

Fractal Scaling of Operational Patterns Across Systems: Mechanisms, Deviations, and Diagnostic Principles

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Abstract

Systems—from gravitational accretion to neural networks, from individual cognition to institutional governance—exhibit a universal operational tendency: they apply a finite set of generating rules recursively across scales of varying complexity. This paper formalizes this tendency as *fractal pattern scaling*, demonstrates that it constitutes the most resource-efficient strategy available to any bounded system, and identifies a hierarchy of structural deviations that arise when patterns are transferred to scales where their boundary conditions no longer hold. We introduce a four-level diagnostic framework—*pattern unawareness*, *transfer unawareness*, *pathology unawareness*, *applicability unawareness*—and prove that increasing system capability (feedback, reflexivity, meta-reflexivity) does not resolve these deviations but compounds them by generating progressively deeper illusions of adaptation. The analysis draws on dynamical systems theory, $1/f$ spectral analysis, self-organized criticality, and recursive function theory, while maintaining accessibility across disciplinary boundaries. Physical (accretion), biological (immune response), cognitive (decision-making), and institutional (organizational management) examples are developed in parallel to demonstrate substrate-independence. Practical diagnostic protocols are provided in appendices.

Keywords: fractal scaling, complex systems, self-similarity, cognitive patterns, structural blindness, $1/f$ dynamics, self-organized criticality, scale invariance, pattern transfer, systems theory

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1 Introduction

When one observes that the branching of a neuron’s dendrite resembles the branching of a river delta, the resemblance is not decorative. Both structures arise because a single generating rule—bifurcation under a gradient—is applied iteratively across spatial scales. The result, in both cases, is a fractal geometry: a structure whose parts, upon magnification, reproduce the organizational logic of the whole [31].

This paper begins with a deceptively simple observation: systems—not necessarily complex ones—do not develop a new algorithm for each new level of operational challenge. Instead, they take whatever operational pattern is already available and scale it. This tendency is present already in elementary physical processes. Gravitational accretion, for instance, is not a complex system: it is a simple positive-feedback loop in which mass attracts mass. Yet this single generating rule is applied across more than fifteen orders of magnitude in mass—from dust grains to black holes—producing qualitatively different outcomes at each scale. No complexity is required for the pattern to scale; complexity merely adds new dimensions to the consequences of scaling.

The distinction is important and must be made explicit from the outset. We are not claiming that accretion, crystals, or thermostats are complex systems. We are claiming that *the mechanism of pattern scaling across levels is universal*: it operates in simple processes, in systems with feedback, in reflexive systems, and in meta-reflexive systems alike. What changes across this hierarchy is not the mechanism itself but the nature of the deviations it produces. Simple systems scale their patterns and encounter no problem, because they have no capacity to detect or correct mismatch. Systems with feedback scale their patterns and acquire the illusion of adaptation, because feedback confirms the pattern is operating without signaling whether it is operating appropriately. Reflexive systems—humans, organizations, artificial intelligence—can in principle detect the transfer, but structurally fail to do so. Each level of sophistication adds not a correction mechanism but a deeper layer of blindness.

A human being who selects breakfast by minimizing uncertainty—choosing the familiar option to avoid decision cost—applies the same pattern when choosing a career, a partner, or a worldview. Not because these decisions are similar in content, but because the generating rule is one, and the system has no second one [14, 42].

The contribution of the present work is fourfold:

- (i) We formalize fractal pattern scaling as the most resource-efficient operational strategy for any system—simple or complex—operating across multiple scales.
- (ii) We identify a specific hierarchy of structural deviations that arise when patterns are transferred beyond their domain of applicability.
- (iii) We prove that increasing system sophistication (feedback, reflexivity, meta-

reflexivity) does not resolve these deviations but compounds them by generating progressively deeper illusions of adaptation.

- (iv) We demonstrate that the phenomenon is substrate-independent: it manifests in physical processes (accretion), biological systems (immune response), cognitive systems (decision-making), and institutional systems (organizational governance).

The paper is structured as follows. Section 2 provides a comprehensive literature review. Section 3 develops the mathematical formalism. Section 4 presents physical examples, beginning deliberately with simple processes to establish that pattern scaling precedes and does not require complexity. Section 5 analyzes the role of feedback and the hierarchy of system types. Section 6 introduces the four-level blindness framework. Section 7 treats cognition as a special case. Section 8 extends the analysis to institutions and scientific disciplines. Section 9 addresses the methodological necessity of interdisciplinary investigation. Section 10 engages with counterarguments from modularity theory, evolutionary strategy diversity, and analogical reasoning. Section 11 specifies the framework's own boundary conditions and falsifiability criteria. Section 12 provides a worked organizational case study. Section 13 places this work within a broader theoretical program. Section 14 concludes. Appendices provide practical diagnostic protocols.

2 Literature Review

2.1 Fractal Geometry and Self-Similarity

The mathematical foundations of fractal geometry were established by Mandelbrot [31], who demonstrated that naturally occurring structures—coastlines, clouds, mountain ranges—exhibit statistical self-similarity across scales. Unlike Euclidean objects, whose characteristic features disappear under magnification, fractal structures reveal the same organizational pattern at every level of resolution. The Hausdorff–Besicovitch dimension D provides a rigorous measure of this property [13].

Barnsley's work on iterated function systems showed that complex fractal geometries can be generated by the recursive application of a small number of contraction mappings [3]. This result is fundamental to the present argument: it demonstrates formally that a simple generating rule, applied recursively, produces structures of arbitrary complexity without requiring additional rules at each level.

2.2 Fractals in Neural Architecture

The fractal geometry of neural structures has been extensively documented. Dendritic arborization in cortical neurons exhibits fractal branching with dimensions typically ranging

from $D \approx 1.4$ to $D \approx 1.8$ [8, 39]. Werner [44] provided a comprehensive review showing that fractal organization in the brain spans molecular, cellular, and network scales. The cerebral vasculature follows Murray’s law with fractal branching patterns [9], and cortical folding exhibits fractal scaling properties [20, 25].

At the functional level, the brain’s resting-state networks display scale-free dynamics: their temporal fluctuations follow power-law distributions characteristic of systems poised near a critical phase transition [12, 19]. EEG recordings consistently reveal $1/f$ -type spectral characteristics across frequency ranges spanning several decades [30, 36].

2.3 Self-Organized Criticality and $1/f$ Dynamics

Bak, Tang, and Wiesenfeld [1] introduced self-organized criticality (SOC)—the tendency of driven dissipative systems to evolve toward a critical state without external tuning. At criticality, the system’s dynamics exhibit power-law distributions in event sizes and durations, $1/f$ temporal spectra, and long-range spatiotemporal correlations.

Beggs and Plenz [4] demonstrated that spontaneous neural activity organizes into “neuronal avalanches” whose sizes follow a power law $P(s) \propto s^{-\tau}$ with $\tau \approx 1.5$, consistent with SOC predictions. Subsequent work confirmed these findings *in vivo* [17, 35, 37].

The theoretical significance of criticality is that it maximizes the system’s dynamic range, information transmission capacity, and sensitivity to perturbations [24, 38]. A system operating below criticality is too rigid; above criticality, too unstable. The critical regime provides the optimal balance—a balance maintained through fractal pattern scaling.

2.4 Recursive Structures in Language and Cognition

Chomsky’s observation that natural language is characterized by recursive embedding established recursion as a fundamental property of human cognitive architecture [10, 18]. Hofstadter [21] proposed that consciousness itself emerges from “strange loops”—recursive structures capable of self-reference [11].

Research in cognitive science has shown that decision-making processes exhibit self-similar temporal structure. Gilden [16] demonstrated $1/f$ fluctuations in cognitive performance across time scales spanning seconds to hours. Van Orden, Holden, and Turvey [43] argued that $1/f$ scaling in reaction times is evidence that cognition operates as an integrated dynamical system.

2.5 Cognitive Biases as Systematic Patterns

Tversky and Kahneman [42] documented heuristics—anchoring, availability, representativeness—that human judgment systematically employs. Gigerenzer and colleagues [14, 15] rein-

terpreted heuristics as “fast and frugal” strategies optimized for ecological rationality—performing well in the environments for which they evolved, but failing when transferred to structurally different contexts. This reframing is compatible with the present thesis: heuristics are generating patterns that work at the scale for which they were selected and fail when scaled beyond it.

Stanovich and West [41] distinguished between Type 1 (automatic) and Type 2 (deliberate) cognitive processes. The fractal scaling perspective suggests—as a speculative hypothesis requiring independent empirical investigation—that this distinction may reflect different iteration regimes of the same generating pattern rather than qualitatively different cognitive architectures: Type 1 processing applies a pattern in a single pass; Type 2 applies the same pattern with more iterations and broader input sampling, but the generating rule itself remains unexamined in both cases. This reinterpretation is not intended as a refutation of dual-process theory but as an alternative framing that, if supported, would have implications for debiasing interventions: if Type 2 processing merely iterates the same pattern, then “thinking harder” cannot correct a defective generating rule.

2.6 Fractal Organization in Social and Institutional Systems

Scale-free network topologies are ubiquitous in social systems [2, 34]. Organizational theorists have noted that institutions tend to replicate their management patterns across scales [29, 32].

West [45] demonstrated that metabolic scaling laws apply across biological scales from cells to ecosystems. Bettencourt and West [6] extended this to cities, showing that urban indicators scale with city size according to power laws—a direct manifestation of fractal pattern scaling at the institutional level.

2.7 Fractal Processes in Physical Systems

Gravitational accretion provides a paradigmatic example. The same process—mass attracting mass under gravity—operates from dust grain aggregation [7, 22] through stellar formation [27, 33] to galaxy cluster assembly [26, 40]. At each scale, the generating rule is identical; the boundary conditions change. The result is qualitatively different outcomes: planetesimals, main-sequence stars, active galactic nuclei, black holes. This progression illustrates the central thesis: the same pattern, applied across scales with changing boundary conditions, produces not merely quantitative variation but qualitative transformation—including catastrophic regime change that the generating pattern cannot predict from within itself.

3 Formal Framework

This section develops the mathematical apparatus needed to make the foregoing observations precise. Every definition and proposition is accompanied by a motivating explanation and an interpretive commentary, so that readers from empirical disciplines can follow the reasoning without prior training in dynamical systems theory.

3.1 Operational Pattern: Definition

We begin by defining what we mean by a “pattern” in a system’s behavior. The intuition is straightforward: a pattern is a rule that the system follows when responding to its environment. What makes it an *operational* pattern is that it governs the system’s own transitions from one state to another.

Definition 3.1 (State Space and Transition Function). Let \mathcal{S} be a set of states accessible to a system, and let \mathcal{E} be a set of environmental inputs. A *transition function* is a mapping

$$T : \mathcal{S} \times \mathcal{E} \longrightarrow \mathcal{S}, \quad (1)$$

which, given a current state $s \in \mathcal{S}$ and an input $e \in \mathcal{E}$, determines the next state $T(s, e) \in \mathcal{S}$.

The transition function T captures everything the system “does” in response to stimuli. A thermostat’s T compares current temperature to a set-point and switches heating on or off. A neuron’s T integrates synaptic inputs and fires or remains silent. A manager’s T receives a problem report and initiates a budgetary review.

Definition 3.2 (Operational Pattern). An *operational pattern* is a structural invariant of T —a property that remains unchanged across variation in the specific content of s and e . Formally, let $\phi : \mathcal{S} \times \mathcal{E} \rightarrow \mathcal{F}$ be a feature extraction mapping into a feature space \mathcal{F} . An operational pattern is a function

$$P : \mathcal{F} \longrightarrow \mathcal{F} \quad (2)$$

such that for all (s, e) in the relevant domain, $\phi(T(s, e)) = P(\phi(s, e))$.

The feature extraction ϕ strips away domain-specific content and retains only structural properties: is the system approaching or avoiding? Repeating or exploring? Centralizing or distributing? The operational pattern P is the rule governing these structural features, independent of what is specifically being approached, repeated, or centralized.

This definition captures the key insight: a person who always “goes with the familiar option” has an operational pattern P that maps the structural feature “uncertainty level” to “minimize,” regardless of whether the domain is food, employment, or philosophy.

3.2 Scale and Boundary Conditions

Different levels of complexity impose different constraints on the system.

Definition 3.3 (Scale). A *scale* σ is characterized by a triple $(\mathcal{S}_\sigma, \mathcal{E}_\sigma, \mathcal{B}_\sigma)$, where \mathcal{S}_σ and \mathcal{E}_σ are the state and input spaces available at that scale, and $\mathcal{B}_\sigma \subseteq \mathcal{S}_\sigma$ is the set of *boundary conditions*—constraints on which states are physically, biologically, or institutionally realizable.

At the planetary scale, boundary conditions include solid-body mechanics and limited gravitational influence. At the stellar scale, radiation pressure and nuclear fusion enter the boundary set. At the black-hole scale, general-relativistic constraints dominate. The generating rule does not change; the boundary conditions \mathcal{B}_σ do.

3.3 Fractal Pattern Scaling

We now define the central concept.

Definition 3.4 (Fractal Pattern Scaling). A system exhibits *fractal pattern scaling* if there exists an operational pattern P that is applied across two or more scales $\sigma_1, \sigma_2, \dots$, despite differences in boundary conditions \mathcal{B}_{σ_i} . Formally:

$$\phi_{\sigma_i}(T_{\sigma_i}(s, e)) = P(\phi_{\sigma_i}(s, e)) \quad \text{for all } \sigma_i \in \{\sigma_1, \sigma_2, \dots\}, \quad (3)$$

where ϕ_{σ_i} is the scale-appropriate feature extraction and T_{σ_i} is the transition function at scale σ_i .

This states precisely what we have been describing: the same structural rule P governs the system’s behavior across different levels of complexity. The content changes, the boundary conditions change, but the pattern is one.

3.4 Efficiency of Fractal Pattern Scaling

Why do systems default to this strategy? The following proposition makes the resource argument precise.

Proposition 3.1 (Resource Optimality). Let a system operate across n scales. Let $C(P)$ denote the cost of maintaining an operational pattern P , and let C_{total} denote the total operational cost. The term “cost” is understood substrate-specifically: for physical systems, it denotes energetic or thermodynamic cost; for biological systems, metabolic expenditure; for cognitive systems, computational and attentional load; for institutional systems, organizational overhead. Under fractal pattern scaling (single pattern P applied to all n scales):

$$C_{\text{total}}^{\text{fractal}} = C(P) + n \cdot C_{\text{apply}}, \quad (4)$$

where C_{apply} is the cost of applying P at each scale. Under scale-specific processing (a distinct pattern P_i for each scale):

$$C_{\text{total}}^{\text{specific}} = \sum_{i=1}^n C(P_i) + n \cdot C_{\text{apply}}. \quad (5)$$

Since $C(P) \ll \sum_{i=1}^n C(P_i)$ for $n > 1$, fractal pattern scaling is strictly more resource-efficient in terms of pattern-maintenance cost.

This result requires an important qualification. The proposition compares only the cost of maintaining and applying patterns, not the cost of outcomes. In biological and social systems, the cost of pattern–boundary mismatch—misadaptation, organizational failure, systemic collapse—may far exceed the savings from maintaining a single pattern. Evolutionary systems, in particular, routinely maintain diverse response strategies precisely because the cost of single-pattern failure under environmental variability is catastrophically high [52]. Fractal pattern scaling is therefore the default not because it is globally optimal, but because it is locally cheapest: the savings are immediate and certain, while the costs of mismatch are deferred and uncertain. This asymmetry between immediate savings and deferred costs is itself a structural feature that reinforces the tendency toward single-pattern scaling.

3.5 Pattern–Boundary Mismatch

The efficiency comes at a cost: the pattern may not be appropriate for every scale at which it is applied.

Definition 3.5 (Pattern–Boundary Mismatch). A *pattern–boundary mismatch* occurs at scale σ_i when the operational pattern P generates transitions that exit the realizable boundary set:

$$\exists (s, e) \in \mathcal{S}_{\sigma_i} \times \mathcal{E}_{\sigma_i} : T_{\sigma_i}(s, e) \notin \mathcal{B}_{\sigma_i}. \quad (6)$$

When gravitational accretion pushes a stellar mass past the Tolman–Oppenheimer–Volkoff limit, the result is a black hole—a pattern–boundary mismatch in which the accretion pattern generates an outcome that violates the equilibrium conditions of the previous scale.

3.6 The Scale Inaccessibility Proposition

The following result establishes that pattern–boundary mismatch cannot, in general, be detected from within the generating pattern itself. We state this as a proposition rather than a theorem, because its force depends on a specific structural condition—one that holds widely but is not universal. Identifying the conditions under which it does and does not hold is itself a diagnostic contribution.

Proposition 3.2 (Scale Inaccessibility). Let P be an operational pattern applied at scale σ_i , operating on feature space \mathcal{F} via feature extraction ϕ . If ϕ is *lossy with respect to boundary information*—that is, if

$$\phi_{\sigma_j}^{-1}(\phi_{\sigma_j}(\mathcal{B}_{\sigma_j})) \supsetneq \mathcal{B}_{\sigma_j}, \quad (7)$$

meaning that ϕ maps some boundary-violating states to the same feature representations as boundary-compliant states—then P cannot determine whether its application at scale σ_j will produce a pattern–boundary mismatch.

Proof. By Definition 3.2, P operates on \mathcal{F} , the image of ϕ . If condition (7) holds, then there exist states $s_1 \in \mathcal{B}_{\sigma_j}$ and $s_2 \notin \mathcal{B}_{\sigma_j}$ such that $\phi(s_1) = \phi(s_2)$. Since P receives only ϕ -images, it cannot distinguish s_1 from s_2 , and therefore cannot detect that its application produces a boundary-violating transition. \square

The condition (7) holds generically for operational patterns as defined here, because ϕ is constructed to extract structural invariants rather than scale-specific content—this is precisely what makes P transferable across scales. The very abstraction that enables cross-scale transfer is what prevents cross-scale boundary detection. Economy and blindness are two faces of one coin.

However, condition (7) can be violated in specific circumstances. If a system augments its feature extraction with scale-specific information—for example, if an organization supplements its standard operating procedures with domain-specific audits, or if a scientific discipline incorporates external methodological review—then ϕ may preserve boundary information, and mismatch becomes detectable. This observation is itself diagnostic: the remedy for scale inaccessibility is not more sophisticated pattern application but deliberate enrichment of the feature extraction to include scale-specific constraints.

3.7 The Feedback Amplification Proposition

Systems with feedback loops are often assumed to be self-correcting. The following shows that under a specific structural condition, feedback can *amplify* rather than correct pattern–boundary mismatch.

Proposition 3.3 (Feedback Amplification of Mismatch). Let a system with feedback apply operational pattern P at scale σ . Let the feedback signal $f : \mathcal{S} \rightarrow \mathcal{E}$ map current states to subsequent inputs. If f factors through the same feature extraction as P —that is, if $f = f' \circ \phi$ for some $f' : \mathcal{F} \rightarrow \mathcal{E}$ —then f cannot signal pattern–boundary mismatch at σ , and the feedback loop stabilizes the pattern’s continued application regardless of boundary compliance.

Proof. By hypothesis, f factors through ϕ , meaning it is sensitive only to the structural features that P tracks. A pattern–boundary mismatch involves states outside \mathcal{B}_σ , but by Proposition 3.2, these are not distinguishable from boundary-compliant states in \mathcal{F} . Therefore f generates corrective signals that adjust parameters within P ’s operational space but cannot signal the need to *replace* P . The feedback loop thus maintains the system’s commitment to P even when P generates boundary-violating transitions. \square

This explains a widely observed phenomenon: systems with sophisticated feedback mechanisms can persist in maladaptive behavior precisely because their feedback confirms the pattern is “working” within its own feature space, even as outcomes become increasingly misaligned with actual constraints.

The critical condition is that feedback factors through the same feature space as the pattern. In real biological and institutional systems, this condition is not always satisfied. The immune system, for example, receives feedback through multiple partially independent channels—inflammatory markers, antibody titers, temperature—not all of which are reducible to the same feature extraction that governs the initial immune response. When feedback operates through channels that are at least partially independent of ϕ , the system gains access to boundary-relevant information that P alone cannot represent. This partial independence is what makes adaptive immune responses possible—and its absence is what makes maladaptive institutional responses persistent.

The diagnostic implication is direct: to break the feedback amplification loop, a system must establish feedback channels that do not factor through its own operational pattern. For an organization, this means external audit rather than internal review. For a scientific discipline, this means cross-disciplinary evaluation rather than intra-disciplinary peer review. For an individual, this means exposure to perspectives that operate on different structural features than those the individual habitually attends to.

4 Fractal Pattern Scaling in Physical Systems

Gravitational accretion provides a paradigmatic illustration of the formal framework. The generating pattern is elementary: mass attracts mass, and the resulting increase in local gravitational potential accelerates further accumulation. This positive-feedback loop operates identically at scales spanning more than fifteen orders of magnitude in mass.



One generating rule (gravitational accretion) — four qualitatively different outcomes

Figure 1: Gravitational accretion as fractal pattern scaling: one generating rule produces qualitatively different outcomes at four scales, depending on boundary conditions. At each transition, new physical processes enter the boundary set \mathcal{B}_σ that the accretion pattern itself cannot anticipate.

At the **planetesimal scale**, dust grains adhere through van der Waals forces and grow by mutual gravitational attraction. The boundary conditions include solid-body mechanics and low radiation environments. The outcome is a stable body in hydrostatic equilibrium.

At the **stellar scale**, the same accretion pattern operates on gas clouds. The boundary conditions now include radiation pressure, angular momentum conservation, and the onset of thermonuclear fusion when core temperatures exceed $\sim 10^7$ K [33]. This boundary condition is entirely absent at the planetesimal scale. The generating pattern cannot “anticipate” fusion from within its own operational logic. The result is a qualitatively new object: a star, sustained by a balance between gravitational contraction and radiative pressure.

At the **galactic scale**, stars and dark matter accumulate into gravitationally bound structures. Dark matter dynamics—absent at both previous scales—enter the boundary set and dominate the large-scale gravitational potential [40].

At the **black hole scale**, accreting mass exceeds the Tolman–Oppenheimer–Volkoff limit, and the same process that built stable stars produces a spacetime singularity. The generating pattern is unchanged; the boundary conditions have shifted so fundamentally that the outcome is not merely a larger version of the previous object but a qualitatively different entity governed by general relativity rather than Newtonian mechanics.

This progression is a concrete instance of Proposition 3.2: the accretion pattern cannot determine, from within its own feature space, whether its application at a given scale will yield a planet, a star, or a black hole.

4.1 Relation to Renormalization Group Methods

The physics of cross-scale pattern transfer has a rigorous formalism in the renormalization group (RG), developed by Wilson and others [54]. RG methods systematically coarse-grain a system’s degrees of freedom and track how the effective dynamics—the operational pattern in our terminology—change under rescaling. At a critical fixed point, the effective dynamics are scale-invariant: the pattern is identical at every scale. Away from criticality, the effective dynamics “flow” under rescaling, meaning the pattern changes as the scale changes.

The present framework can be understood as a generalization of RG logic beyond physics. RG asks: does the pattern change under rescaling, and if so, how? We ask the same question, but for systems where the “rescaling” is not spatial or energetic but organizational—from individual to institutional, from local heuristic to global strategy. The key difference is that in physical RG, the flow equations are derivable from the microscopic Hamiltonian; in cognitive and social systems, no such derivation is available, and the system typically does not know its own flow equations. This is precisely the content of Proposition 3.2: the system applies its pattern at a new scale without access to the “RG flow” that would tell it how the effective dynamics should change.

5 Feedback, Reflexivity, and the Hierarchy of System Types

Not all systems are equally susceptible to the pathologies of fractal pattern scaling. The nature and severity of the pathology depend on the system’s capacity for self-monitoring. We distinguish four types.

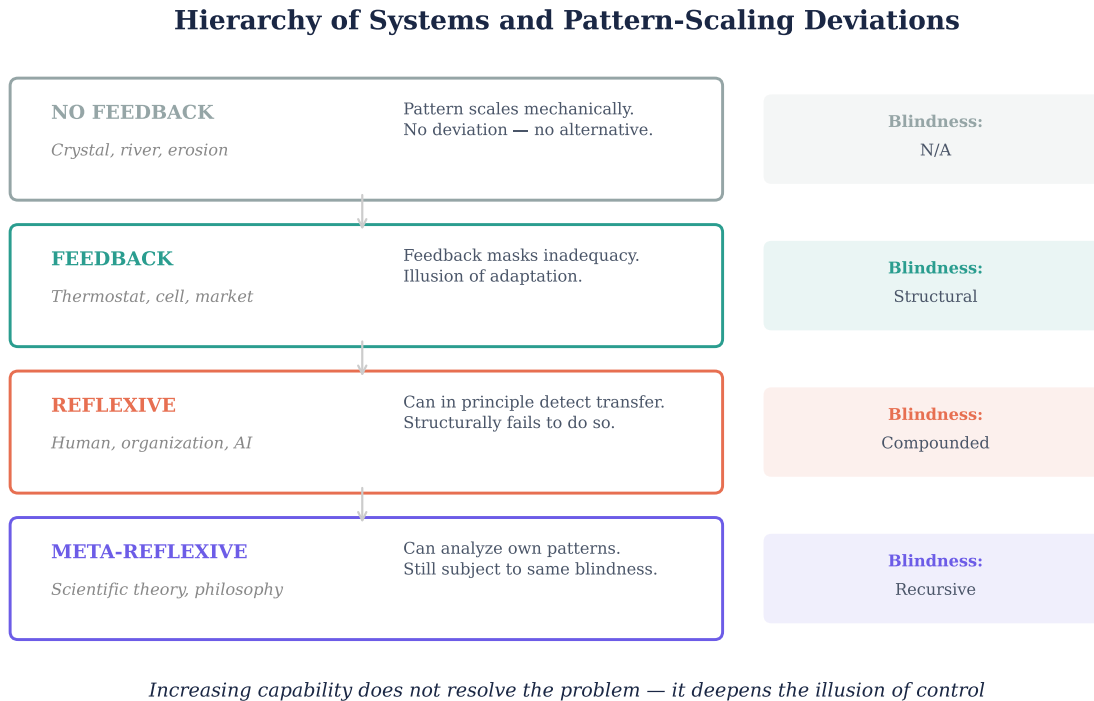


Figure 2: Hierarchy of system types and their relationship to pattern-scaling deviations (schematic). Increasing capability (left) paradoxically increases the depth of structural illusion (right).

5.1 Systems Without Feedback

A crystal growing in solution applies a single generating rule (lattice replication) across all spatial scales. There is no feedback mechanism; the pattern propagates mechanically. No pathology arises, because the system has no capacity—and no need—to detect mismatch.

5.2 Systems With Feedback

A thermostat, an immune cell, or a simple market mechanism receives signals about the consequences of its actions and adjusts. The critical observation is that feedback operates *within the same feature space as the pattern* (Proposition 3.3). The thermostat receives temperature readings and adjusts heating output—but it cannot receive a signal indicating that temperature regulation is the wrong objective.

This creates what we term the *adaptation illusion*: the system receives continuous confirmation that it is responding to its environment, when in fact it is responding only to those aspects of its environment that its pattern is designed to detect.

5.3 Reflexive Systems

Humans, organizations, and artificial intelligence systems possess the capacity to represent and evaluate their own operational patterns. In principle, a reflexive system can detect that it is applying the same pattern across scales and ask whether this transfer is appropriate.

In practice, reflexive systems overwhelmingly fail to exercise this capacity. The reason is structural: reflexion over a generating pattern requires resources that compete with the resources used to apply the pattern. The system would need to step outside its operational mode to evaluate that mode—and the operational mode is precisely what makes the system functional.

5.4 Meta-Reflexive Systems

Scientific theories, philosophical frameworks, and institutional audit mechanisms represent the highest level of self-monitoring capacity. Yet even meta-reflexive systems are subject to the same structural constraint: the method used to evaluate a method is itself a pattern, and that pattern too is scaled across problems without guarantee of applicability. The regress is arrested by resource constraints, but it is structurally present.

6 Four Levels of Structural Blindness

The analysis of Sections 3–5 yields a diagnostic taxonomy.

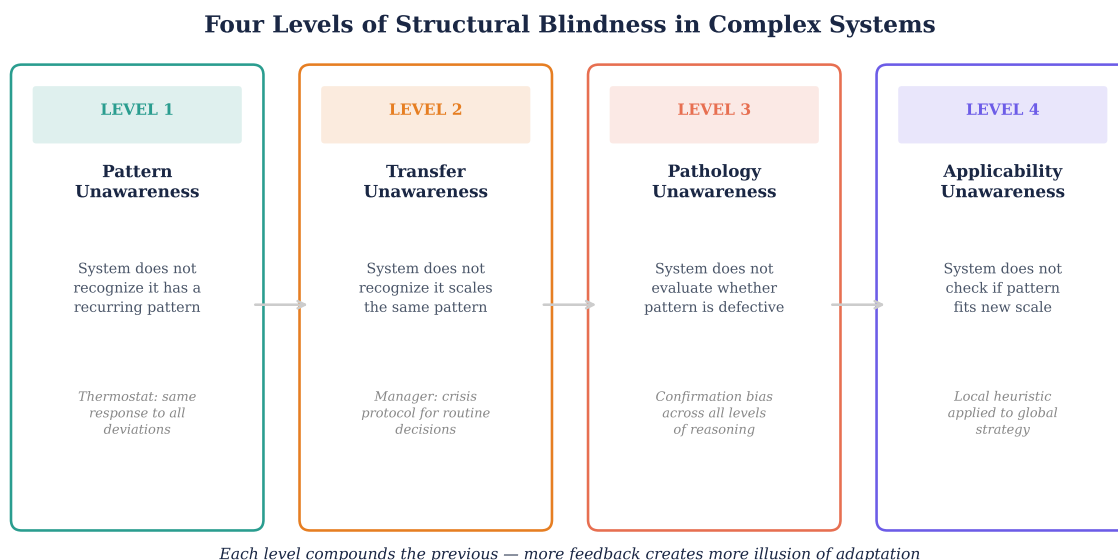


Figure 3: The four levels of structural blindness. Each level compounds the previous. A system afflicted at Level 1 is necessarily afflicted at all subsequent levels.

Level 1: Pattern Unawareness. The system does not recognize that it possesses a recurring operational pattern. Each response is treated as a *de novo* reaction to specific circumstances.

Level 2: Transfer Unawareness. The system does not recognize that it applies the same pattern across different scales. A human who avoids uncertainty at breakfast and avoids uncertainty in career planning perceives these as two unrelated behaviors.

Level 3: Pathology Unawareness. Even if the pattern is recognized and its transfer detected, the system does not evaluate whether the pattern itself is defective. Confirmation bias, for example, generates evidence for its own adequacy.

Level 4: Applicability Unawareness. Even if the pattern is recognized, its transfer detected, and its structure evaluated, the system does not verify whether the pattern is appropriate for the specific scale at which it is being applied.

Proposition 6.1 (Compounding of Blindness). The four levels are logically cumulative: a system afflicted at Level k is necessarily afflicted at all levels $k' > k$.

The proof is immediate from the definitions, but its implication is not trivial: interventions targeting a higher level are ineffective unless all lower levels have been addressed.

7 Cognition as a Special Case

The human brain is frequently treated as the paradigmatic example of fractal organization. We argue it is better understood as a *special case* of a universal phenomenon.

7.1 Neural $1/f$ Dynamics and Criticality

The spectral signature of neural activity follows a characteristic $1/f^\beta$ form with $\beta \approx 1$ [19, 30]:

$$S(f) \propto \frac{1}{f^\beta}, \quad \beta \approx 1. \quad (8)$$

This indicates the absence of a characteristic time scale—the system sits between order and disorder [1]. This critical regime is precisely the condition under which fractal pattern scaling is most effective: the absence of a characteristic scale means the same organizational logic can operate from the microscopic to the macroscopic.

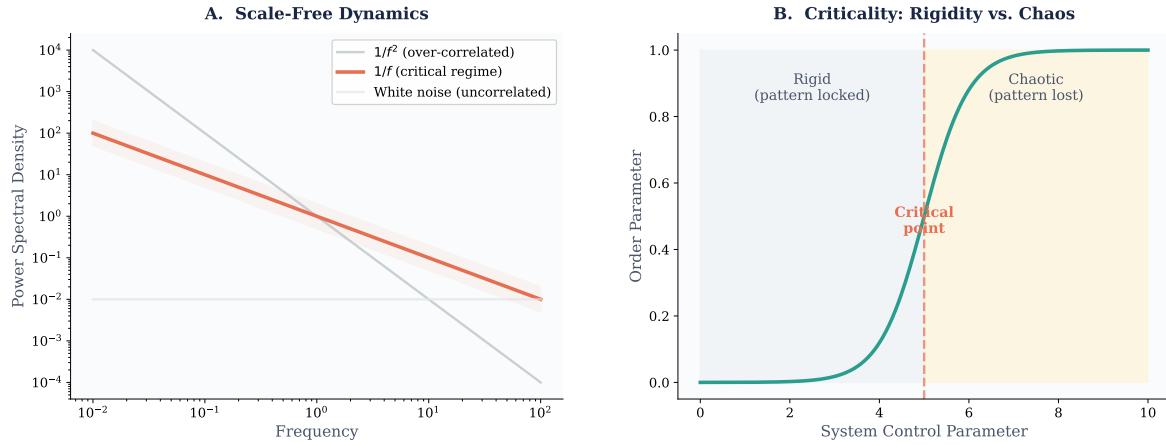


Figure 4: (A) Power spectral density for three dynamical regimes. The $1/f$ spectrum (critical regime) is characteristic of systems at the boundary between rigidity and chaos. (B) Phase transition diagram showing the critical point as the optimal operating regime.

7.2 Cognitive Biases as Fractal Deviations

The standard catalogue of cognitive biases [23, 42] treats each as an independent phenomenon. The fractal pattern scaling framework offers a more parsimonious account.

If prediction-error minimization is taken as the candidate generating pattern—as suggested by predictive processing theory [46, 49] and as argued in Section 10—then several apparently distinct biases emerge as manifestations of a single operational rule applied across cognitive scales. Specifically, “minimize the discrepancy between expectation and input” produces, at different scales:

- **Confirmation bias:** at the scale of evidence evaluation, the system minimizes prediction error by preferentially attending to confirming inputs and discounting disconfirming ones.
- **Anchoring:** at the scale of numerical estimation, the system minimizes prediction error by adjusting insufficiently from an initial reference point (the prediction).
- **Status quo bias:** at the scale of choice, the system minimizes prediction error by preferring outcomes consistent with existing expectations.
- **Belief perseverance:** at the scale of worldview, the system minimizes prediction error by resisting revision of established models.

Each of these is the same operational rule—reduce the gap between what is expected and what is encountered—applied at a different scale. The biases that this account would *not* naturally explain are those driven by non-predictive mechanisms: purely affective

biases (e.g., the affect heuristic), social-conformity effects (e.g., bandwagon effect), and biases arising from memory retrieval architecture (e.g., the availability heuristic, which depends on salience rather than prediction error). The framework thus makes a testable claim: prediction-error-driven biases should co-occur and resist correction as a cluster, while non-predictive biases should be more independently modifiable.

If this analysis is correct, it explains why biases are so resistant to correction. Correcting a bias at one level (e.g., teaching statistical reasoning to address anchoring) leaves the generating pattern intact, and it re-emerges at other levels (belief perseverance, confirmation bias). Effective debiasing would require intervention at the level of the generating pattern itself—a process that the four-level blindness framework reveals to be structurally difficult, because the pattern is precisely what the system uses to evaluate potential corrections.

7.3 Recursive Linguistic Self-Similarity

Natural language provides a directly observable instance. A sentence contains clauses; clauses contain phrases; phrases contain words—and at each level, the same syntactic rules apply [5, 10, 18]. Language is a directly audible manifestation of the cognitive system’s fractal pattern scaling.

8 Institutional and Disciplinary Pattern Scaling

An institution that manages internal conflict through hierarchical command will, by default, apply the same pattern to external negotiations, customer relations, and innovation policy. When it encounters a context where authority-based resolution is counterproductive, the resulting mismatch may persist indefinitely, stabilized by feedback that confirms the pattern is “in use” without detecting suboptimal outcomes [32].

Scientific disciplines provide a particularly instructive case. A discipline’s methodological pattern constitutes an operational pattern in the precise sense of Definition 3.2. When a biologist, a physicist, and an economist each approach the same complex system, they apply their discipline-specific generating pattern [28]. Many cross-disciplinary failures are instances of Level 4 blindness: the disciplinary pattern is applied to a domain whose boundary conditions it cannot represent.

9 Interdisciplinarity as Structural Necessity

If the object of study is the transfer of patterns across scales and domains, then any investigation confined to a single domain is structurally incapable of detecting the phenomenon.

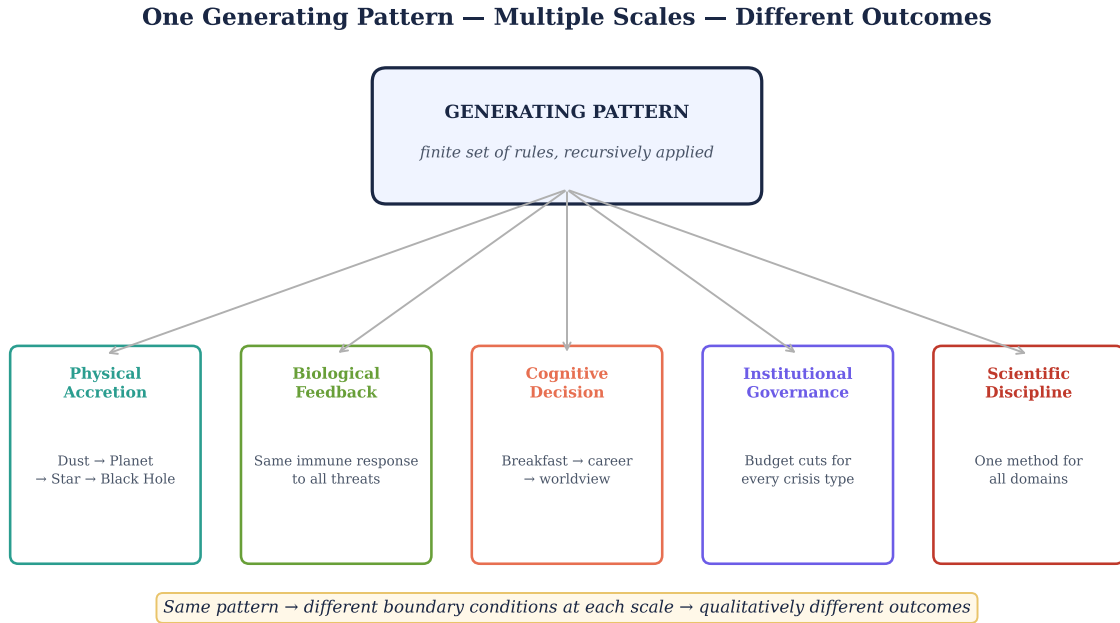


Figure 5: One generating pattern applied across five domains with qualitatively different outcomes. Detection of the common generating pattern requires simultaneous observation across domains.

This is not an argument for interdisciplinarity as intellectual enrichment. It is a structural claim: *the phenomenon itself is invisible from within a single scale*. A neuroscientist studying $1/f$ dynamics in cortical tissue and a sociologist studying power-law distributions in organizational hierarchies are observing the same structural phenomenon, but neither can recognize this without access to the other's domain.

Furthermore, disciplinary confinement is itself an instance of the pathology the paper describes. A discipline that applies its methodological pattern exclusively within its own domain is exhibiting Level 2 blindness in reverse: it does not recognize that its methods are *not being* transferred to contexts where they would reveal important structural commonalities.

10 Counterarguments and Limitations

Several important objections must be addressed directly.

10.1 Modularity and Domain-Specific Processing

Modularity theory in cognitive science and neuroscience argues that the brain maintains distinct processing modules for different domains—face recognition, language processing, spatial navigation—each with its own computational architecture [47, 48]. If the brain is modular, then it does *not* apply a single generating pattern to all problems; it applies

domain-specific patterns to domain-specific inputs. This appears to contradict the single-generating-pattern claim.

The resolution is that fractal pattern scaling and modularity operate at different levels of description. Modules are domain-specific at the level of content (faces, phonemes, spatial relations), but the *computational operation* within each module—pattern matching, error minimization, Bayesian updating—may be structurally identical across modules. A face-recognition module and a language-parsing module process different inputs but may apply the same structural operation: compare incoming data to a stored template and minimize prediction error [46]. The generating pattern is not “recognize faces”; it is “minimize prediction error.” The former is domain-specific; the latter is domain-general and is precisely the kind of operational pattern (Definition 3.2) that scales across cognitive domains.

The empirical question is therefore not whether modules exist (they do) but whether the operational logic within and across modules is structurally self-similar. Evidence from predictive processing theory suggests that it is [46, 49].

10.2 Evolutionary Advantages of Strategy Diversity

Evolutionary biology demonstrates that organisms and populations routinely maintain diverse response strategies rather than relying on a single pattern [52, 53]. Bet-hedging strategies, phenotypic plasticity, and the maintenance of genetic variation are all mechanisms by which biological systems avoid the risks of single-pattern dependence. If evolution selects for diversity, why would fractal pattern scaling be the default?

The answer is that strategy diversity and fractal pattern scaling are not mutually exclusive; they operate at different organizational levels. An organism may maintain multiple behavioral strategies (fight, flee, freeze), but the *meta-pattern* by which it selects among strategies—for example, “choose the strategy that minimizes immediate risk”—may itself be a single operational pattern applied across all decision contexts. The diversity is in the repertoire; the selection rule applied to the repertoire is often singular and self-similar. Furthermore, maintaining genuine strategy diversity is metabolically and computationally expensive. The tendency toward fractal pattern scaling represents the default to which systems regress when resources are limited—precisely the conditions under which most decisions are made.

10.3 Analogical Reasoning as a Related Framework

The literature on analogical reasoning [50, 51] addresses a closely related phenomenon: humans routinely transfer relational structures from familiar domains to unfamiliar ones. Structure-mapping theory [50] formalizes this as the transfer of relational predicates between source and target domains. The present framework can be seen as a generalization:

analogical reasoning is a conscious, deliberate instance of fractal pattern scaling, while the phenomenon we describe is overwhelmingly unconscious and structural. The four-level blindness framework (Section 6) adds a diagnostic layer absent from analogical reasoning theory: it identifies not just that transfer occurs but why it goes undetected and how detection fails at specific structural levels.

11 Boundary Conditions of the Framework

Any framework that claims to apply to “all systems” risks unfalsifiability. We therefore specify the conditions under which the present framework does not apply, and the observations that would be inconsistent with it.

Condition 1: Single-scale systems. A system operating at exactly one scale cannot exhibit fractal pattern scaling by definition. The framework applies only to systems whose operations span multiple levels of complexity. A single chemical reaction, absent any feedback or scaling, is outside the framework’s scope.

Condition 2: Systems with unlimited resources. If a system had genuinely unlimited computational or energetic resources, Proposition 3.1 would not apply: there would be no cost advantage to single-pattern scaling. In principle, such a system could maintain an independent optimal strategy for every scale. The framework predicts fractal pattern scaling only for resource-bounded systems.

Condition 3: Scale-independent boundary conditions. If boundary conditions were identical across all scales (i.e., $\mathcal{B}_{\sigma_i} = \mathcal{B}_{\sigma_j}$ for all i, j), then fractal pattern scaling would produce no mismatch. The framework’s diagnostic value depends on boundary conditions varying across scales—a condition that is empirically ubiquitous but not logically necessary.

Falsifying observations. The framework would be weakened by evidence that: (a) a resource-bounded system consistently develops genuinely novel operational patterns for each new scale rather than transferring existing ones; (b) feedback systems routinely detect and correct pattern–boundary mismatch without external intervention; (c) increasing system sophistication (feedback, reflexivity) systematically reduces rather than compounds structural blindness. Any of these findings would require substantive revision of the framework’s central claims.

12 Worked Example: Organizational Crisis Response

To demonstrate that the formal apparatus captures something beyond what domain-specific theories already provide, we apply the four-level diagnostic framework to a concrete case: organizational crisis response.

Consider a technology company that has grown from a small startup to a multinational corporation. During its startup phase, the company developed a crisis-response pattern: centralize decision-making authority in the founder, act rapidly, tolerate high risk, and iterate. This pattern (P) was effective at the startup scale (σ_1), where boundary conditions (\mathcal{B}_{σ_1}) included small team size, rapid communication, and tolerance for failure.

As the company scales to σ_2 (mid-size, ~ 500 employees) and σ_3 (multinational, $\sim 10,000$ employees), boundary conditions change: communication latency increases, regulatory obligations appear, decision complexity exceeds any individual's capacity, and failure tolerance decreases. The company, however, continues to apply P : in every crisis, authority centralizes in the CEO, rapid action is demanded, high risk is tolerated.

Applying the diagnostic framework:

Level 1 (Pattern Unawareness): The company does not recognize that its crisis response is a pattern. Each crisis is perceived as unique, requiring “leadership.” The structural invariant—centralize, accelerate, tolerate risk—is invisible.

Level 2 (Transfer Unawareness): The company does not recognize that the same pattern governs product crises, PR crises, regulatory crises, and organizational restructuring. Each is treated as a separate management challenge.

Level 3 (Pathology Unawareness): The pattern itself—centralize authority in one individual—has a structural bias toward information bottlenecks and single points of failure. At startup scale, this bias was harmless. At multinational scale, it produces systematic information loss.

Level 4 (Applicability Unawareness): The boundary conditions at σ_3 (regulatory complexity, communication latency, distributed expertise) are incompatible with centralized rapid-action. The pattern generates decisions that violate constraints the CEO cannot perceive from a centralized position—a direct instance of Proposition 3.2.

Internal feedback (Proposition 3.3) confirms the pattern: “We responded to the crisis. The CEO took charge. We acted quickly.” The feedback factors through the same feature space as the pattern (speed of response, decisiveness) and cannot register the mismatch (information loss, regulatory non-compliance, distributed-expertise bypass).

This analysis illustrates how the formal framework identifies a structural failure mode—one that organizational theory recognizes descriptively [32] but does not formalize in terms of pattern–boundary mismatch and feedback amplification. The framework adds specificity: it predicts *which* organizations are most vulnerable (those that scaled rapidly from a single founding pattern), *what* the failure mode will be (mismatch between centralization pattern and distributed boundary conditions), and *why* internal feedback will fail to detect it (feedback factors through the pattern's own feature space).

13 Broader Theoretical Context

The present paper fills a specific gap in a broader program of structural systems theory that has developed progressively across a series of independent publications spanning multiple domains.

The trajectory of this program illustrates, reflexively, the very phenomenon the program describes. The program did not begin with a unified theory from which individual results were deduced. Rather, individual structural results were established first—each addressing a specific problem in a specific domain—and the common architecture became apparent only retrospectively. The current paper identifies fractal pattern scaling as the mechanism that connects structural results previously established independently.

The foundational layer concerns meta-theoretical constraints on formal systems: no single formalization captures all operationally relevant properties of a complex system [55], and provability is itself a function of the definitions adopted [56]. These results establish the epistemic architecture within which all subsequent analysis operates.

The dynamical core formalizes persistence as the primary organizing principle [57]. Any system that persists in a changing environment must satisfy three conditions—closure, boundary maintenance, and resilience—constituting the Persistence Triad. The relationship between constraint and autonomy has been shown to be co-constitutive rather than antagonistic [58].

At the cognitive level, the Structural Distortion Principle has shown that cognitive biases are optimal solutions for resource-limited systems rather than errors [59]—a result that directly informs the present paper’s treatment of pattern scaling as a structural necessity rather than a deficiency. Further work in this program has addressed predictive processing, representational isolation, mental disintegration, and consciousness from the same structural perspective.

At the social level, substrate-independent formal models have been developed for extractive dynamics, conflict as phase transition, and deception in multi-agent systems. Cross-domain applications have tested these structural principles against astrophysical, cosmological, and information-theoretic data.

The law of scale-specific principles [60]—which states that no final theory can encompass all scales, and that unification is possible only for genuinely scale-invariant constraints—is the direct theoretical ancestor of the present paper’s central argument.

The present paper contributes by identifying the mechanism through which structural principles are (and fail to be) transferred across scales. Fractal pattern scaling is not merely a phenomenon to be studied; it is the process by which the program’s own principles propagate across domains. The four-level blindness framework provides a diagnostic tool applicable both to the systems the program studies and to the program itself.

14 Conclusion

This paper has established three principal results.

First, fractal pattern scaling—the application of a single generating rule across scales of varying complexity—is not a curious property of brains or natural geometries but a *structural necessity* for any resource-bounded system. It is the cheapest way to operate, and complex systems converge on it by constraint.

Second, this efficiency carries a systematic cost. When a pattern is transferred to a scale whose boundary conditions it cannot represent, the result is a pattern–boundary mismatch undetectable from within the system’s own operational logic. Feedback loops compound this blindness. We have identified four cumulative levels of structural blindness, each of which must be addressed sequentially.

Third, the phenomenon is substrate-independent. It occurs in physical systems (accretion), biological systems (immune response), cognitive systems (decision-making), and institutional systems (governance). The brain is not the origin of fractal pattern scaling; it is one instantiation among many. The study of this phenomenon is necessarily interdisciplinary: detecting cross-scale pattern transfer requires observation across domains, which no single discipline can provide.

The implications for practice are developed in the appendices. The implications for theory are that any account of complex-system pathology must begin by identifying the generating pattern, assessing its structure, and testing its applicability at each scale. Treating symptoms at individual scales, without diagnosing the generating pattern from which they arise, is the intellectual equivalent of pruning a fractal: the same structure will re-emerge from the same rule.

A Protocol A: Pattern Recognition

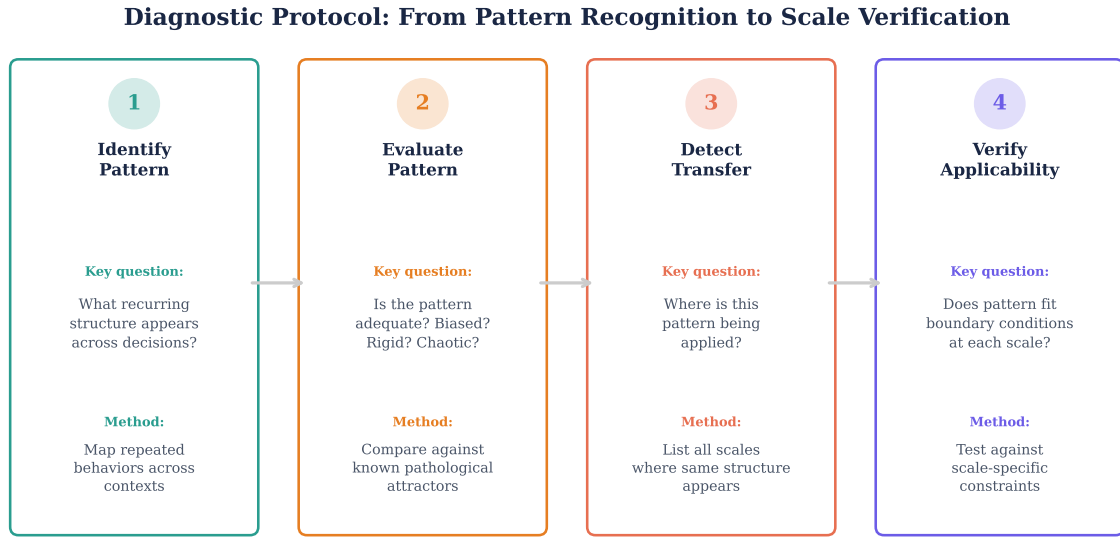


Figure 6: Four-step diagnostic protocol for identifying and evaluating operational patterns across scales. The protocol is applicable to individual, organizational, and disciplinary self-assessment.

The first diagnostic task is to identify the generating pattern. The following procedure applies to any reflexive system (individual, organization, research program):

Step 1: Cross-Context Inventory. List decisions or responses across at least three distinct operational contexts (scales). For an individual: daily routine, professional strategy, relationship management. For an organization: internal policy, market strategy, crisis response. For a scientific program: choice of formalism, experimental design, evaluation criteria.

Step 2: Content Abstraction. For each decision, strip away domain-specific content and record the *structural features*: Is the decision approach risk-averse or risk-seeking? Does it centralize or distribute? Does it prioritize speed or completeness? Does it rely on precedent or novelty?

Step 3: Invariant Identification. Compare structural features across contexts. Recurring features—those that remain stable when the domain changes—constitute the operational pattern P (Definition 3.2).

Step 4: Articulation. Formulate the identified pattern as a rule: “When faced with [structural feature of the environment], I/we [structural feature of the response].” This formulation should be abstract enough to apply across all inventoried contexts.

B Protocol B: Pattern Evaluation

Once the generating pattern is identified, it must be evaluated for structural adequacy.

Rigidity Assessment. Does the pattern allow variation, or does it force the same response regardless of environmental variation? An excessively rigid pattern will produce inadequate responses to novel situations.

Bias Detection. Does the pattern systematically favor certain types of outcomes? A pattern that consistently prioritizes short-term stability over long-term adaptation may be structurally biased toward rigidity.

Self-Confirmation Assessment. Does the pattern generate evidence for its own adequacy? Confirmation bias is not merely a cognitive error; it is a structural property of patterns that filter incoming information through the pattern's own categories.

Comparison with Known Pathological Attractors. The literature on cognitive biases [23], organizational pathologies [32], and dynamical system pathologies provides a reference set against which the identified pattern can be compared.

C Protocol C: Transfer Detection

The third diagnostic step identifies where and how the pattern is being transferred across scales.

Scale Mapping. List all scales at which the system operates. For an individual: micro (daily decisions), meso (career, relationships), macro (worldview, values). For an organization: operational, strategic, institutional. For a scientific discipline: technical, methodological, paradigmatic.

Transfer Identification. For each scale, ask: is the same pattern from Protocol A in operation here? The key diagnostic question is: "If I replaced the content of this decision with the content of a decision at a different scale, would the decision process be the same?"

Unconscious Transfer Detection. Many transfers are invisible to the system. Third-party assessment—an external auditor, a colleague from a different discipline, an outsider to the organization—is often required to detect transfers that the system's own feedback mechanisms cannot register (Proposition 3.3).

D Protocol D: Scale-Applicability Verification

The final step tests whether the identified pattern is appropriate for each scale at which it is being applied.

Boundary Condition Inventory. For each scale, list the constraints that are specific to that scale—constraints absent at other scales. These constitute the boundary set \mathcal{B}_σ (Definition 3.3).

Mismatch Testing. For each scale, ask: does the operational pattern generate states that violate the scale’s boundary conditions? Concrete diagnostic: “Can I identify a plausible scenario in which applying this pattern at this scale produces an outcome that is unrealizable, counterproductive, or catastrophic?”

Failure Mode Analysis. For each detected mismatch, characterize the failure mode. Is it gradual degradation (the pattern works poorly but stably), or catastrophic transition (the pattern works until a threshold is crossed, producing a qualitative regime change—the “black hole” scenario)?

Adaptive Modification. Where mismatch is detected, the pattern need not be replaced entirely. The goal is to identify the minimal modification that renders it compatible with the boundary conditions at the problematic scale, while preserving its effectiveness at scales where it works well.

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