```
import numpy
import urllib
import scipy.optimize
import random
from math import exp
from math import log
def parseData(fname):
  for l in urllib.urlopen(fname):
    yield eval(1)
print("Reading data...")
data = list(parseData("http://jmcauley.ucsd.edu/cse190/data/beer/beer_50000.json"))
print("done")
def feature(datum):
  feat = [1, datum['review/taste'], datum['review/appearance'], datum['review/aroma'],
datum['review/palate'], datum['review/overall']]
  return feat
X = [feature(d) for d in data]
y = [d[beer/ABV'] >= 6.5 \text{ for d in data}]
def inner(x,y):
  return sum([x[i]*y[i] \text{ for } i \text{ in } range(len(x))])
def sigmoid(x):
  return 1.0 / (1 + \exp(-x))
# Logistic regression by gradient ascent
# NEGATIVE Log-likelihood
def f(theta, X, y, lam):
  loglikelihood = 0
  for i in range(len(X)):
    logit = inner(X[i], theta)
```

```
loglikelihood = log(1 + exp(-logit))
     if not y[i]:
       loglikelihood -= logit
  for k in range(len(theta)):
     loglikelihood -= lam * theta[k]*theta[k]
  # for debugging
  # print("ll =" + str(loglikelihood))
  return -loglikelihood
# NEGATIVE Derivative of log-likelihood
def fprime(theta, X, y, lam):
  dl = [0]*len(theta)
  for i in range(len(X)):
     logit = inner(X[i], theta)
     for k in range(len(theta)):
       dl[k] += X[i][k] * (1 - sigmoid(logit))
       if not y[i]:
         dl[k] = X[i][k]
  for k in range(len(theta)):
     dl[k] = lam*2*theta[k]
  return numpy.array([-x for x in dl])
cutlen=len(data)/3
print(cutlen)
ranstart=random.sample(range(cutlen),1)[0]
print(ranstart)
x_train=X[ranstart:(ranstart+cutlen)]
y_train=y[ranstart:(ranstart+cutlen)]
x valid=X[(ranstart+cutlen):(ranstart+2*cutlen)]
y_valid=y[(ranstart+cutlen):(ranstart+2*cutlen)]
x_test=X[(ranstart+2*cutlen):]+X[:ranstart]
y_test=y[(ranstart+2*cutlen):]+y[:ranstart]
# Train
def train(lam):
  theta, _, = scipy.optimize.fmin_l_bfgs_b(f, [0]*len(X[0]), fprime, pgtol = 10, args =
(x_train, y_train, lam))
  return theta
```

```
# Predict
def performance(theta):
  res_train = [inner(theta,x) for x in x_train]
  res_valid = [inner(theta,x) for x in x_valid]
  res test = [inner(theta,x) for x in x test]
  pred_train = [s > 0 \text{ for s in res_train}]
  pred_valid = [s > 0 \text{ for } s \text{ in } res_valid]
  pred_test = [s > 0 \text{ for } s \text{ in } res_test]
  correct_train = [(a==b) for (a,b) in zip(pred_train,y_train)]
  correct_valid = [(a==b) for (a,b) in zip(pred_valid,y_valid)]
  correct\_test = [(a==b) for (a,b) in zip(pred\_test,y\_test)]
  acc_train = sum(correct_train) * 1.0 / len(correct_train)
  acc_valid = sum(correct_valid) * 1.0 / len(correct_valid)
  acc_test = sum(correct_test) * 1.0 / len(correct_test)
  return acc train, acc valid, acc test
# Validation pipeline
lam = 1.0
theta = train(lam)
acc_train, acc_valid, acc_test = performance(theta)
print("train=" + str(acc_train))
print("valid=" + str(acc_valid))
print("test=" + str(acc_test))
1
train=0.8301932077283092
valid=0.6176647065882636
test=0.5680345572354212
```

2. Modify the "Predict" and "Validation pipeline" parts to the following code.

```
# Predict
def performance(theta):
   res_train = [inner(theta,x) for x in x_train]
  res valid = [inner(theta,x) for x in x valid]
   res test = [inner(theta,x) for x in x test]
   pred_train = [s > 0 \text{ for } s \text{ in } res_train]
   pred_valid = [s > 0 \text{ for } s \text{ in } res_valid]
   pred_test = [s > 0 \text{ for } s \text{ in } res_test]
   correct_train = [(a==b) for (a,b) in zip(pred_train,y_train)]
   correct_valid = [(a==b) for (a,b) in zip(pred_valid,y_valid)]
   correct\_test = [(a==b) for (a,b) in zip(pred\_test,y\_test)]
   acc_train = sum(correct_train) * 1.0 / len(correct_train)
   acc valid = sum(correct valid) * 1.0 / len(correct valid)
   acc_test = sum(correct_test) * 1.0 / len(correct_test)
   scores test = [inner(theta, x) for x in x test]
   predictions_test = [s>0 for s in scores_test]
   positives=sum([a for (a, b) in zip(predictions_test, y_test)])
   negatives=sum([b for (a, b) in zip(predictions_test, y_test)])
   true_positives = sum([a and b for (a, b) in zip(predictions_test, y_test)])
   false_positives = sum([a and not b for (a, b) in zip(predictions_test, y_test)])
   true_negatives = sum([not a and not b for (a, b) in zip(predictions_test, y_test)])
   false_negatives = sum([not a and b for (a, b) in zip(predictions_test, y_test)])
   return acc train, acc valid,
acc_test,positives,negatives,true_positives,false_positives,true_negatives,false_negatives
# Validation pipeline
lam = 1.0
theta = train(lam)
```

```
acc_train, acc_valid,
acc_test,positives,negatives,true_positives,false_positives,true_negatives,false_negatives
= performance(theta)
print("train=" + str(acc_train))
print("valid=" + str(acc_valid))
print("test=" + str(acc_test))
print("Positives="+str(positives))
print("Negetives="+str(negatives))
print ("True Positives="+str(true_positives))
print ("True Negatives="+str(true_negatives))
print ("False Positives="+str(false_positives))
print ("False Negatives="+str(false_negatives))
```

train=0.8174726989079563 valid=0.6350654026161047 test=0.5941924646028318 Positives=13413 Negetives=8245 True Positives=7447 True Negatives=2457 False Positives=5966 False Negatives=798

3. Multiply likelihood with 10 while y==False and logit >0

4.

adopt the "acc_valid" to judge the best model.

16666

11140

0:0.6213248529941198

0.01:0.6196447857914317

0.1:0.6194647785911437

1:0.6159246369854794

100:0.5493819752790111

But we can see from here that the performance is very close. However, we are picking 0 for λ .

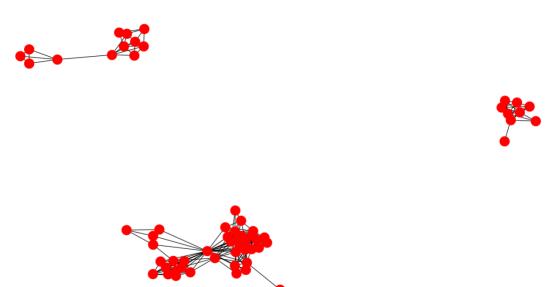
Then repeat question1:

train=0.7250690027601104

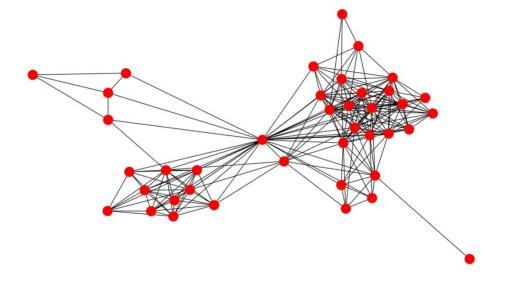
valid=0.8696147845913836

test=0.47546196304295657

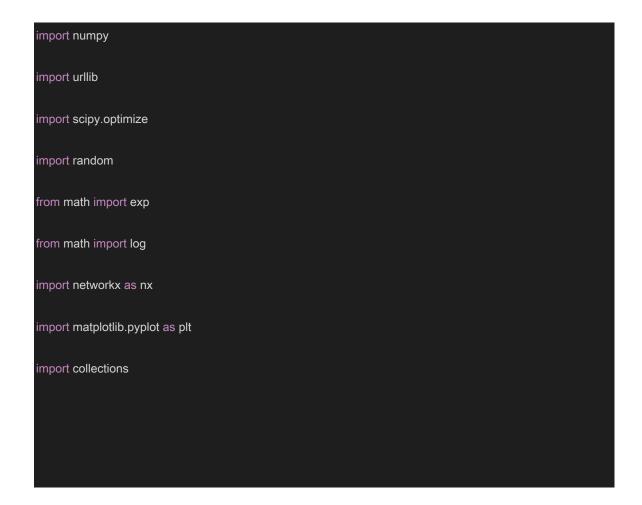
5.



Obviously there are three connected components, and 40 nodes are in the largest one.



6.



```
# Karate club
G = nx.karate_club_graph()
nx.draw(G)
# plt.show()
plt.clf()
edges = set()
nodes = set()
for edge in urllib.urlopen("http://jmcauley.ucsd.edu/cse255/data/facebook/egonet.txt", 'r'):
  x,y = edge.split()
  x,y = int(x), int(y)
  edges.add((x,y))
  edges.add((y,x))
  nodes.add(x)
  nodes.add(y)
G = nx.Graph()
for e in edges:
  G.add_edge(e[0],e[1])
```

```
# plt.show()
plt.clf()
print("start bfs")
visited={}
graphs=[]
def BFS(node,nodes,visited):
  graph=set()
  queue=collections.deque([node])
  while queue:
    curr=queue.popleft()
    graph.add(curr)
    visited[curr]=True
    for next_node in nodes:
       if (curr,next_node) in edges and not visited[next_node]:
         queue.append(next_node)
  return graph
```

```
for node in nodes:
  visited[node]=False
  print(node)
print("build graphs")
for node in nodes:
  if not visited[node]:
    temp=BFS(node,nodes,visited)
    print(temp)
    graphs.append(temp)
print(graphs)
largest=sorted(list(graphs[0]))
print(largest)
cluster1=largest[:(len(largest)/2)]
cluster2=largest[(len(largest)/2):]
print(cluster1)
print(cluster2)
def normalized_cut(edges,cluster1,cluster2):
  edge_count=0
  degree1,degree2=0,0
```

```
for edge in edges:
    if edge[0] in cluster1 and edge[1] in cluster1:
      degree1+=0.5
    elif edge[0] in cluster2 and edge[1] in cluster2:
      degree2+=0.5
    elif edge[0] in cluster1 and edge[1] in cluster2:
      degree1+=1
      degree2+=1
      edge_count+=1
  normalized_cut=(edge_count/degree1+edge_count/degree2)/2
  return normalized_cut
minimum=normalized_cut(edges,cluster1,cluster2)
print(minimum)
[697, 703, 708, 713, 719, 729, 745, 747, 753, 769, 772, 774, 798, 800, 803, 804,
 805, 810, 811, 819]
[823, 825, 828, 830, 840, 856, 861, 863, 864, 869, 876, 878, 880, 882, 884, 886,
 888, 889, 890, 893]
0.422
7.
```





```
queue=collections.deque([node])
  while queue:
    curr=queue.popleft()
    graph.add(curr)
    visited[curr]=True
    for next_node in nodes:
      if (curr,next_node) in edges and not visited[next_node]:
         queue.append(next_node)
  return graph
for node in nodes:
  visited[node]=False
  print(node)
print("build graphs")
for node in nodes:
  if not visited[node]:
    temp=BFS(node,nodes,visited)
    print(temp)
    graphs.append(temp)
print(graphs)
```

```
largest=sorted(list(graphs[0]))
print(largest)
cluster1=largest[:(len(largest)/2)]
cluster2=largest[(len(largest)/2):]
print(cluster1)
print(cluster2)
def normalized_cut(edges,cluster1,cluster2):
  edge_count=0
  degree1,degree2=0,0
  for edge in edges:
    if edge[0] in cluster1 and edge[1] in cluster1:
      degree1+=0.5
    elif edge[0] in cluster2 and edge[1] in cluster2:
      degree2+=0.5
    elif edge[0] in cluster1 and edge[1] in cluster2:
      degree1+=1
      degree2+=1
      edge_count+=1
  print(degree1)
```

```
print(degree2)
  print(edge_count)
  normalized_cut=(edge_count/degree1+edge_count/degree2)/2
  return normalized_cut
minimum=normalized_cut(edges,cluster1,cluster2)
print(minimum)
change1,change2=[],[]
for i in range(len(cluster1)):
  temp1=cluster1[:i]+cluster1[i:]
  temp2=cluster2+[cluster1[i]]
  print(temp1,temp2)
  temp=normalized_cut(edges,temp1,temp2)
  if temp<minimum:
    minimum=temp
    change1.append(cluster1[i])
for move_node in cluster2:
  temp1=cluster1+[cluster2[i]]
  temp2=cluster2[:i]+cluster2[i:]
  temp=normalized_cut(edges,temp1,temp2)
```

```
if temp<minimum:
    minimum=temp
    change2.append(move_node)
for node in change1:
  cluster1.remove(node)
  cluster2.append(node)
for node in change2:
  cluster1.append(node)
  cluster2.remove(node)
print(cluster1)
print(cluster2)
print(minimum)
```

```
[703, 713, 719, 745, 747, 753, 769, 772, 774, 798, 800, 803, 804, 805, 810, 811, 819]
[823, 825, 828, 830, 840, 856, 861, 863, 864, 869, 876, 878, 880, 882, 884, 886, 888, 889, 890, 893, 697, 708, 729]
```