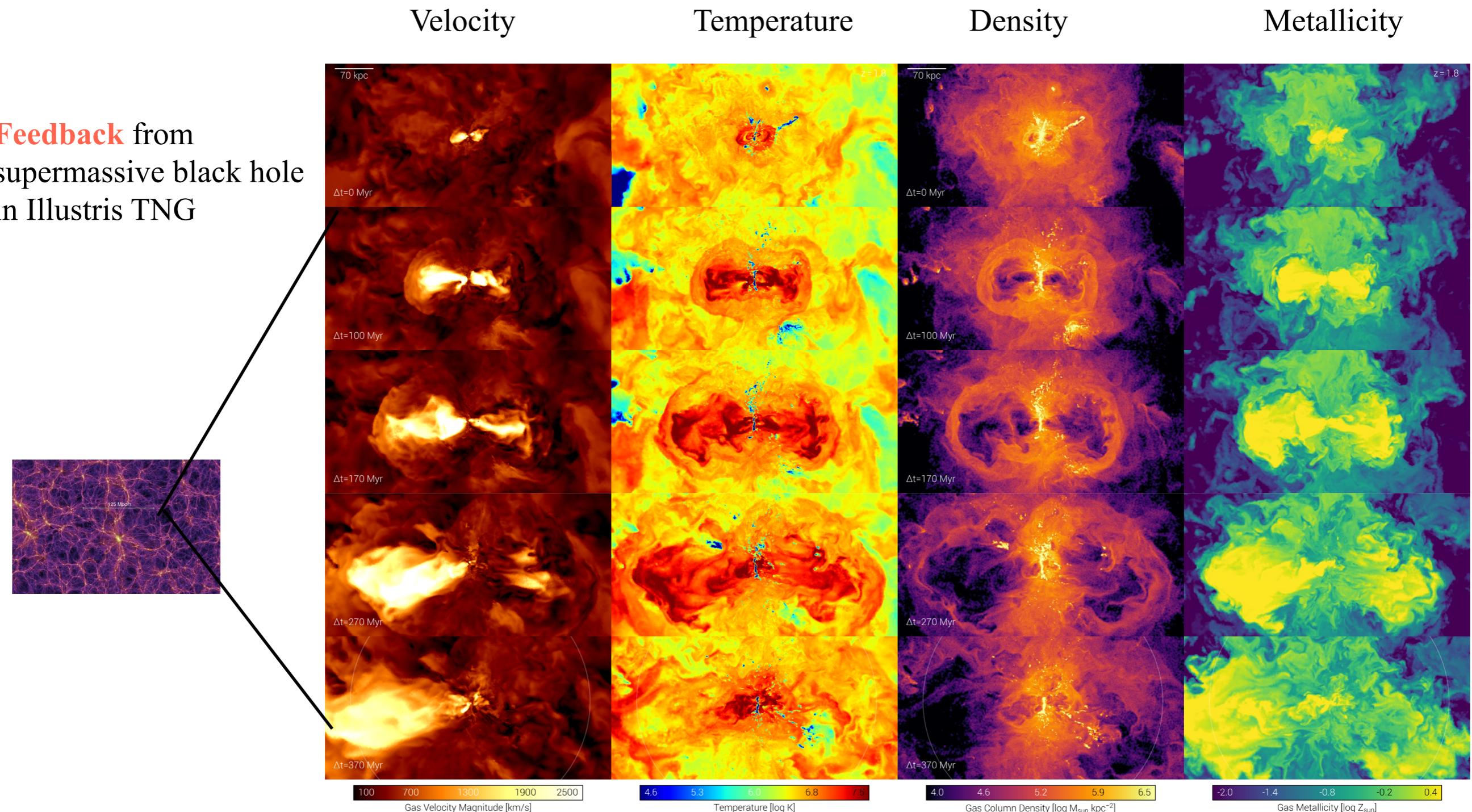
- Is the **model** wrong?

SZ
Tight constraints
on cosmology.
Test of Λ CDM.

See Bolliet, Comis, Komatsu, Macias-Perez 2018
Bolliet et al 2019



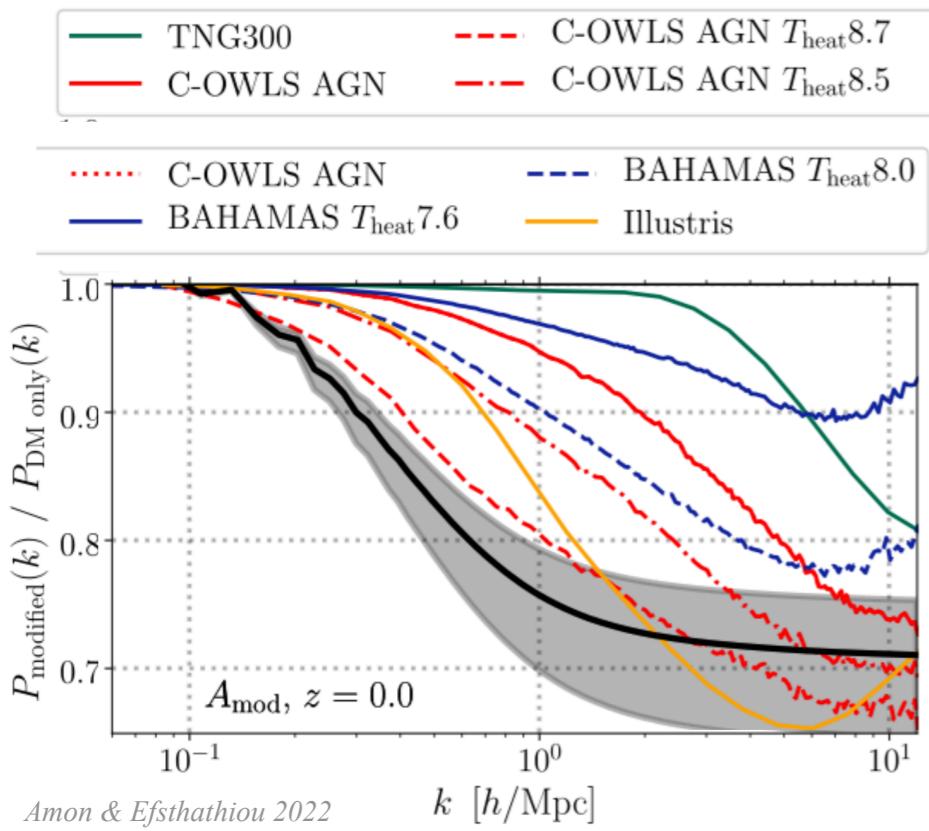
Is the **data** wrong? Systematics (instrumental and **modeling**)



Baryonic feedback (Black holes, AGN, SN) processes convert **gravitational energy into heat**, altering the distribution of matter around galaxies, **extending to the virial radius and beyond**

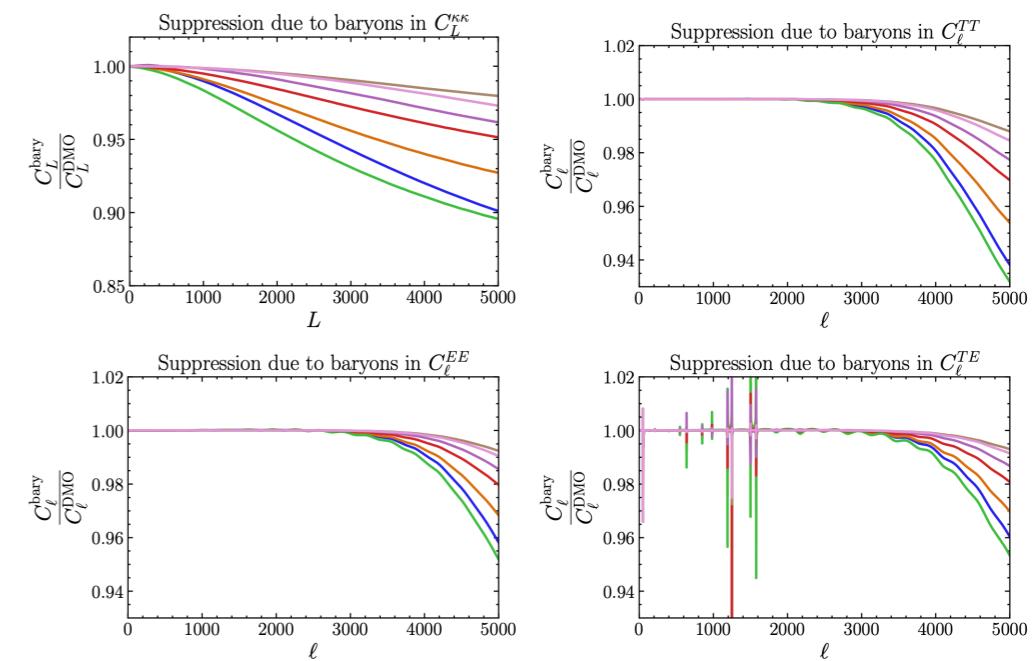
Poorly understood due to current **scarcity of observational data**....

Altered matter distribution from **baryonic effects** translates into **suppression of small-scale** matter power spectrum compared to a “dark matter only” prediction.



Small-scale Matter
P(k) is the central
brick for
observables
associated with
weak lensing and
clustering

Example: **Lensed CMB** power spectra



McCarthy et al 2021

- **Biased** cosmological constraints (σ_8 , neutrino mass,...), e.g., systematics that **need to be quantified**.
- Effect on **higher-order statistics** ?

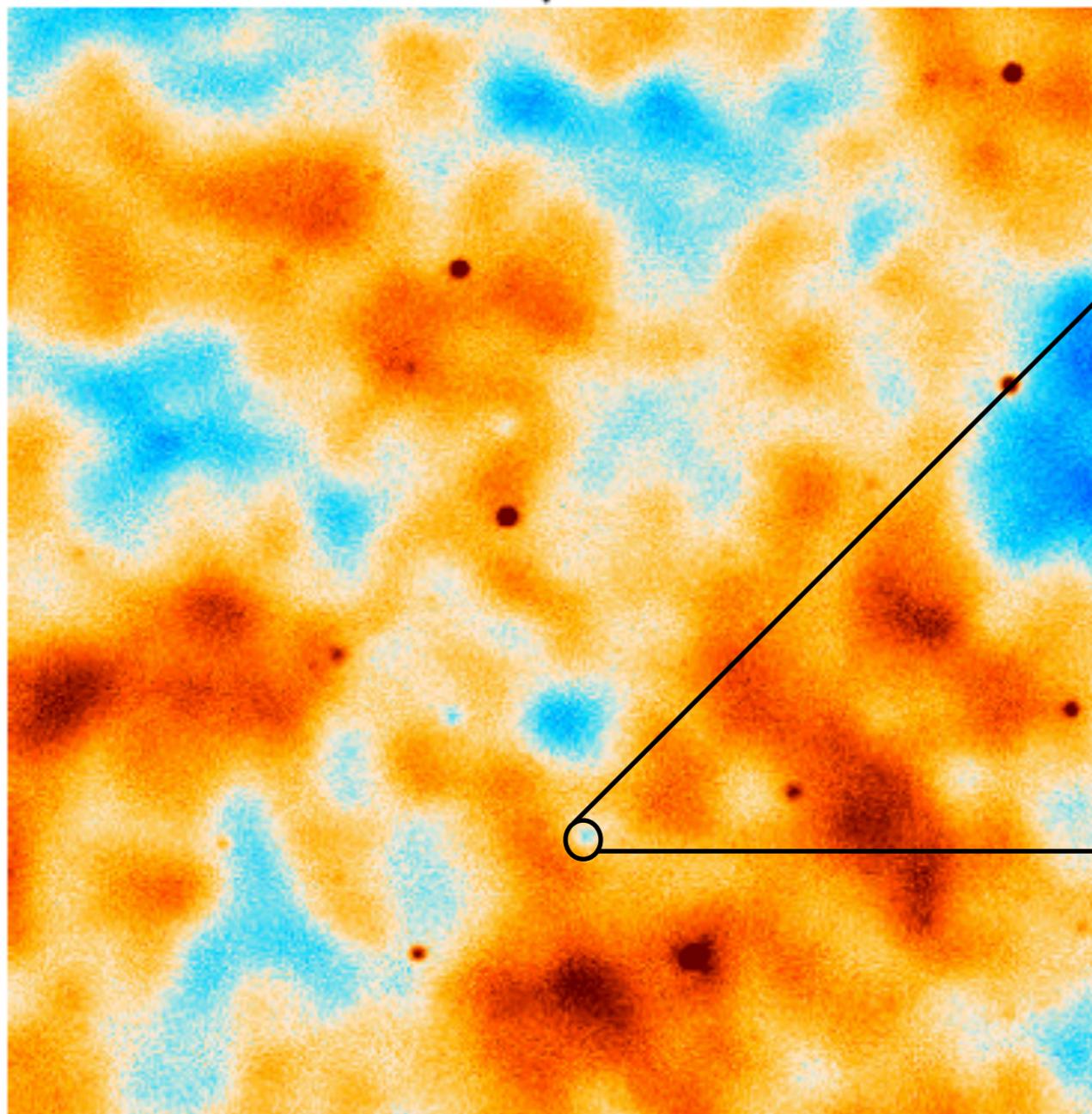
See Foreman et al, Barreira et al 2019

NASA Decadal Survey

Of all the observational diagnostics at our disposal, the **SZ effect most directly constrains** the **energy content of gas** in galactic halos produced by the combined effects of gravitational collapse and stellar and black hole **feedback**.

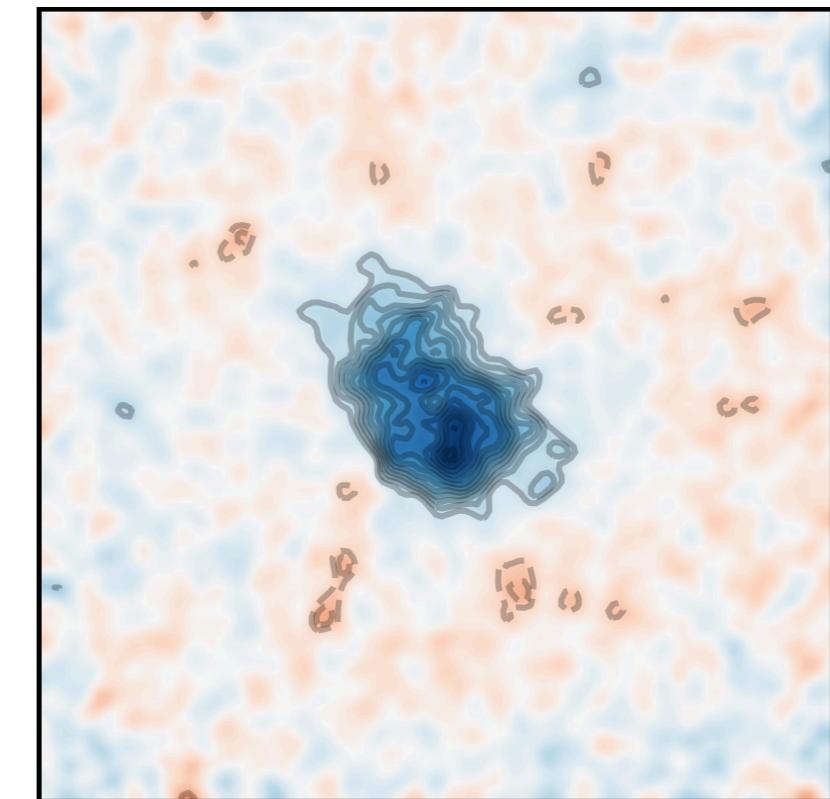
- High-resolution data

ACT+Planck



Naess et al 2020

NIKA2

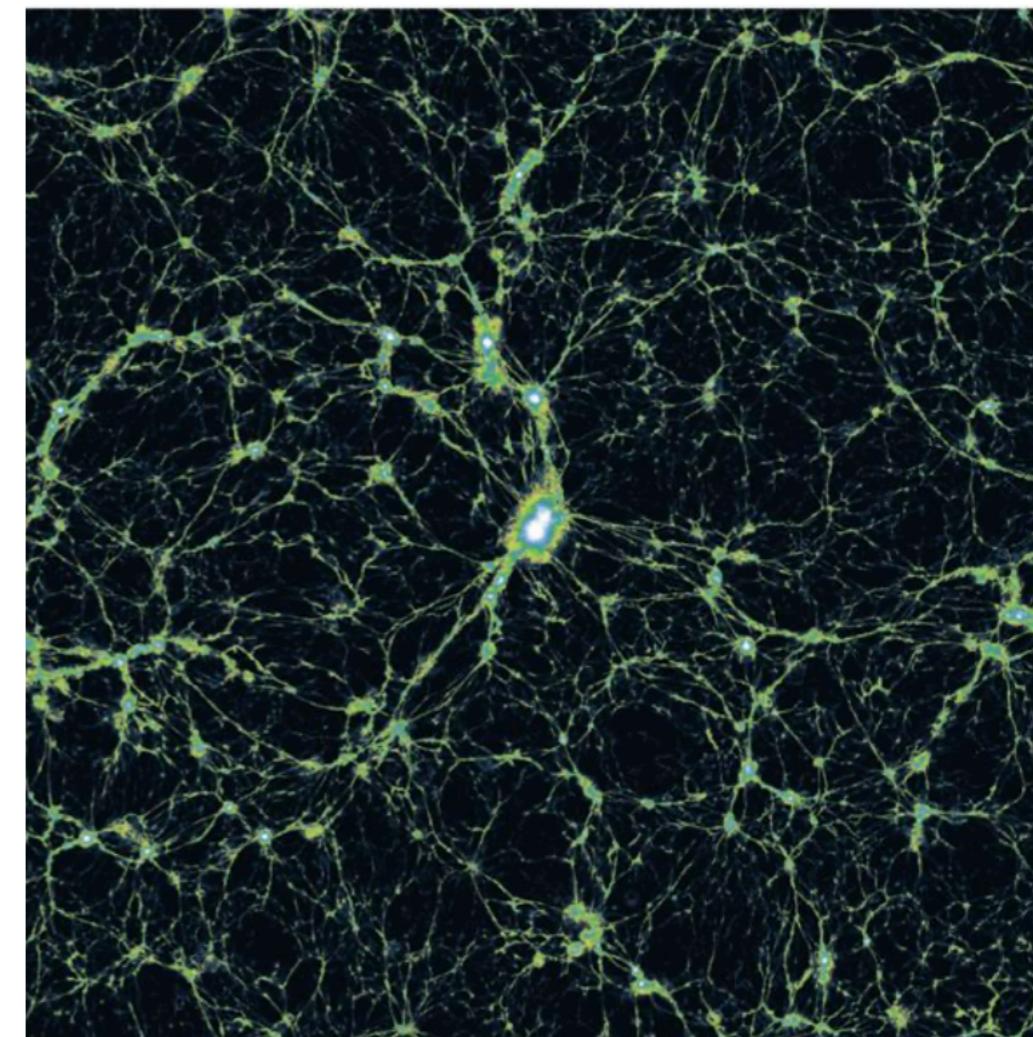
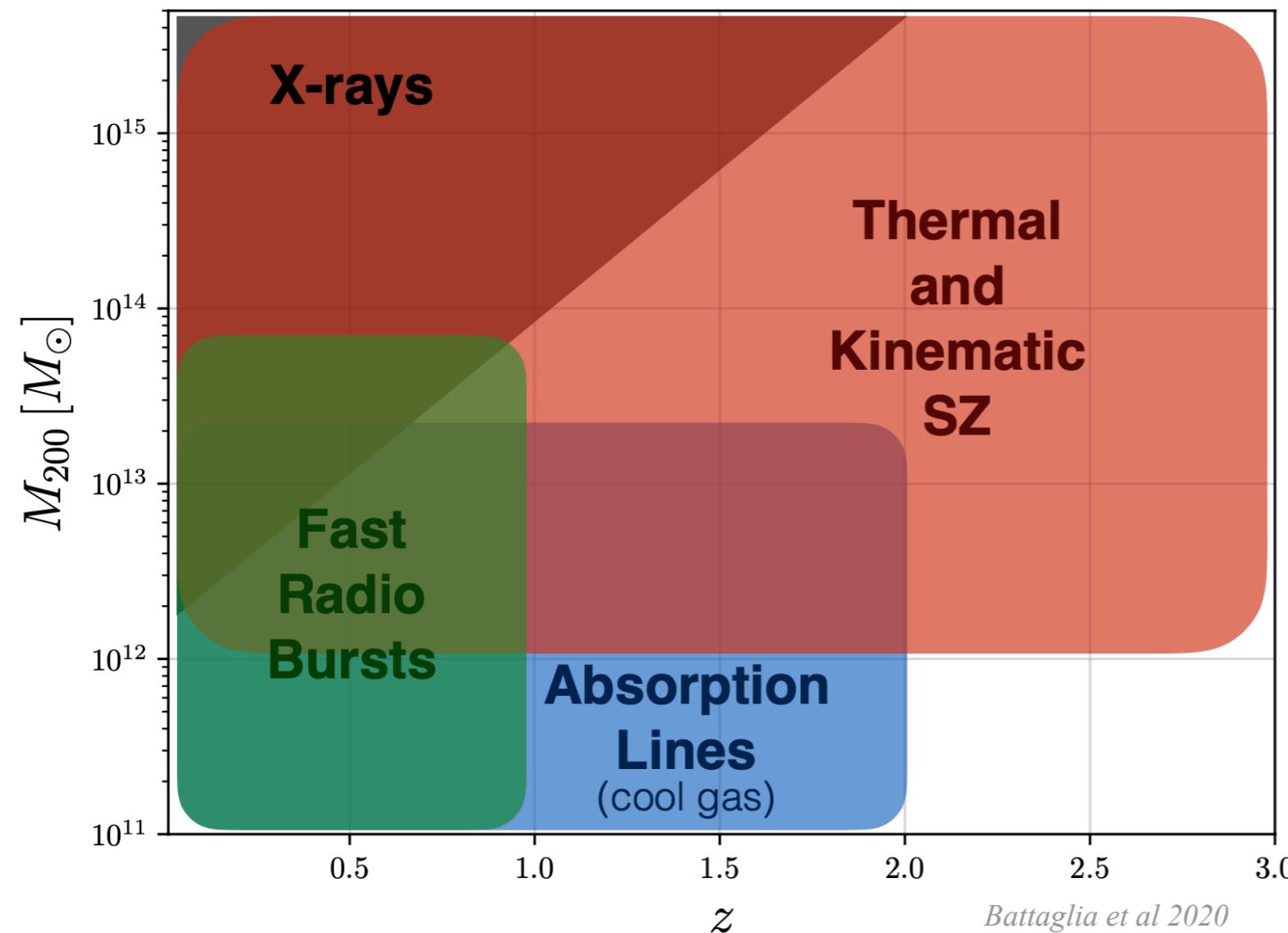


Artis et al 2022



- And... compared to other probes, **SZ** reaches **high redshift** and **low-mass halos**

Sensitivity to Gas Properties Near r_{200}



Illustris TNG

Able to **map the ionized gas** at the boundaries of galaxies

HOW?

1. Where do the SZ **cosmological constraints** come from?

- tSZ cluster counts
- tSZ power spectrum
- tSZ cross-correlations

kSZ tomography

2. How do we measure **baryons** with SZ?

- tSZ power spectrum
- tSZ cross-correlations

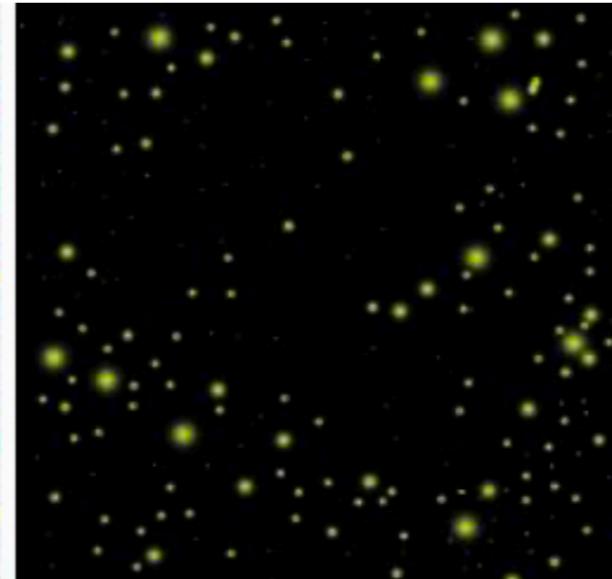
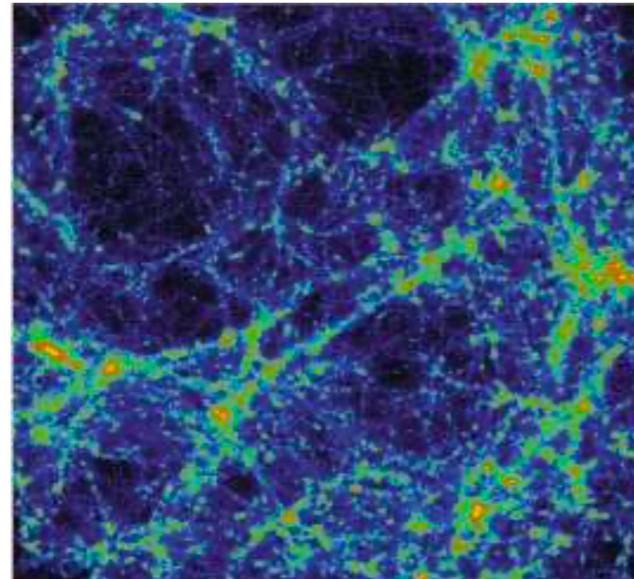
tSZ and kSZ stacking analyses

kSZ cross-correlations

- Number of clusters, **abundance** of clusters of a given mass at a given time, can be **predicted in Λ CDM** (and extensions)
- Steep function of **cosmological parameters** σ_8 and Ω_m (and others)

$$N_{\text{theory}} \propto \sigma_8^{9.8} \Omega_m^{2.9}$$

Total number of clusters



Cooray & Sheth 2002



Wikipedia

- **Given number of clusters, infer cosmological parameters** with maximum likelihood method (Poisson):

$$\ln \mathcal{L} = N_{\text{data}} \ln N_{\text{theory}} - N_{\text{theory}} - \ln(N_{\text{data}} !)$$

- Can do this in **bins of redshift** and **masses signal-to-noise** $\xi = Y(M, z)/\sigma_Y$

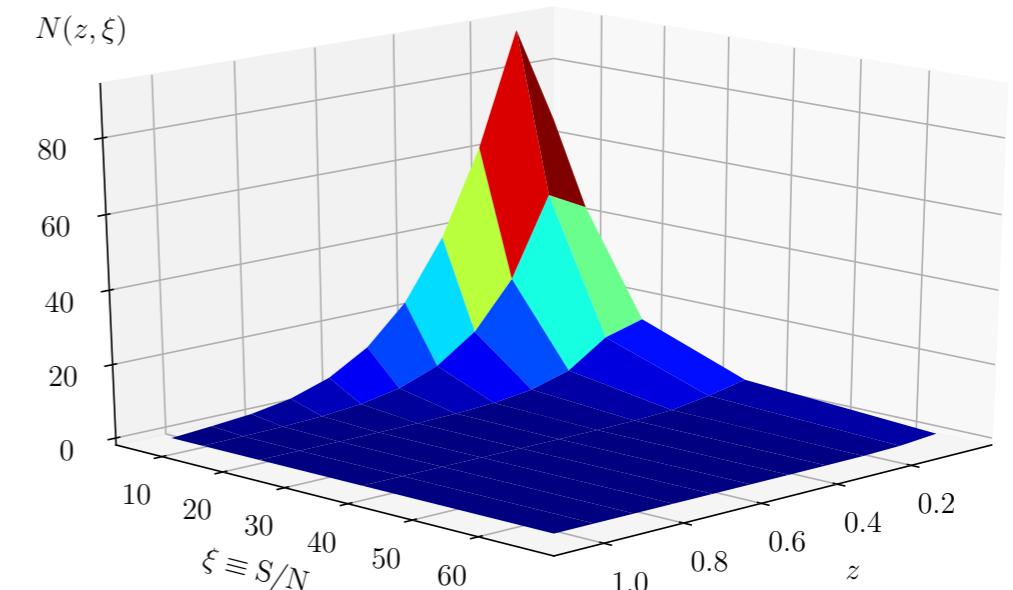
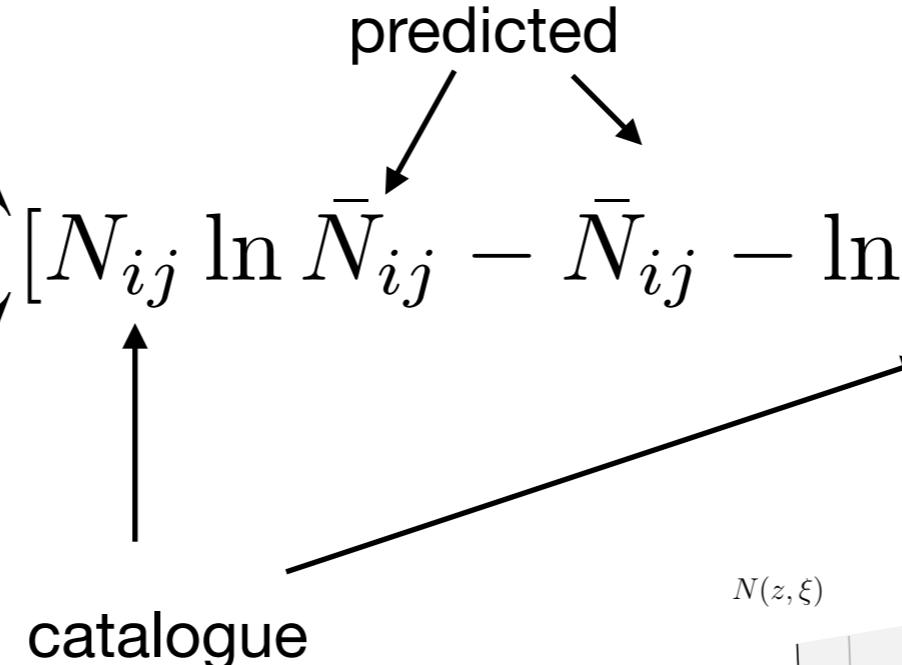
$$\bar{N}_{ij} = \frac{dN}{dz d\xi} \Delta z_i \Delta \xi_j$$

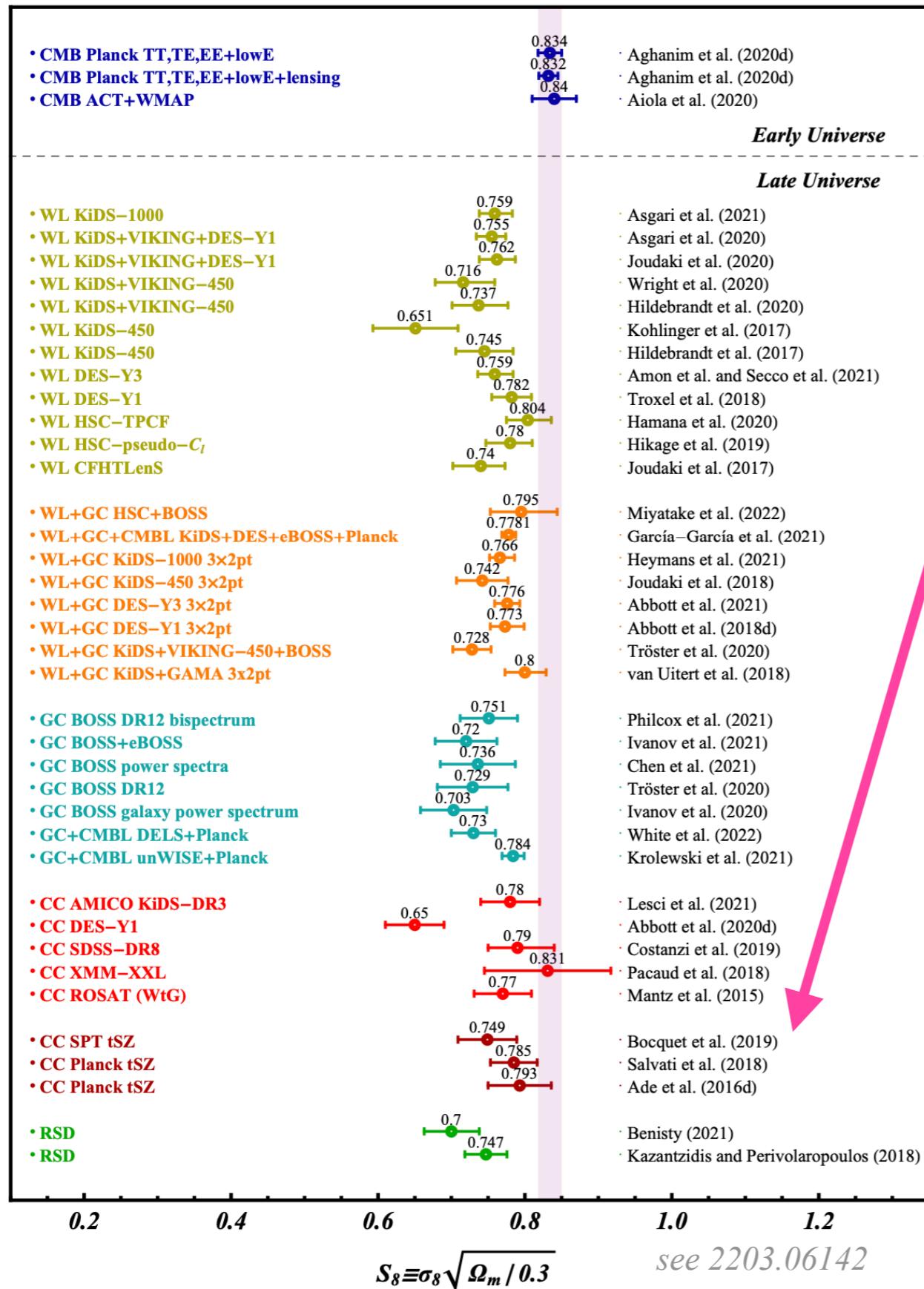
$$\frac{dN}{dz d\xi} = \int d\Omega \int dM \frac{dV}{dz d\Omega} \frac{dN}{dM dV} \mathcal{P}(\xi, \xi_j)$$

- Maximum likelihood

$$\ln \mathcal{L} = \sum_{ij} [N_{ij} \ln \bar{N}_{ij} - \bar{N}_{ij} - \ln(N_{ij}!)]$$

Bin index
 (z_i, ξ_j)





- Simple and clean probe

- **Current constraints** from Planck and SPT are **competitive**

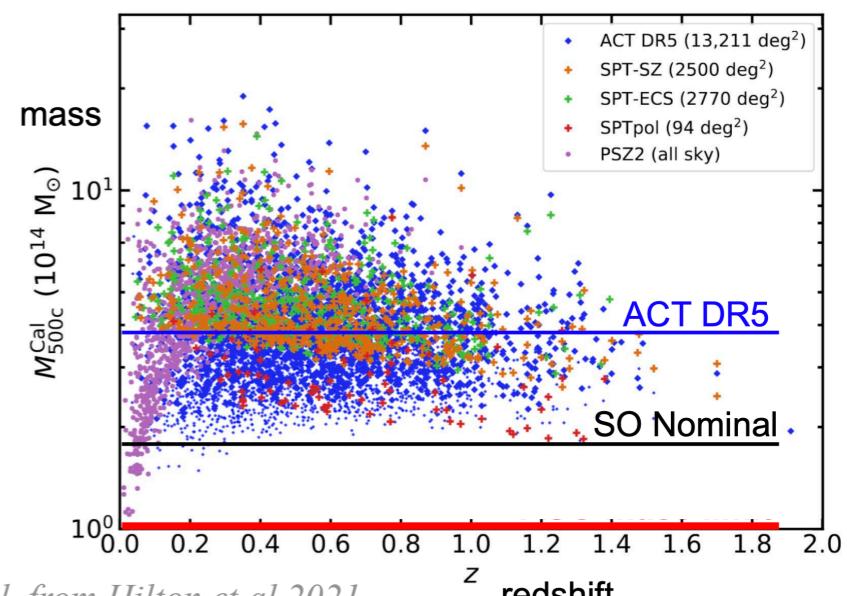
- co-Leading analysis with **ACT data**



Nick Battaglia (Cornell)
Eunseong Lee (Cornell)
Matt Hilton (KwaZulu-Natal)
Andrina Nicola (Bonn)

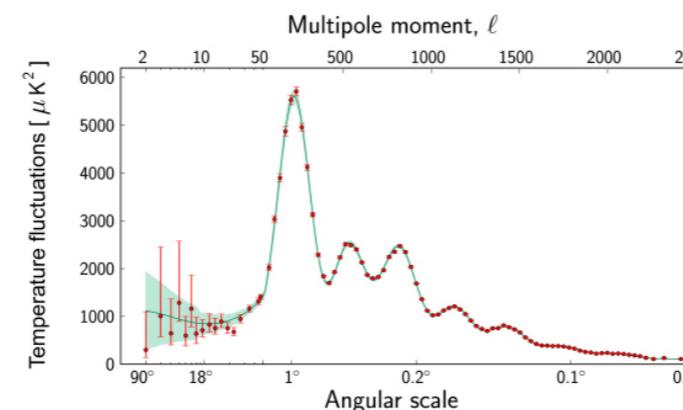
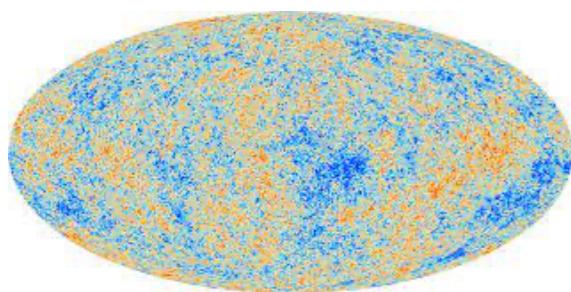
Planck 2015: 439 with SNR>6, **ACT DR5 = 3xPlanck**
SPT 2019: 343 with SNR>5, **ACT DR5 = 7xSPT**

- New **SZ S8 constraints coming-up**

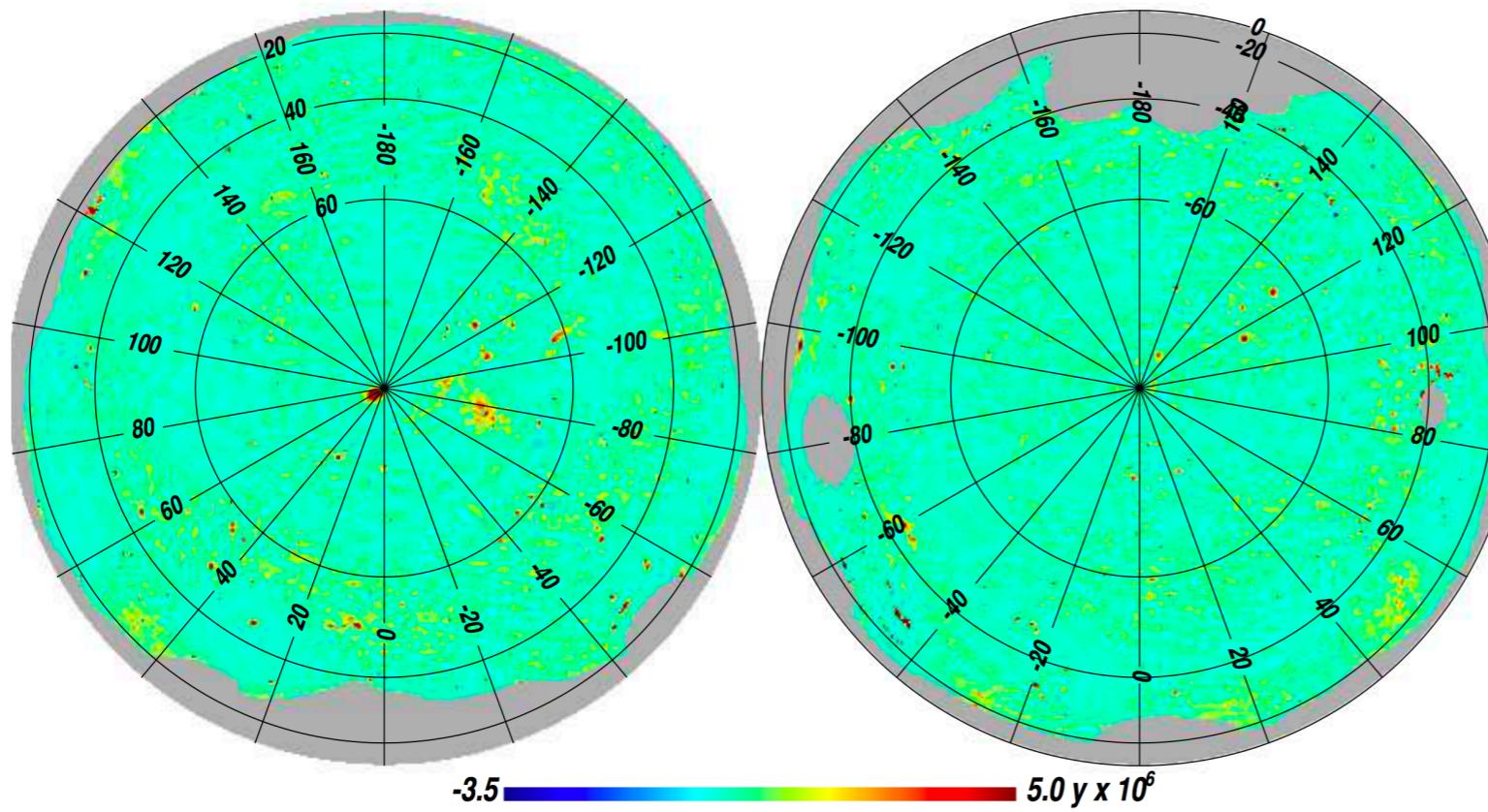


Credit: Hill, from Hilton et al 2021

CMB power spectra



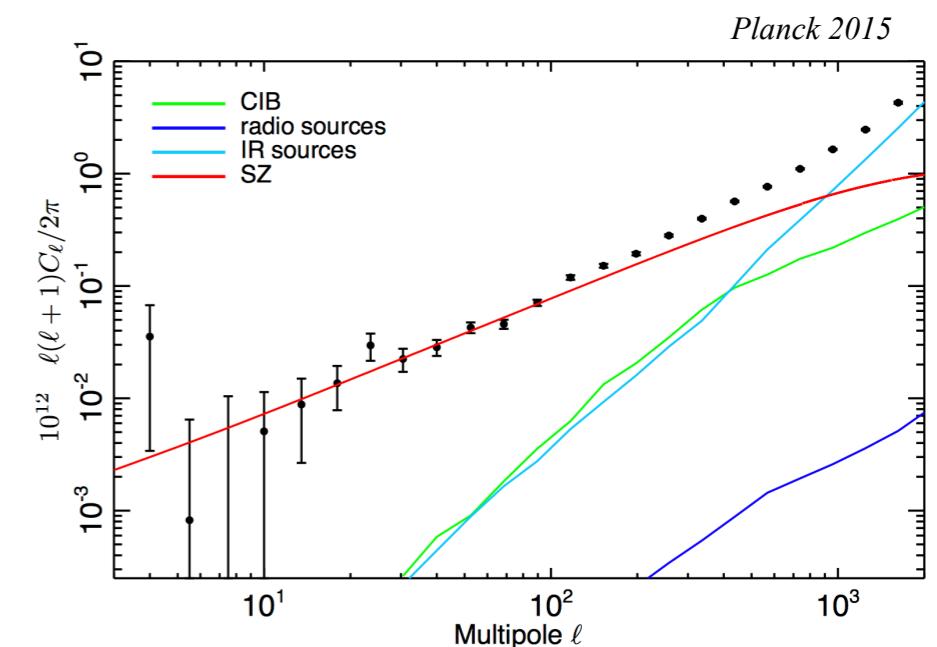
- Analog to CMB temperature anisotropy power spectrum from CMB map

Planck “y-map”

Map of the thermal Sunyaev Zeldovich effect

$$y = \frac{\sigma_T}{m_e c^2} \int P ds$$

- Requires **component separation**

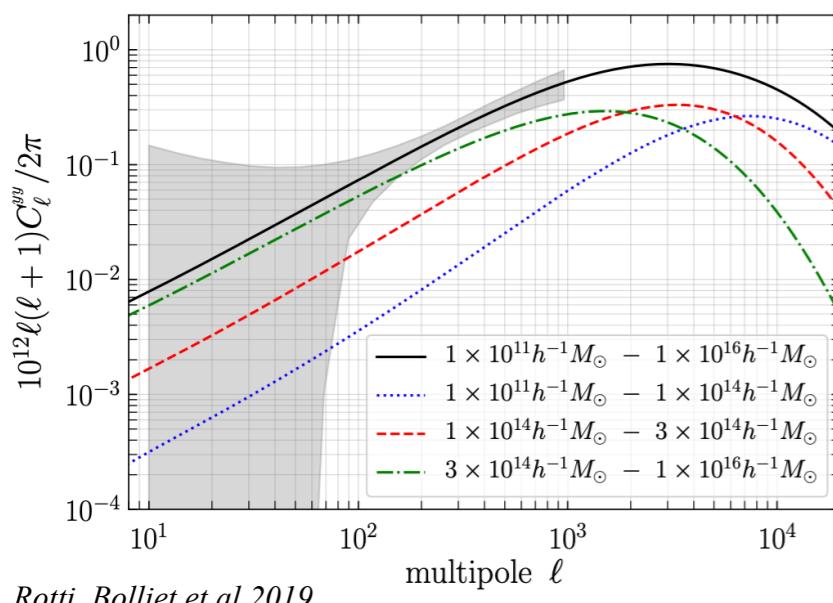


- **tSZ power spectrum from y-map**
- ACT y-map in the making

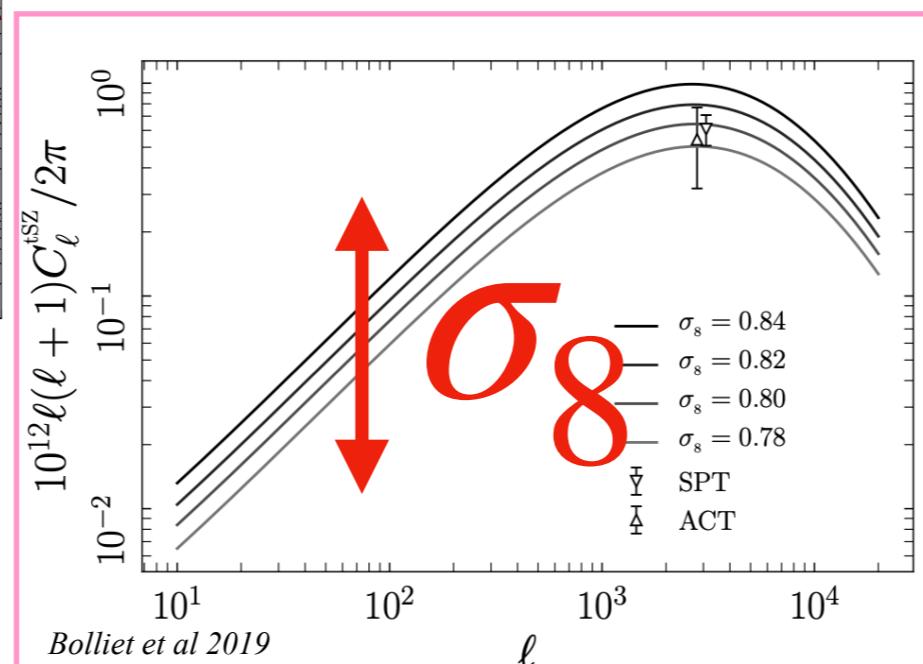
- tSZ power spectrum formula

$$C_\ell^{\text{tSZ}} = \int_{z_{\min}}^{z_{\max}} dz \frac{dV}{dz d\Omega} \int_{\ln M_{\min}}^{\ln M_{\max}} d \ln M \frac{dn}{d \ln M} |y_\ell(M, z)|^2$$

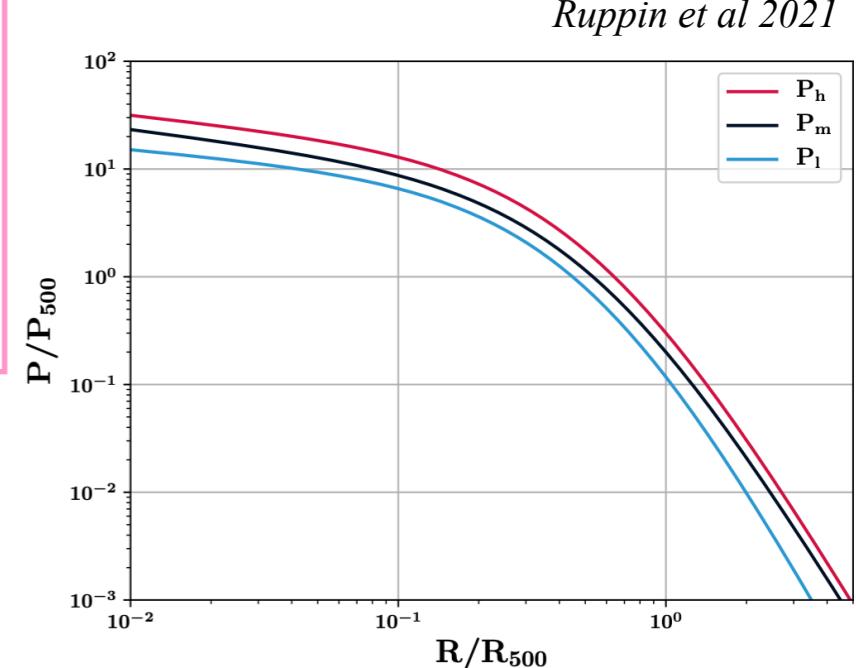
Komatsu & Kitayama 1999, Komatsu & Seljak 2002



Rotti, Bolliet et al 2019



Bolliet et al 2019

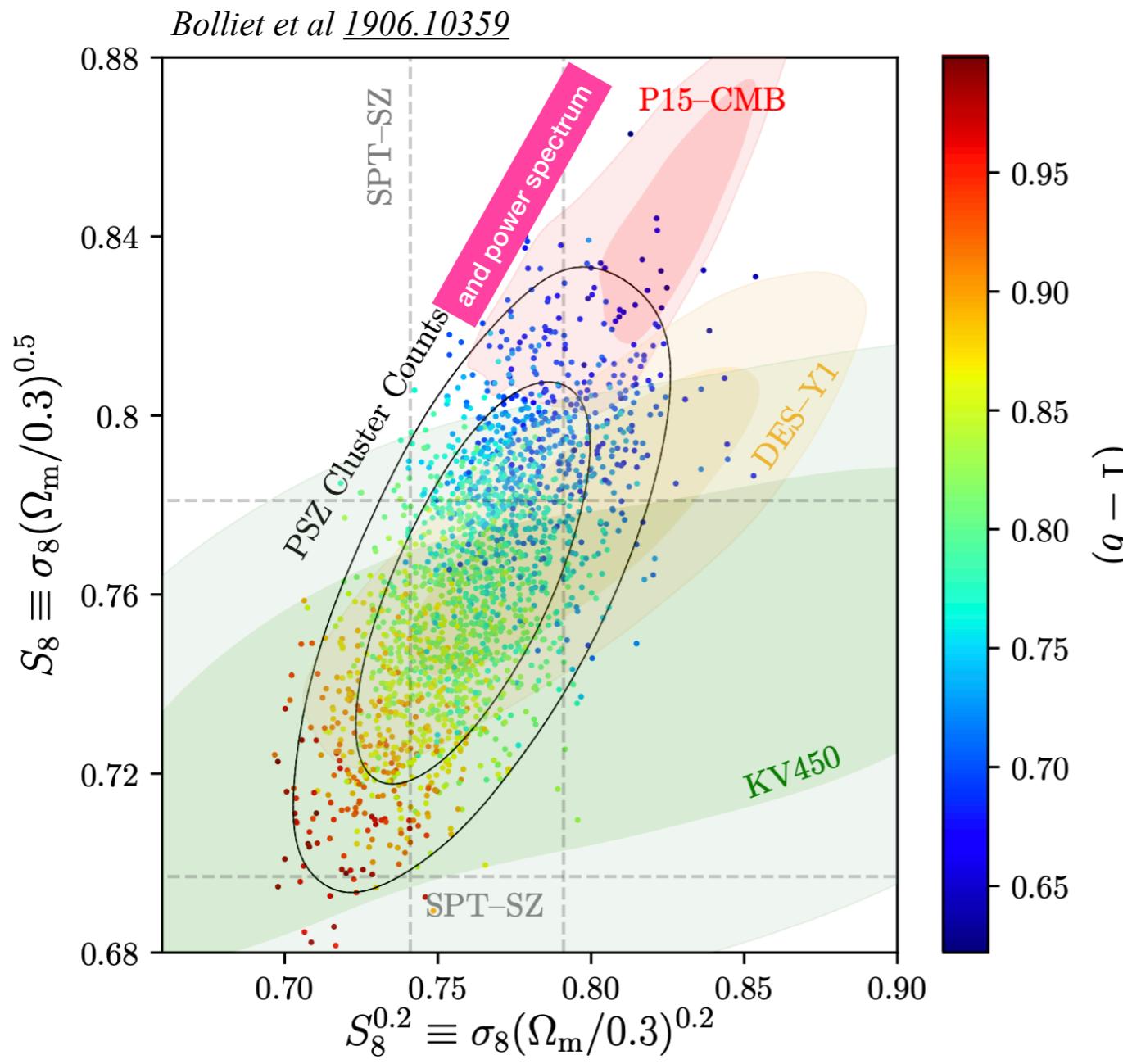


Ruppin et al 2021

- Sensitive probe of cosmology

- Expect important input from **NIKA2** data.... And **upcoming ACT data!**

- Agreement between Planck tSZ power spectrum and cluster counts, and SPT constraints (cluster counts)
- Consistent with weak-lensing/clustering constraints (KIDS/DES/HSC)
- 2-3 σ lower than CMB



KV450 from Hildebrandt et al 1812.06076 (shear)
DES Y1 from 1810.02499 (3x2pt)
SPT SZ from bocquet et al 1812.01679

Reconcile CMB and SZ?

1. Large feedback/Non thermal pressure...
(i.e., change normalization of Mass-Observable relation)
2. $\Sigma m_\nu \approx 0.3 \text{ eV}$
(i.e., lower $P(k)$ at high- k)
see Bolliet, Salvati, McCarthy, SPT
3. Systematics in X-ray temperature calibration
(i.e., change normalization of Mass-Observable relation)
4. Systematics in pressure profile/HMF calibration
see Ruppin et al 2021, Artis et al 2021

SZ cosmology will be robust when astrophysics degeneracy (baryons) is solved

HOW?

1. Where do the SZ **cosmological constraints** come from?

- tSZ cluster counts**
- tSZ power spectrum**
- tSZ cross-correlations

kSZ tomography

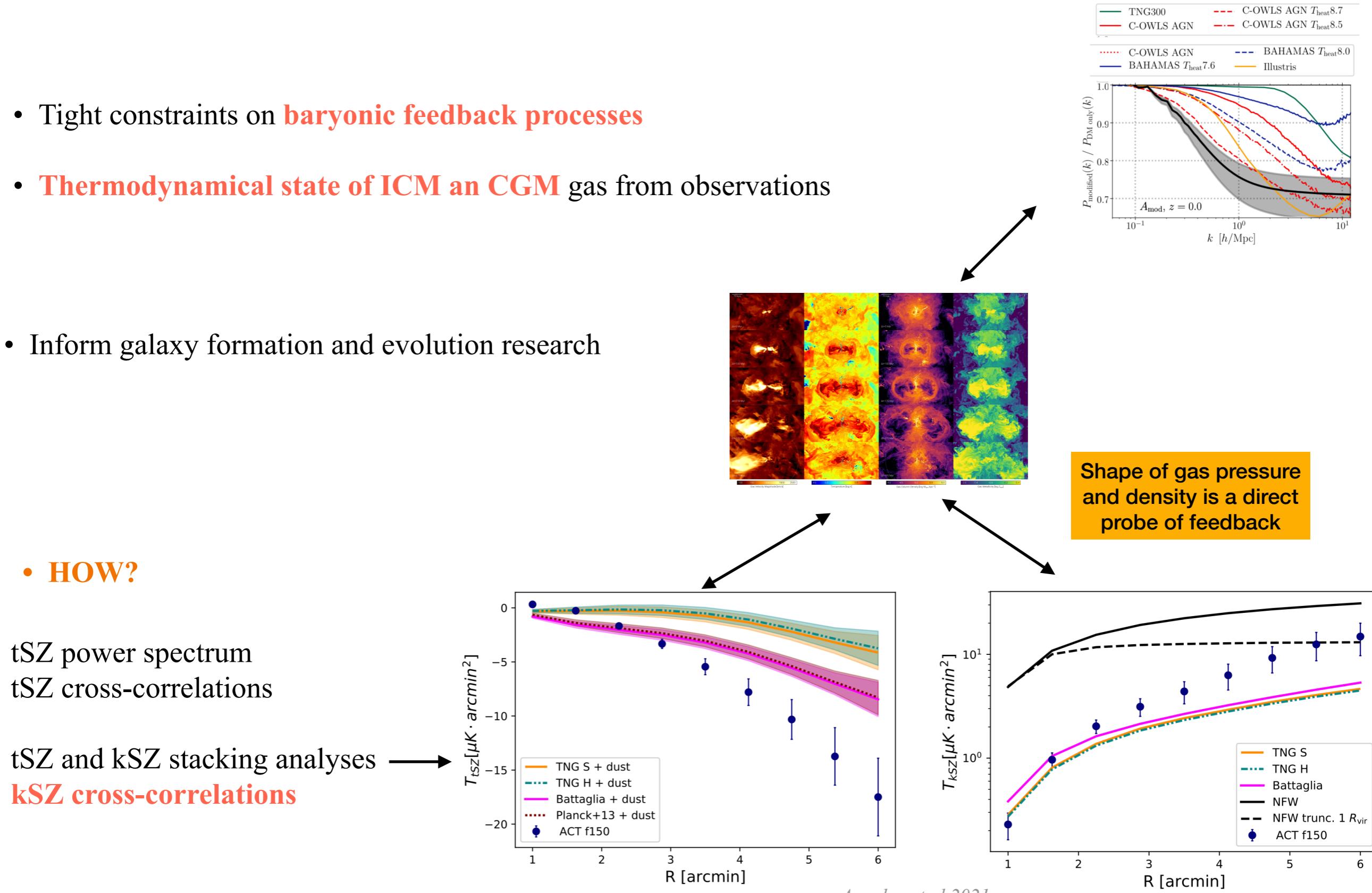
2. How do we measure **baryons** with SZ?

- tSZ power spectrum
- tSZ cross-correlations

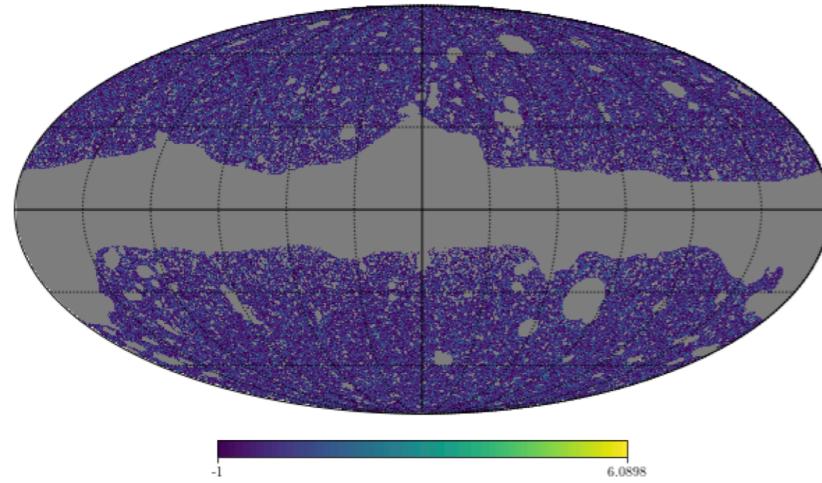
tSZ and kSZ stacking analyses

kSZ cross-correlations

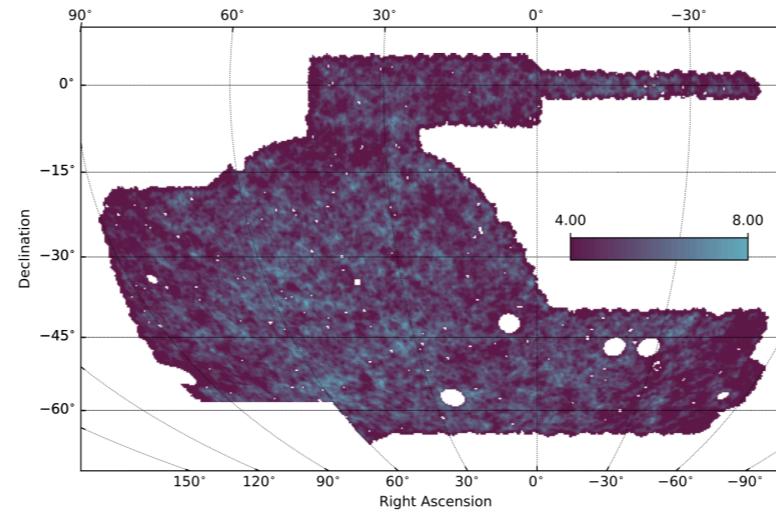
- Crucial for precision cosmology, to assert robustness of constraints from weak lensing and SZ



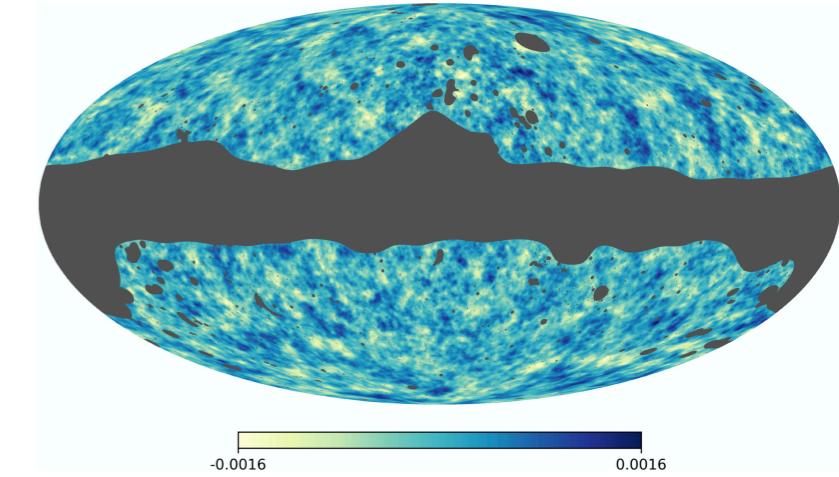
- Can probe gas in clusters/groups relevant to each **large scale structure tracer experiment**



$$\delta_g$$



$$\kappa_g$$



$$\kappa_{\text{cmb}}$$

Current: unWISE, CMASS

DES

Planck, ACT

Future: Rubin, Euclid

Rubin, Euclid

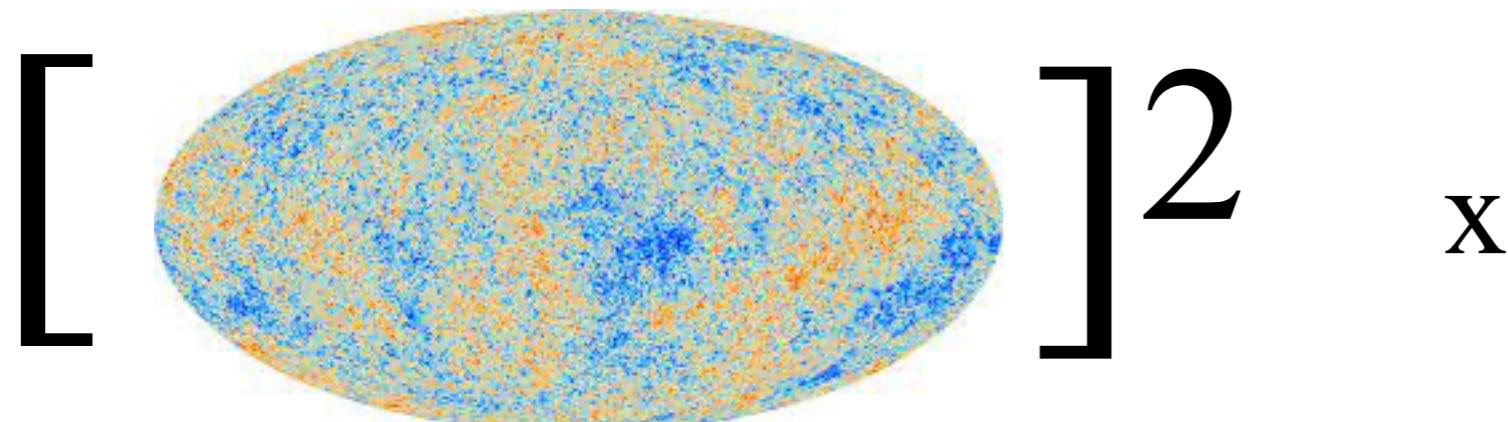
AdvACT, SO, S4

- Possible with **photometric surveys** (other kSZ methods often require spectroscopic redshifts)
- Ingredients: **foreground cleaned CMB map**, projected **map of LSS tracers**

$$\frac{\delta T_{\text{kSZ}}}{T_0}(\hat{\mathbf{r}}) = - \int dl \sigma_T n_e \frac{\mathbf{v} \cdot \hat{\mathbf{r}}}{c}$$

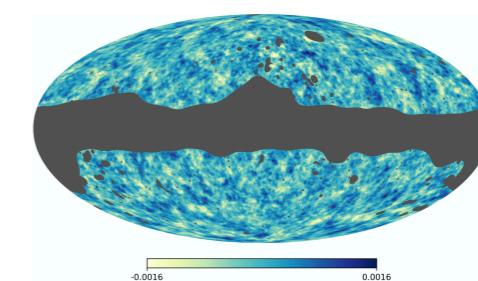
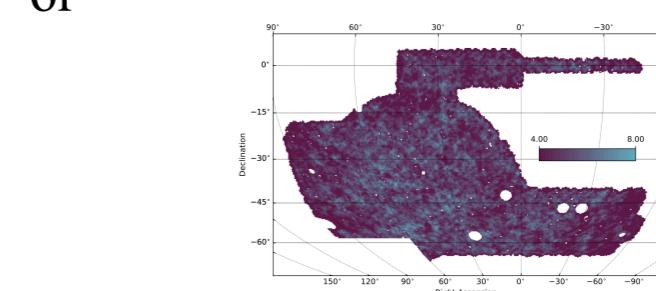
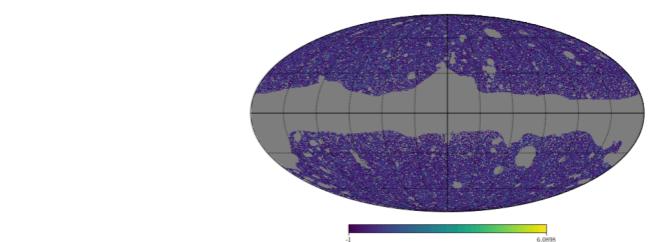
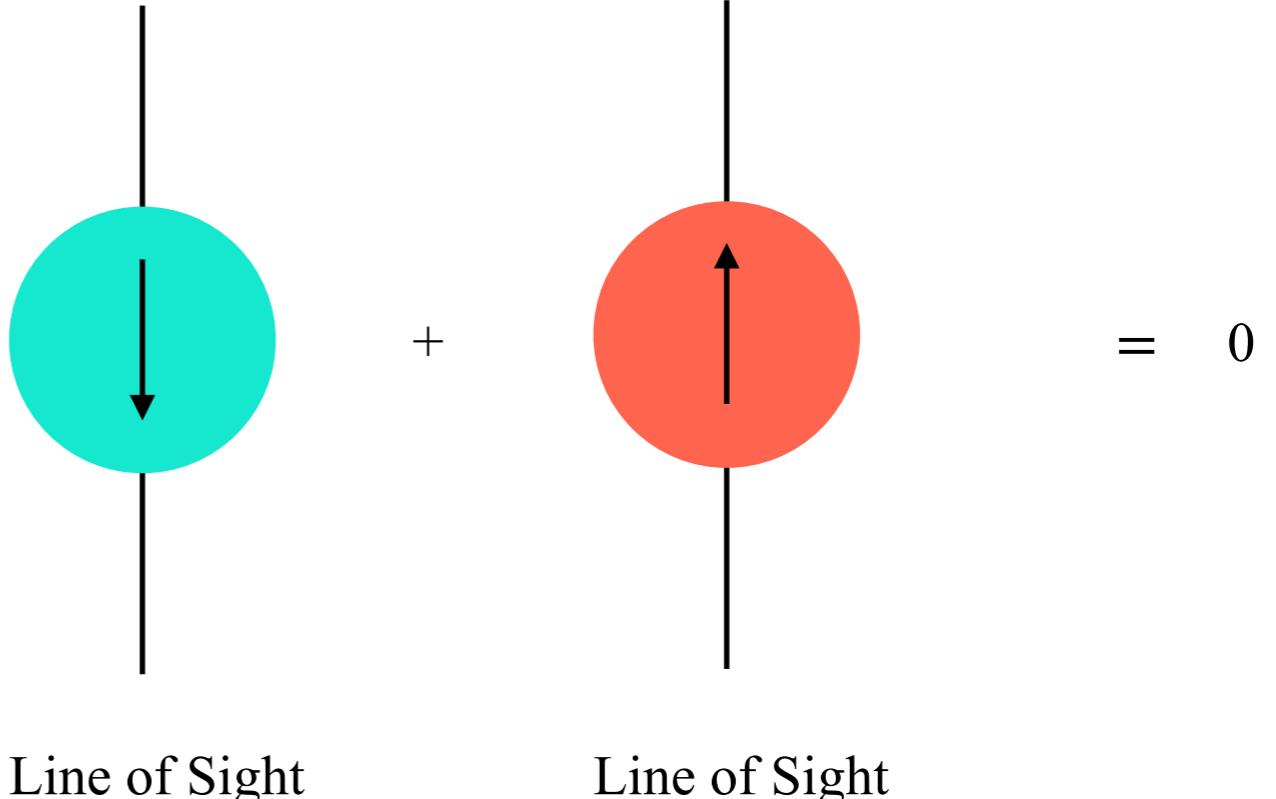
goal to measure gas density

- Avoid velocity cancellation by **squaring CMB map**

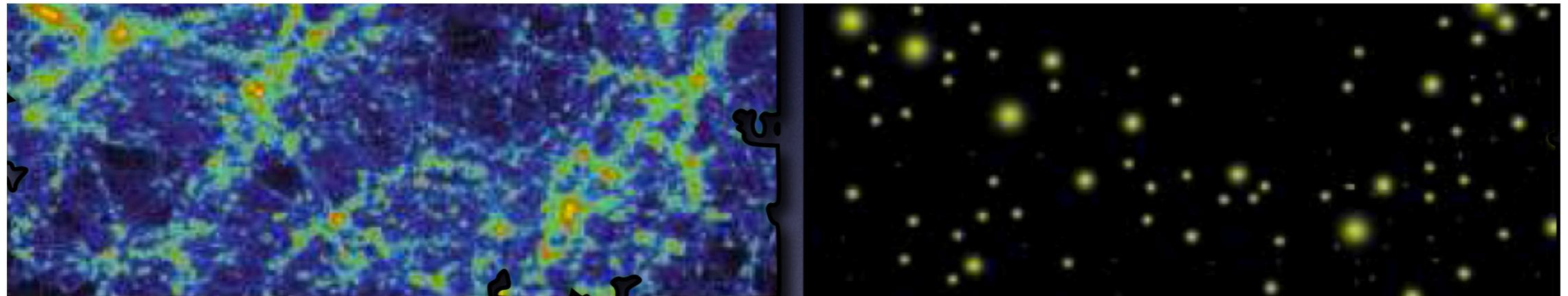


- Model?

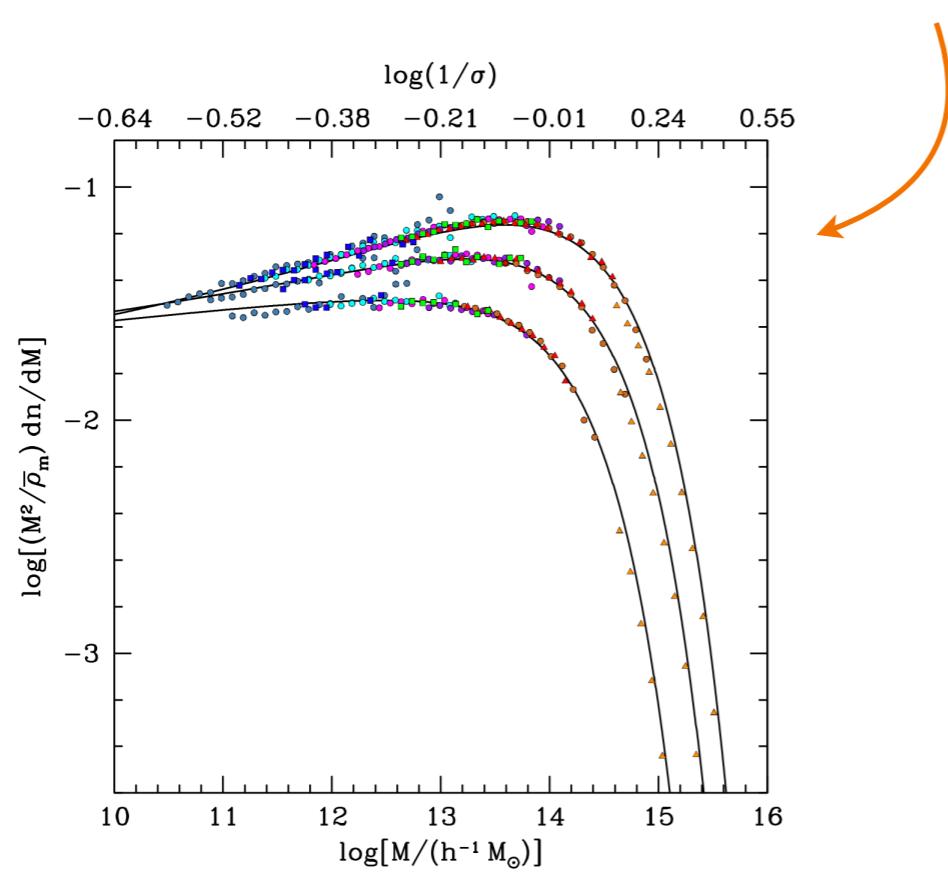
See Bolliet, Hill, Ferraro, Kusiak, Krolewski 2022



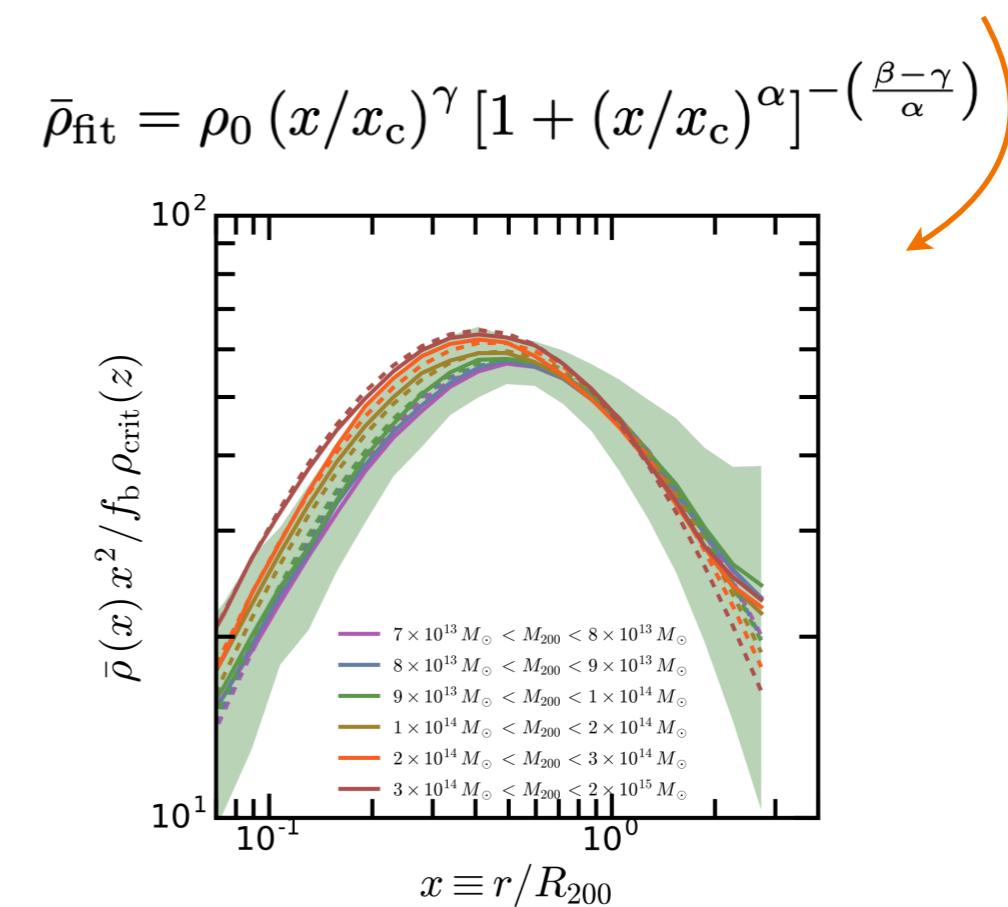
- Develop theoretical framework to accommodate parameterized density profiles: **Halo Model**



Main theory ingredients: **halo mass function** and **radial distribution of tracers within halos**

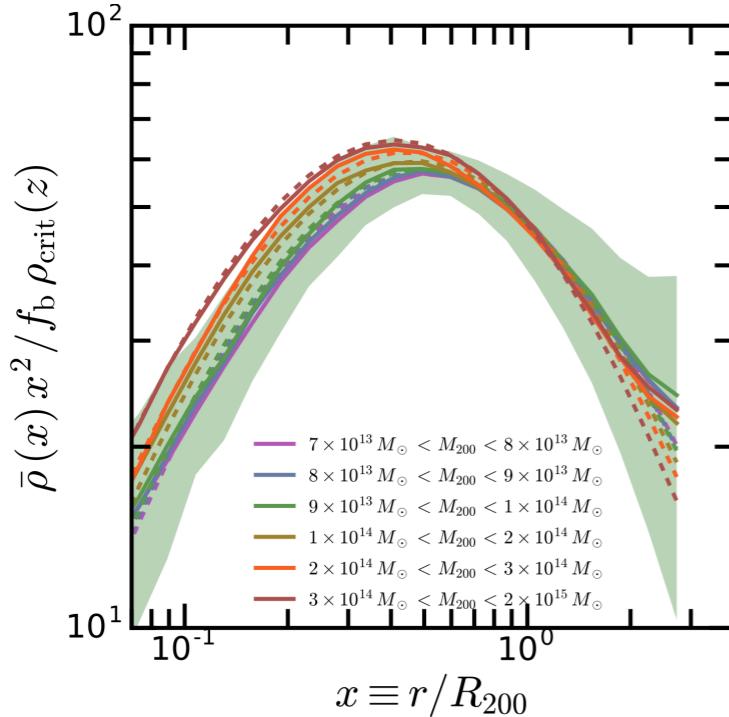


Tinker et al 2008
halo mass function



Battaglia et al 2010
density profile

$$\bar{\rho}_{\text{fit}} = \rho_0 (x/x_c)^\gamma [1 + (x/x_c)^\alpha]^{-\left(\frac{\beta-\gamma}{\alpha}\right)}$$



Battaglia et al 2010
density profile

*Density profile of the **gas***

We employ the **GNFW parameterization**, with slopes having a mass and redshift dependence.

(Dark matter profile is always assumed to follow NFW)

$$\rho_{\text{gas}}(r) = f_b \rho_{\text{crit}}(z) u_{\text{gas}}^{\text{gNFW}}(r) \quad \text{with} \quad u_{\text{gas}}^{\text{gNFW}}(r) = C \left(\frac{r}{x_c r_{200c}} \right)^\gamma \left[1 + \left(\frac{r}{x_c r_{200c}} \right)^\alpha \right]^{-\frac{\beta+\gamma}{\alpha}} \quad (26)$$

where we adopt a mass definition at $\Delta = 200$, keep the inner slope parameter fixed to $\gamma = -0.2$ and use $x_c = 0.5$ as in Battaglia (2016). The functions $\{C, \alpha, \beta, \gamma\}$ are fitted to hydrodynamical simulations and written as

$$p = A_0 \left(\frac{m_{200c}}{10^{14} M_\odot} \right)^{A_m} (1+z)^{A_z} \quad \text{for} \quad p \in \{C, \alpha, \beta, \gamma\}. \quad (27)$$

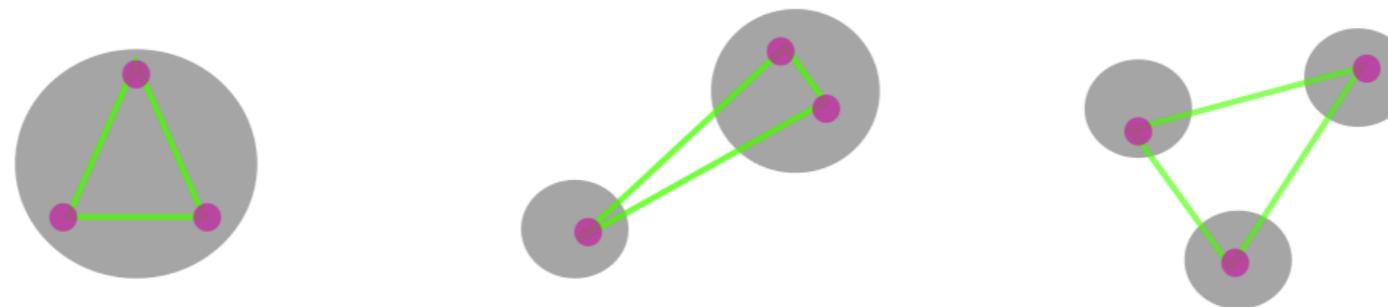
- The projected-field kSZ power spectrum is an integral/convolution of the kSZ² × LSS **bispectrum**

$$C_\ell^{\text{kSZ}^2 X} = \int d\chi W^{\text{kSZ}}(\chi)^2 W^X(\chi) T(\ell, \chi) \quad \text{with} \quad T(\ell, \chi) = \int \frac{d^2 \ell'}{(2\pi)^2} f(\ell') f(|\ell + \ell'|) B_{v_g^2 X}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3)$$

Redshift kernel of kSZ and X

Wiener filter
(data analysis trick
to maximize SNR)

- Halo model **bispectrum** expression

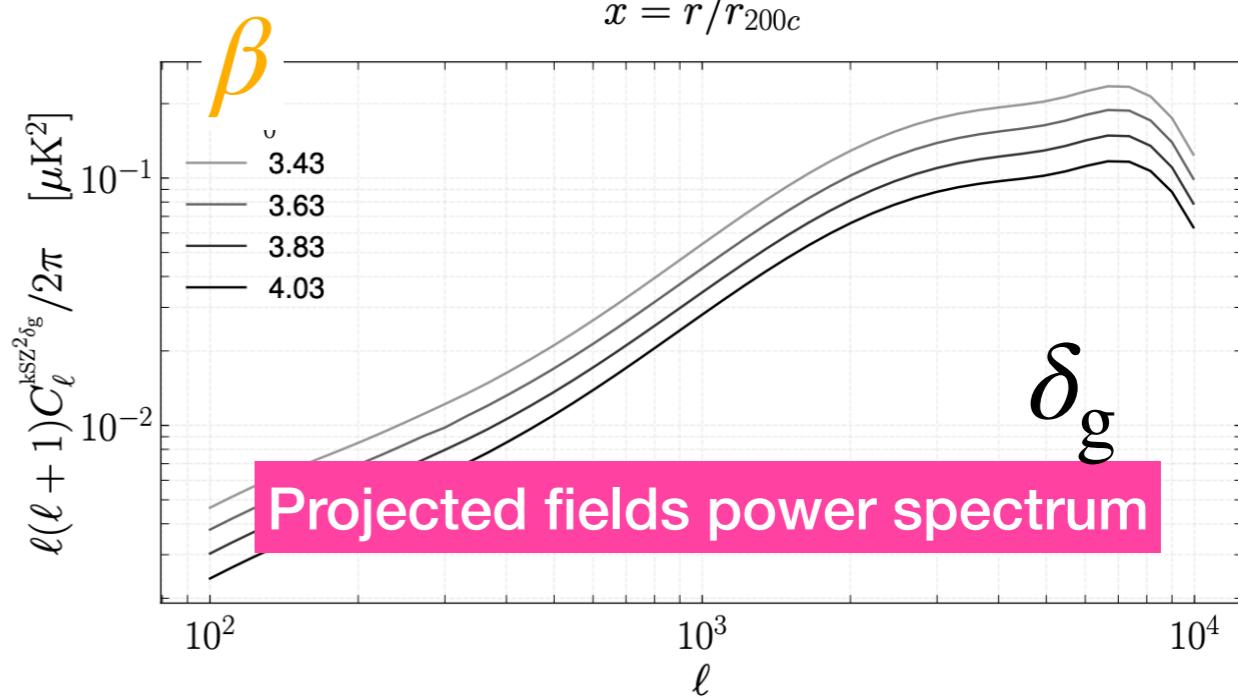
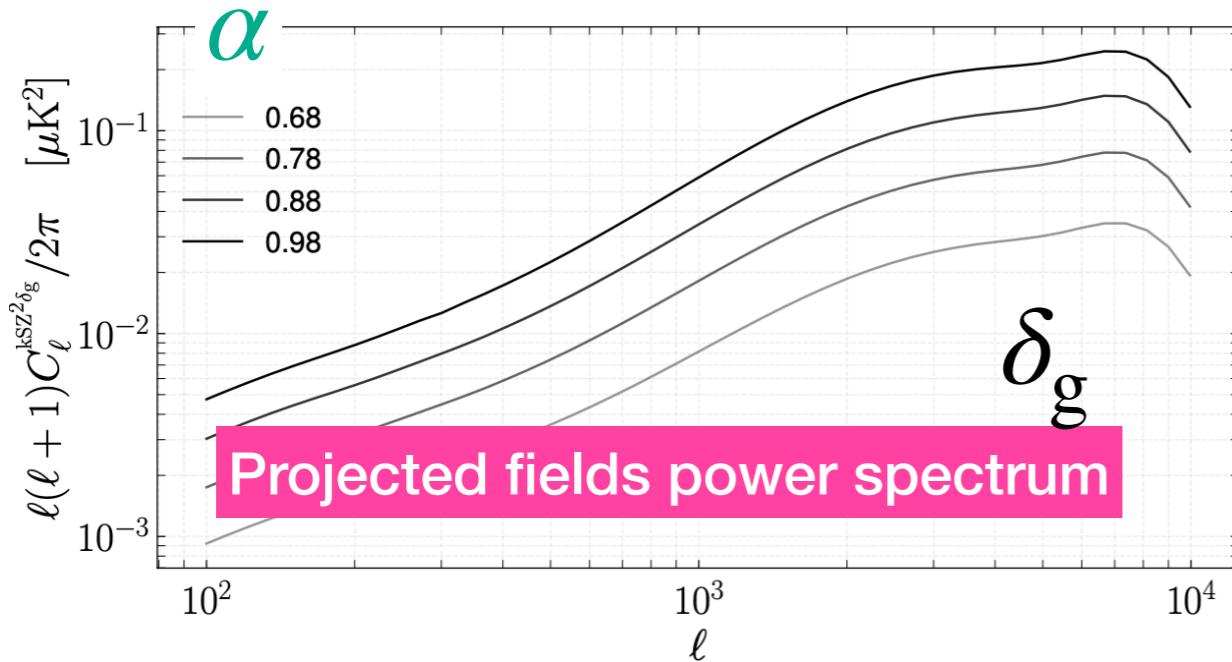
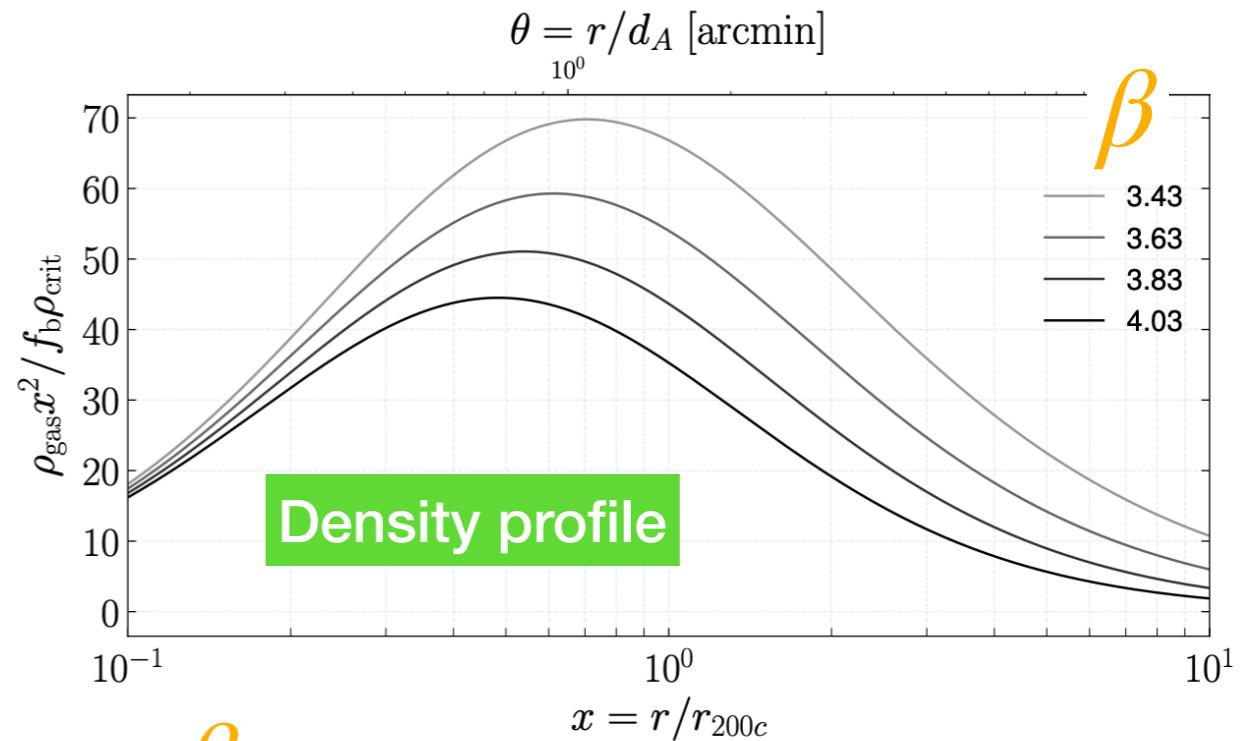
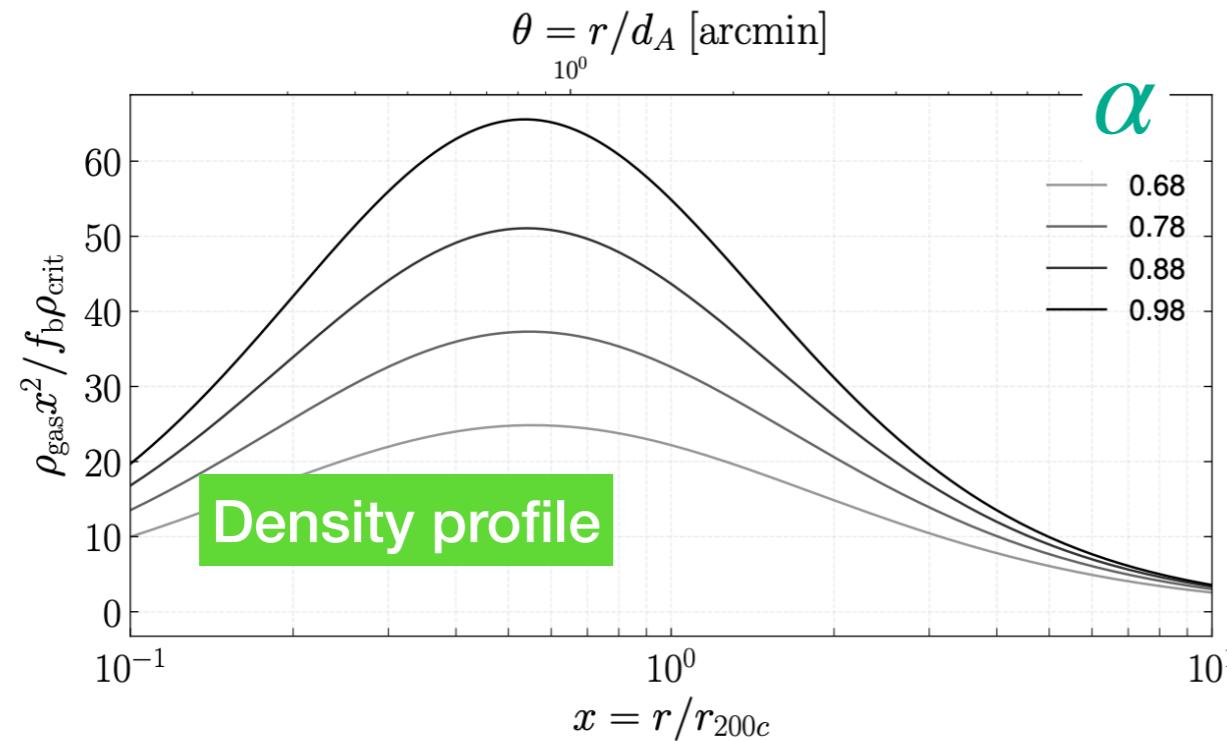


$$B^{1h} = \int dn_1 \hat{u}_{k_1}^X(m_1) \hat{u}_{k_2}^Y(m_1) \hat{u}_{k_3}^Z(m_1)$$

$$B^{2h} = \int dn_1 \hat{u}_{k_1}^X(m_1) \hat{u}_{k_2}^Y(m_1) \int dn_2 \hat{u}_{k_3}^Z(m_2) P_L(k_3) + 2\text{cyc}$$

$$\begin{aligned} B^{3h} = & 2 \int dn_1 b^{(1)}(m_1) \hat{u}_{k_1}^X(m_1) P_L(k_1) \int dn_2 b^{(1)}(m_2) \hat{u}_{k_2}^Y(m_2) P_L(k_2) \int dn_3 b^{(1)}(m_3) \hat{u}_{k_3}^Z(m_3) F_2(k_1, k_2, k_3) \\ & + \int dn_1 b^{(1)}(m_1) \hat{u}_{k_1}^X(m_1) P_L(k_1) \int dn_2 b^{(1)}(m_2) \hat{u}_{k_2}^Y(m_2) P_L(k_2) \int dn_3 b^{(2)}(m_3) \hat{u}_{k_3}^Z(m_3) + 2\text{cyc} \end{aligned}$$

*Separable expression+convolution:
can use FFTs (thanks Mat M.!)*

Changing the **slopes** of the gas **density profile**

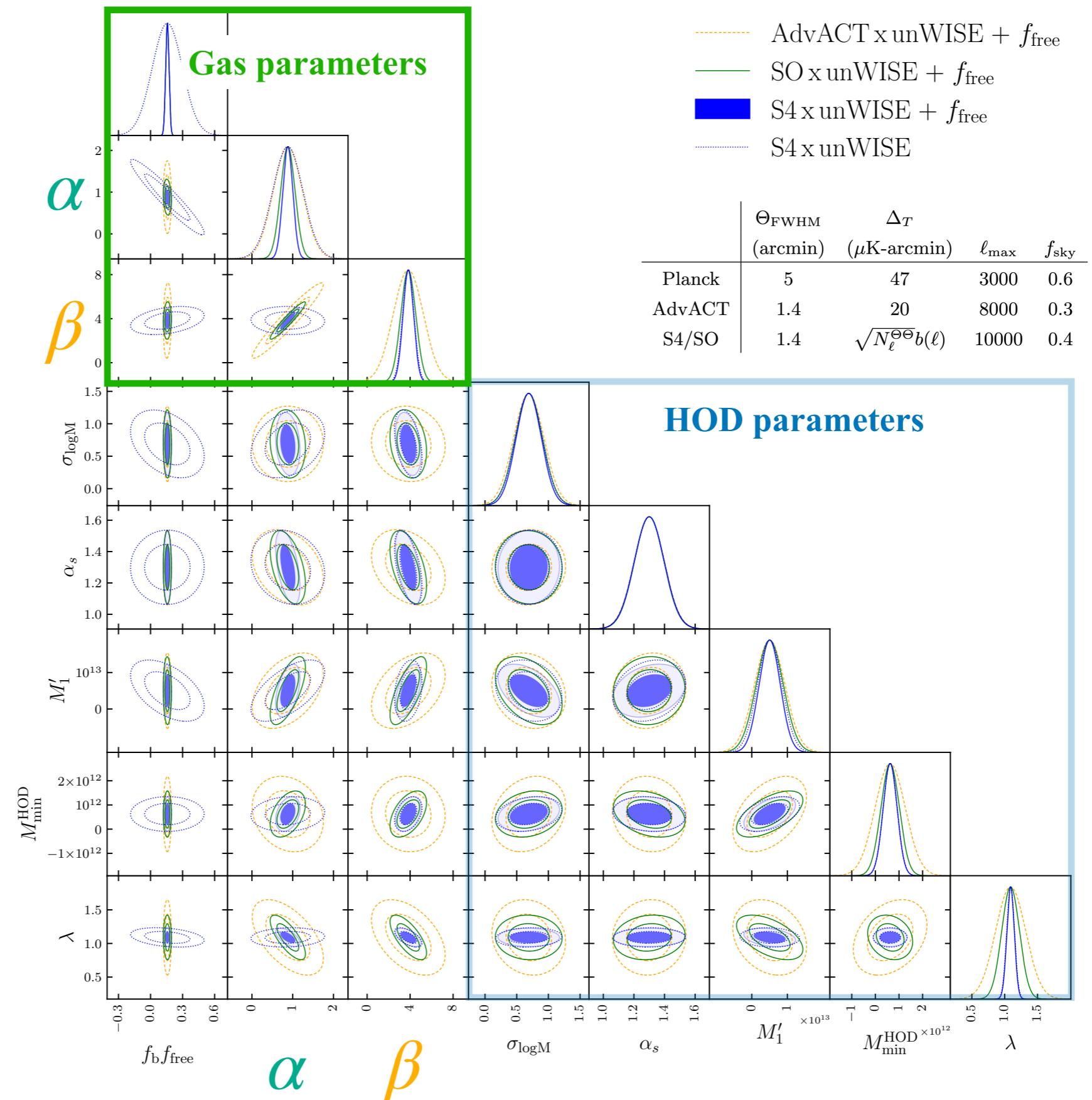
- Goal is to measure these parameters
- Fast and accurate **numerical code**
(used as a reference by DESC/CCL for CIB and SZ)

- Fisher matrix calculations

$$C_{\ell}^{kSZ^2 \delta_g}$$

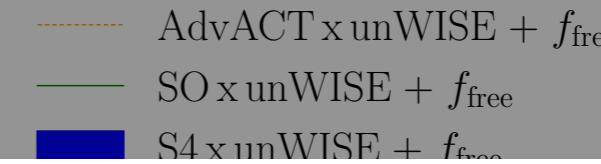
Typical halo mass

$$1 - 5 \times 10^{13} M_{\text{sun}}/h$$



- Fisher matrix calculations

Gas parameters



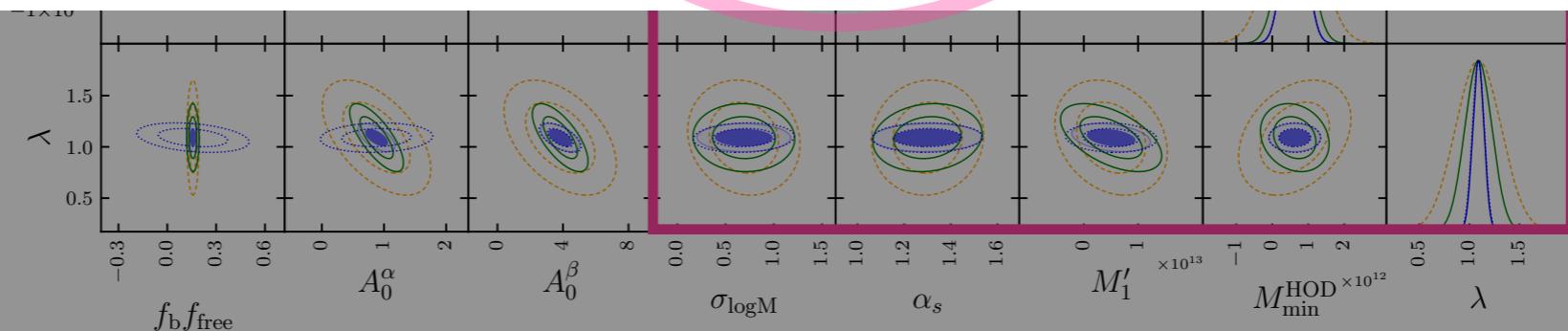
	SNR_{tot}	$(\frac{\Delta A_0^\beta}{A_0^\beta})^{-1}$	$(\frac{\Delta A_0^\alpha}{A_0^\alpha})^{-1}$	$(\frac{\Delta f_{\text{free}}}{f_{\text{free}}})^{-1}$	
δ_g	<i>Planck</i> \times <i>unWISE</i>	1.7	0.18 (0.37)	0.29 (0.38)	0.19 (10)
	AdvACT \times <i>unWISE</i> ...	17.8	1.72 (2.87)	2.22 (2.54)	0.71 (10)
	SO \times <i>unWISE</i>	61.9	3.70 (5.51)	2.07 (4.98)	0.78 (10)
	CMB-S4 \times <i>unWISE</i>	102.9	7.32 (7.83)	2.38 (7.18)	1.12 (10)
κ_g	AdvACT \times DES	2.24	0.28 (0.79)	0.59 (0.88)	0.09 (10)
	AdvACT \times VRO/ <i>Euclid</i>	5.98	0.92 (2.11)	1.72 (2.44)	0.31 (10)
	SO \times DES	6.14	1.03 (2.75)	0.93 (2.34)	0.23 (10)
	SO \times VRO/ <i>Euclid</i>	18.81	3.89 (6.84)	3.24 (8.22)	0.88 (10)
	CMB-S4 \times DES	9.71	2.19 (4.36)	1.33 (5.23)	0.40 (10)
	CMB-S4 \times VRO/ <i>Euclid</i>	29.72	8.57 (13.07)	4.71 (15.08)	1.51 (10)
κ_{cmb}	SO	16.39	0.92 (2.84)	1.72 (2.72)	0.94 (10)
	CMB-S4	34.52	2.76 (7.01)	5.75 (7.79)	2.4 (10)

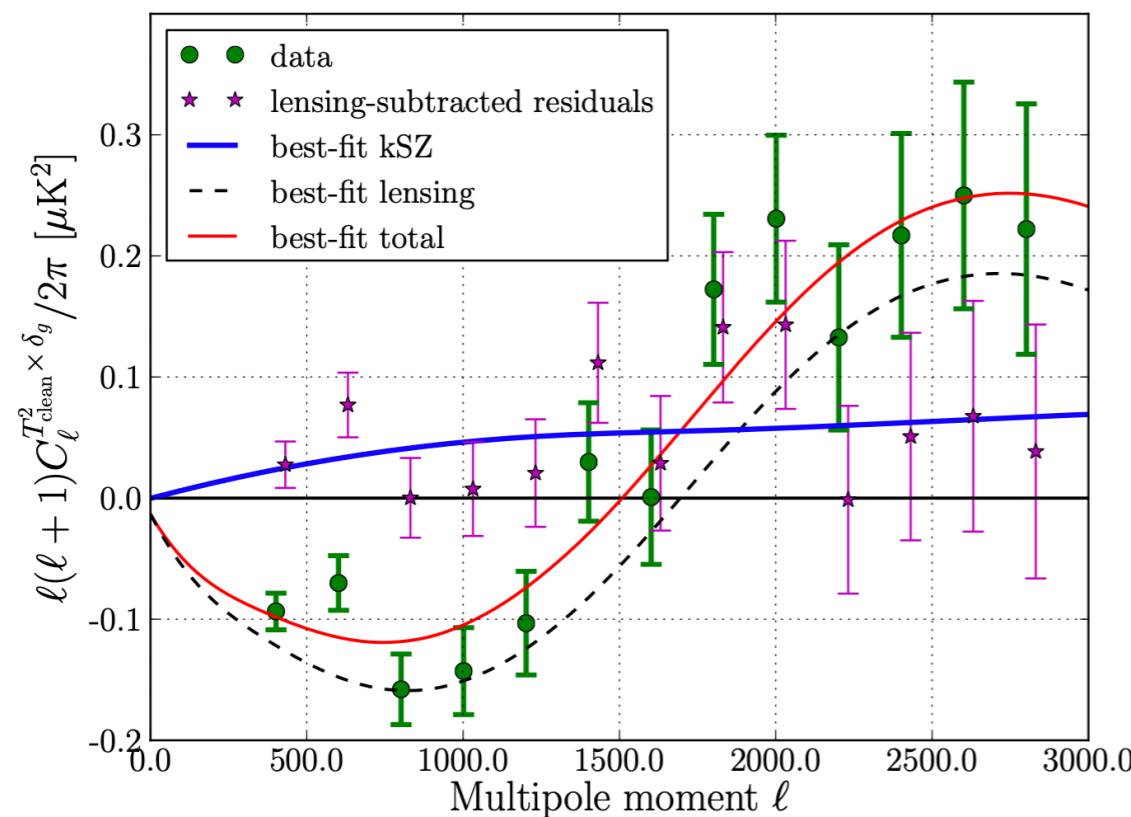
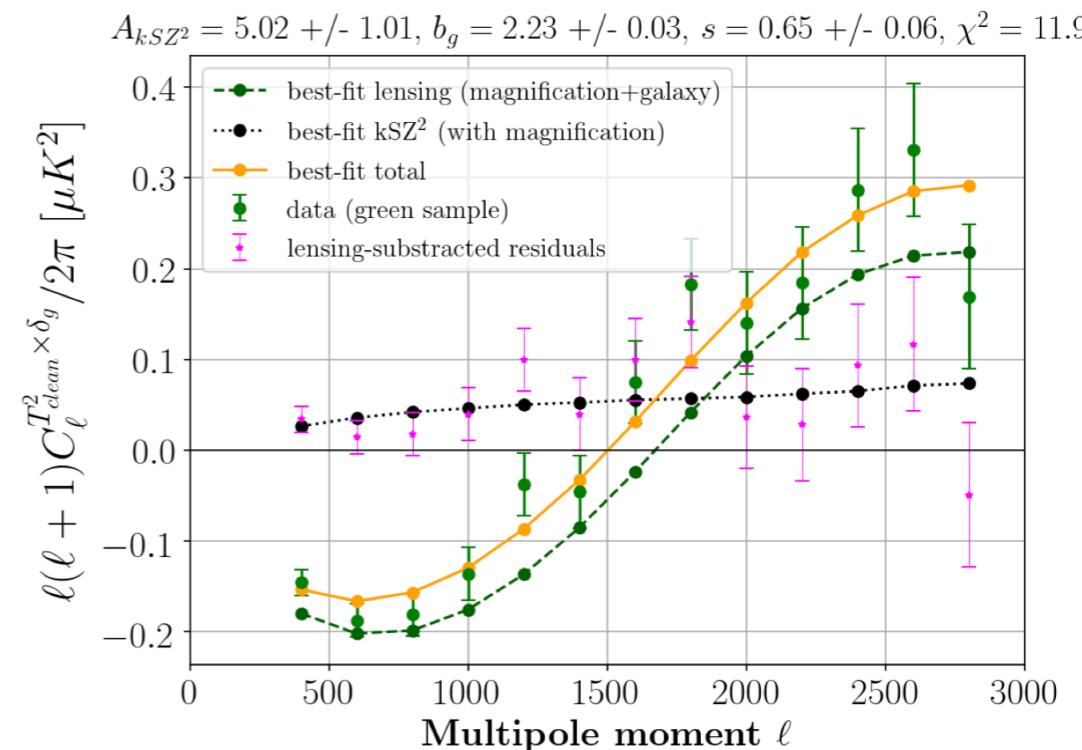
→ **Data available**

→ **Gas profile**

→ **First detection**

→ **First detection**



 δ_g  δ_g

First Detections of projected fields kSZ

$4 - 5 \sigma$

Hill, Ferraro, Battaglia, Liu, Spergel 2016
Planck WISE

Kusiak, Bolliet, Ferraro, Hill, Krolewski 2021
Planck unWISE

- First detections **very recent**, only able to detect the signal... not sensitive to radial shape of the gas
- **Data already on hand** (ACT) should allow **first detections** of **kSZ-galaxy lensing cross-correlations**
- **Shape of the gas** will be measured with next generation CMB maps: SO and S4, providing **cutting-edge baryonic feedback constraints**, enabling calibration of baryonic effects in precision cosmology

WHAT?

Inverse Compton-scattering (thermal) and Doppler shift (kinetic) probes pressure and momentum of the gas around galaxies.

WHY?

We need measurements of ICM/CGM gas thermodynamical state to reduce uncertainty in precision cosmology, also to learn about galaxy formation and evolution.

With ACT, SO, S4 SZ is the way to go.

HOW?

For cosmology:
Cluster counts, tSZ power spectrum, kSZ tomography.

For baryons:
Cross-correlations. Stacking. Projected-field kSZ power spectrum.

The “how” is **fully dependent on synergies with LSS surveys**, like Rubin and Euclid.

Thanksz !