
CSC172 PROJECT 3

POINT LOCATION

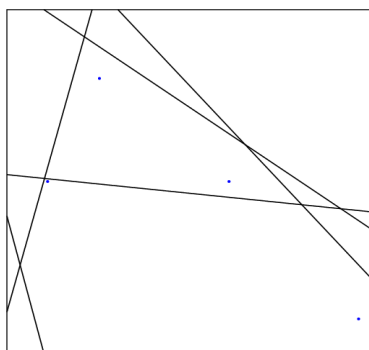
1 Introduction

Write a program to solve the *point location problem* among line arrangements in the plane¹. Your program should build a data structure from a set of lines that allows it to, when given a pair of points, quickly determine whether any of the lines goes between the two points. The brute-force solution to this problem is to test that both points are on the same side of each of the N lines. The goal of this assignment is to build a data structure that cuts the number of lines to be tested down to be proportional to $\log N$.

Input format. For simplicity, you may assume that all the lines cross the unit square (where both coordinates are between 0 and 1), and that you only have to work with points and line segments in that region. Use the following input format:

```
5
0.00 0.12 0.23 1.00
1.00 0.41 0.00 0.52
1.00 0.20 0.30 1.00
0.00 0.40 0.10 0.00
1.00 0.35 0.10 1.00

0.25 0.80 0.60 0.50
0.95 0.10 0.11 0.50
```



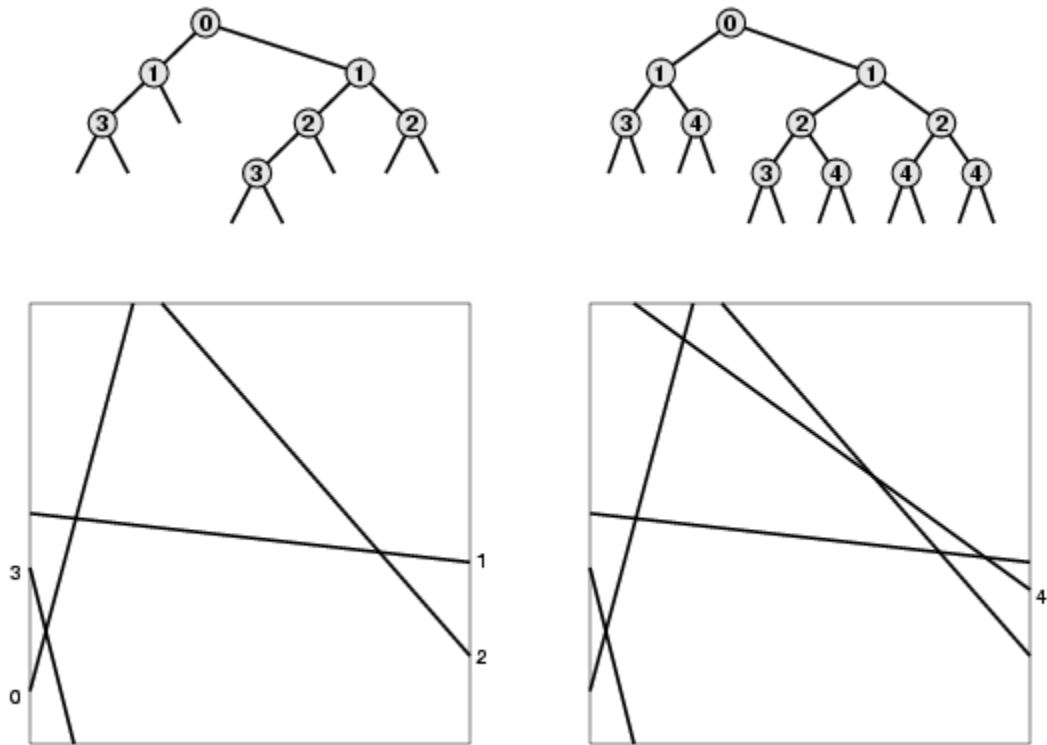
The input is begins with an integer N , then N lines, each defined by four real numbers that give the endpoints of the line segments. Since they represent intersections with the edge of the unit square, each line segment endpoint has at least one coordinate with value 0 or 1. Following the N lines is a sequence of pairs of points that you will be evaluating to see if they're in the same region or not.

You do not have to worry about handling all possible degenerate cases, but you shouldn't completely ignore them, either. Certainly you will want to get your program working on straightforward inputs before worrying about degenerate examples such as three lines intersecting in a point, or where precision in the calculation affects a decision. In your design, you should be cognizant of places where your program might be exposed to trouble for a degenerate case, whether or not you get around to fixing it up. Include test files of your own design and describe the situations they test in your README file.

¹ This assignment originally by R. Sedgewick - <http://www.cs.princeton.edu/courses/archive/spr07/cos226/assignments/locate.html>

2 Binary Trees

An *arrangement* is the planar subdivision defined by the lines. The diagram below is the arrangement for the set of lines given above. Every point in the unit square falls into some region; every region is bounded by some subset of the line segments. Your task is to be able to determine quickly whether or not two given input points fall into the same region or not.



One way to solve this problem is to build a binary tree with internal nodes corresponding to line segments and external nodes corresponding to regions in the plane, as shown in the example. This is similar to a 2D tree. A search in this tree involves comparing a point against the line segment at the root, then going left if it is on one side and right if it is on the other side. If the search for two points ends up at the same external node, they must be in the same region. There are at most N^2 regions and one external node corresponding to each region, so we expect that the time should be proportional to $\log(N^2) = 2 \log N$ for random data. Figuring out how to build this tree for arbitrary lines is the main challenge of this assignment.

3 Details

You should implement your own binary tree class. It is ok to use code from the book if you give credit to the author in your writeup.

Getting started. You will need some geometry primitives: a test whether a point is on one side of a line or the other and a routine to compute the intersection point of two lines. The former is essentially the `ccw()` function on the next page.

```

int ccw(Point p0, Point p1, Point p2) {
    double dx1 = p1.x - p0.x;
    double dy1 = p1.y - p0.y;
    double dx2 = p2.x - p0.x;
    double dy2 = p2.y - p0.y;
    if (dx1*dy2 > dy1*dx2) return COUNTERCLOCKWISE;
    else if (dx1*dy2 < dy1*dx2) return CLOCKWISE;
    else if ((dx1*dx2 < 0) || (dy1*dy2 < 0)) return CLOCKWISE;
    else if ((dx1*dx1+dy1*dy1) < (dx2*dx2+dy2*dy2)) return COUNTERCLOCKWISE;
    else return COLINEAR;
}

```

The latter requires some high-school geometry, coupled with some computer-science considerations having to do with precision and degenerate cases (lines consisting of a single point, parallel lines, and so forth).

Output. For each pair of query points, indicate whether or not they are separated by a line, and if they are, print out one such line to the console. Also, instrument your program to count the number of external nodes and the average path length (external path length divided by number of external nodes) for the trees that you construct. Include these numbers (for various test cases), and a discussion of how they grow, in your writeup.

4 Hand In

Hand in the source code from this lab at the appropriate location on the Blackboard system at my.rochester.edu. You should hand in a single compressed/archived (i.e. “zipped” file that contains the following.)

1. A plain text file named README that includes your contact information, a detailed synopsis of how your code works and any notable obstacles you overcame, and a list of all files included in the submission.
2. Source code files (you may decide how many you need) representing the work accomplished in this project. All source code files should contain author identification in the comments at the top of the file.
3. A plain text file named OUTPUT that includes author information at the beginning and shows the compile and run steps of your code. The best way to generate this file is to cut and paste from the command line.
4. Any additional files containing extra test cases and your program's corresponding output. These cases should be described in your README so the grader knows what you were testing and what the expected results were.

5 Grading

60% Functionality

20% Testing (correctness)

10% Code Style

10% README

Up to 15% extra credit is available if you make a graphical interface for the application that displays the given lines and lets the user select points to compare with their mouse.