Calorie Consumption During Bicycle Work: A Statistical Analysis of an Incomplete Dataset

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1 Introduction

This project aimed to examine data originally gathered by Macdonald (1914) and conveyed to us by Greenwood and TF (1918), consisting of observations on seven people performing work using a bicycle ergometer, although our current dataset appears to include extra values and data not found in Greenwood and TF (1918), though these values may indeed be present in Macdonald (1914), access to which could not be obtained in a timely manner. Hitherto it shall be assumed that every row in our dataset represents a separate individual, giving a total of 24 separate individuals across 24 rows. The dataset includes three separate measurements - weight of the individuals, calories per hour spent by individuals which serves as a measure of workout intensity, and calories spent during the task.

2 Methods and procedure

2.1 Data exploration

First we load and examine the data.

| ## | | weight | ${\tt calhour}$ | ${\tt calories}$ |
|----|---|--------|-----------------|------------------|
| ## | 1 | 43.7 | 19.0 | NA |
| ## | 2 | 43.7 | 43.0 | 279 |
| ## | 3 | 43.7 | 56.0 | 346 |
| ## | 4 | 54.6 | 13.0 | NA |
| ## | 5 | 54.6 | 19.0 | NA |
| ## | 6 | 54.6 | 43.0 | 280 |
| ## | 7 | 54.6 | 56.0 | 335 |

```
## 8
        55.7
                 13.0
                            NA
## 9
        55.7
                 26.0
                           212
## 10
        55.7
                 34.5
                           244
## 11
        55.7
                 43.0
                           285
## 12
        58.8
                 13.0
                            NA
## 13
        58.8
                 43.0
                           298
## 14
        60.5
                 19.0
                            NA
## 15
        60.5
                 43.0
                           317
## 16
        60.5
                 56.0
                            347
## 17
        61.9
                 13.0
                            NA
## 18
        61.9
                 19.0
                           216
## 19
        61.9
                 34.5
                           265
## 20
        61.9
                 43.0
                           306
## 21
        61.9
                 56.0
                           348
## 22
        66.7
                 13.0
                            NA
## 23
                            324
        66.7
                 43.0
## 24
        66.7
                 56.0
                           352
```

And the summary:

| ## | weight | calhour | calories |
|----|--------------|--------------|-------------|
| ## | Min. :43.7 | Min. :13.0 | Min. :212 |
| ## | 1st Qu.:54.6 | 1st Qu.:19.0 | 1st Qu.:276 |
| ## | Median:58.8 | Median:38.8 | Median:302 |
| ## | Mean :57.5 | Mean :34.0 | Mean :297 |
| ## | 3rd Qu.:61.9 | 3rd Qu.:43.0 | 3rd Qu.:338 |
| ## | Max. :66.7 | Max. :56.0 | Max. :352 |
| ## | | | NA's :8 |

Here are some descriptive statistics.

Some exploratory statistics for all individuals:

| ## | | weight | calhour | calories |
|----|--------------|-----------|----------|-----------|
| ## | nbr.val | 24.0000 | 24.0000 | 16.0000 |
| ## | nbr.null | 0.0000 | 0.0000 | 0.0000 |
| ## | nbr.na | 0.0000 | 0.0000 | 8.0000 |
| ## | min | 43.7000 | 13.0000 | 212.0000 |
| ## | max | 66.7000 | 56.0000 | 352.0000 |
| ## | range | 23.0000 | 43.0000 | 140.0000 |
| ## | sum | 1381.0000 | 817.0000 | 4754.0000 |
| ## | median | 58.8000 | 38.7500 | 302.0000 |
| ## | mean | 57.5417 | 34.0417 | 297.1250 |
| ## | SE.mean | 1.3453 | 3.3396 | 11.4669 |
| ## | CI.mean.0.95 | 2.7829 | 6.9085 | 24.4412 |
| ## | var | 43.4338 | 267.6721 | 2103.8500 |
| ## | std.dev | 6.5904 | 16.3607 | 45.8677 |
| ## | coef.var | 0.1145 | 0.4806 | 0.1544 |

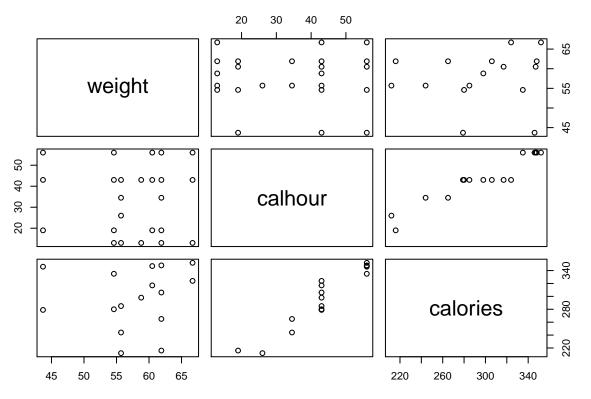


Figure 1: Summary plots for the dataset.

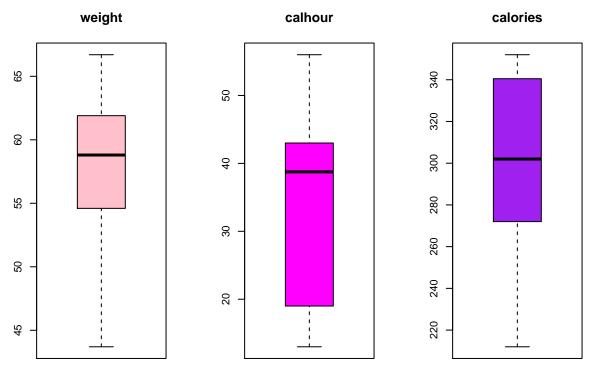
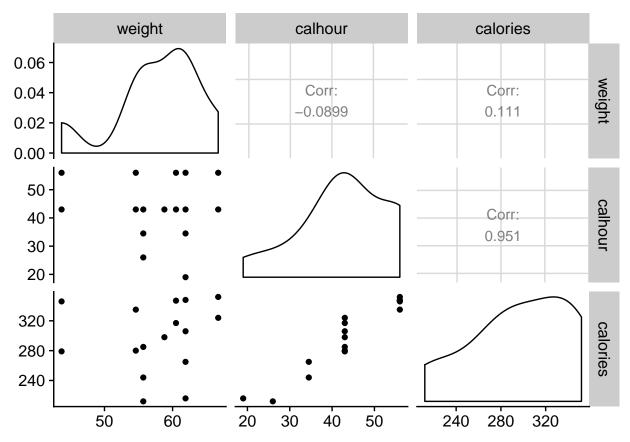
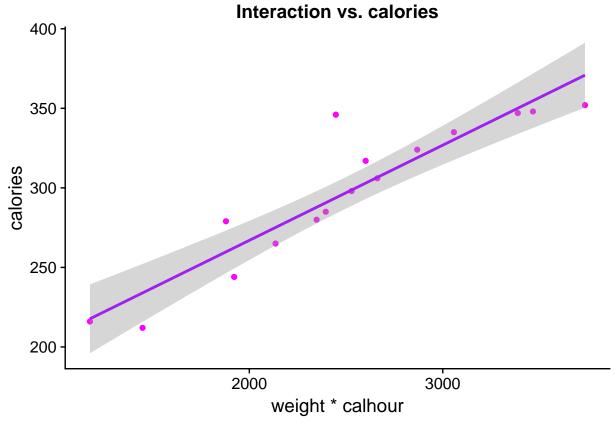


Figure 2: Boxplots



Here we see that there is a strong positive correlation between callour and calories (0.95). Whereas, a slightly positive correlation between weight and calories (0.11). Scatterplot with interaction and calories:



Calculating the correlation if we exclude missing data:

```
## [1] 0.9511
```

Testing the population correlation $L_0: correlation = 0; H1: correlation \neq 0; 95\%CI.$

```
##
## Pearson's product-moment correlation
##
## data: muscledata_edit$calhour and muscledata_edit$calories
## t = 12, df = 14, p-value = 2e-08
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.8615 0.9832
## sample estimates:
## cor
## 0.9511
```

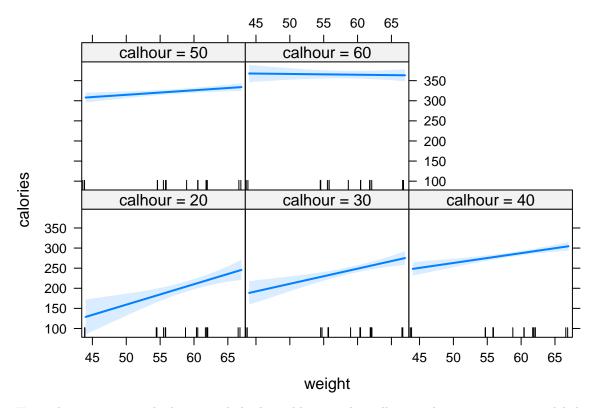
This saying that there is no direct relation between weights and calories.

Let's try to explain heat production in function of weight and intensity of the workout, whilst allowing for interaction of the 2 predictors (whilst increasing intensity of workout, a higher weight could result in a different speed of heat production increase):

```
##
## Call:
## lm(formula = calories ~ weight + calhour + weight * calhour,
## data = muscledata_edit)
##
## Residuals:
```

```
##
      Min
              10 Median
                             3Q
                                   Max
  -12.48
           -5.70
                  -1.04
                           2.39
                                 16.95
##
##
##
  Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
  (Intercept)
                  -330.884
                               124.674
                                         -2.65
                                                0.02102 *
##
## weight
                     7.728
                                 2.106
                                          3.67
                                                0.00321 **
## calhour
                    11.787
                                 2.548
                                          4.63
                                                0.00058 ***
  weight:calhour
                    -0.132
                                 0.043
                                         -3.07
                                                0.00977 **
##
## Signif. codes:
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9.12 on 12 degrees of freedom
## Multiple R-squared: 0.968, Adjusted R-squared: 0.96
## F-statistic: 123 on 3 and 12 DF, p-value: 2.89e-09
```

weight*calhour effect plot



Using the summary method, we conclude that adding weight, calhour and interaction to a model that already has the other possible components results in a significant increase in explanatory power. (note to group: was explained in last 10 slides of chapter 1, he'll probably ask about this if we don't mention it since using the anova method results in a different interpretation).

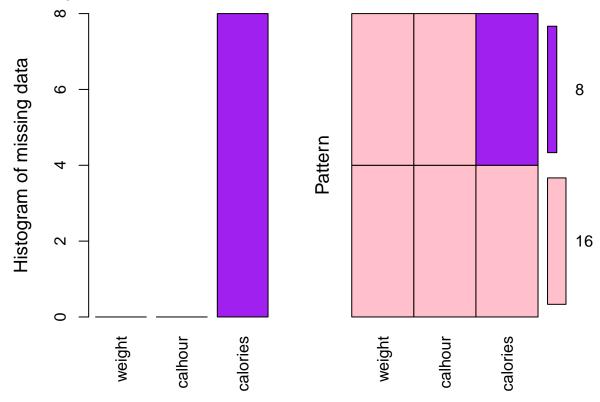
```
##
## Pearson's product-moment correlation
##
## data: muscledata_edit$weight and muscledata_edit$calories
## t = 0.42, df = 14, p-value = 0.7
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
```

```
## -0.4068 0.5753
## sample estimates:
## cor
## 0.1114
```

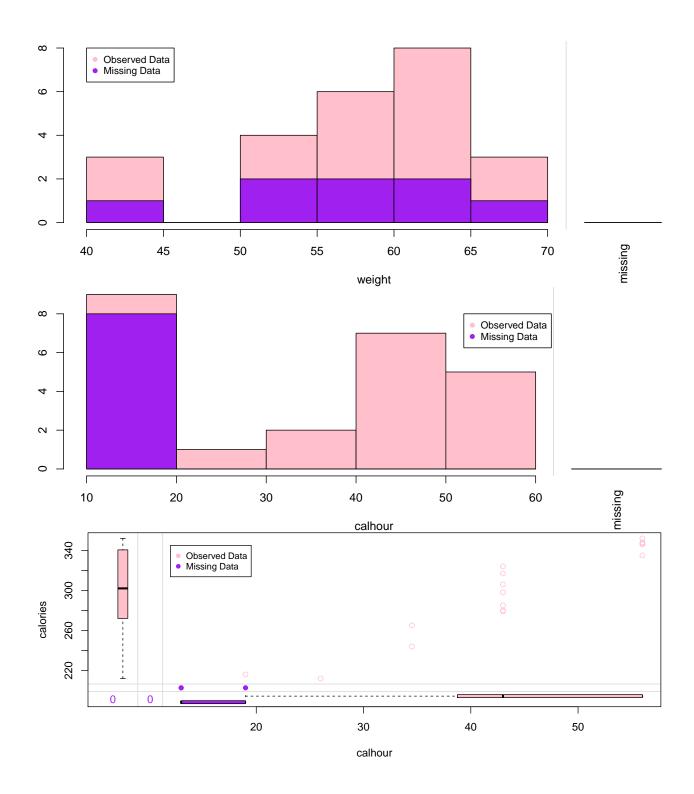
2.2 Missing data exploration

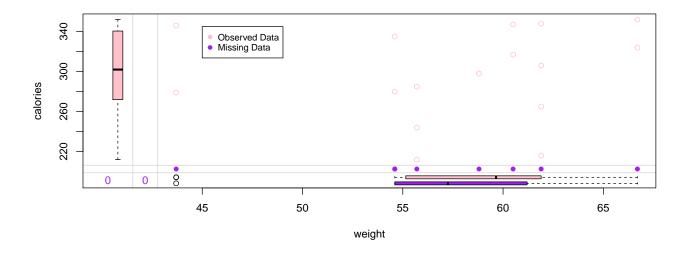
Let's explore the missingness of our data:

All missing is in calories.



In second and third we see that the missing data is distributed among weights but it is biased in calhour. The missing data is present in the lower values of calhour. We assume that this might be because of the machine that is not efficiently working with such small heat produced by the participants. This suggests MAR as a plausible missingness mechanism. Boris explain what is MAR to the client.





2.3 Complete case analysis

First we need to select the best linear model to use for CC - we can do this using stepwise AIC.

Using the stepwise method, we conclude that adding weight, calhour and interaction to a model that already has the other possible components results in a significant increase in explanatory power. (note to group: was explained in last 10 slides of chapter 1, he'll probably ask about this if we don't mention it since using the anova method reults in a different interpretation).

```
## Start: AIC=123.4
##
   calories ~ 1
##
##
             Df Sum of Sq
                                   AIC
                             RSS
## + calhour
                    28544
                           3014 87.8
##
  <none>
                           31558 123.4
  + weight
                      392 31166 125.2
##
## Step: AIC=87.81
  calories ~ calhour
##
             Df Sum of Sq
##
                             RSS
                                   AIC
## + weight
                     1234
                            1780
                                  81.4
##
  <none>
                            3014
                                  87.8
##
   - calhour
                    28544 31558 123.4
             1
##
## Step: AIC=81.39
## calories ~ calhour + weight
##
##
                    Df Sum of Sq
                                    RSS
                                          AIC
                              782
                                    998
                                         74.1
## + weight:calhour
  <none>
                                   1780
                                         81.4
  - weight
                             1234
                                   3014
                                         87.8
##
                     1
##
   - calhour
                      1
                            29386 31166 125.2
##
## Step: AIC=74.13
## calories ~ calhour + weight + calhour:weight
##
##
                    Df Sum of Sq RSS AIC
## <none>
                                   998 74.1
```

```
## - calhour:weight 1 782 1780 81.4
```

Thus we deduce that the best-fitting model is:

```
calories_i = \beta_0 + \beta_1 * weight_i + \beta_2 * calhour_i + \beta_3 * (weight_i * calhour_i) + \epsilon_i
```

The R summary for this model:

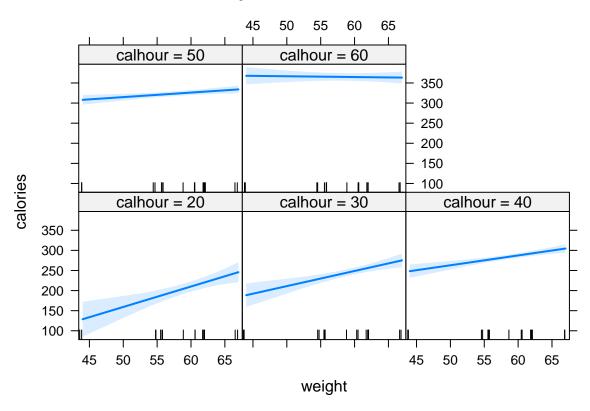
```
##
## Call:
## lm(formula = calories ~ weight + calhour + weight * calhour,
##
      data = muscledata_edit)
## Residuals:
     Min
             1Q Median
                           3Q
                                 Max
## -12.48 -5.70 -1.04
                         2.39
                               16.95
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 -330.884
                             124.674
                                       -2.65 0.02102 *
                    7.728
                               2.106
                                        3.67 0.00321 **
## weight
## calhour
                   11.787
                               2.548
                                        4.63 0.00058 ***
## weight:calhour
                   -0.132
                               0.043
                                       -3.07 0.00977 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 9.12 on 12 degrees of freedom
## Multiple R-squared: 0.968, Adjusted R-squared: 0.96
## F-statistic: 123 on 3 and 12 DF, p-value: 2.89e-09
```

Let's try to explain heat production in function of weight and intensity of the workout, whilst allowing for interaction of the 2 predictors (whilst increasing intensity of workout, a higher weight could result in a different speed of heat production increase):

This plot telling us that there is a decrease in coeficient between calhour and calories as calhour is increasing.

```
##
## Call:
## lm(formula = calories ~ weight + calhour + weight * calhour,
##
       data = muscledata edit)
## Residuals:
     Min
             1Q Median
                           3Q
                                 Max
## -12.48 -5.70 -1.04
                         2.39
                               16.95
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 -330.884
                             124.674
                                       -2.65 0.02102 *
                    7.728
                               2.106
                                        3.67 0.00321 **
## weight
## calhour
                   11.787
                               2.548
                                        4.63 0.00058 ***
                               0.043
                                       -3.07 0.00977 **
## weight:calhour
                   -0.132
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 9.12 on 12 degrees of freedom
## Multiple R-squared: 0.968, Adjusted R-squared: 0.96
## F-statistic: 123 on 3 and 12 DF, p-value: 2.89e-09
```

Complete Case Effects Plot



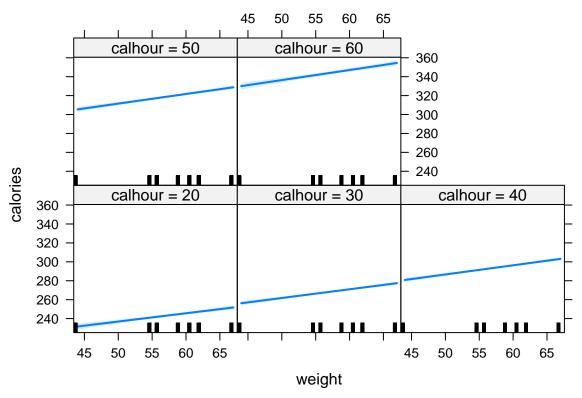
2.4 Multiple imputation analysis

Put in a short desc of multiple imputation here

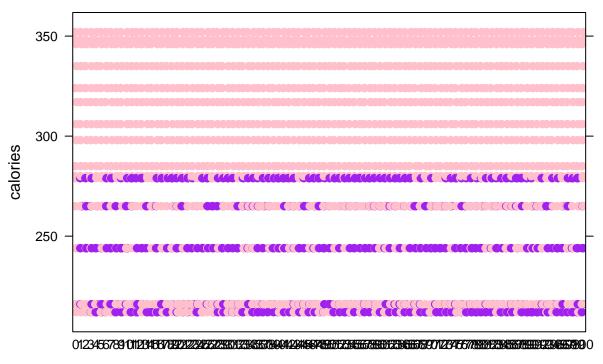
First we use the PMM method:

```
##
                                                   df Pr(>|t|)
                                                                   lo 95
                         est
                                    se
## (Intercept)
                  1.485e+02 172.04352 0.86318 7.765
                                                        0.4139 -250.3258
## weight
                  7.753e-01
                               2.94850 0.26293 7.795
                                                        0.7994
                                                                 -6.0552
## calhour
                                                        0.5665
                                                                 -6.2309
                  2.243e+00
                               3.77804 0.59377 9.534
## weight:calhour 4.832e-03
                               0.06475 0.07463 9.561
                                                        0.9420
                                                                 -0.1403
##
                                   fmi lambda
                    hi 95 nmis
## (Intercept)
                  547.336
                             NA 0.6449 0.5639
## weight
                    7.606
                              0 0.6433 0.5622
## calhour
                   10.717
                              0 0.5518 0.4667
## weight:calhour
                    0.150
                             NA 0.5504 0.4653
```

PMM Effects Plot



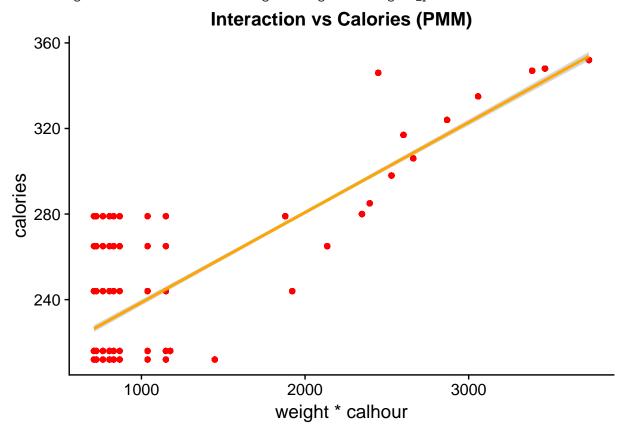
Original data vs. generated data (PMM)



Imputation number

Warning: Removed 8 rows containing non-finite values (stat_smooth).

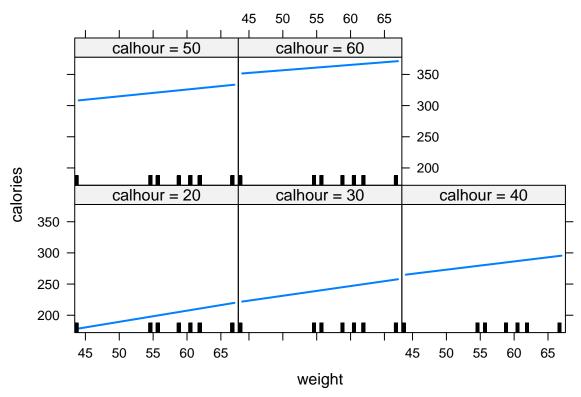
Warning: Removed 8 rows containing missing values (geom_point).



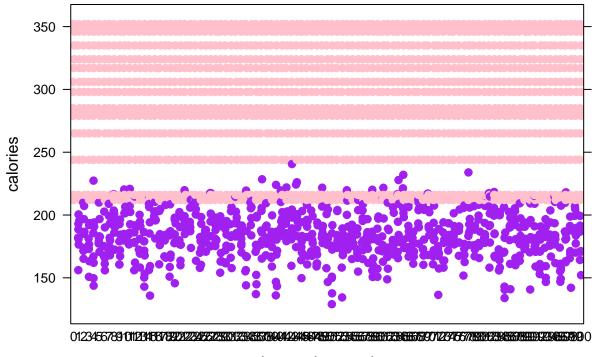
What if we use the Bayesian norm method?

```
##
                       est
                                  se
                                            t
                                                 df Pr(>|t|)
                                                                 lo 95
                                                                          hi 95
## (Intercept)
                  -6.58574 86.98470 -0.07571 6.746
                                                     0.94184 -213.8511 200.680
## weight
                   2.24900
                            1.44719
                                     1.55405 7.189
                                                     0.16300
                                                               -1.1549
                                                                          5.653
## calhour
                   5.33763
                            1.88390 2.83329 8.505
                                                     0.02073
                                                                 1.0378
                                                                          9.637
## weight:calhour -0.02315
                            0.03145 -0.73598 8.997
                                                     0.48049
                                                                -0.0943
                                                                          0.048
##
                  nmis
                          fmi lambda
## (Intercept)
                    NA 0.6985 0.6206
## weight
                     0 0.6752 0.5959
## calhour
                     0 0.6060 0.5231
## weight:calhour
                    NA 0.5800 0.4960
```

NORM effects plot



Original data vs. generated data (NORM)

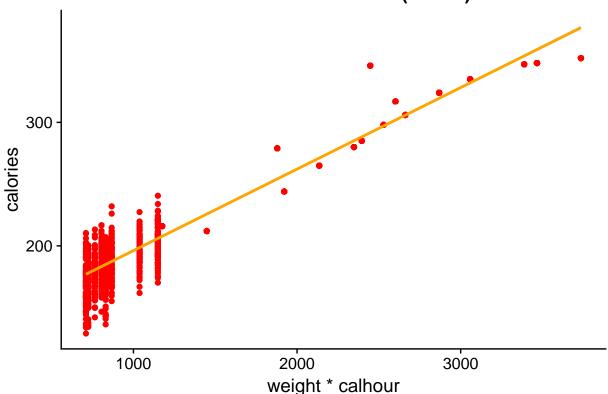


Imputation number

Warning: Removed 8 rows containing non-finite values (stat_smooth).

Warning: Removed 8 rows containing missing values (geom_point).

Interaction vs Calories (NORM)

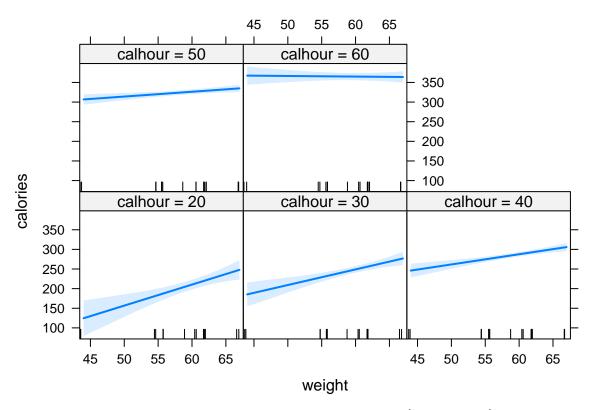


2.5 IPW analysis

```
## Warning: In lm.fit(x, y, offset = offset, singular.ok = singular.ok, ...) :
    extra argument 'family' will be disregarded
##
## Call:
## lm(formula = r ~ calhour, data = IPWanal_muscledata, family = binomial)
##
## Residuals:
##
      Min
              1Q Median
                            3Q
                                  Max
  -0.299 -0.203 -0.153 0.115 0.701
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -0.1646
                            0.1318
                                     -1.25
                                               0.22
                 0.0244
                            0.0035
                                      6.97 5.4e-07 ***
## calhour
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.275 on 22 degrees of freedom
## Multiple R-squared: 0.688, Adjusted R-squared: 0.674
## F-statistic: 48.6 on 1 and 22 DF, p-value: 5.37e-07
##
```

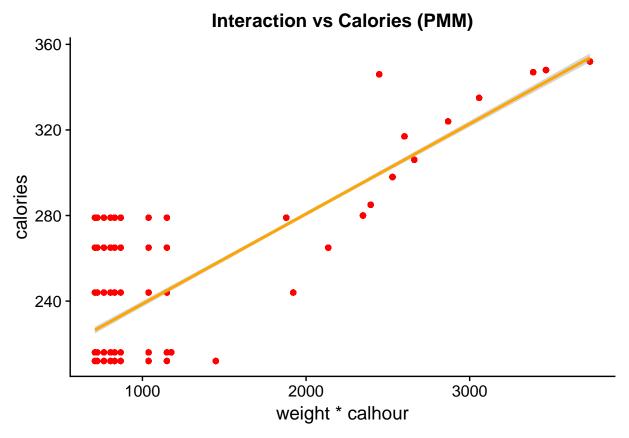
```
## Call:
## lm(formula = calories ~ weight + calhour + weight * calhour,
      data = IPWanal_muscledata, weights = muscledata$w)
##
##
  Weighted Residuals:
     Min
             1Q Median
##
                            3Q
                                  Max
   -91.0 -40.5 -11.0
                          20.1
                               129.8
##
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
  (Intercept)
                  -353.7928
                              129.1577
                                        -2.74 0.01796 *
                                         3.74 0.00283 **
## weight
                    8.1131
                                2.1698
                                2.6513
                                         4.58 0.00064 ***
## calhour
                   12.1321
## weight:calhour
                                0.0445
                                        -3.10 0.00926 **
                   -0.1378
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 68.2 on 12 degrees of freedom
     (8 observations deleted due to missingness)
## Multiple R-squared: 0.97, Adjusted R-squared: 0.962
## F-statistic: 128 on 3 and 12 DF, p-value: 2.25e-09
```

IPW effects plot



Warning: Removed 8 rows containing non-finite values (stat_smooth).

Warning: Removed 8 rows containing missing values (geom_point).



We can take a look at the AIC values of the complete case and IPW models to compare:

[1] 121.5

[1] 121.1

3 Discussion

Due to the NA values, we conducted a full model analysis with a complete case and three NA comparsions (you can write this better) models. Beacuse the NA values are not evenly distrubited among calhour, we decided to try different approaches for NA handling.

PMM generates the data according to the pattern in the observed ones. in our cases, the data is discreted by the body weight, so pmm generated the data discreted as well. in norm method, the data is generated based on normal distribution.

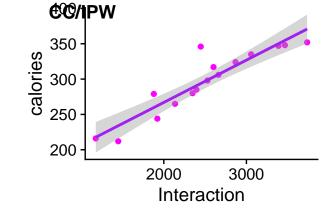
In the following three graphs we can see that the behaviour of the interaction factor vs. calories is similar for the cc model and the two models created under MI. This three graphs are relevant to see how the two different methods chose in MI generate the new values.

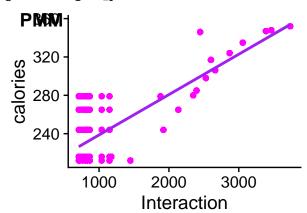
IPW assigns weights to each observation so it uses already available ones. Since all calories values in calhour 13 are missing, the method cannot assign a weight, no value can represent this group, other missing values fall into calhour 19, while a higher weight is assigned to the only available data in calhour 19, so the only difference between cc and ipw is only based on this value, thus the graph is the mostly the same for both CC and IPW and that's why we chose to represent both with the same graph.

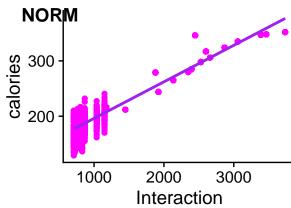
Warning: Removed 8 rows containing non-finite values (stat_smooth).

Warning: Removed 8 rows containing missing values (geom_point).

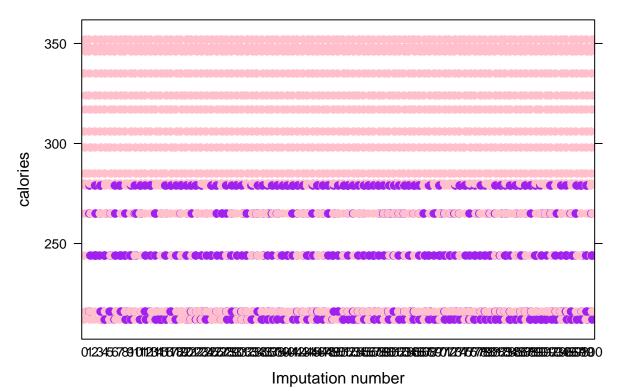
- ## Warning: Removed 8 rows containing non-finite values (stat_smooth).
- ## Warning: Removed 8 rows containing missing values (geom_point).



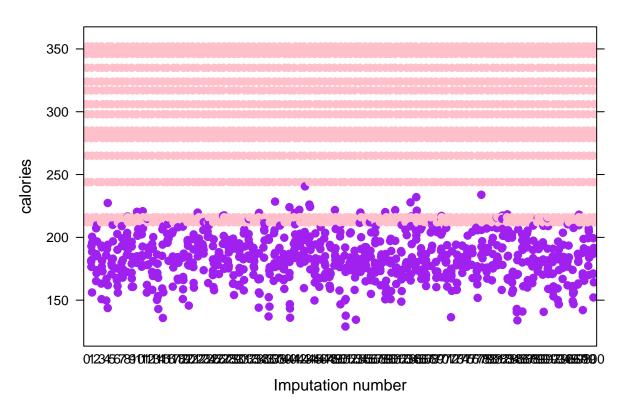




Original data vs. generated data (PMM)

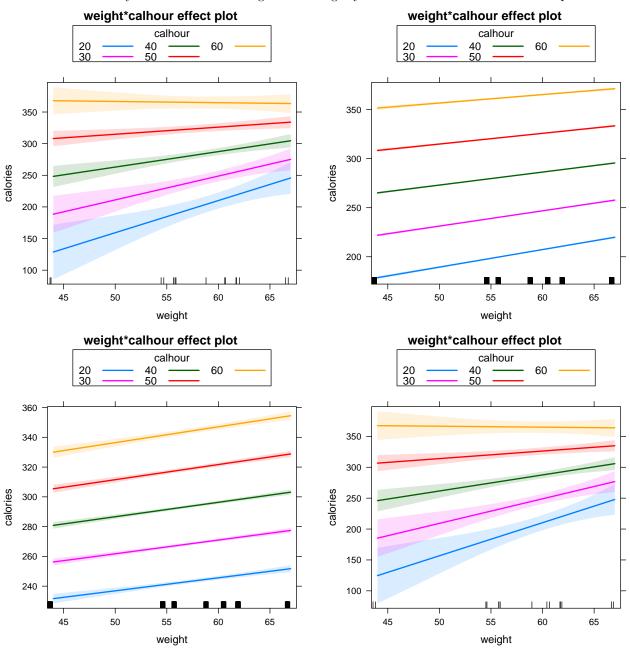


Original data vs. generated data (NORM)



Because there are no calorie values for calhour 13, there are no data to atributte weights to. So, IPW will

make a difference only for calhour 19. This gives us a slightly better model with IPW than complete case.



4 Conclusion

In our case, IPW doesn't come as an improvement in comparison to the CC model. and using standard error

The missing data is correlated with the calhour - intensity of the exercise - hence there is something wrong with the experimental design. Such as the way they measured heat production, so they could not accurately measure calorie burning. While we have no data for low calhour values, attributing weights to the values we have is not workable for the 13 calhour data point. That being said, the MI approach provides a more robust estimates for missing data.

References

Greenwood, M, and Captain RAMC TF. 1918. "On the Efficiency of Muscular Work." $Proc.\ R.\ Soc.\ Lond.\ B$ 90 (627). The Royal Society:199–214.

Macdonald, JS. 1914. "The Mechanical Efficiency of Man." Proc. Phys. Soc. In Journ. Of Physiol 48.