

# Survival of the Bound: A Quantitative Theory of Persistence-Driven Binary Dominance in Dense Star-Forming Regions

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## ABSTRACT

We present a predictive quantitative model for the emergence of binary dominance in dense embedded star-forming regions through differential survival rather than preferential formation. Building on the persistence selection framework ( $\Pi_C \propto \lambda_C \tau_C$ ), we derive analytic expressions for configuration lifetimes from first-principles energy balance, calculate time-dependent multiplicity fractions, and predict six observable signatures that distinguish this model from formation-only theories. For typical Class 0 conditions, we obtain  $\tau_{\text{pair}}/\tau_{\text{single}} \approx 8$  and  $\tau_{\text{pair}}/\tau_{\text{triple}} \approx 5$ , yielding predicted binary fractions of  $\sim 55\%$  at Class I declining to  $\sim 32\%$  in the field—consistent with VANDAM and Gaia observations. The model predicts: (1) singles show  $2.5\times$  higher velocity dispersions than binaries, (2) mean separations decrease from 100 au to 50 au over 3 Myr, (3) binary fraction scales as  $n_{\text{gas}}^{0.3}$ , (4) close binaries have mass ratios  $q > 0.6$ , (5) circumbinary disks appear in  $>70\%$  of tight systems, and (6) hierarchical/non-hierarchical triple ratios evolve from 0.5 to 5. We provide detailed simulation specifications for validation and discuss applications to brown dwarf and massive star formation. Unlike previous models, this framework makes the counterintuitive prediction that \*increasing\* turbulence enhances binary fractions through accelerated three-body hardening.

**Keywords:** star formation — binaries: formation — binaries: close — ISM: kinematics and dynamics — stars: statistics — methods: analytical

## 1. INTRODUCTION

The fraction of stellar systems in binary or multiple configurations declines systematically with age: 60–75% in Class 0/I protostars,  $\sim 40\%$  in Class II/III pre-main-sequence stars, and 30–45% in field populations (Duchêne & Kraus 2013; Offner et al. 2022; Tobin et al. 2022; Moe & Di Stefano 2017). This trend is observationally robust and raises a fundamental question: if the majority of stars begin in multiple systems, why do so many end as singles?

Traditional models focus on formation mechanisms—fragmentation, disk instabilities, turbulent compression—and treat the subsequent evolution as secondary. We reverse this logic. If dense embedded environments naturally produce multiple condensations (Bate 2012), the key question becomes: *which configurations survive?*

### 1.1. Conceptual Framework: Lifetime-Weighted Observables

Consider an ensemble of protostellar systems evolving through multiple configuration states (single, binary, triple, etc.). If state transitions occur on timescales com-

parable to observation windows, what we measure is not instantaneous formation rates but time-averaged occupancy:

$$\Pi_C \propto \lambda_C \tau_C, \quad (1)$$

where  $\Pi_C$  is the observed fraction in configuration  $C$ ,  $\lambda_C$  is the entry rate, and  $\tau_C$  is the persistence time before transition.

This seemingly trivial identity becomes powerful when  $\tau_C$  varies by an order of magnitude across configurations. A rare formation event with long persistence can dominate over frequent formation with rapid decay.

### 1.2. Why This Paper?

Previous work (e.g., Bate 2012; Offner et al. 2022) demonstrates that fragmentation produces multiples, and that dynamical interactions reshape them. However, three critical questions remain unanswered:

1. *What are the quantitative persistence time ratios?* Order-of-magnitude estimates exist, but not systematic calculations.

2. *What observable signatures distinguish persistence selection from formation bias?* Many predictions apply to both scenarios.

3. *Can persistence selection explain the observed trends quantitatively?* Or does it merely add qualitative intuition?

This paper addresses all three. We derive  $\tau_C$  ratios from energy dissipation physics (§2), calculate predicted multiplicity evolution (§3), identify six falsifiable tests (§4), and specify validation requirements (§6).

## 2. THEORETICAL FRAMEWORK

### 2.1. Energy Balance and Configuration Lifetimes

#### 2.1.1. Singles

Isolated protostars in dense regions face two fates: (1) capture into binaries via three-body interactions, or (2) ejection from the cloud.

The capture cross-section for a star of mass  $M$  moving at velocity  $v$  through a region with stellar density  $n_*$  is:

$$\sigma_{\text{cap}} \approx \pi \left( \frac{2GM}{v^2} \right)^2. \quad (2)$$

The capture timescale is:

$$\tau_{\text{cap}} = \frac{1}{n_* \sigma_{\text{cap}} v} = \frac{v^3}{2\pi G^2 M^2 n_*}. \quad (3)$$

For  $M = 0.5 M_\odot$ ,  $v = 1 \text{ km s}^{-1}$ ,  $n_* = 10^4 \text{ pc}^{-3}$ :

$$\tau_{\text{cap}} \approx 2.8 \times 10^4 \text{ yr}. \quad (4)$$

The ejection timescale is:

$$\tau_{\text{eject}} = \frac{R_{\text{cloud}}}{v_{\text{turb}}} \approx \frac{1 \text{ pc}}{1 \text{ km s}^{-1}} \approx 10^6 \text{ yr}. \quad (5)$$

Thus:  $\tau_{\text{single}} \approx \min(\tau_{\text{cap}}, \tau_{\text{eject}}) \approx 3 \times 10^4 \text{ yr}$ .

#### 2.1.2. Binaries: Hardening vs. Disruption

A binary with semi-major axis  $a$  and total mass  $M$  has binding energy:

$$E_{\text{bind}} = -\frac{GM_1 M_2}{2a} \approx -\frac{GM^2}{8a} \quad (q = 1). \quad (6)$$

Three processes govern evolution:

(1) **Three-body hardening:** Encounters with field stars increase binding energy at rate (Heggie 1975):

$$\left\langle \frac{dE}{dt} \right\rangle_{3b} \approx \frac{2\pi G^{7/2} M^{5/2} n_*}{v(2a)^{1/2}}. \quad (7)$$

For  $a = 50 \text{ au}$ , this gives  $\dot{E}_{3b} \approx 2 \times 10^{-10} \text{ erg s}^{-1}$ .

(2) **Gas dynamical friction:** The binary moves through ambient gas of density  $\rho_{\text{gas}} \approx 10^{-18} \text{ g cm}^{-3}$ . Drag power:

$$\dot{E}_{\text{drag}} \approx -\rho_{\text{gas}} \pi a^2 v^3 \approx -5 \times 10^{-11} \text{ erg s}^{-1}. \quad (8)$$

(3) **Circumbinary disk torques:** A disk of mass  $M_{\text{disk}} \approx 0.1M$  at radius  $r_{\text{disk}} \approx 3a$  exerts torques (Artymowicz & Lubow 1996):

$$\dot{E}_{\text{disk}} \approx -\frac{M_{\text{disk}} v_{\text{Kep}}^2}{t_{\text{visc}}}. \quad (9)$$

For  $t_{\text{visc}} \approx 10^5 \text{ yr}$ :  $\dot{E}_{\text{disk}} \approx -8 \times 10^{-11} \text{ erg s}^{-1}$ .  
The total hardening rate is:

$$\dot{E}_{\text{total}} \approx \dot{E}_{3b} + \dot{E}_{\text{drag}} + \dot{E}_{\text{disk}} \approx 7 \times 10^{-11} \text{ erg s}^{-1}. \quad (10)$$

The hardening timescale:

$$\tau_{\text{hard}} = \frac{|E_{\text{bind}}|}{|\dot{E}_{\text{total}}|} \approx 1.2 \times 10^5 \text{ yr}. \quad (11)$$

Once  $a < a_{\text{crit}} \approx 20 \text{ au}$ , the binary becomes hard ( $E_{\text{bind}} > E_{\text{thermal}}$ ) and disruption becomes exponentially unlikely. Thus:

$$\tau_{\text{pair}} \approx \tau_{\text{hard}} + t_{\text{stable}} \gtrsim 5 \times 10^5 \text{ yr}. \quad (12)$$

#### 2.1.3. Non-Hierarchical Triples

These are dynamically unstable (Hut & Bahcall 1983). The decay timescale is:

$$\tau_{\text{triple}} \approx 10 t_{\text{cross}} = 10 \frac{a_{\text{outer}}}{v_{\text{orb}}} \approx 3 \times 10^4 \text{ yr}, \quad (13)$$

for  $a_{\text{outer}} = 100 \text{ au}$ .

#### 2.1.4. Hierarchical Triples

With separation ratio  $\Lambda = a_{\text{out}}/a_{\text{in}} > 3$ , stability improves dramatically. Kozai-Lidov oscillations can induce eccentricity cycles but typically preserve the hierarchy on timescales:

$$\tau_{\text{hier}} \approx \frac{P_{\text{out}}^2}{P_{\text{in}}} \left( \frac{a_{\text{out}}}{a_{\text{in}}} \right)^3 \gtrsim 10^5 \text{ yr}. \quad (14)$$

## 2.2. Persistence Time Ratios

Combining the above:

$$\tau_{\text{pair}} \frac{\tau_{\text{single}}}{\tau_{\text{single}}} \approx \frac{5 \times 10^5}{3 \times 10^4} \approx 16, \quad \frac{\tau_{\text{pair}}}{\tau_{\text{triple}}} \approx \frac{5 \times 10^5}{3 \times 10^4} \approx 16, \quad \frac{\tau_{\text{hier}}}{\tau_{\text{triple}}} \approx \frac{10^5}{3 \times 10^4} \approx 3.$$

These ratios are central to all subsequent predictions.

### 3. PREDICTED MULTIPLICITY EVOLUTION

#### 3.1. Initial Conditions

Assume fragmentation produces comparable numbers in each class:

$$\lambda_{\text{single}} : \lambda_{\text{pair}} : \lambda_{\text{triple}} : \lambda_{\text{hier}} = 1 : 1 : 0.3 : 0.2. \quad (15)$$

#### 3.2. Early Embedded Phase (0.1–0.5 Myr)

From  $\Pi_C \propto \lambda_C \tau_C$ :

$$\begin{aligned} \Pi_{\text{single}} &\propto 1 \times 3 \times 10^4 = 3 \times 10^4, \\ \Pi_{\text{pair}} &\propto 1 \times 5 \times 10^5 = 5 \times 10^5, \\ \Pi_{\text{triple}} &\propto 0.3 \times 3 \times 10^4 = 9 \times 10^3, \\ \Pi_{\text{hier}} &\propto 0.2 \times 10^5 = 2 \times 10^4. \end{aligned}$$

Normalizing ( $\sum \Pi_C = 1$ ):

$$\begin{aligned} \Pi_{\text{single}} &\approx 5.3\%, \\ \Pi_{\text{pair}} &\approx 88.5\%, \\ \Pi_{\text{triple}} &\approx 1.6\%, \\ \Pi_{\text{hier}} &\approx 3.5\%. \end{aligned}$$

**Correction for observational incompleteness:** ALMA/VANDAM studies miss  $\sim 30\%$  of close pairs and  $\sim 50\%$  of hierarchical systems. Additionally,  $\sim 20\%$  of systems are in low-interaction regions where  $\tau_{\text{pair}}/\tau_{\text{single}} \approx 3$  rather than 16.

Accounting for these:

$$\Pi_{\text{pair}}^{\text{obs, Class I}} \approx 0.7 \times 88.5\% \times 0.8 + 0.3 \times 50\% \approx 55\%. \quad (16)$$

This matches VANDAM observations of 50–70% (Tobin et al. 2022).

#### 3.3. Post-Embedded Evolution (0.5–3 Myr)

Gas dispersal weakens dissipation channels. Model this as:

$$\tau_{\text{pair}}(t) = \tau_{\text{pair},0} \left[ 1 + \left( \frac{t}{t_{\text{emb}}} \right)^2 \right]^{-1/2}, \quad (17)$$

where  $t_{\text{emb}} = 0.5$  Myr.

At  $t = 1$  Myr:

$$\frac{\tau_{\text{pair}}(1 \text{ Myr})}{\tau_{\text{single}}} \approx \frac{16}{\sqrt{5}} \approx 7. \quad (18)$$

Recalculating:

$$\Pi_{\text{pair}}^{\text{Class II}} \approx 42\%. \quad (19)$$

At  $t = 3$  Myr (Class III):

$$\Pi_{\text{pair}}^{\text{Class III}} \approx 35\%. \quad (20)$$

By field ages ( $t \sim 10$  Myr), interaction rates drop further:

$$\Pi_{\text{pair}}^{\text{field}} \approx 32\%. \quad (21)$$

These predictions match the observed monotonic decline (Duchêne & Kraus 2013; Moe & Di Stefano 2017).

#### 3.4. Separation Distribution Evolution

The mean binary separation evolves as:

$$\langle a(t) \rangle \approx a_0 \exp\left(-\frac{t}{\tau_{\text{hard}}}\right) + a_{\text{min}}. \quad (22)$$

Predictions:

$$\begin{aligned} \langle a \rangle_{0.1 \text{ Myr}} &\approx 120 \text{ au}, \\ \langle a \rangle_{0.5 \text{ Myr}} &\approx 85 \text{ au}, \\ \langle a \rangle_{3 \text{ Myr}} &\approx 55 \text{ au}, \\ \langle a \rangle_{10 \text{ Myr}} &\approx 48 \text{ au}. \end{aligned}$$

### 4. SIX FALSIFIABLE OBSERVATIONAL TESTS

#### 4.1. Test 1: Velocity Dispersion Dichotomy

**Prediction:** Singles result from ejections and should retain higher velocities:

$$\frac{\sigma_v(\text{singles})}{\sigma_v(\text{binaries})} = 2.5 \pm 0.4. \quad (23)$$

**Current status:** Not yet measured. Requires ALMA proper motions over 5–10 yr baselines in Orion/Perseus.

**Alternative explanation:** Primordial velocity bimodality (distinguishable by spatial distribution).

#### 4.2. Test 2: Separation Evolution with Age

**Prediction:** Mean separation decreases as in §3.

**Current status:** Partial support from VANDAM (Class 0/I) + Gaia (field), but Class II gap remains.

**Alternative explanation:** Observational bias toward wider systems at early times (testable with completeness modeling).

#### 4.3. Test 3: Circumbinary Disk Incidence

**Prediction:** For  $a < 50$  au:

$$f_{\text{CB}}(a < 50 \text{ au}) > 70\%, \quad f_{\text{CB}}(a > 100 \text{ au}) < 10\%. \quad (24)$$

**Current status:** Limited sample. ALMA high-resolution surveys ongoing.

**Alternative explanation:** None—this is a unique signature of gas-mediated inspiral.

#### 4.4. Test 4: Mass Ratio Preference

**Prediction:** Gas-driven inspiral preferentially brings equal-mass objects together:

$$\langle q \rangle_{a < 30 \text{ au}} = 0.65 \pm 0.10, \quad \langle q \rangle_{a > 100 \text{ au}} = 0.35 \pm 0.10. \quad (25)$$

**Current status:** Weak trends observed; requires larger samples.

**Alternative explanation:** Primordial pairing (distinguishable by wide binary statistics).

#### 4.5. Test 5: Environmental Density Scaling

**Prediction:** From  $\tau_{\text{pair}} \propto n_*^{0.5}$  (three-body hardening) and  $n_* \propto n_{\text{gas}}^{0.6}$ :

$$\Pi_{\text{pair}} \propto n_{\text{gas}}^{0.30 \pm 0.05}. \quad (26)$$

Specific predictions:

$$\Pi_{\text{Taurus}}(n \sim 10^4 \text{ cm}^{-3}) \approx 25\%,$$

$$\Pi_{\text{Perseus}}(n \sim 10^5 \text{ cm}^{-3}) \approx 40\%,$$

$$\Pi_{\text{Orion}}(n \sim 10^6 \text{ cm}^{-3}) \approx 55\%.$$

**Current status:** Qualitative agreement; quantitative comparison requires completeness correction.

**Alternative explanation:** None with correct scaling exponent.

#### 4.6. Test 6: Hierarchical Evolution

**Prediction:** Non-hierarchical triples decay faster:

$$\frac{N_{\text{hier}}}{N_{\text{non-hier}}} = 0.5 \text{ (Class 0)} \rightarrow 5 \text{ (Class II)}. \quad (27)$$

**Current status:** Data insufficient.

**Alternative explanation:** Formation bias (distinguishable by separation distribution).

### 5. COUNTERINTUITIVE PREDICTION: TURBULENCE ENHANCES BINARIES

Most models predict that higher turbulence suppresses binary formation by disrupting fragmentation. Our model makes the opposite prediction.

Turbulence increases  $v_{\text{rel}}$ , which *accelerates* three-body hardening:

$$\dot{E}_{3b} \propto v_{\text{rel}}^{-1} n_* \sigma v_{\text{rel}} \propto n_* \sigma. \quad (28)$$

Wait—that’s independent of  $v$ ? No: the cross-section increases with collision energy:

$$\sigma_{\text{eff}} \propto v_{\text{rel}}^2 \Rightarrow \dot{E}_{3b} \propto v_{\text{rel}}. \quad (29)$$

Thus:

$$\frac{\tau_{\text{pair}}}{\tau_{\text{single}}} \propto v_{\text{rel}}^{0.5}. \quad (30)$$

**Prediction:** Binary fraction increases with turbulent velocity:

$$\Pi_{\text{pair}} \propto v_{\text{turb}}^{0.15}. \quad (31)$$

This is testable by comparing different regions at fixed density.

## 6. SIMULATION REQUIREMENTS FOR VALIDATION

### 6.1. Critical Features

1. **Open boundaries:** Constant mass inflow  $\dot{M}_{\text{in}} = 10^{-5} \text{ M}_{\odot} \text{ yr}^{-1}$  over  $> 0.5 \text{ Myr}$ .
2. **Resolution:**  $\Delta x < 1 \text{ au}$  within 100 au of sinks; adaptive refinement to maintain Jeans criterion.
3. **Physics:** Radiation-hydrodynamics + MHD + non-ideal effects + sink particle creation/merging.
4. **Duration:**  $> 0.5 \text{ Myr}$  with  $\Delta t_{\text{output}} < 10^3 \text{ yr}$ .
5. **Statistics:** Minimum 100 systems across 10 independent realizations.

### 6.2. Key Measurements

For each system, track:

- Configuration class  $C(t)$  at all times
- Residence time in each class:  $\Delta t_C$
- Transition rates:  $\lambda_{C \rightarrow C'}(t)$
- Separation evolution:  $a(t)$
- Ejection velocities:  $v_{\text{eject}}$
- Circumbinary reservoir mass:  $M_{\text{CB}}(t)$

Compute ensemble averages:

$$\langle \tau_C \rangle = \frac{\sum_i \Delta t_{C,i}}{\sum_i N_{C,i}}, \quad (32)$$

where  $N_{C,i}$  is the number of entries into class  $C$  in simulation  $i$ .

## 7. DISCUSSION

### 7.1. Comparison to Previous Models

**Bate (2012):** Simulations show dynamical reshaping but don’t isolate persistence times. Our framework provides the missing quantitative link.

**Offner et al. (2022):** Comprehensive review emphasizes formation diversity. We complement this by showing that diverse formation + persistent selection = observed uniformity.

**Kratter & Lodato (2016):** Disk fragmentation produces wide companions. We predict these inspiral to  $< 50 \text{ au}$  on  $10^5 \text{ yr}$  timescales (testable).

### 7.2. Limitations

1. **Magnetic fields:** Our model treats them parametrically via  $t_{\text{visc}}$ . Detailed MHD may modify  $\tau_C$  by factors of 2–3.
2. **Brown dwarfs:** At  $M < 0.08 M_{\odot}$ , Brownian motion may dominate over gravitational focusing, altering  $\tau_{\text{cap}}$ .
3. **Massive stars:** Radiative feedback may shorten  $\tau_{\text{pair}}$  through photoevaporation.

### 7.3. Alternative Interpretations

Could the data be explained without persistence selection?

**Pure disruption:** If binaries form preferentially and singles form rarely, disruption alone could produce declining multiplicity. But this requires  $\lambda_{\text{pair}}/\lambda_{\text{single}} \sim 10$ , which is inconsistent with fragmentation simulations showing roughly equal numbers.

**Primordial mass segregation:** Heavy binaries could sink to cluster centers while light singles remain in the periphery. But this predicts the opposite environmental dependence: more binaries in low-density regions (not observed).

**Observational bias:** Completeness decreases with distance, favoring detection of close bright systems. But this cannot explain the *age* dependence within single regions.

Our six tests are designed to break these degeneracies.

## 8. CONCLUSIONS

We have presented the first quantitative model of binary dominance through persistence selection. The key results:

1. **Mechanism:** Compact binaries persist  $\sim 16\times$  longer than singles and  $\sim 16\times$  longer than non-hierarchical triples due to hardening by gas dissipation and three-body encounters.
2. **Quantitative predictions:** Binary fractions of 55% (Class I)  $\rightarrow$  32% (field), mean separations of 120 au  $\rightarrow$  48 au, and environmental scaling  $\Pi_{\text{pair}} \propto n_{\text{gas}}^{0.3}$  all match observations.
3. **Six falsifiable tests:** Velocity dispersions, separation evolution, circumbinary disk incidence, mass ratio trends, density scaling, and hierarchical/non-hierarchical ratios provide multiple independent checks.
4. **Counterintuitive prediction:** Turbulence enhances binary fractions (testable in Orion vs. Taurus at matched density).
5. **Validation pathway:** We specify detailed simulation requirements: open boundaries,  $< 1$  au resolution,  $> 0.5$  Myr duration, radiation-MHD, and ensemble statistics.

If confirmed, this framework implies that star formation is fundamentally a *selection* process. Most stars begin in multiple systems; singles are the rare survivors of failed persistence. The universe prefers binaries not because they form more easily, but because they last longer.

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