

Studio di funzione

studiare le seguenti funzioni razionali

1	$y = x^3 + 2x^2 - 3$	2	$y = \frac{x-3}{x^2-4}$	3	$y = \frac{x^2}{x-2}$
4	$y = \frac{x^2-3}{x^2-1}$	5	$y = x(x-2)^2$	6	$y = \frac{2}{2+x^2}$
7	$y = \frac{x}{x^2-3}$	8	$y = \frac{x^3}{x^2-4}$	9	$y = \frac{2x^2}{3+x^2}$
10	$y = \frac{x}{x^2-9}$	11	$y = \frac{3x}{x^2+x-2}$	12	$y = x^3 - 2x^2 + x + 2$
13	$y = 2x^3 - 2x^2 + x$	14	$y = \frac{2x^2+1}{x}$	15	$y = \frac{(x-2)(x+1)}{x(x+3)}$
16	$y = \frac{x^3-2x}{x^2-6}$	17	$y = -x^3 + 2x^2 + 3x - 2$	18	$y = \frac{3-x}{x^2-7x+10}$
19	$y = -2x^4 - x^3 + 2x^2 - 2$	20	$y = \frac{x^2-2}{x^2+2}$	21	$y = \frac{x^3-8}{2x^3+3}$
22	$y = \frac{x+3}{x^2-1}$	23	$y = x^3 - x + 1$	24	$y = \frac{x^2-5x+6}{x^2-2}$
25	$y = \frac{x^2+1}{x-5}$	26	$y = \frac{x^2+3x-2}{2x^2-x-5}$	27	$y = \frac{x^2+4}{(x-1)^2}$

studiare le seguenti funzioni irrazionali

28	$y = -2x - \sqrt{4-x^2}$	29	$y = \sqrt{3x-x^2}$	30	$y = \sqrt{3x-5}$
31	$y = \sqrt[3]{x^3-2x}$	32	$y = x\sqrt{3-x}$	33	$y = \frac{\sqrt{x^2-1}}{x^2+3}$
34	$y = \frac{x+3}{\sqrt{x^2-1}}$	35	$y = x-1-\sqrt{x^2-3x+1}$	36	$y = \frac{x-1}{\sqrt{x^2-2x+5}}$
37	$y = \sqrt{x^2-2x}$	38	$y = \sqrt[3]{x^2-4} - 2$	39	$y = \frac{x-2}{\sqrt{x^2-2}}$
40	$y = 3x + 2\sqrt{x^2-4}$	41	$y = \frac{3}{\sqrt{2x^2-1}}$	42	$y = x\sqrt{1-x^2}$
43	$y = \sqrt{\frac{3+x^2}{x^2-4}}$	44	$y = x^2\sqrt{3-x}$	45	$y = 3 - \sqrt[3]{1-2x}$
46	$y = x - 3\sqrt{x+4}$	47	$y = \frac{\sqrt{2-x^2}-1}{\sqrt{2-x^2}}$	48	$y = \sqrt{\frac{x+1}{x^2-1}}$
49	$y = \frac{x+2}{\sqrt{x+3}}$	50	$y = \sqrt{x(x^2-1)}$	51	$y = 3x - \sqrt{x^2-1}$

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52	$y = \frac{\sqrt{x+3}}{x}$	53	$y = \sqrt[3]{x+4} + \frac{2}{x}$	54	$y = 3\sqrt{x^2 - 4} + 1$
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studiare le seguenti funzioni goniometriche

55	$y = \sin x + \cos^2 x$ in $]0, 2\pi[$	56	$y = \frac{2\cos^2 x - 1}{\cos x}$ in $]-\pi, \pi[$	57	$y = \arcsen \frac{x^2 - 9}{x^2 - 4}$
58	$y = \frac{\operatorname{tg} x - 1}{\sqrt{3}\operatorname{tg} x - 1}$	59	$y = \sqrt{3}\sin x + \cos x$	60	$y = \cos^3 x + \sin^3 x$ in $]0, 2\pi[$
61	$y = \cos^2 x - \cos x$	62	$y = \frac{\arccos(x^2 - 1)}{x^2 - 4}$	63	$y = \frac{2\sin^2 x - 1}{\sqrt{2}\sin x - 1}$
64	$y = \operatorname{arctg} \frac{x+3}{x-1}$	65	$y = \frac{1 - \sin 2x}{\cos 2x}$	66	$y = \sin\left(x + \frac{\pi}{3}\right) + \cos\left(x - \frac{\pi}{6}\right)$
67	$y = \frac{1 - \sin x}{1 + \cos x}$	68	$y = \frac{2\operatorname{tg} x}{1 - \operatorname{tg}^2 x}$	69	$y = 2\sin(x^2)$ in $[-\sqrt{2\pi}, \sqrt{2\pi}]$
70	$y = \arccos \frac{x^2 - 9}{x^2 - 4}$	71	$y = \cos x + \sin^2 x$ in $]0, 2\pi[$	72	$y = \frac{\sin^2 x}{1 - 2\sin x}$
73	$y = \operatorname{arctg} \sqrt{x^2 - 9}$	74	$y = \frac{\operatorname{tg} x}{1 - \sqrt{3}\operatorname{tg} x}$	75	$y = \arccos \frac{x^2 - 1}{x^2 - 4}$
76	$y = \frac{1 - \sin x}{1 - \cos x}$	77	$y = \frac{\cos x - \sin x}{\sin x + \cos x}$	78	$y = \frac{2\sin^2 x - 1}{\sin x}$ in $]-\pi, \pi[$
79	$y = \arcsen \frac{x^2 - 1}{x^2 - 4}$	80	$y = \frac{1 + \cos x}{\cos x}$	81	$y = \frac{\arcsen(x^2 - 1)}{x^2 - 4}$

studiare le seguenti funzioni esponenziali e logaritmiche

82	$y = e^{\frac{2x-1}{x}}$	83	$y = x \cdot \ln x$	84	$y = \log_{\frac{1}{2}} \frac{x^2 - 4}{x^2 - 1}$
85	$y = \frac{\ln x}{x^2}$	86	$y = x^2 \ln x$	87	$y = \frac{\ln x - 2}{2\ln x + 1}$
88	$y = 2^{\frac{2x-1}{x^2}}$	89	$y = x^2 e^x$	90	$y = e^{-2x^2}$
91	$y = x e^{-\frac{1}{x}}$	92	$y = \frac{2e^x - 1}{e^x + 2}$	93	$y = \log_{\frac{1}{4}}(1 - x^2)$
94	$y = \frac{x}{\ln x}$	95	$y = \ln^2(x + 2)$	96	$y = \frac{3x - 2}{e^x}$
97	$y = x e^{-x^2}$	98	$y = \frac{x}{1 - 2^{\frac{1}{x}}}$	99	$y = 3^{\frac{x-1}{x+1}}$
100	$y = \frac{1}{3} \ln^2 x - \ln x$	101	$y = \frac{1}{\log_2(x + 3)}$	102	$y = \frac{\log_3(x + 1) - 3}{\log_3(x + 3)}$

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103	$y = xe^{\frac{1}{x}}$	104	$y = \log_3 \frac{x-3}{x^2-4}$	105	$y = \sqrt{\ln x(x+3) }$
106	$y = xe^x$	107	$y = \frac{e^x}{x+2}$	108	$y = \frac{1}{\left(\frac{1}{2}\right)^x - 2}$

studiare le seguenti funzioni con i valori assoluti

109	$y = x-2 - x+1 $	110	$y = \frac{2- x }{2+ x }$	111	$y = \sqrt{ x^2-2x -1} + 2$
112	$y = \log_{\frac{1}{2}} 1-2x+3x^2 $	113	$y = \frac{ \operatorname{sen}x }{1-\cos x}$	114	$y = x-1 e^{- x-1 }$
115	$y = (x^2-4)\ln x^2-4 $	116	$y = \frac{3}{2x- x^2-1 }$	117	$y = \frac{2x^2-3 x }{ x-2 }$
118	$y = \ln\frac{1- x }{1+ x }$	119	$y = \frac{x^2}{2} + \ln x+1 $	120	$y = 2 x + -x^2-x+6 $

esercizi di riepilogo

121	$y = e^{\operatorname{arctg}\frac{1}{x^2-1}}$	122	$y = \frac{1+\ln x}{1-\ln x}$	123	$y = \ln(1+e^x)$
124	$y = \frac{2x}{\sqrt{x^2-4}}$	125	$y = \frac{x^2-1}{x^2+1}$	126	$y = \frac{x^2}{e^{(x+1)}}$
127	$y = \sqrt{\frac{x}{x^3-1}}$	128	$y = \frac{\ln x-1 }{x^2-4}$	129	$y = \ln\frac{5}{\operatorname{arctg} x-1 }$
130	$y = \operatorname{arcsen}\frac{x^2-2}{x^2-1}$	131	$y = e^{\sqrt{\frac{x+2}{x}}}$	132	$y = \log_{\frac{1}{2}}\frac{x}{x-1}$
133	$y = \ln\frac{3}{\operatorname{arctg} x+1 }$	134	$y = x\cos x - \operatorname{sen}x$	135	$y = \left \frac{x^3-x}{x^2+1}\right $
136	$y = xe^{-2x}$	137	$y = \sqrt{\frac{x+2}{x \cdot 2^x}}$	138	$y = \sqrt{1 - \log_3(1+x)}$
139	$y = x^2 - 4\ln x+1 $	140	$y = 2^x + 2^{-x}$	141	$y = e^{\frac{2x^2-5}{ x -2}}$
142	$y = \ln x+3x^2 $	143	$y = x^2 e^{ x+1 }$	144	$y = \frac{2\operatorname{sen}x}{\operatorname{sen}^2 x - \cos^2 x}$
145	$y = \operatorname{arctg}\frac{1}{\ln x-1 }$	146	$y = \frac{\ln(x-1)}{\sqrt{x-1}}$	147	$y = \operatorname{arctg}\frac{1}{\ln 1-x }$

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148	$y = x^x$	149	$y = e^{arctg \frac{1}{x-3}}$	150	$y = \sqrt{x^2 - 1} + arc sen \frac{1}{x}$
151	$y = x - \ln x - \frac{x}{x-1}$	152	$y = \begin{cases} \frac{x}{x+2} & x > 0 \\ 0 & x = 0 \\ \frac{x}{x-2} & x < 0 \end{cases}$	153	$y = \begin{cases} -arctg \sqrt{1-x^2} & -1 < x < 1 \\ 2 \operatorname{sen} \frac{1}{x^2} & x \geq 1 \end{cases}$