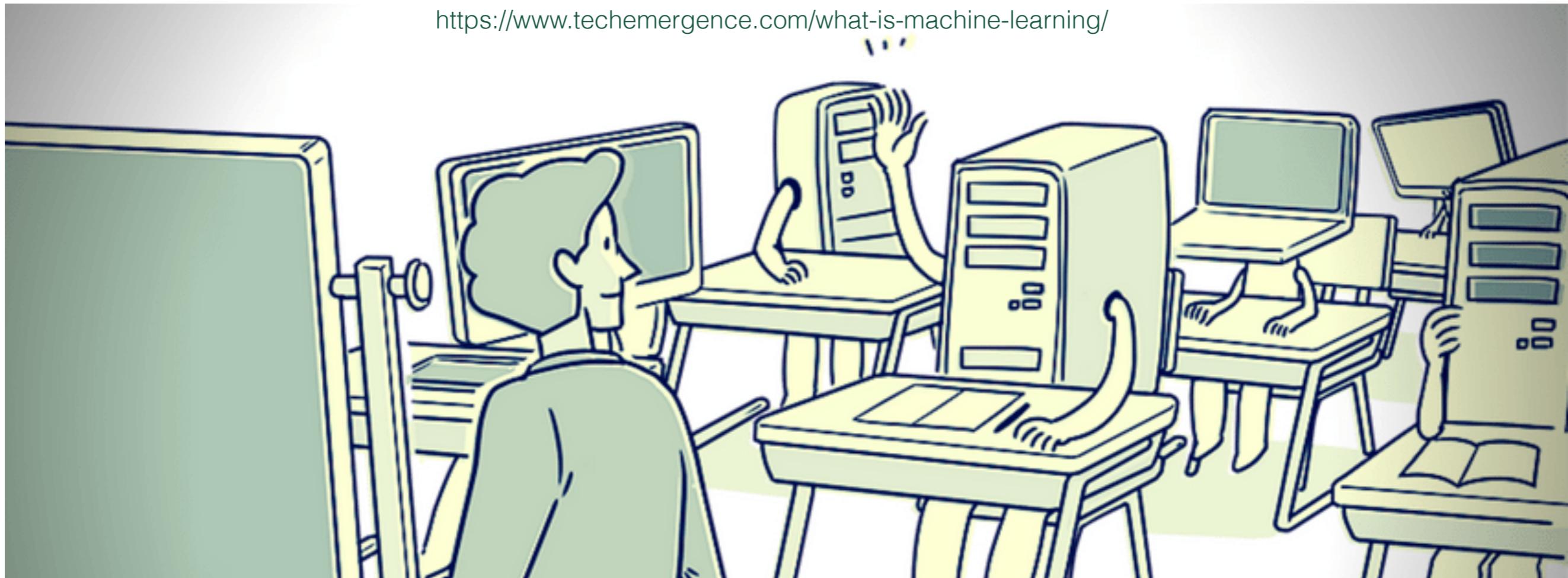


# Introduction to Machine Learning

## Lecture 1

<https://www.techemergence.com/what-is-machine-learning/>



QUC Winter School 2021  
KIAS  
December 2021

# List of resources

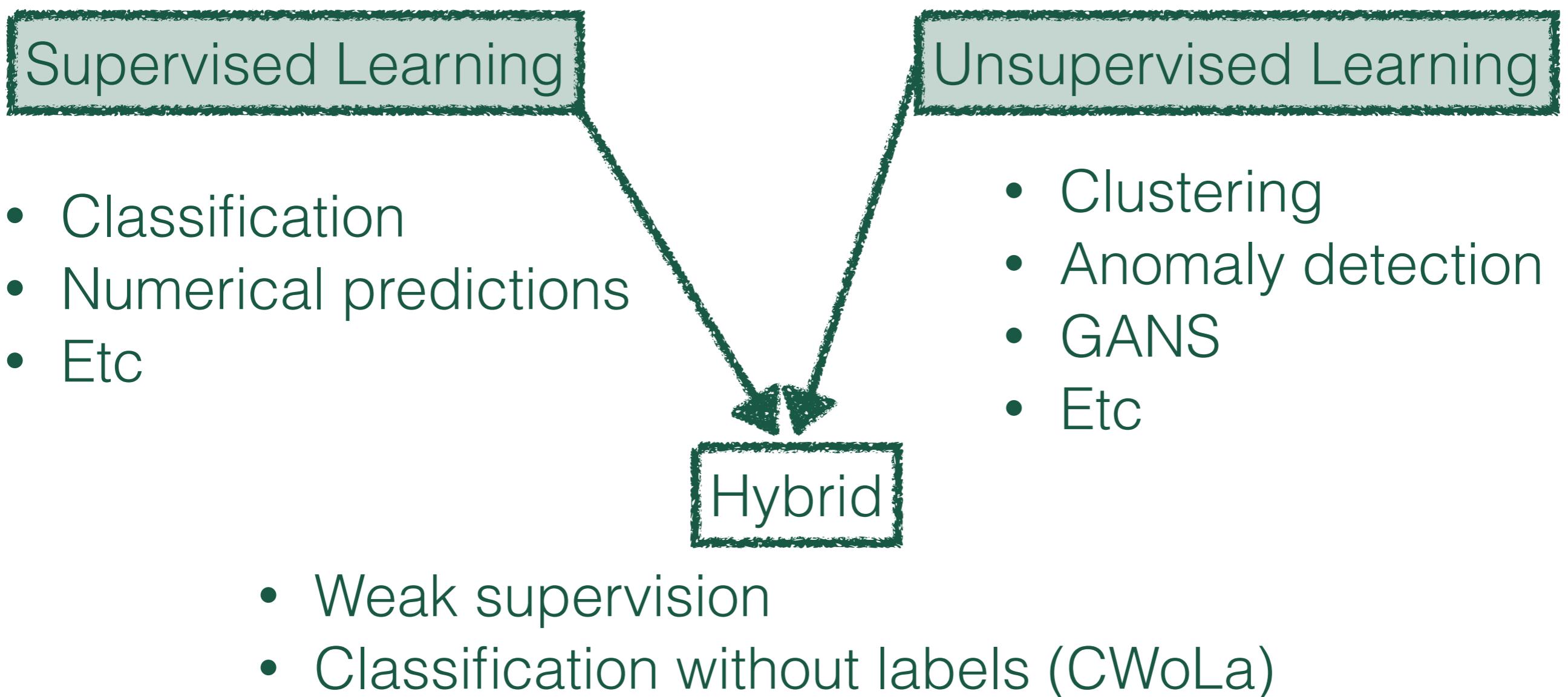
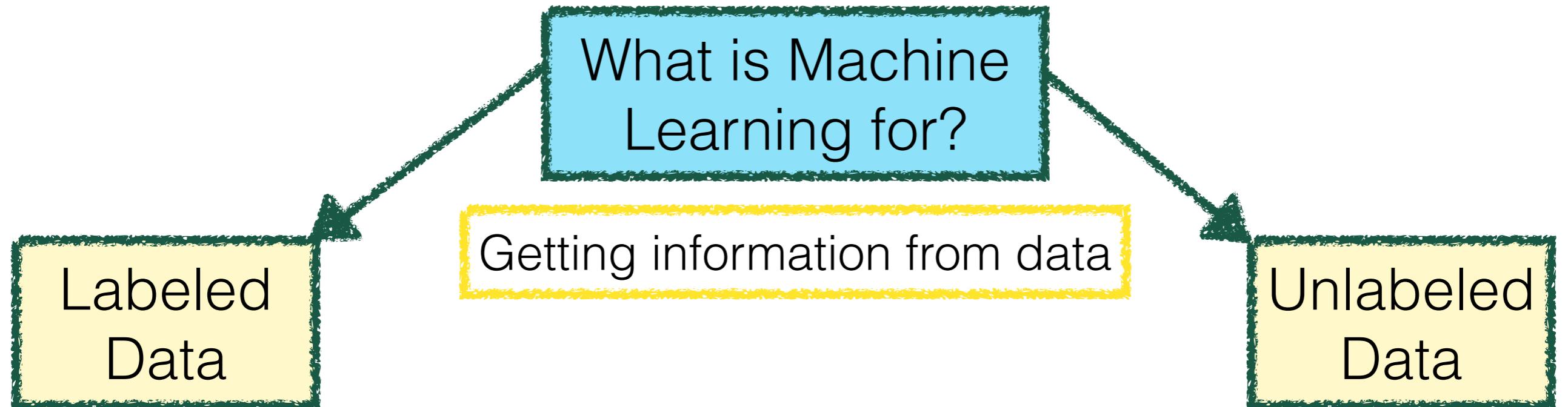
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[https://github.com/bostdiek/KIAS\\_Winter\\_School](https://github.com/bostdiek/KIAS_Winter_School)

<https://iml-wg.github.io/HEPML-LivingReview/>

<https://www.kaggle.com/>

<https://www.coursera.org/specializations/deep-learning>



# Machine learning in High Energy Physics

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Great collection of HEP machine learning resources  
<https://iml-wg.github.io/HEPML-LivingReview/>

# Machine learning in High Energy Physics

PHYSICAL REVIEW D

VOLUME 46, NUMBER 11

1 DECEMBER 1992

**Snagging the top quark with a neural net**

Howard Baer  
*Physics Department, Florida State University, Tallahassee, Florida 32306*

Debra Dzialo Karatas  
*Center for Particle Physics, The University of Texas, Austin, Texas 78712*

Gian F. Giudice  
*Theory Group, Department of Physics, The University of Texas, Austin, Texas 78712*  
(Received 20 December 1991)

The search for the top quark at  $p\bar{p}$  colliders in the one-lepton-plus-jets channel is plagued by an irremovable background from  $W$ -boson-plus-multijet production. In this paper, we show how the top-quark signal can be distinguished from background in the distribution of neural network output. By making a cut on the network output, we maximize the ratio of signal to background in a final event sample, and compare our results with those obtained by making kinematical cuts on the data sample. We also demonstrate the robustness of the neural network method by training the neural network on signal events of one top mass and testing upon another.

PACS number(s): 13.85.Qk, 14.80.Dq

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arXiv.org > hep-ex > arXiv:0707.1712 Search...  
Help | Advanced

High Energy Physics – Experiment

**B-Tagging at CDF and DO, Lessons for LHC**

T. Wright, for the CDF, DØ Collaborations  
(Submitted on 11 Jul 2007)

The identification of jets resulting from the fragmentation and hadronization of b quarks is an important part of high-pT collider physics. The methods used by the CDF and DO collaborations to perform this identification are described, including the calibration of the efficiencies and fake rates. Some thoughts on the application of these methods in the LHC environment are also presented.

Comments: Proceedings of Hadron Collider Physics 2006; 6 pages, 8 figures

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PHYSICAL REVIEW D

VOLUME 46, NUMBER 11

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Snagging the to

Physics Department, Florida

Deb

Center for Particle Physics, I

arXiv.org > hep-ex > arXiv:0702.071

The ATLAS Collaboration

High Energy Physics – Experiment

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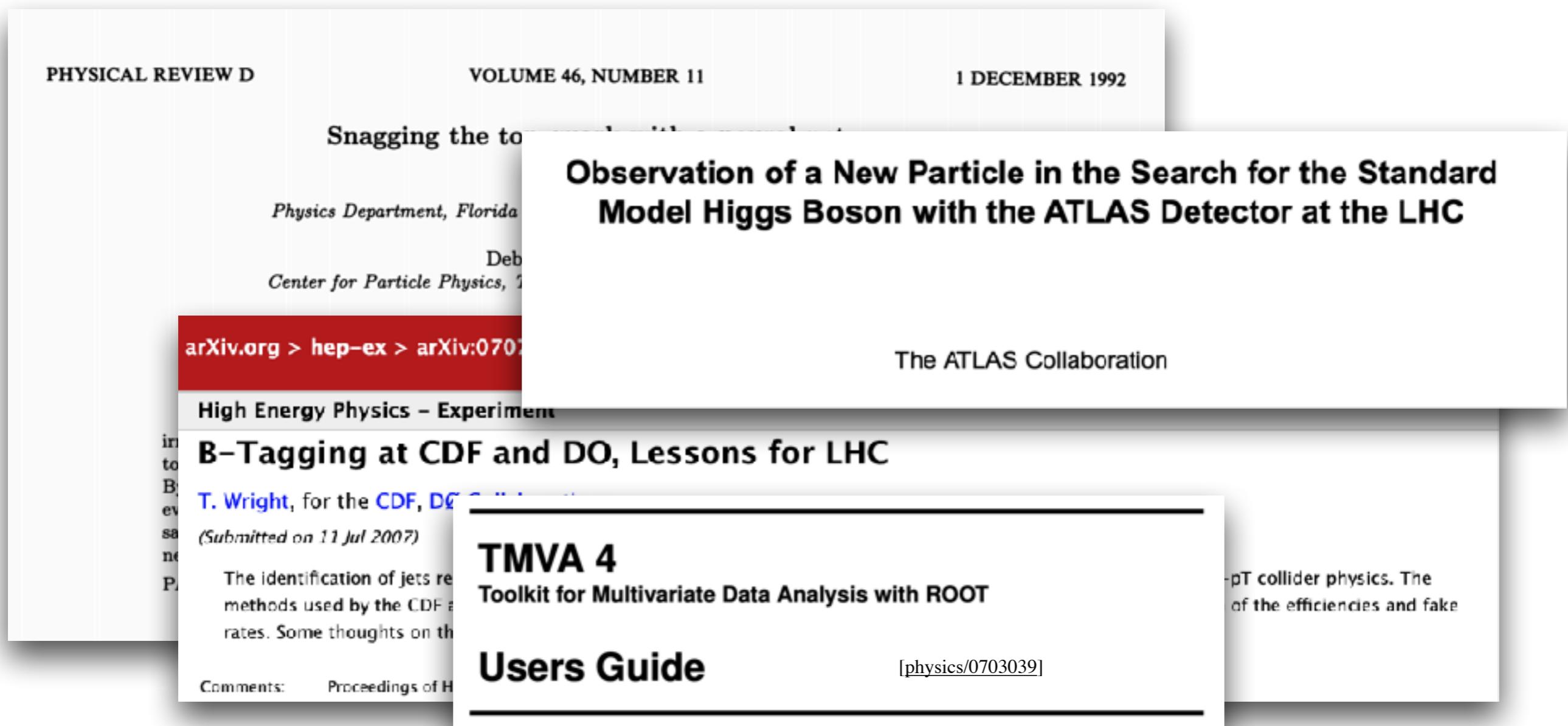
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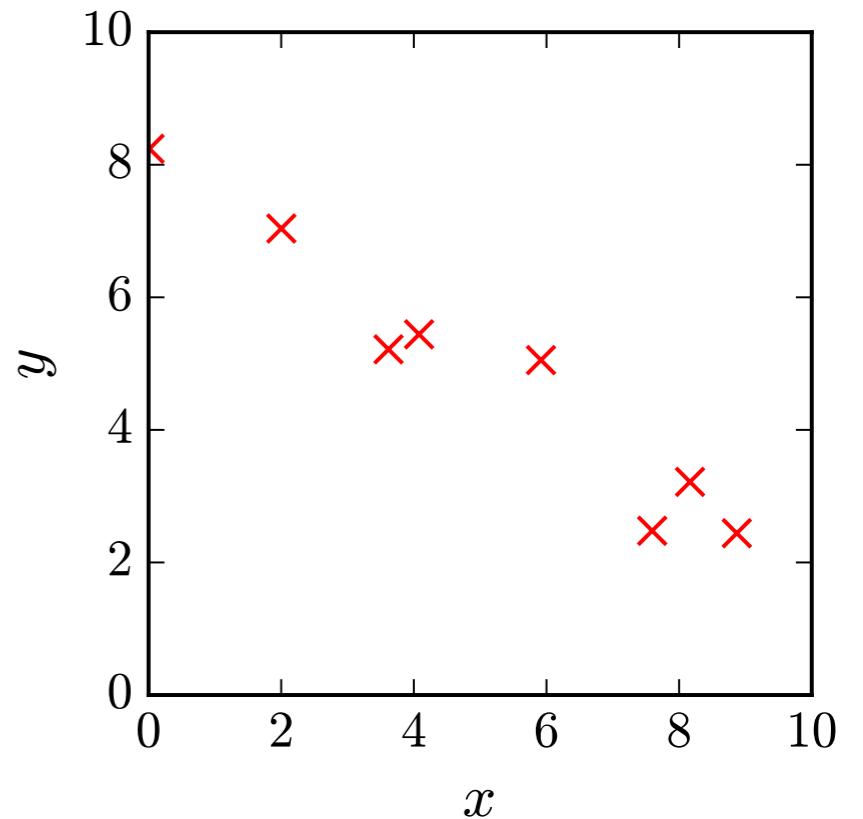


Object tagging, calibrations (systematic regression),  
event-level analysis

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# Review: Linear Regression

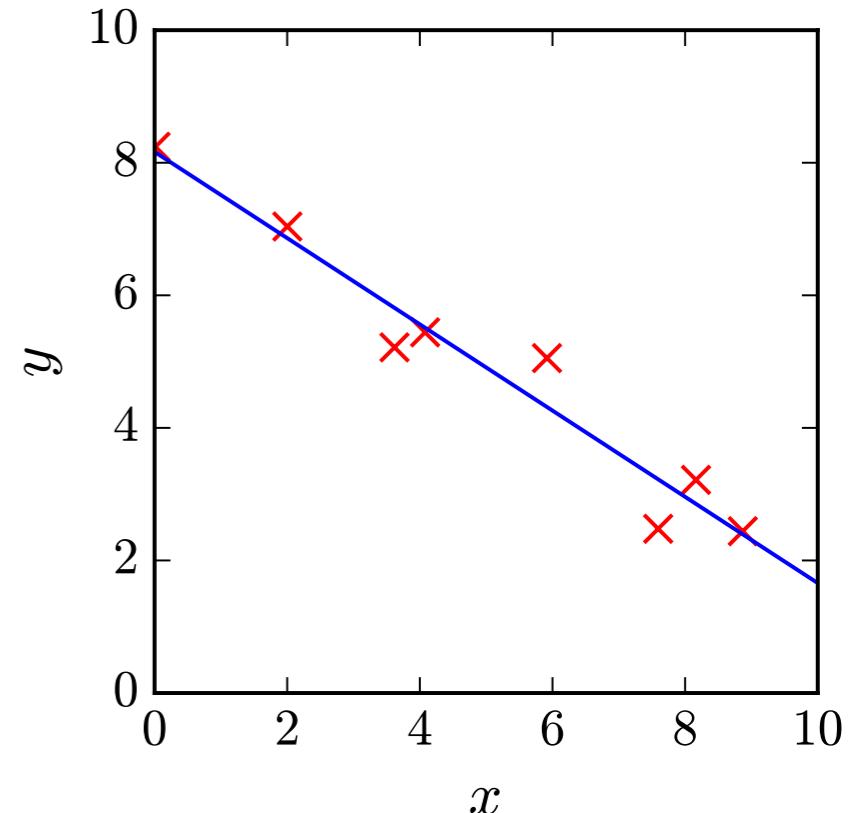
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# Review: Linear Regression

## How to fit data

1. Plot the data
2. Define the function
  - $f(x, \vec{a}) = a_0 + a_1 x$
3. Choose how to know what fits best
  - a.k.a. *Loss Function*



- MSE:  $L(x, y, \vec{a}) = \frac{1}{N} \sum_{i=1}^N (f(x_i, \vec{a}) - y_i)^2$
5. Find the minimum error (loss) (cost)
  - $a_{\text{best}} = a$  when  $\left( \frac{\partial L(x, y, \vec{a})}{\partial \vec{a}} \Big|_{x,y} = 0 \right)$

# Review: Linear Regression

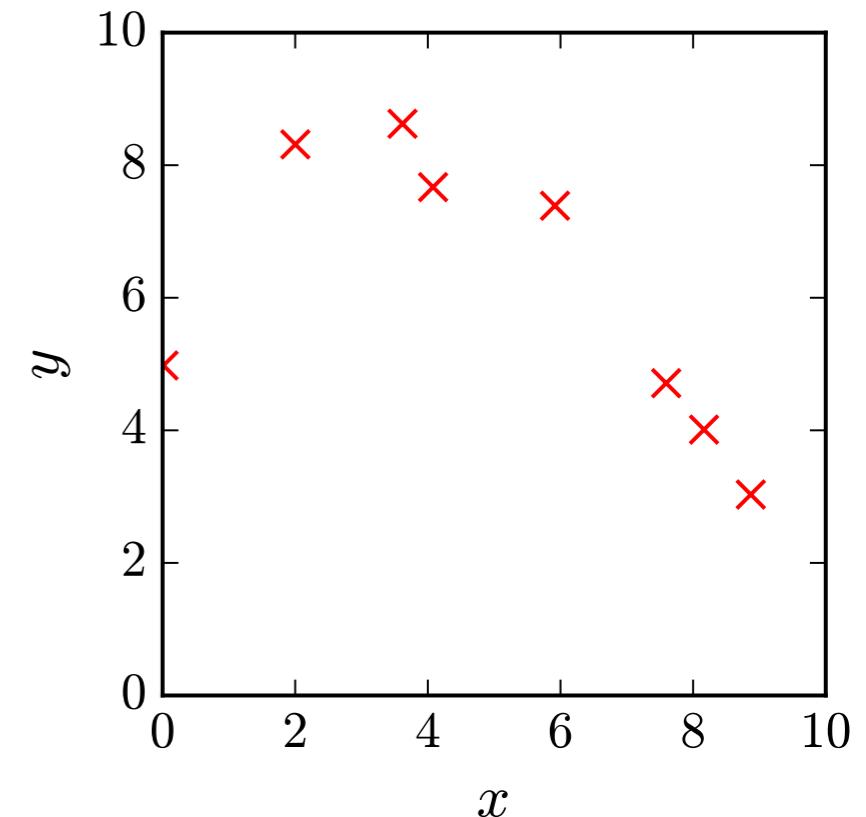
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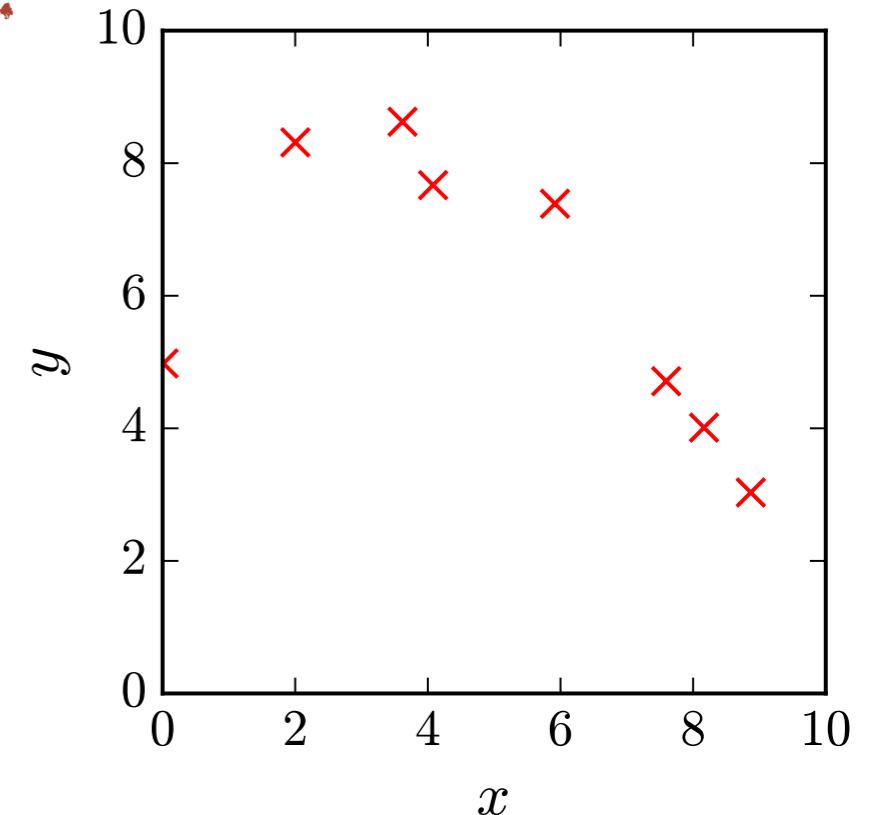
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# Review: ~~Linear~~ Regression

Quadratic?

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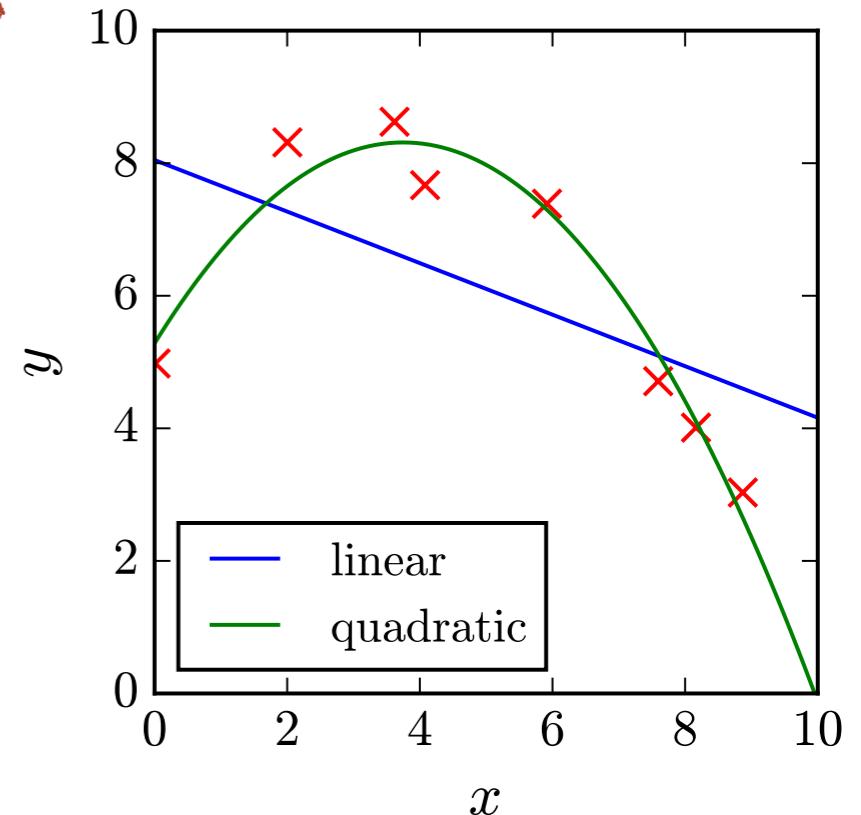
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# Review: ~~Linear~~ Regression

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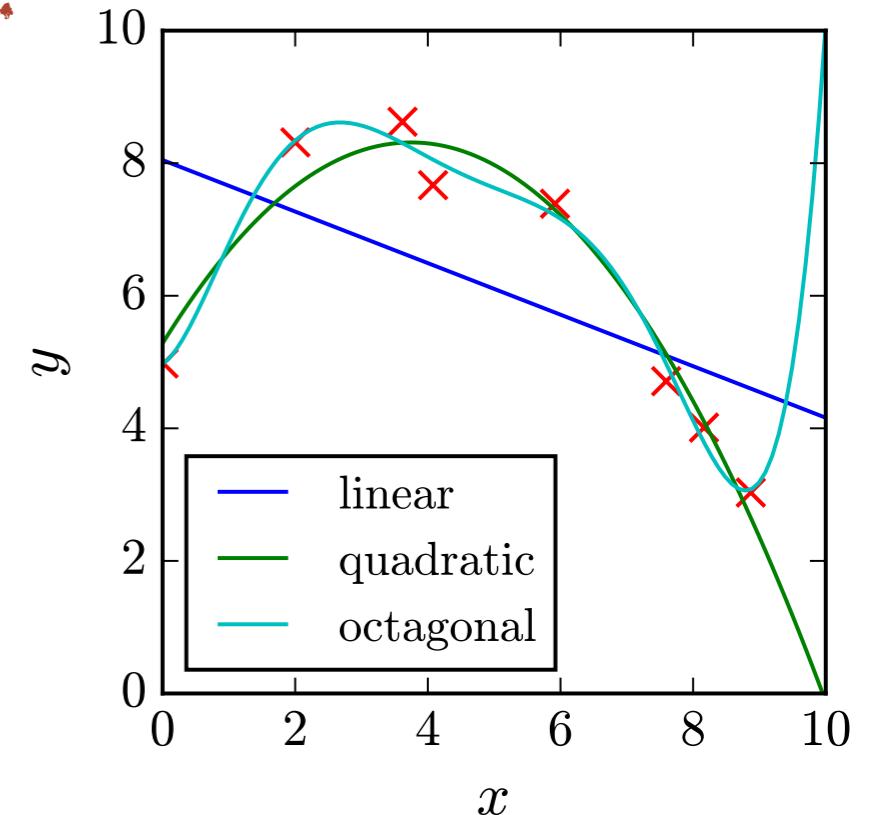
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Is that good enough?  
How many  
parameters can we  
add?

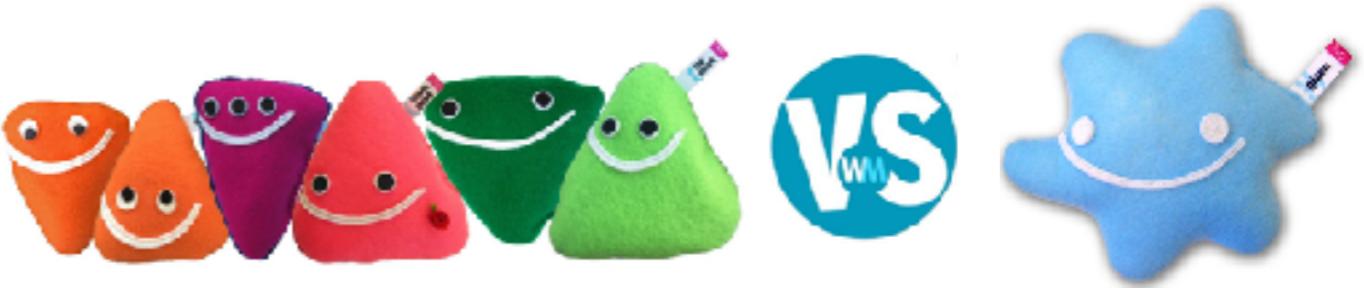
# Logistic Regression

What if we want to predict a class, not a number?

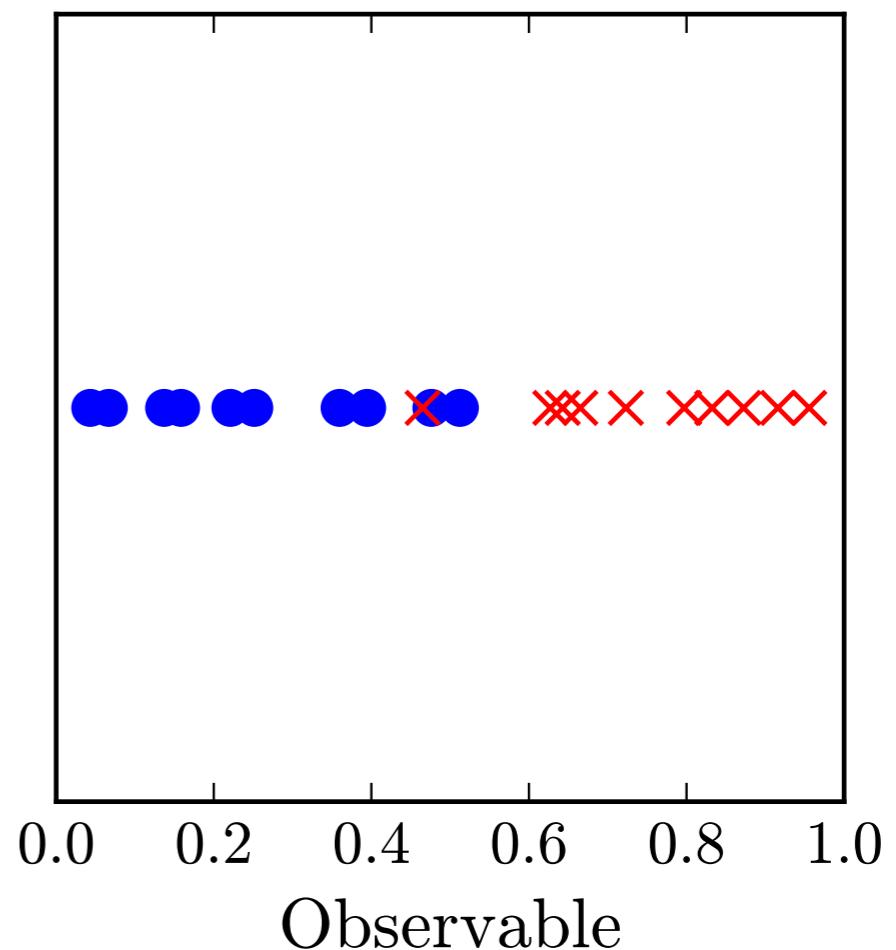


# Logistic Regression

What if we want to predict a class, not a number?



What is the y-value we are trying to fit/predict?



# Logistic Regression

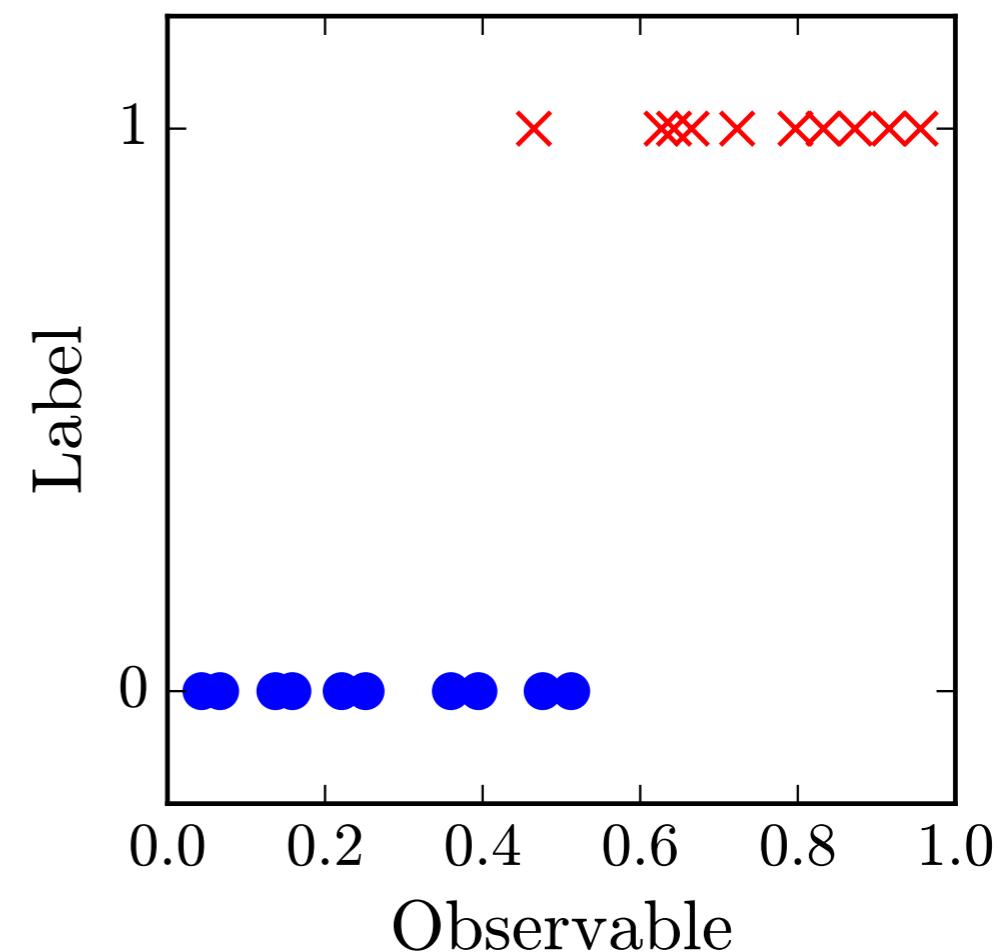
What if we want to predict a class, not a number?



What is the y-value we are trying to fit/predict?

Define one class as 1 (Signal)

Other class as 0 (Background)



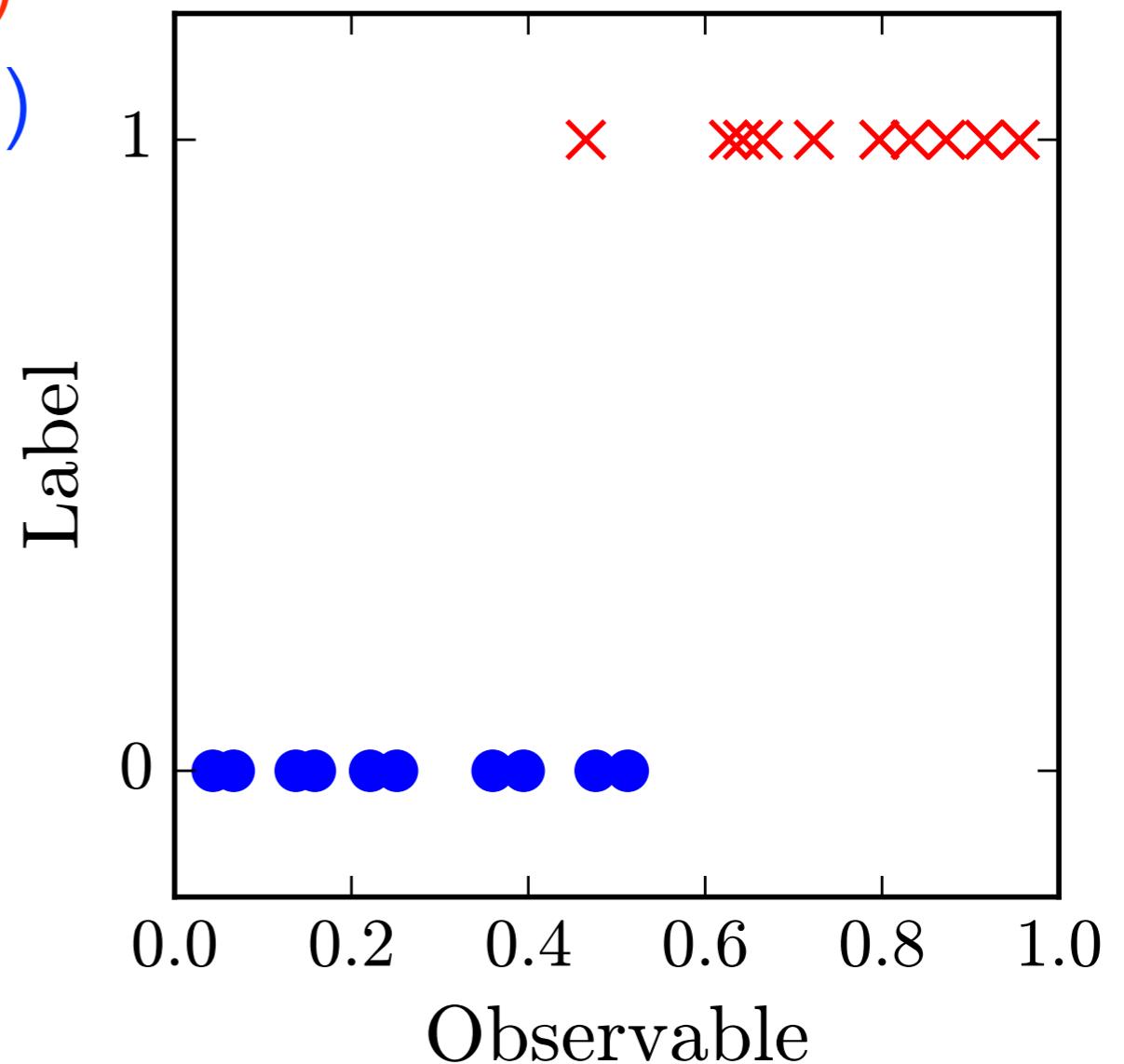
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# Logistic Regression

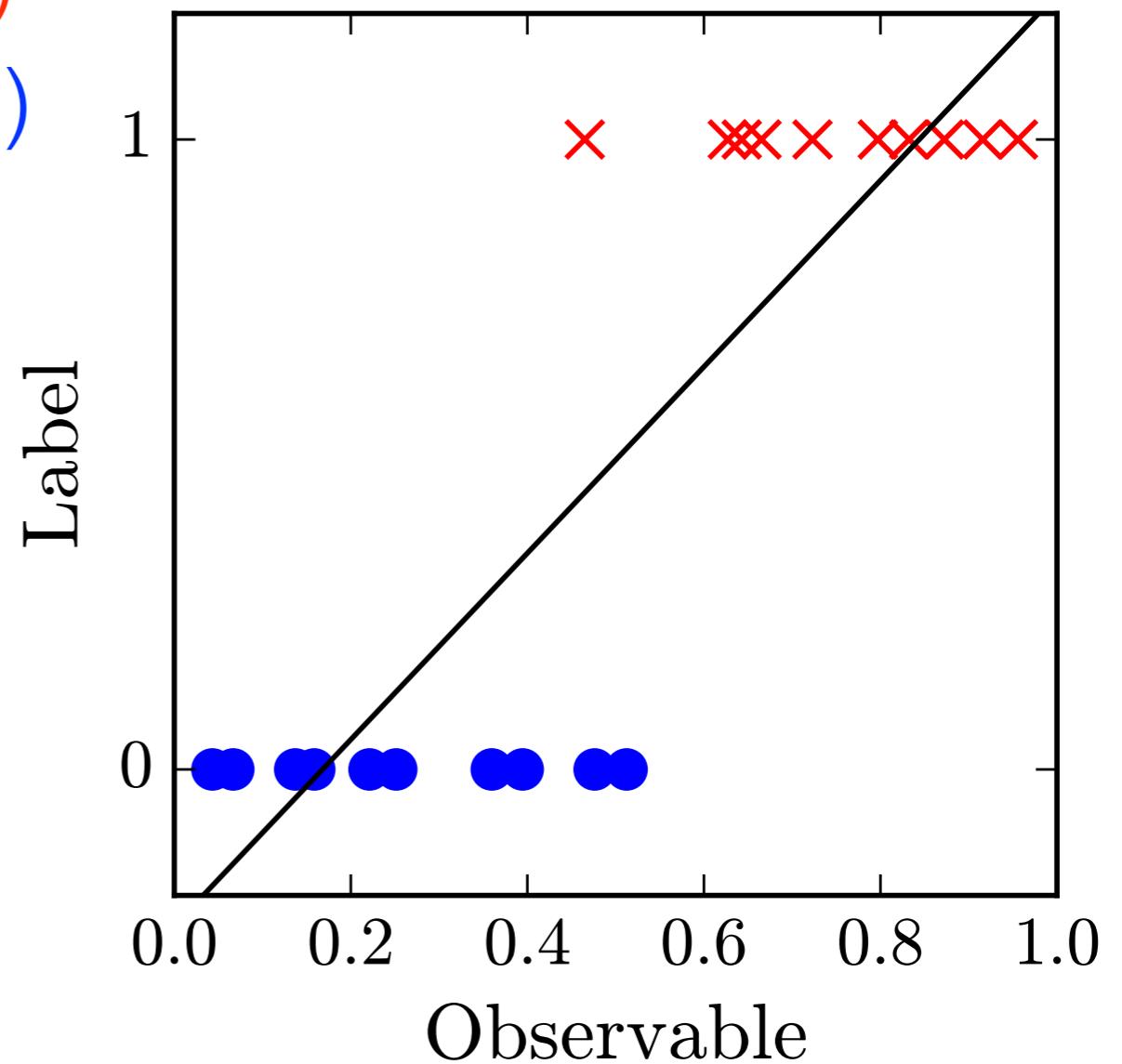
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- Linear Fit?



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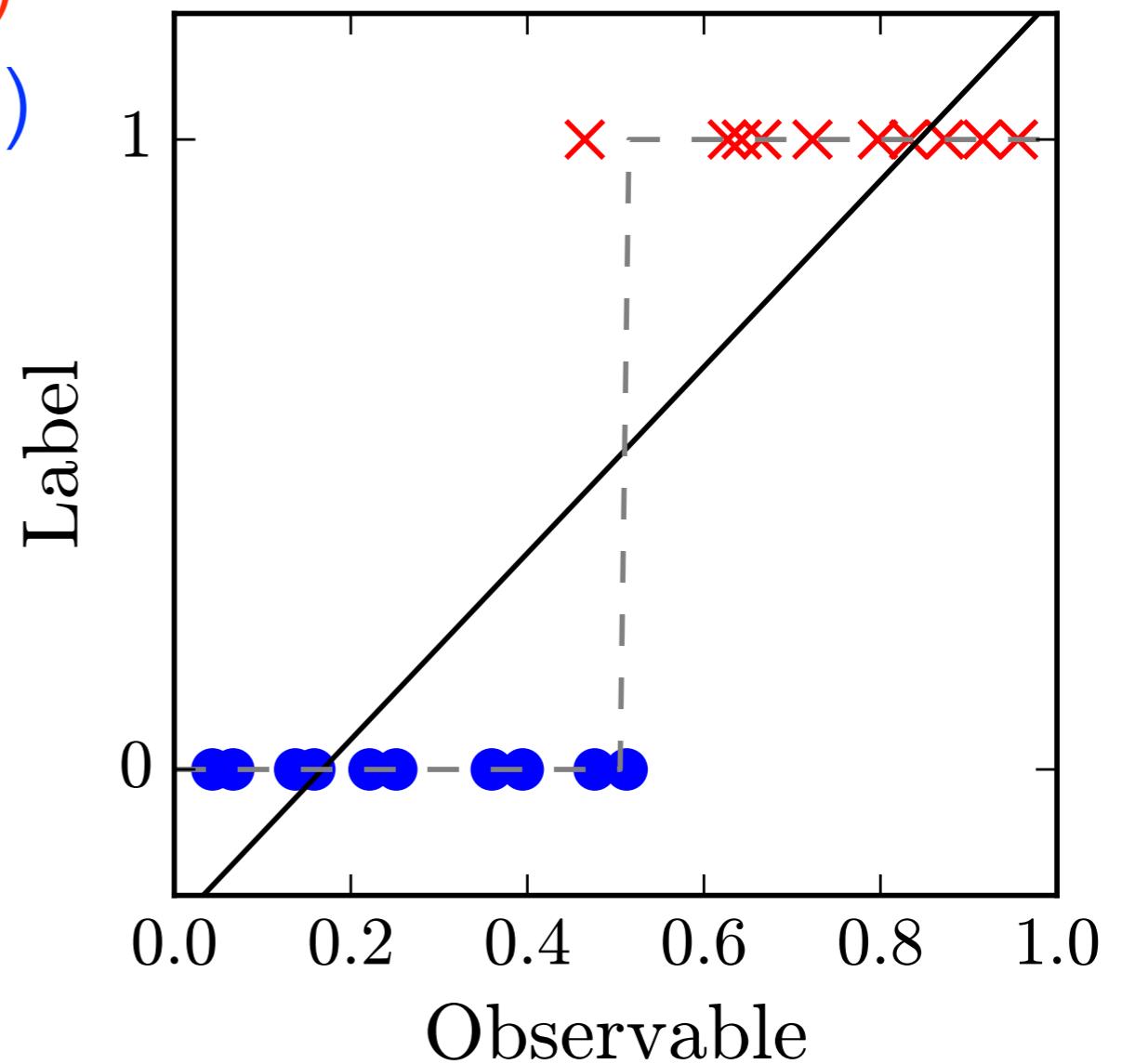
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- Linear Fit?

- Round to nearest number?



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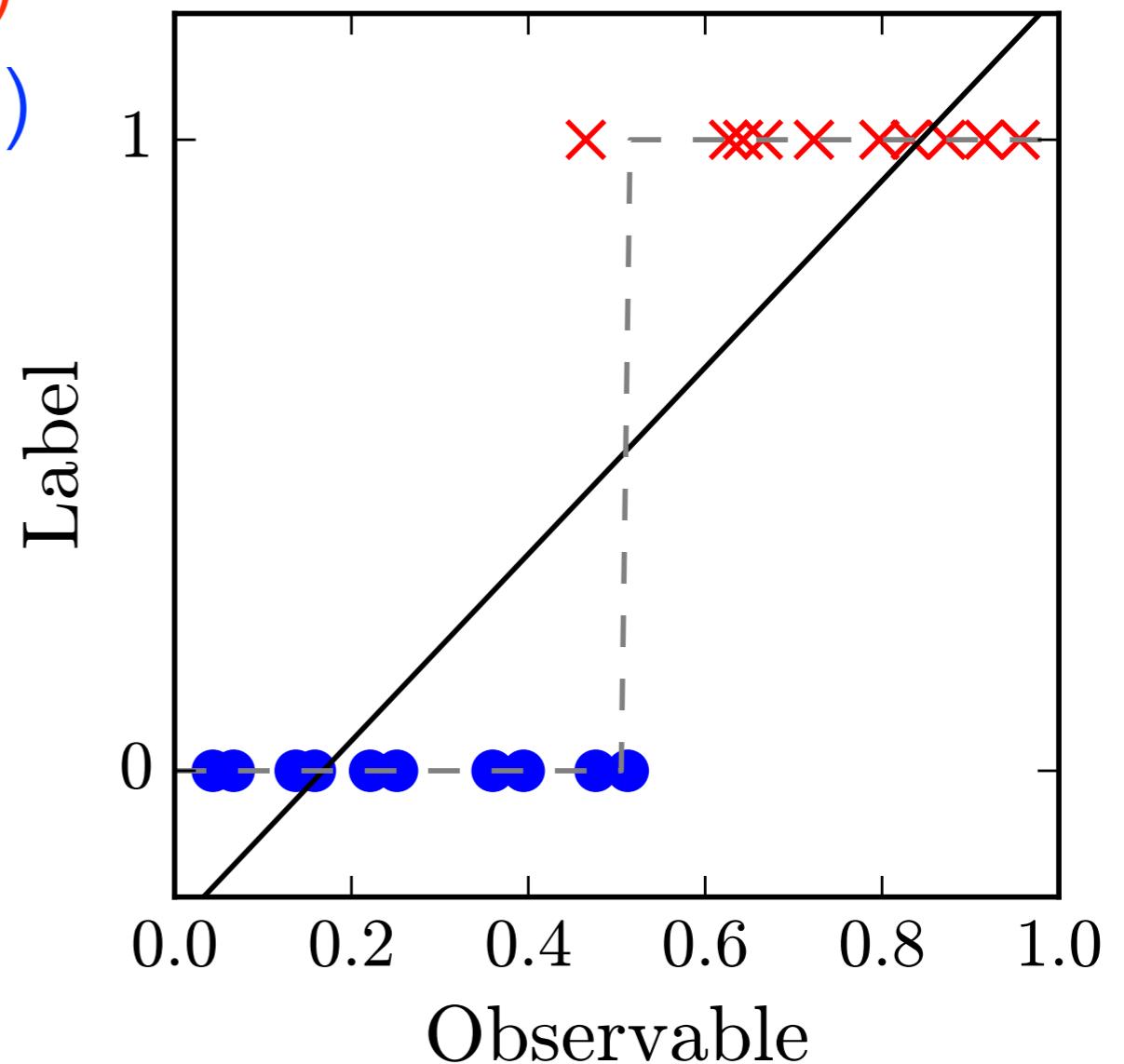
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Other class as 0 (Background)

- Linear Fit?

- Round to nearest number?

- How does it generalize to more data?



# Logistic Regression

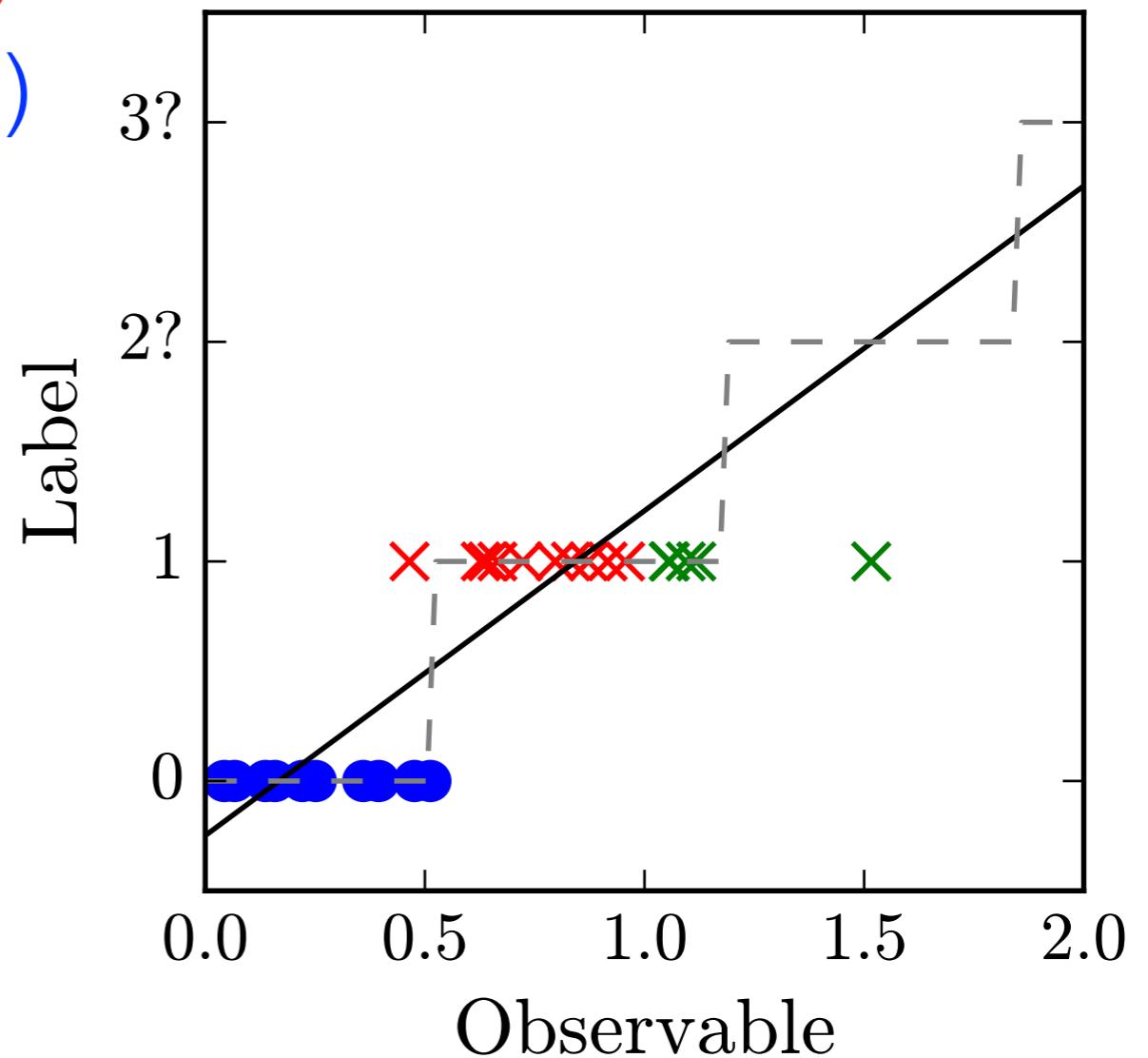
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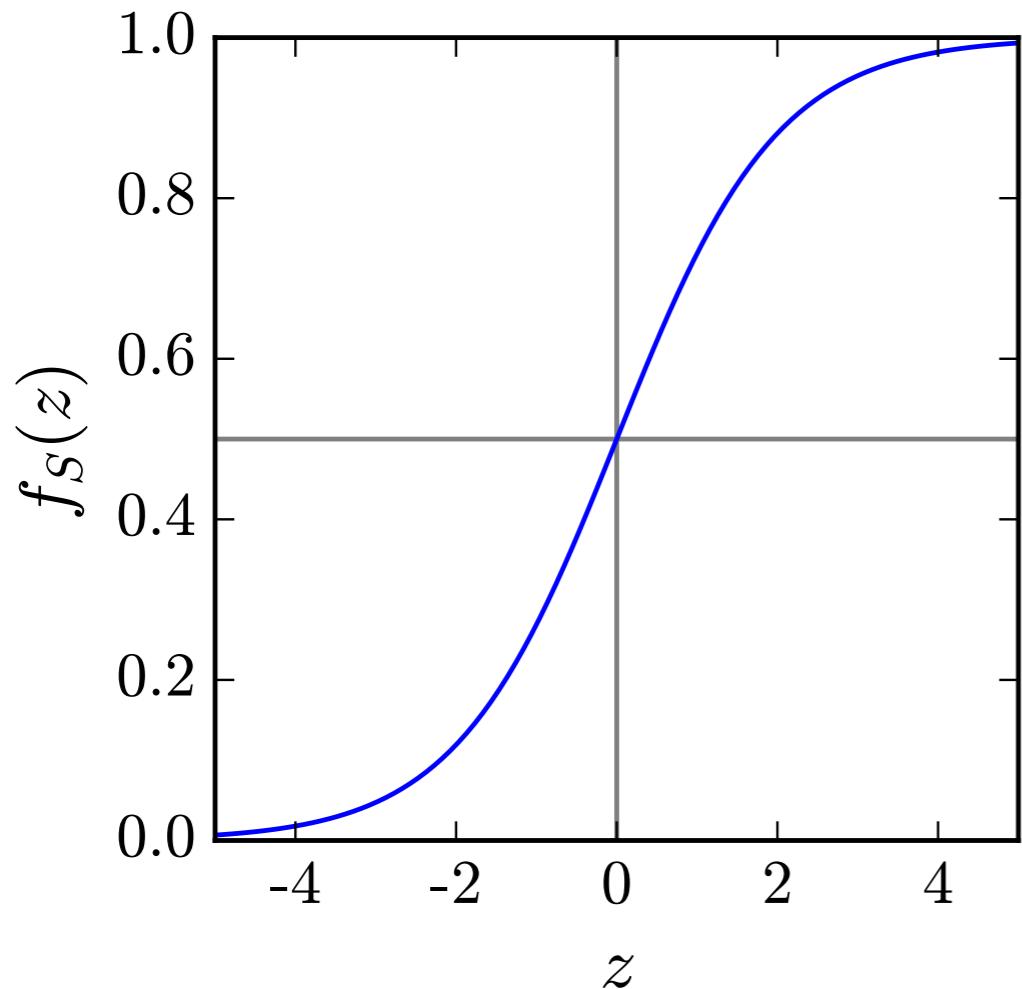
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- Round to nearest number?
- How does it generalize to more data?



# Logistic Regression

What if we want to predict a class, not a number?

- Change the shape of function: Logistic/Sigmoid function



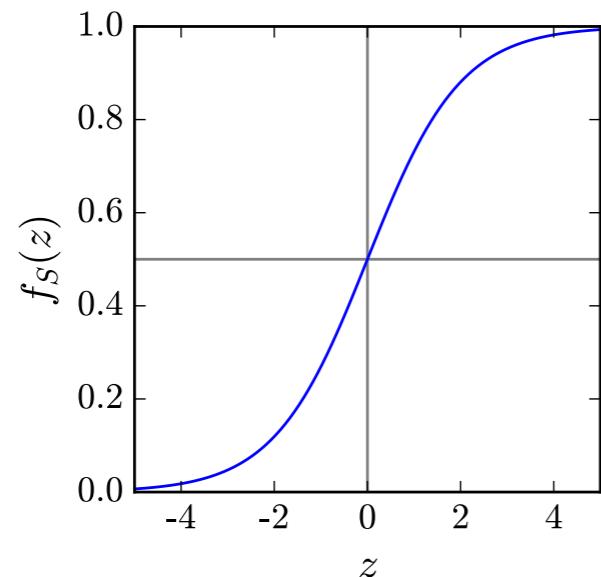
$$f_S(z) = \frac{1}{1 + e^{-z}}$$

Does not add  
parameters

# Logistic Regression

What if we want to predict a class, not a number?

- Change the shape of function: Logistic/Sigmoid function



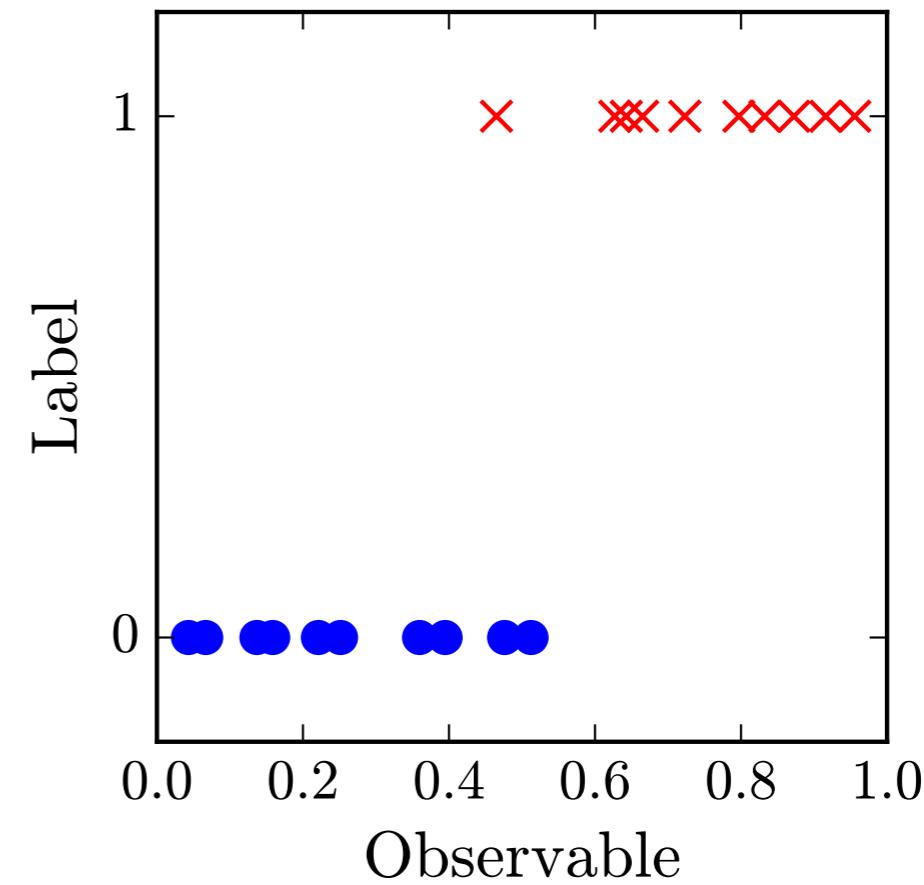
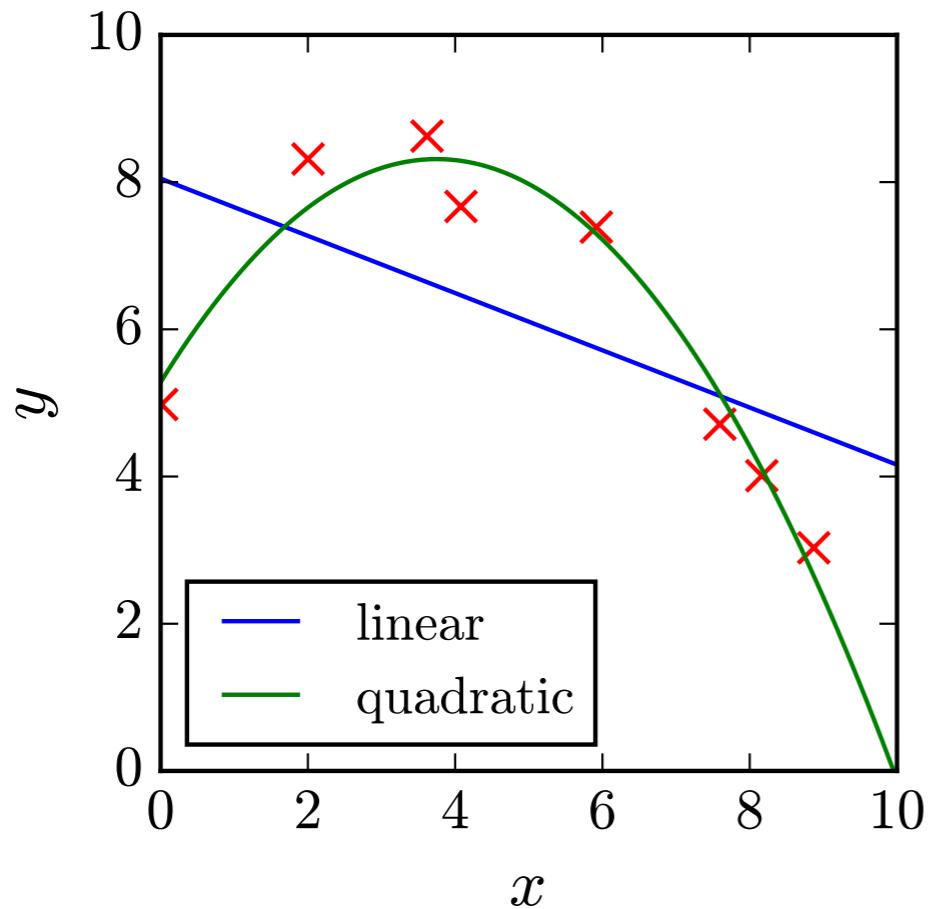
$$f_S(z) = \frac{1}{1 + e^{-z}}$$

- Is the mean squared error still a good loss function?
  - What happens if a prediction is very far off?
  - What does it mean to be “far off”

# Logistic Regression

What if we want to predict a class, not a number?

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# Logistic Regression

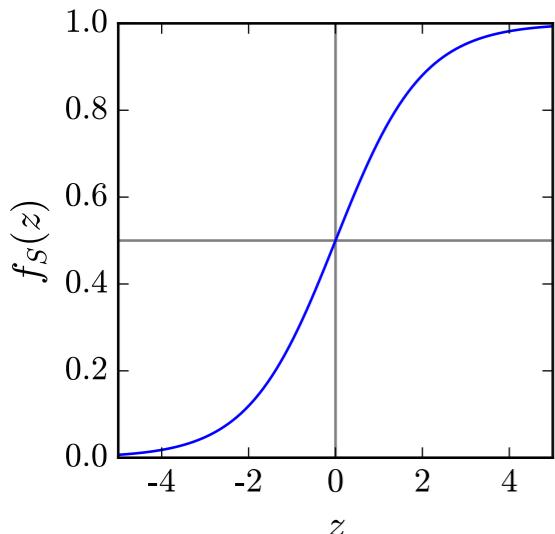
What if we want to predict a class, not a number?

- Is the mean squared error still a good loss function?
  - What happens if a prediction is very far off?
  - What does it mean to be “far off”
- Change the loss function: Binary Cross Entropy
  - Can be penalized for “confident” but wrong predictions

$$L(\vec{\text{pred}}, \vec{y}, \vec{a}) = -\frac{1}{N} \sum_{i=1}^N \left( y_i \log \text{pred}_i + (1 - y_i) \log (1 - \text{pred}_i) \right)$$

# Logistic Regression

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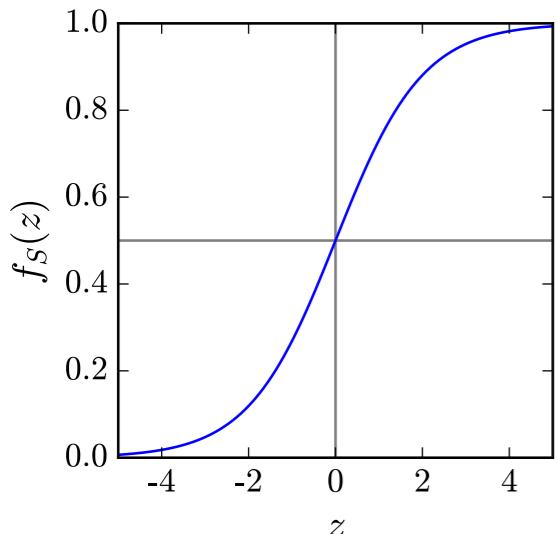


$$L(\vec{x}, \vec{y}, \vec{a}) = -\frac{1}{N} \sum_{i=1}^N \left( y_i \log(f_S(p(x, a))) + (1 - y_i) \log(1 - f_S(p(x, a))) \right)$$

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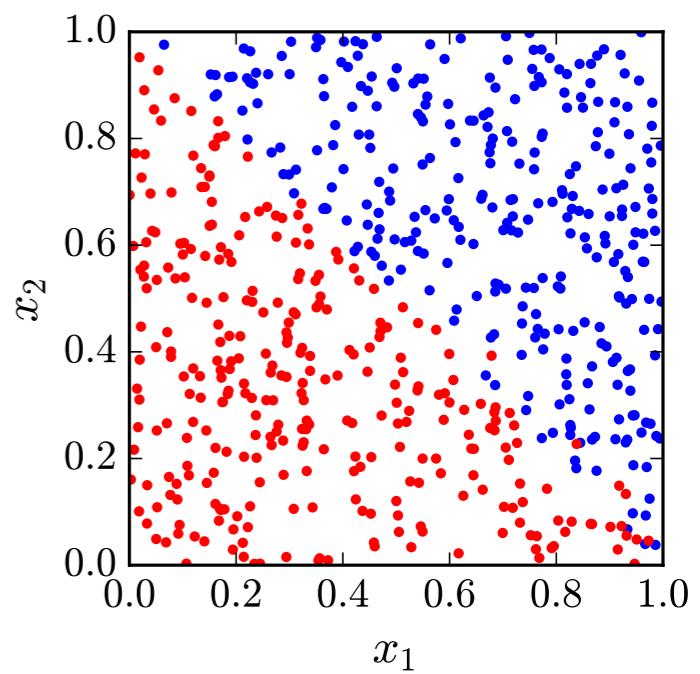
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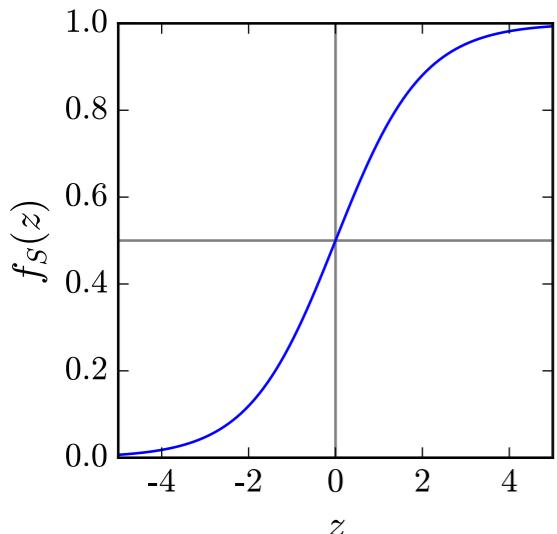
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What is  $p(x, a)$  ?



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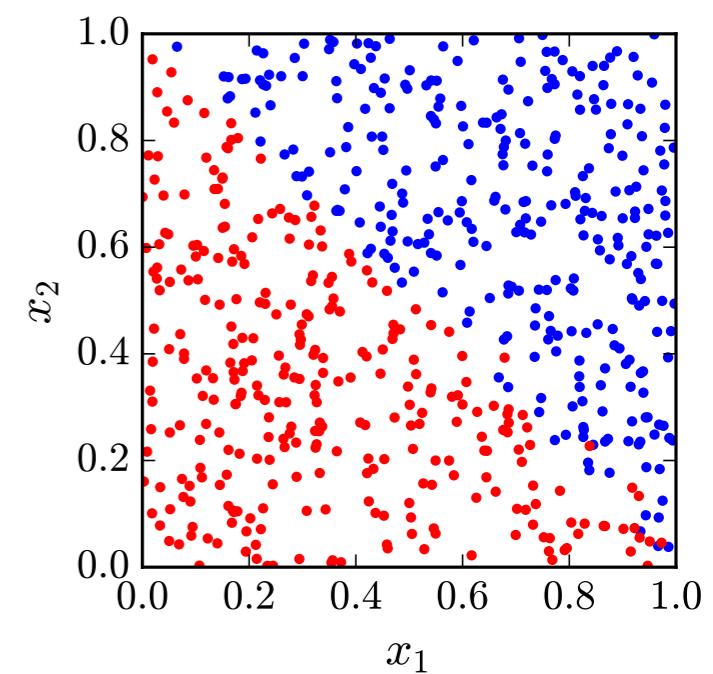
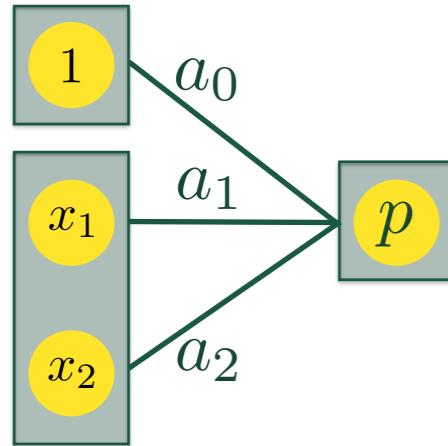


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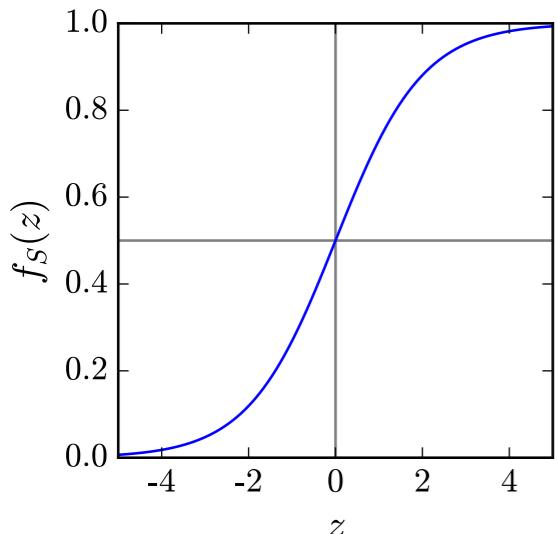
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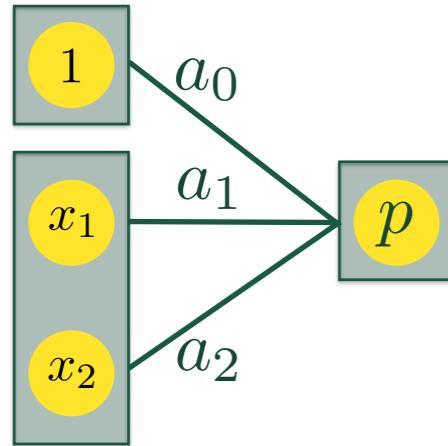


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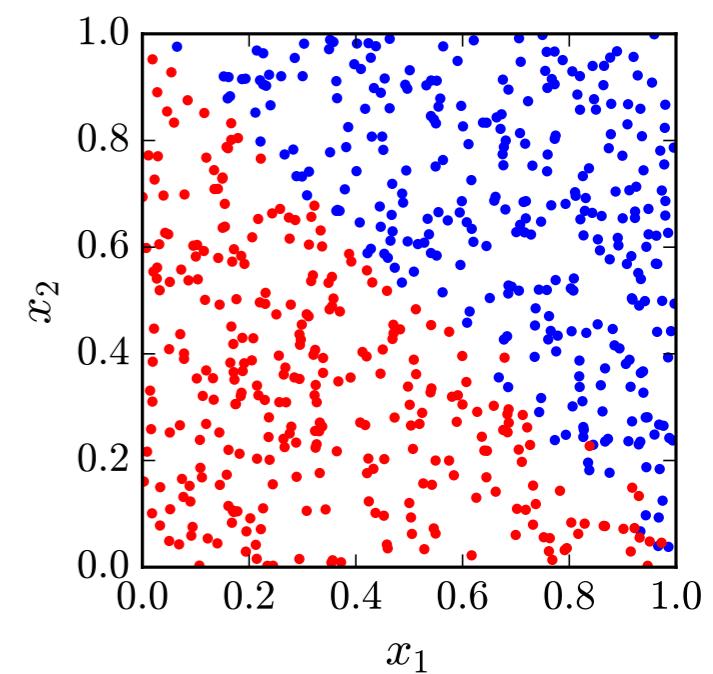
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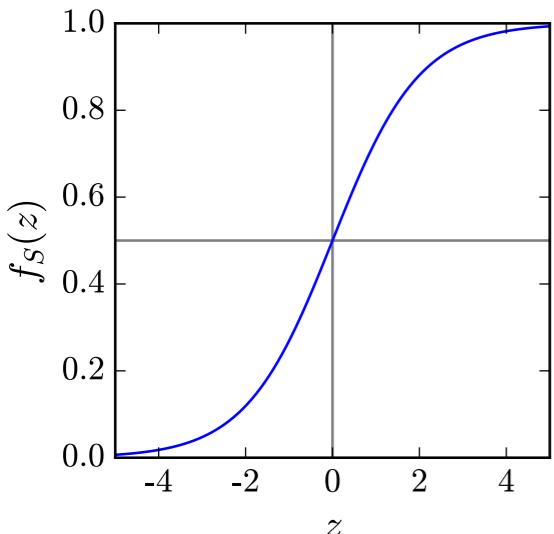
Minimize the loss with respect to  $\vec{a}$

Boundary at  $p(x, a) = 0$



# Logistic Regression

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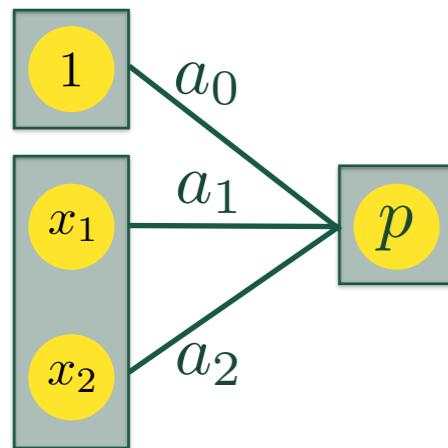


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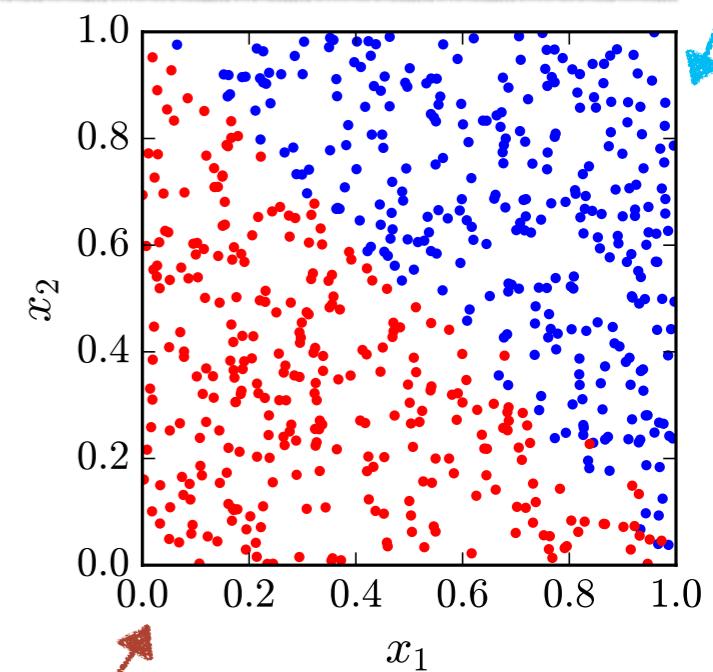
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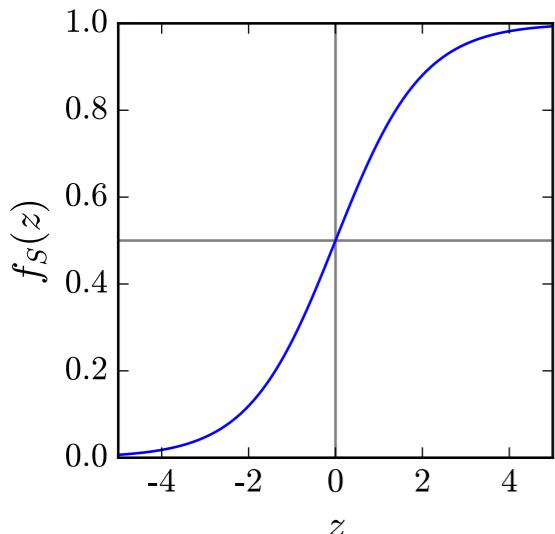
Large + values of  $p$



Large - values of  $p$

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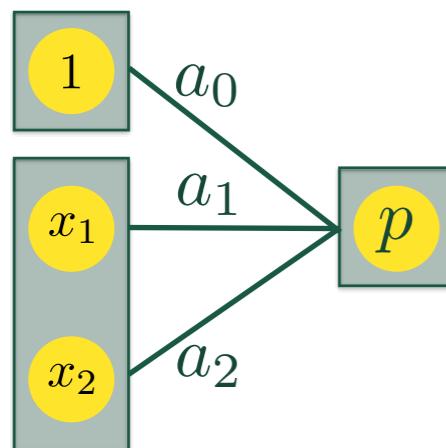


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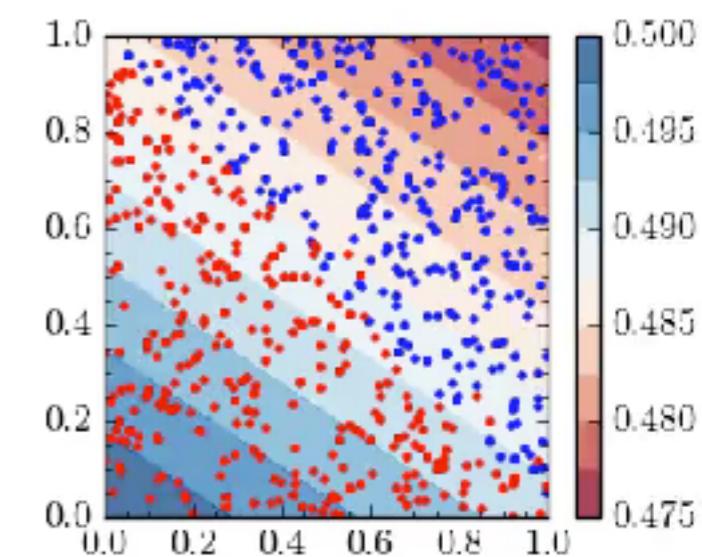
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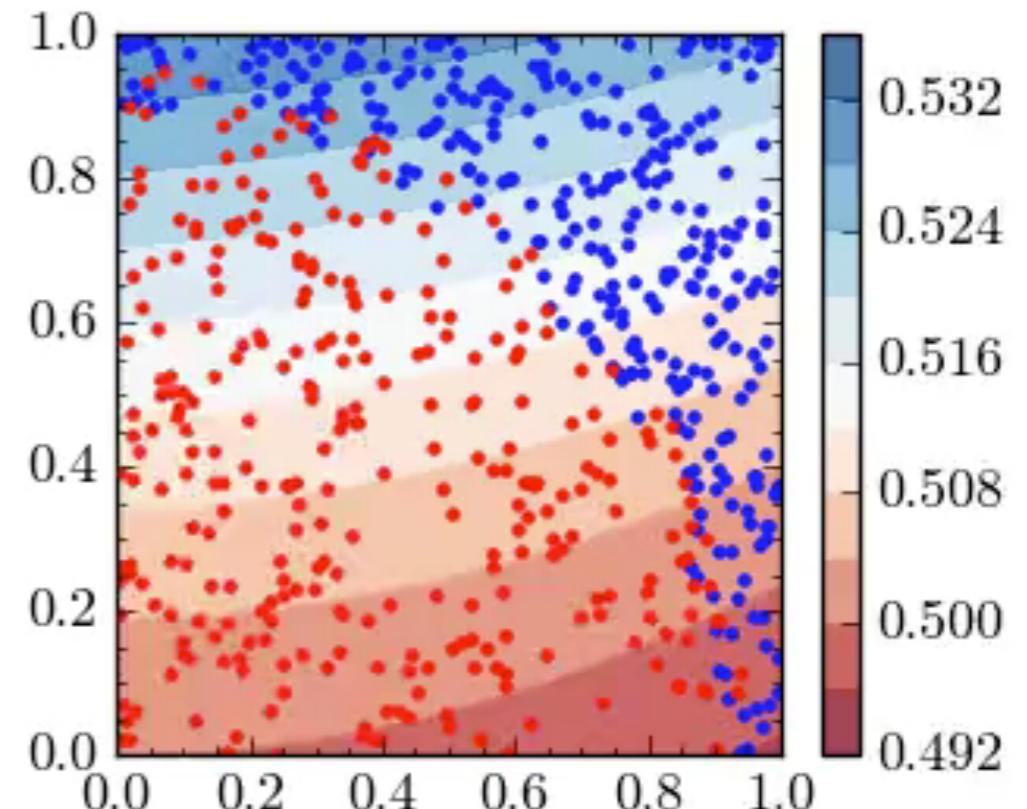
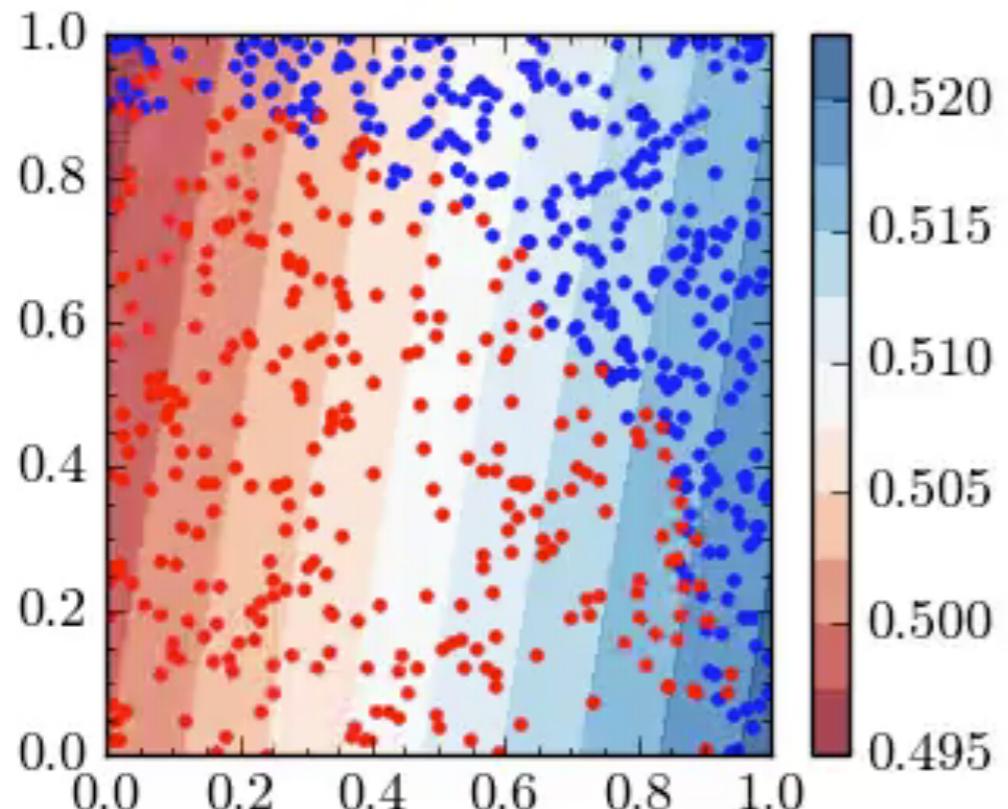


# Logistic Regression

What if there is a shape in the data?

$$p(x, a) = a_0 + x_1 a_1 + x_2 a_2$$

$$\begin{aligned} p(x, a) = & \ a_0 + a_1 x_1 + a_2 x_2 \\ & + a_3 x_1^2 + a_4 x_2^2 + a_5 x_1 x_2 \end{aligned}$$

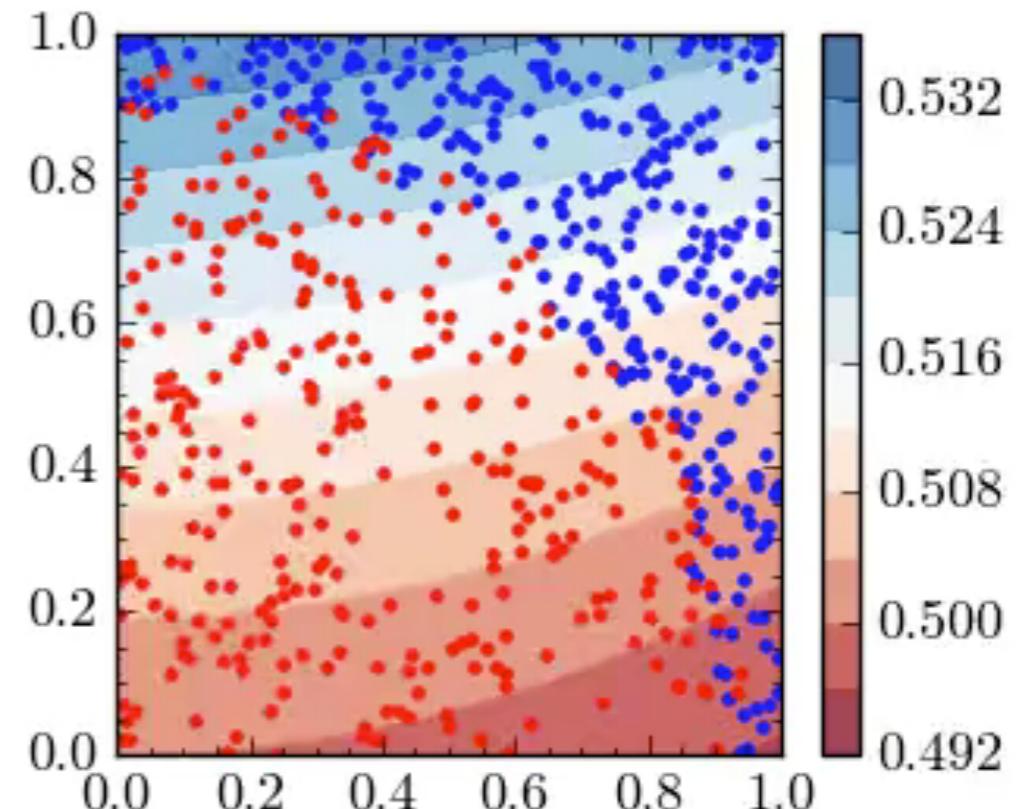
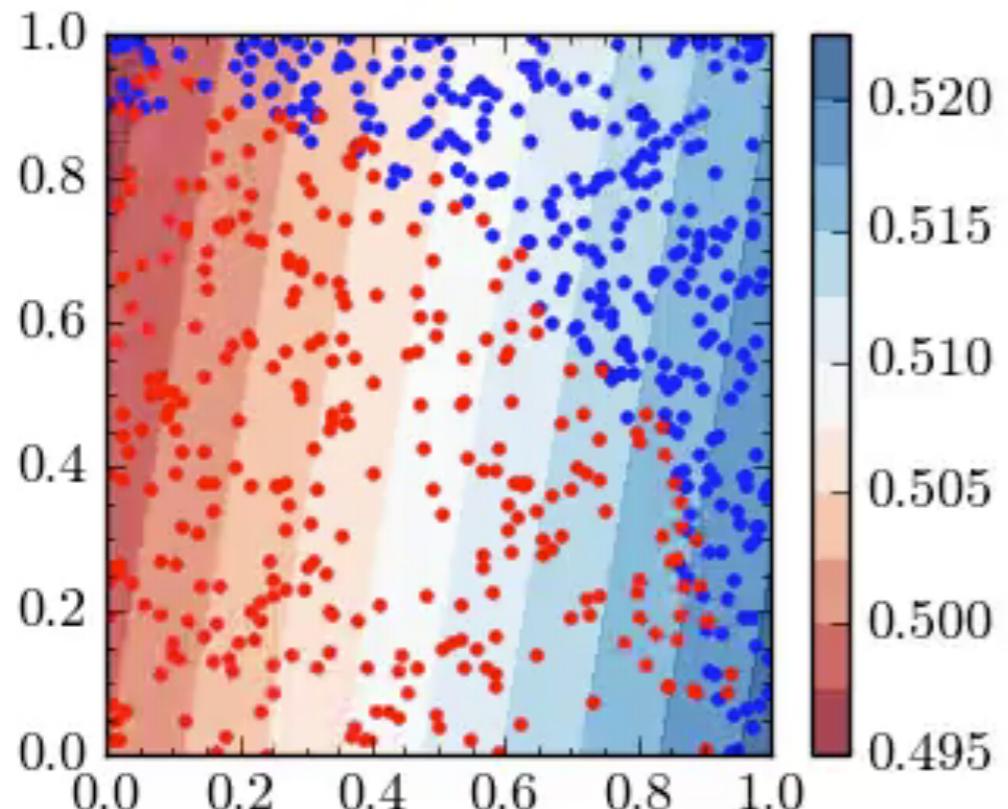


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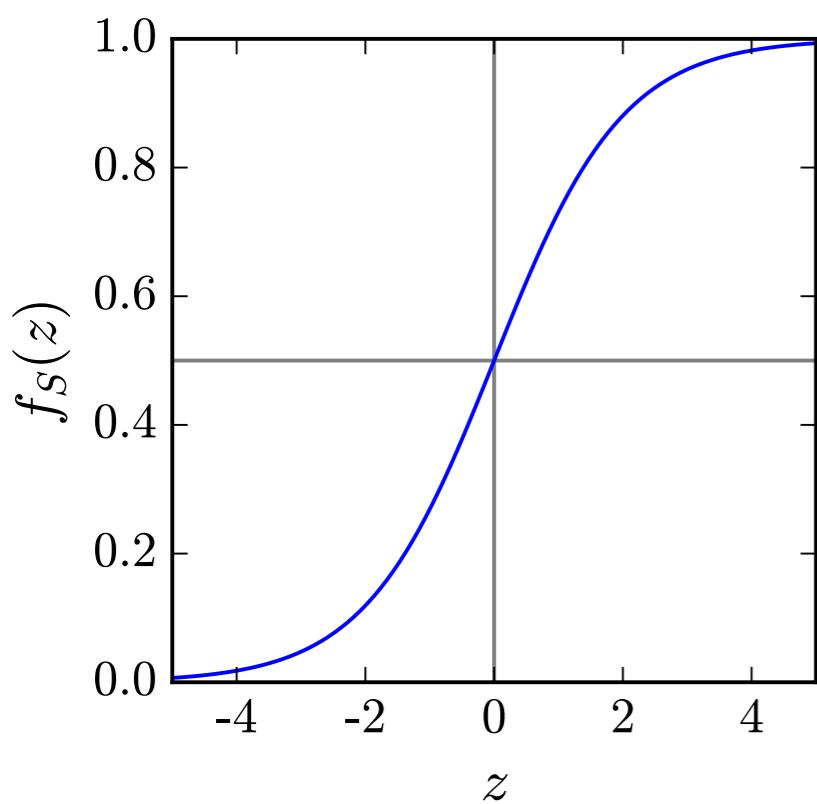
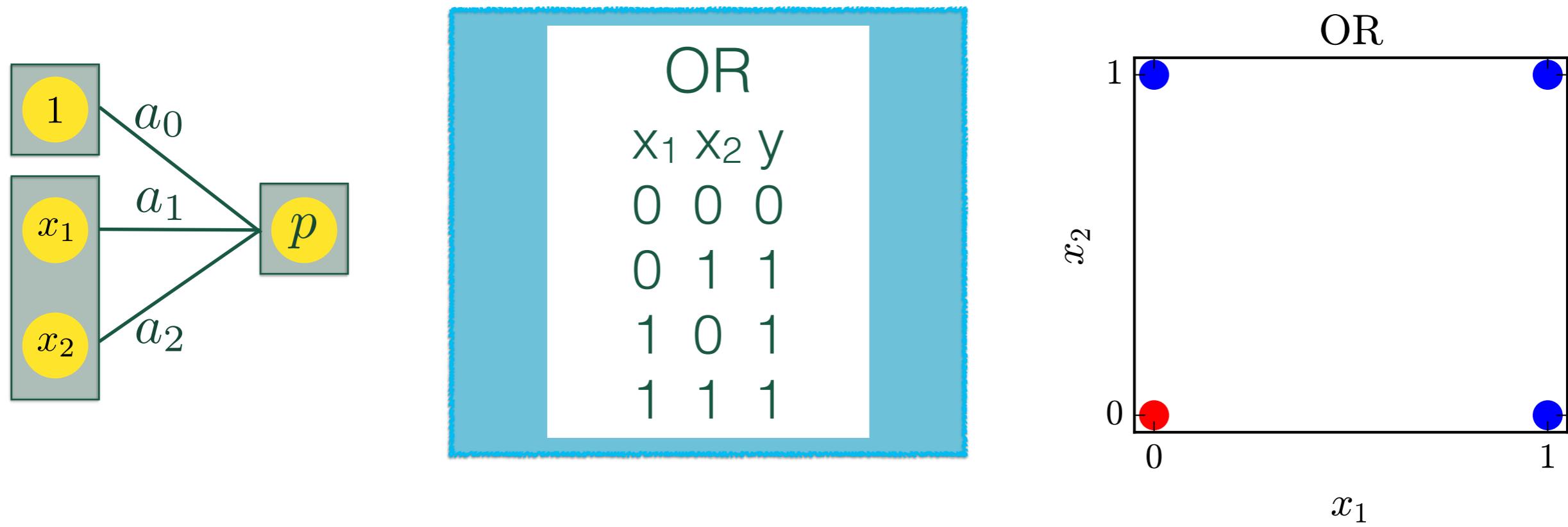


# Logistic Regression

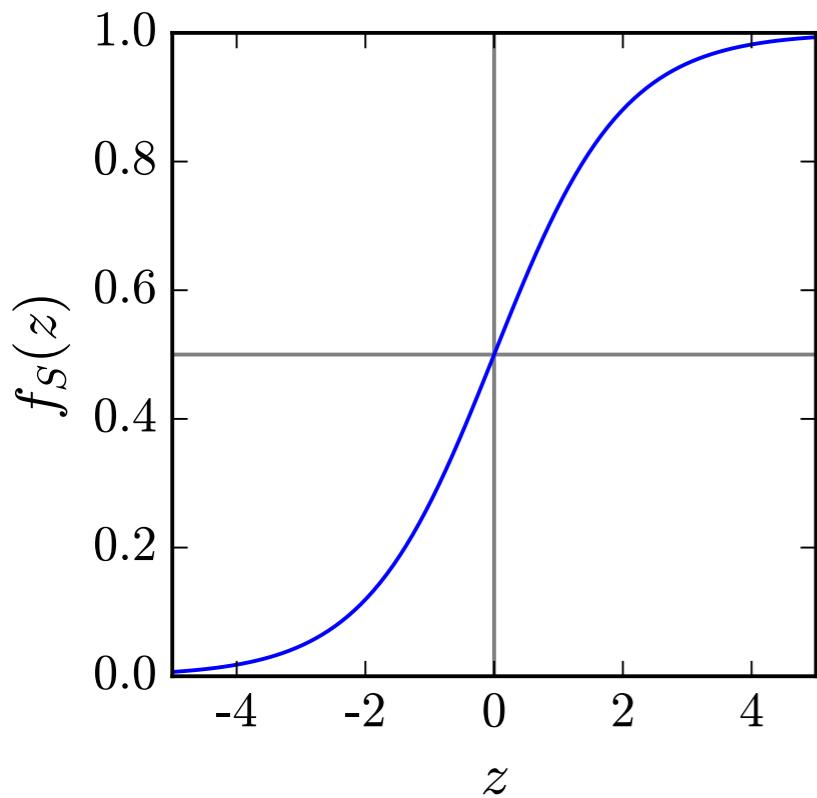
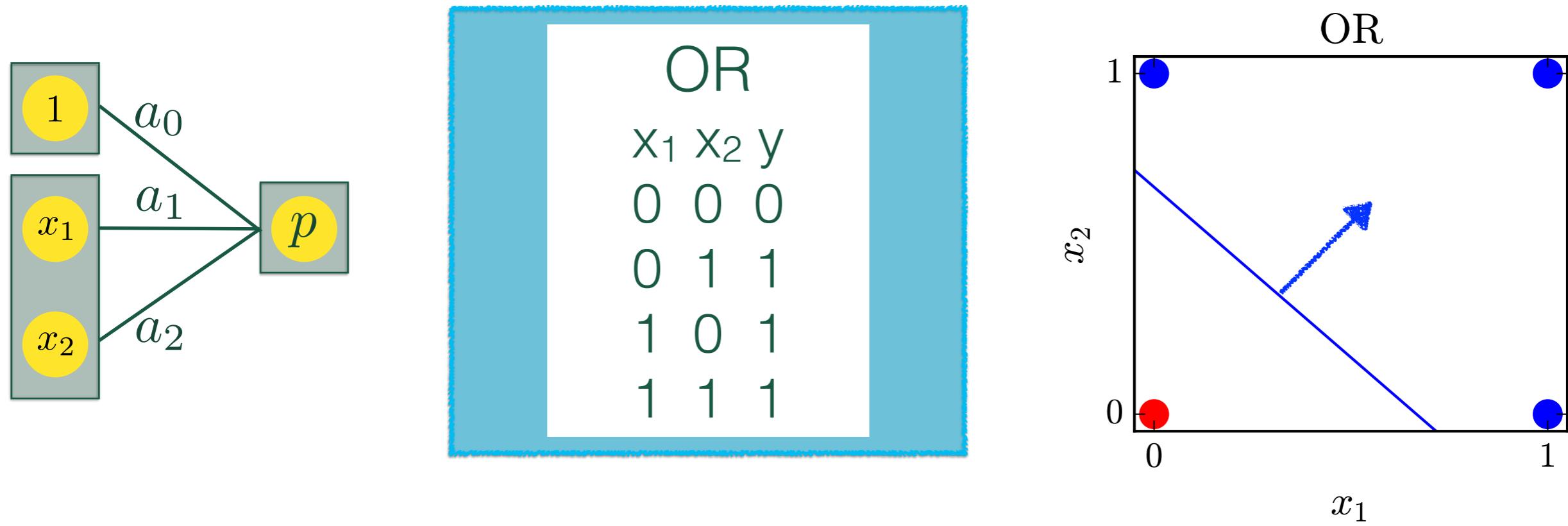
1. Can use nearly the same process for fitting a curve (predicting a number) or classification
2. Minimize a defined cost function
3. Easy to add parameters if shape is unknown — worry about over-fitting
4. If many inputs and complicated shapes, number of parameters necessary grows very quickly

Why use more complicated algorithms?

# Neural Networks

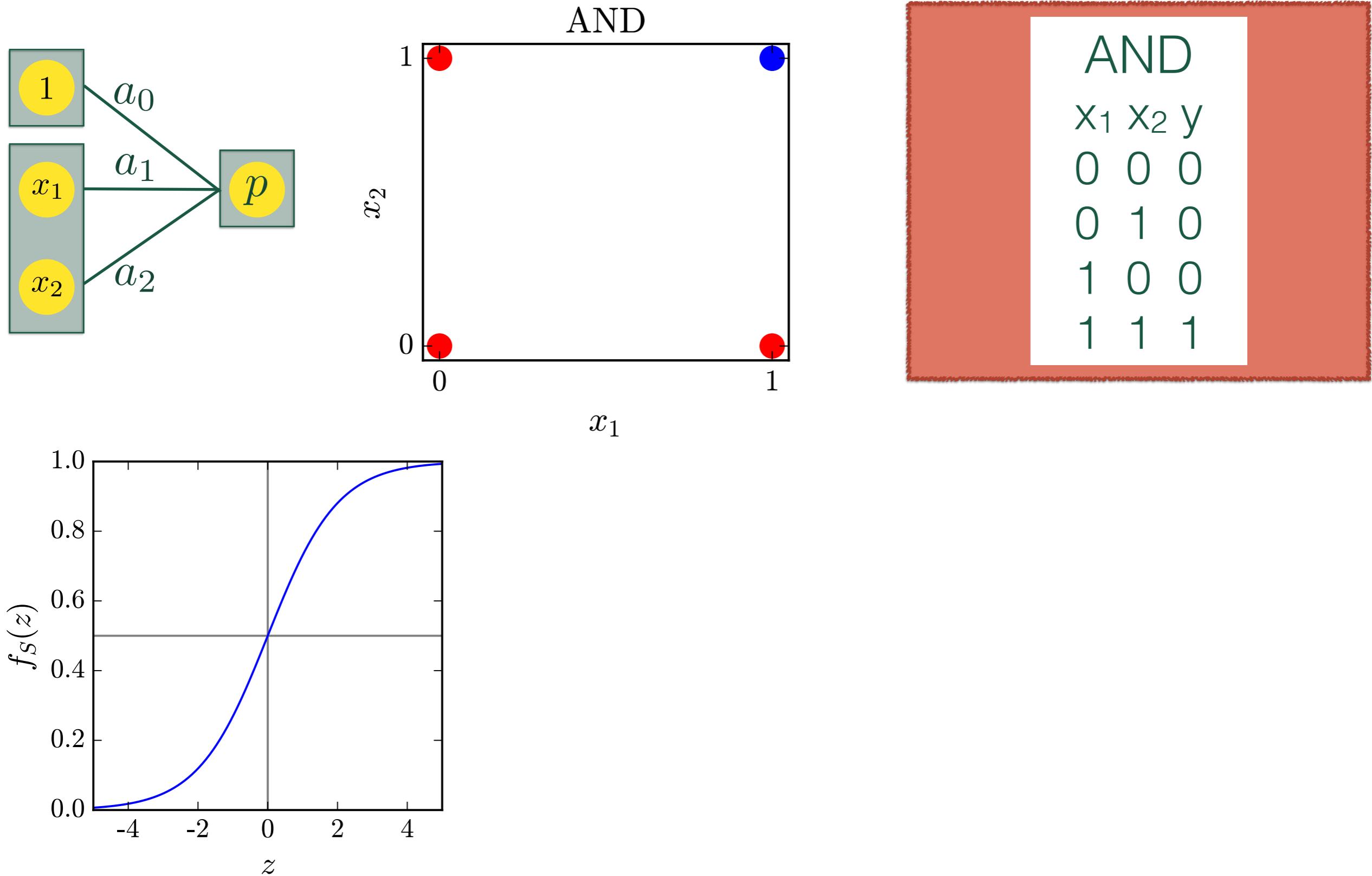


# Neural Networks

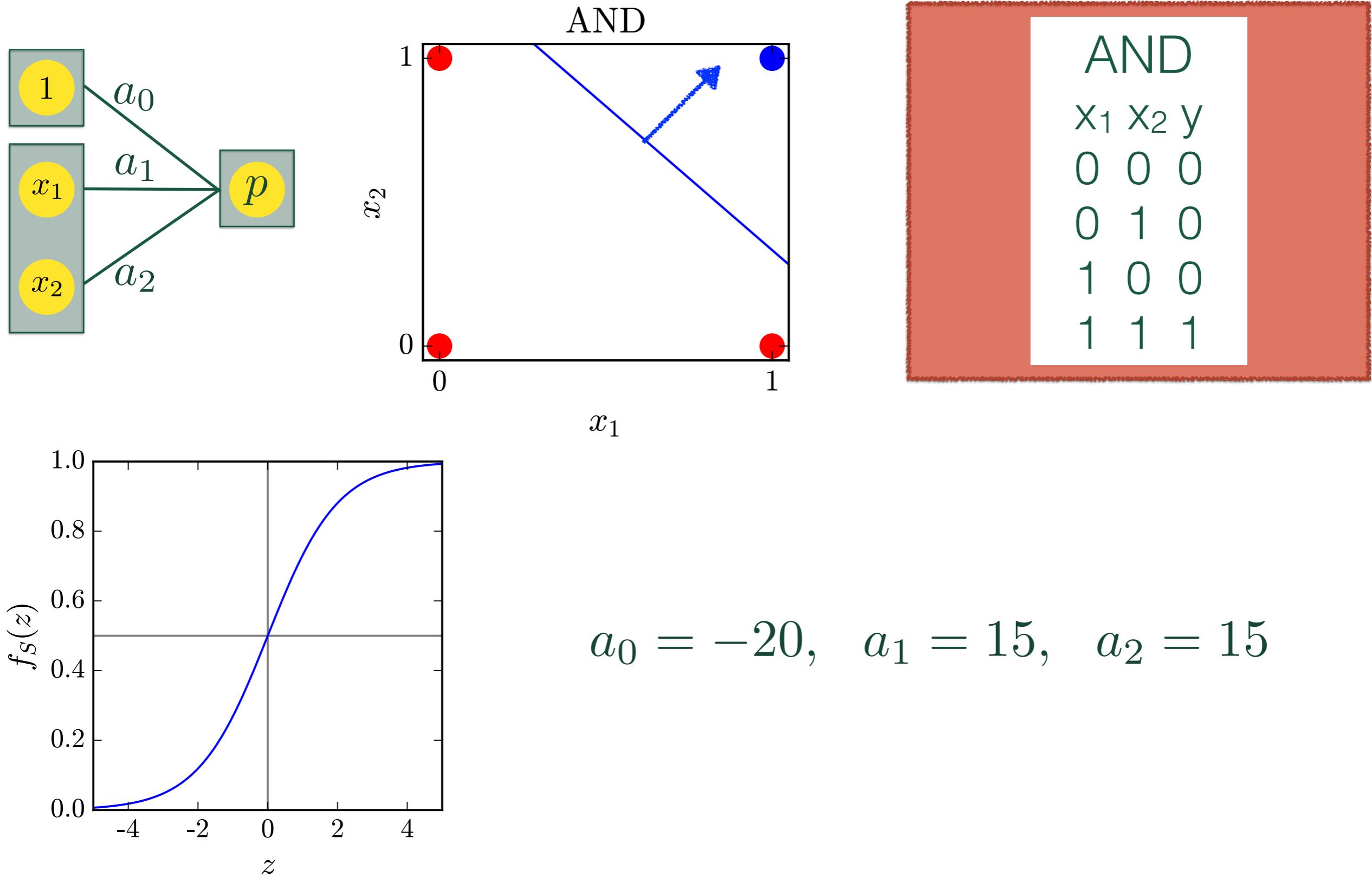


$$a_0 = -10, \quad a_1 = 15, \quad a_2 = 15$$

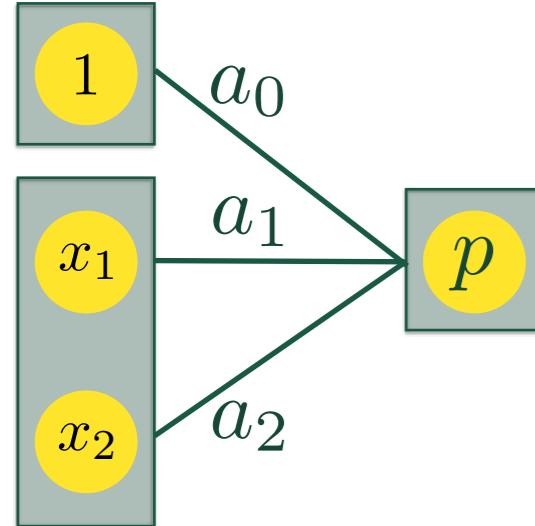
# Neural Networks



# Neural Networks



# Neural Networks



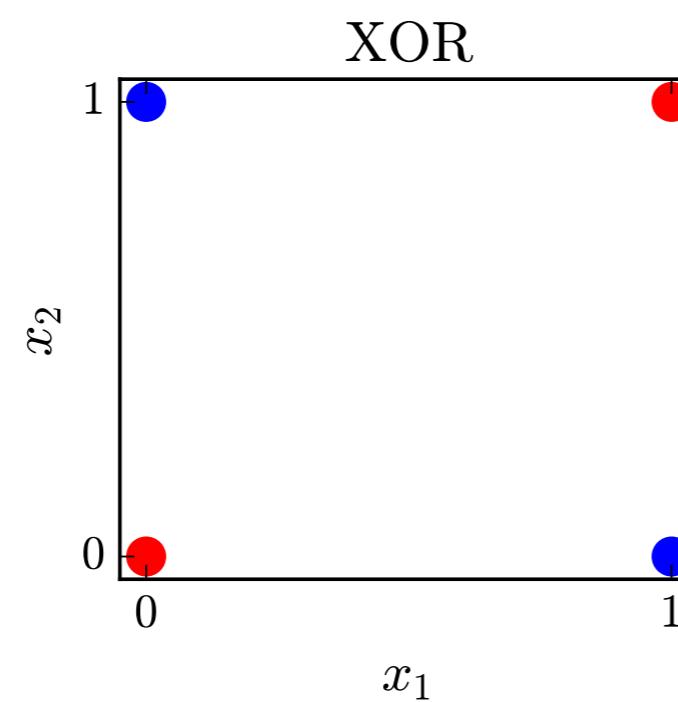
OR		
$x_1$	$x_2$	y
0	0	0
0	1	1
1	0	1
1	1	1

AND		
$x_1$	$x_2$	y
0	0	0
0	1	0
1	0	0
1	1	1

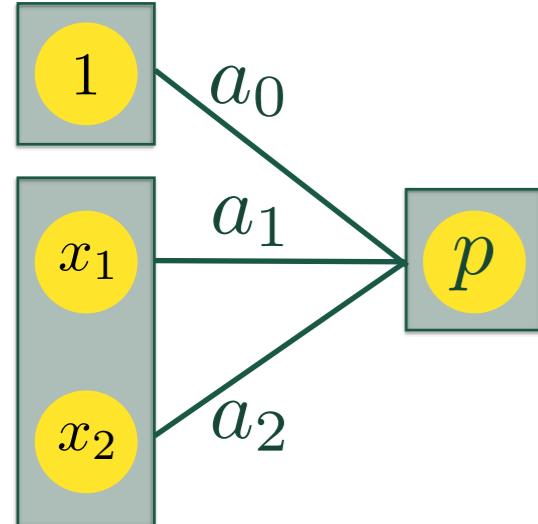
$$a_0 = -10, \quad a_1 = 15, \quad a_2 = 15$$

$$a_0 = -20, \quad a_1 = 15, \quad a_2 = 15$$

XOR		
$x_1$	$x_2$	y
0	0	0
0	1	1
1	0	1
1	1	0



# Neural Networks



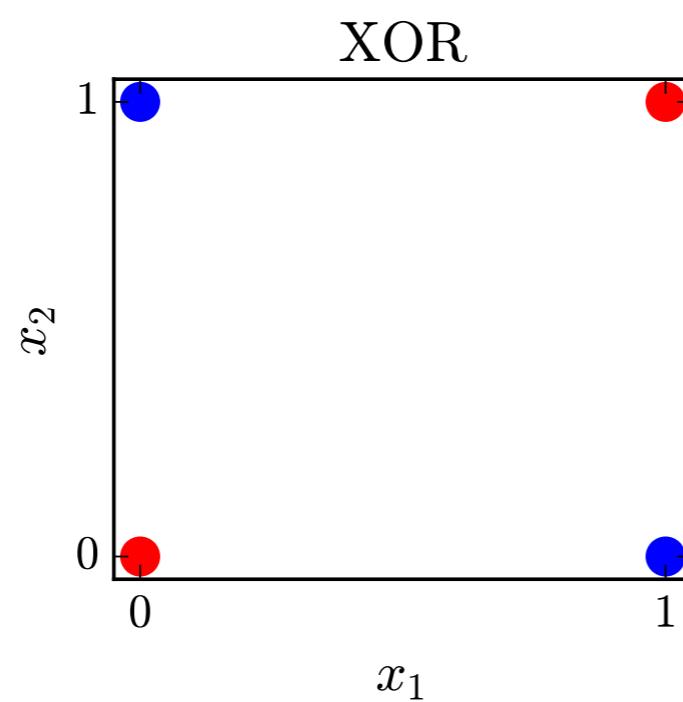
OR		
$x_1$	$x_2$	y
0	0	0
0	1	1
1	0	1
1	1	1

AND		
$x_1$	$x_2$	y
0	0	0
0	1	0
1	0	0
1	1	1

$$a_0 = -10, \quad a_1 = 15, \quad a_2 = 15$$

$$a_0 = -20, \quad a_1 = 15, \quad a_2 = 15$$

XOR		
$x_1$	$x_2$	y
0	0	0
0	1	1
1	0	1
1	1	0

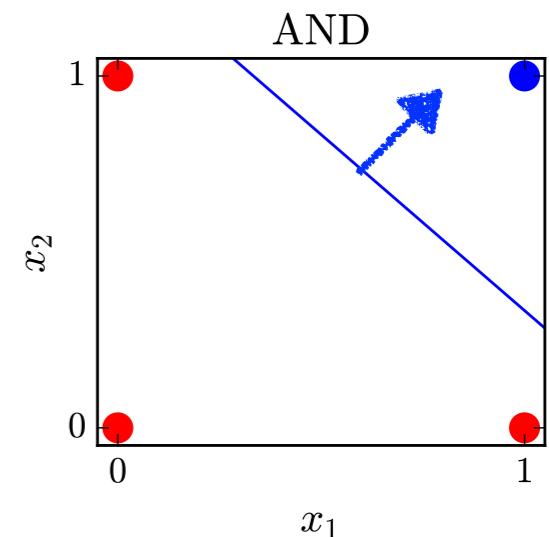
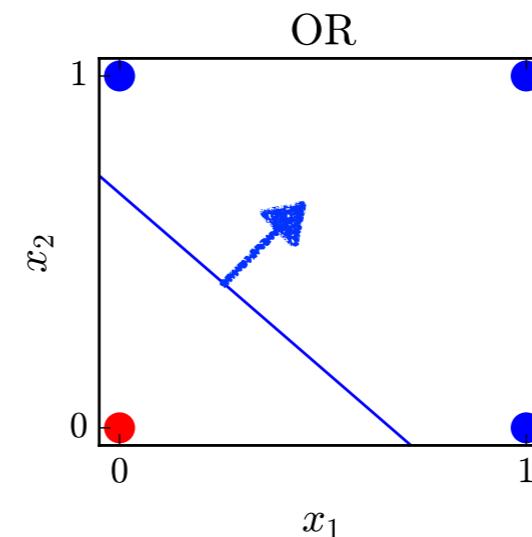
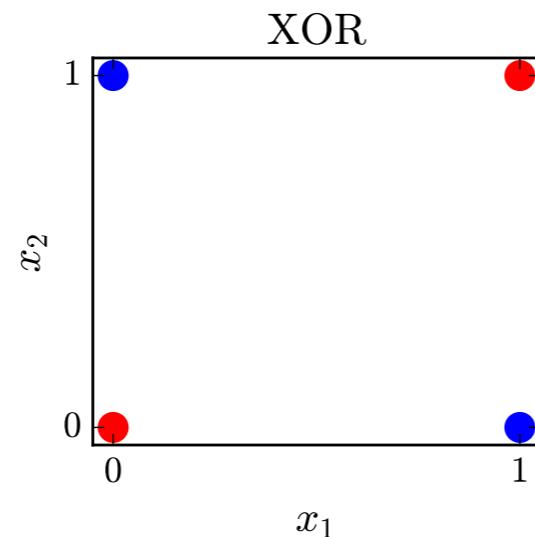


This system cannot produce XOR

(cannot make a two sided cut)

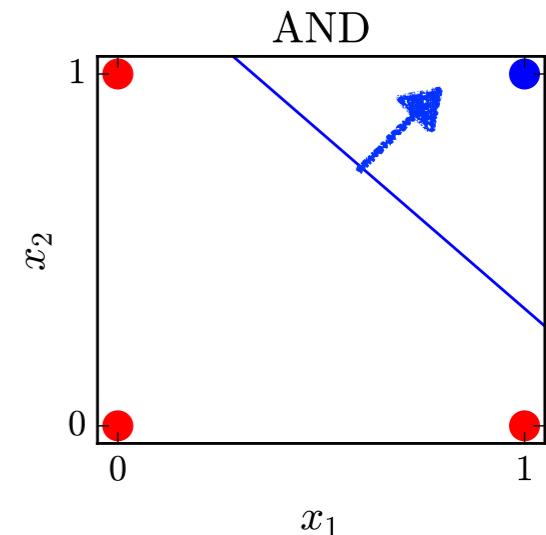
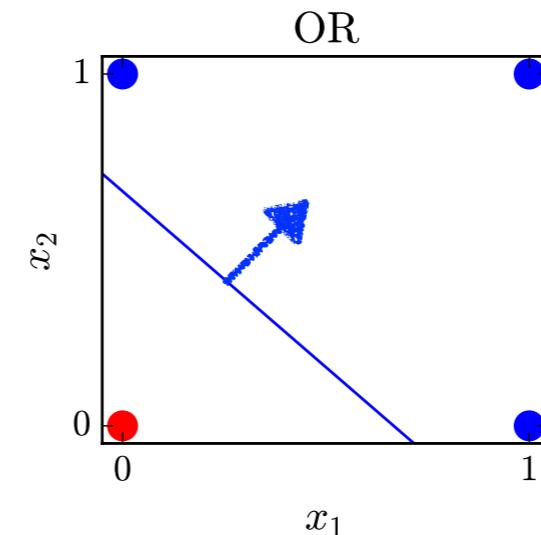
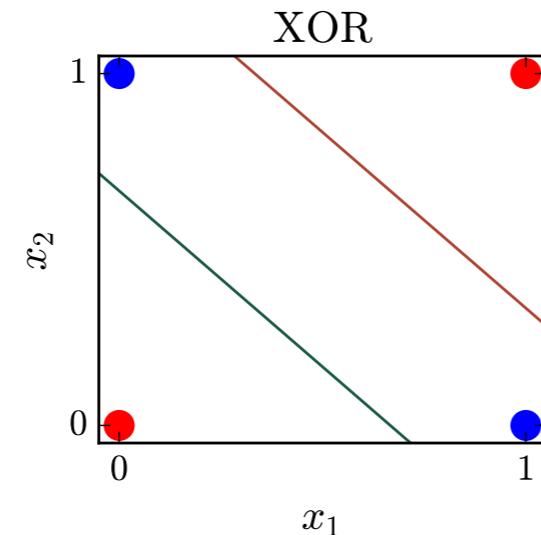
# Neural Networks

XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



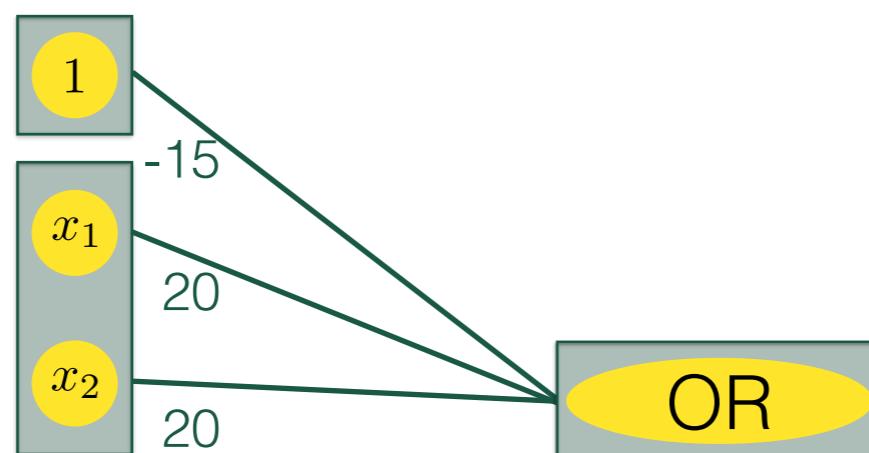
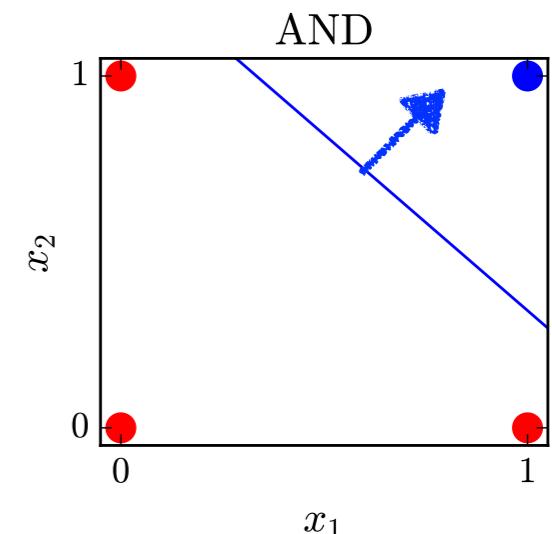
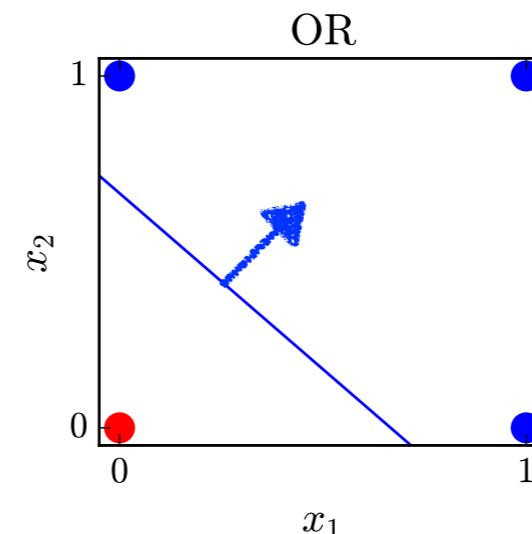
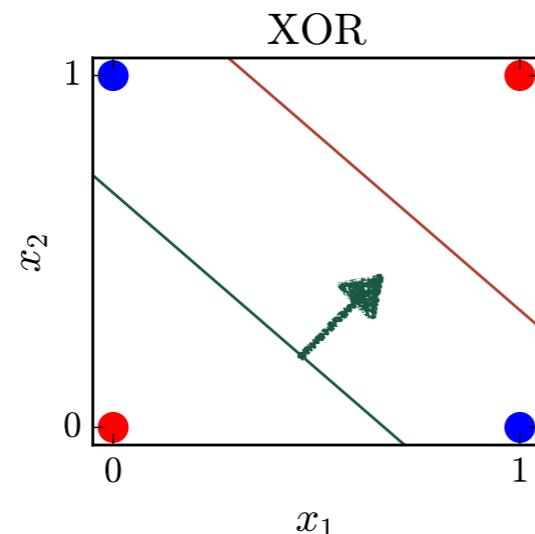
# Neural Networks

XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



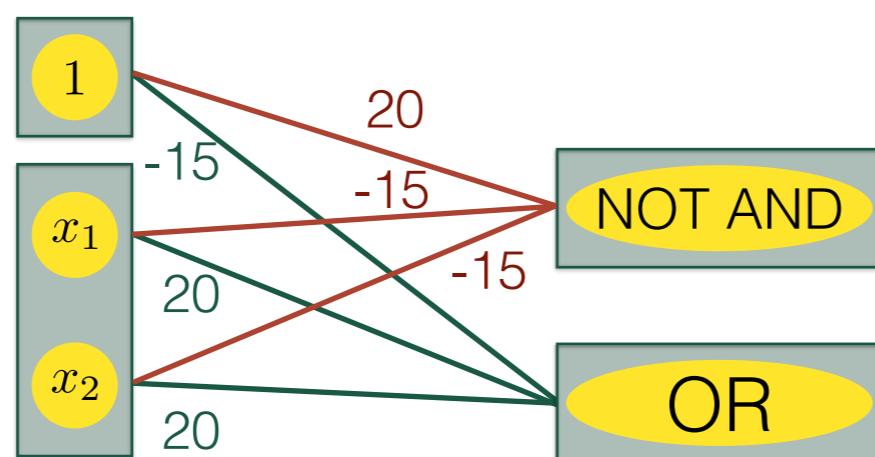
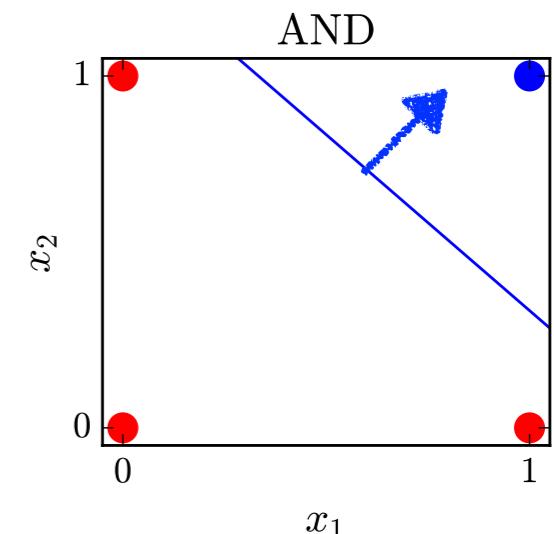
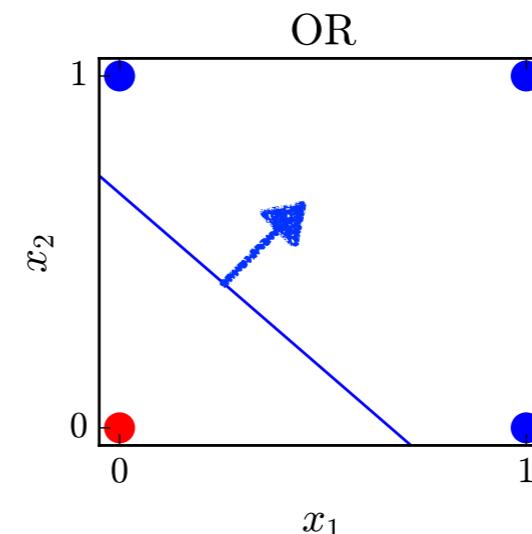
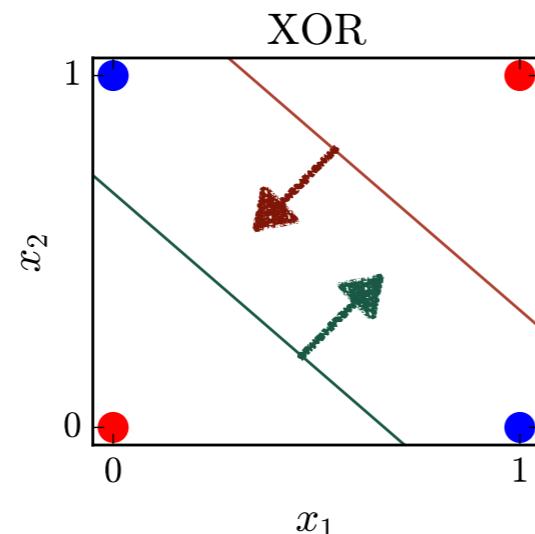
# Neural Networks

XOR		
$x_1$	$x_2$	y
0	0	0
0	1	1
1	0	1
1	1	0



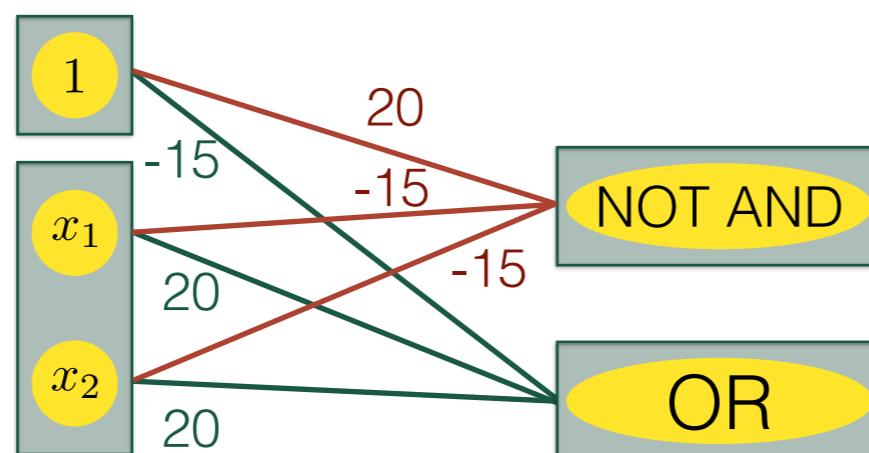
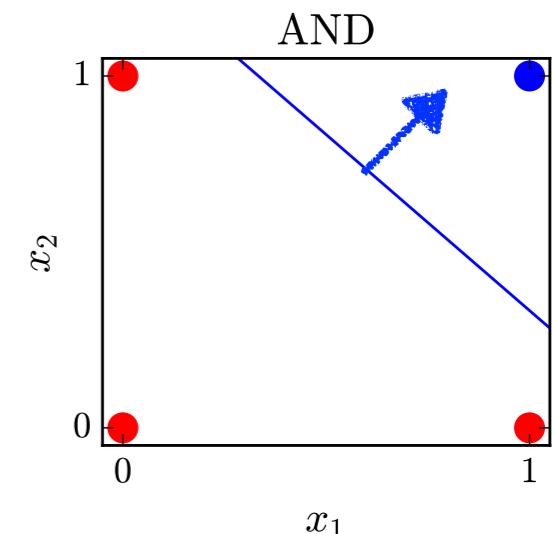
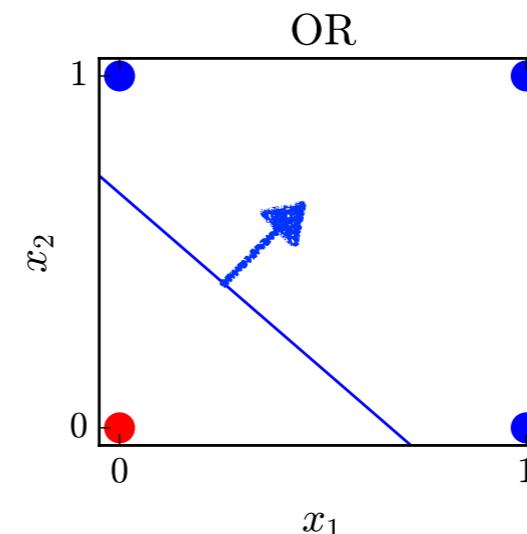
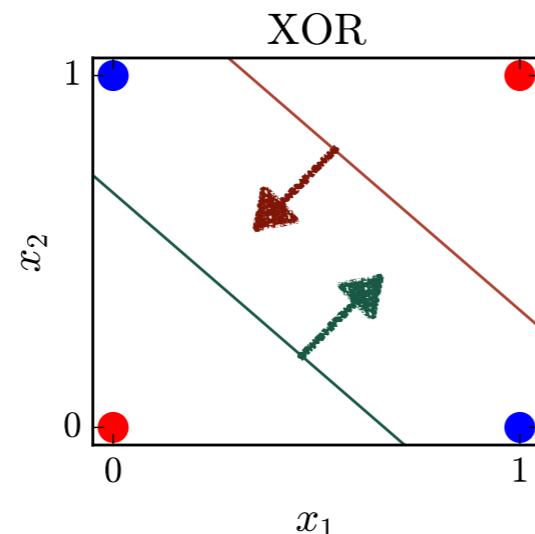
# Neural Networks

XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



# Neural Networks

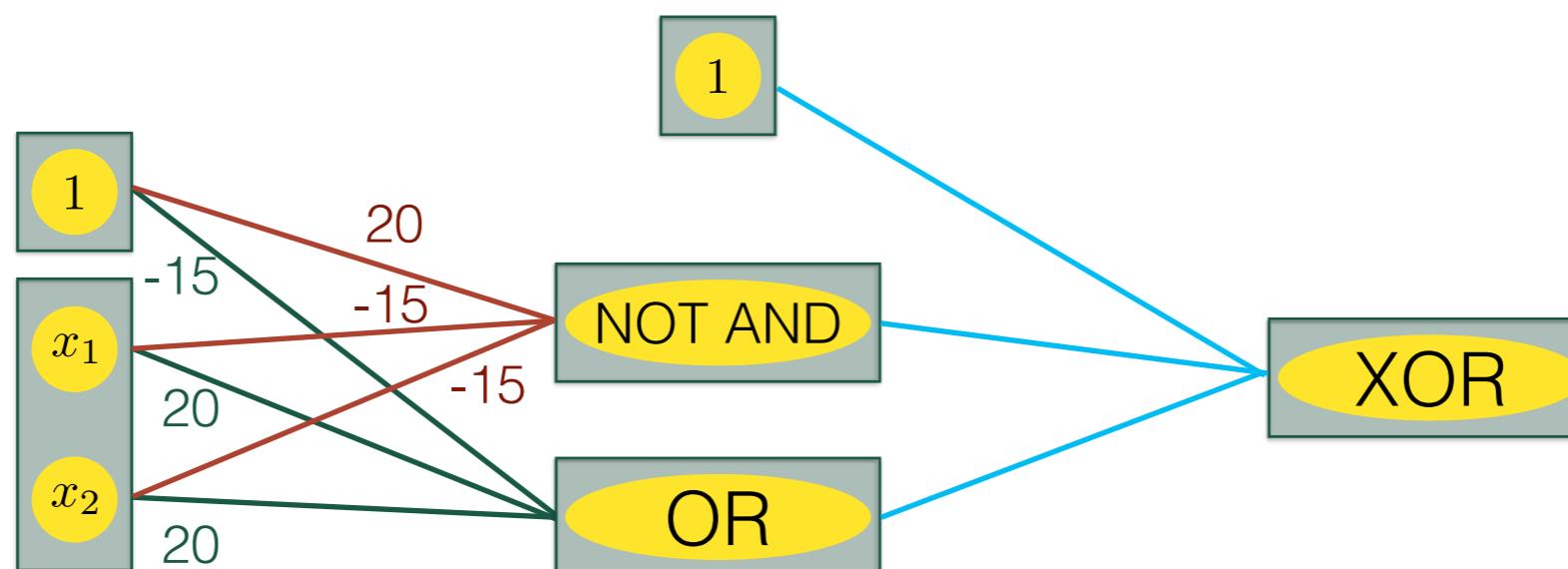
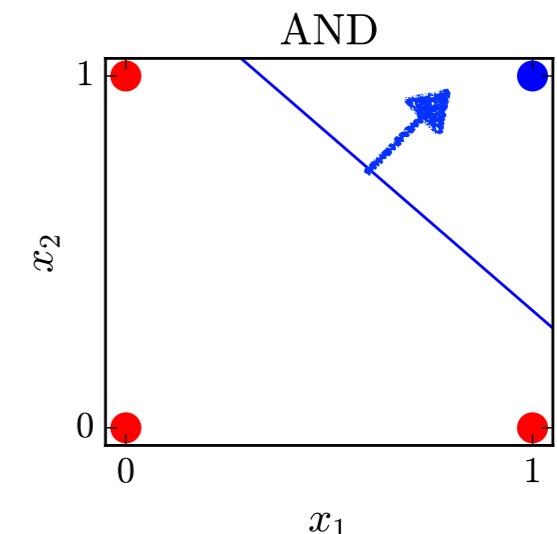
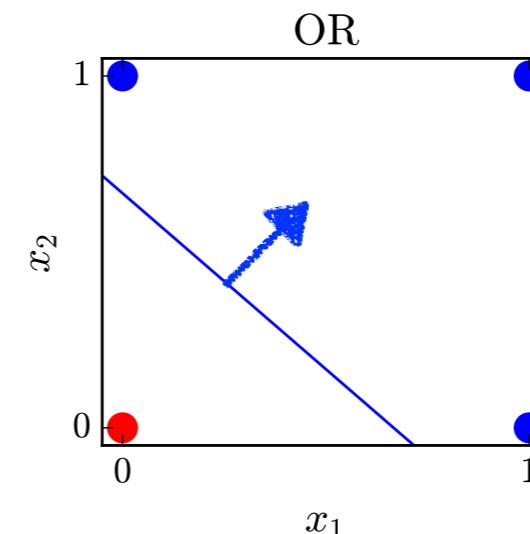
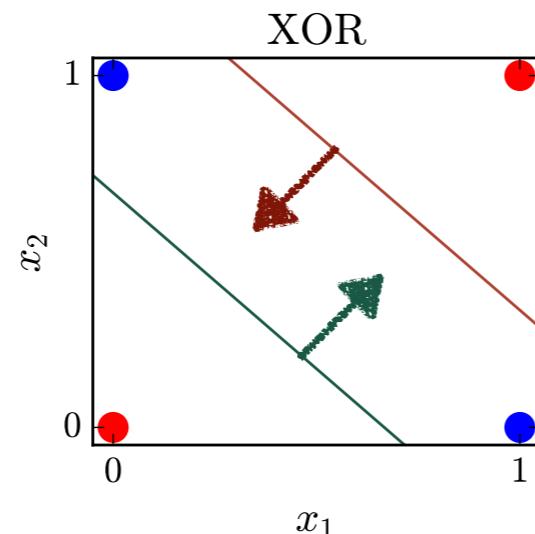
XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



$x_1$	$x_2$	OR	NOT AND	XOR
0	0	0	1	0
0	1	1	1	1
1	0	1	1	1
1	1	1	0	0

# Neural Networks

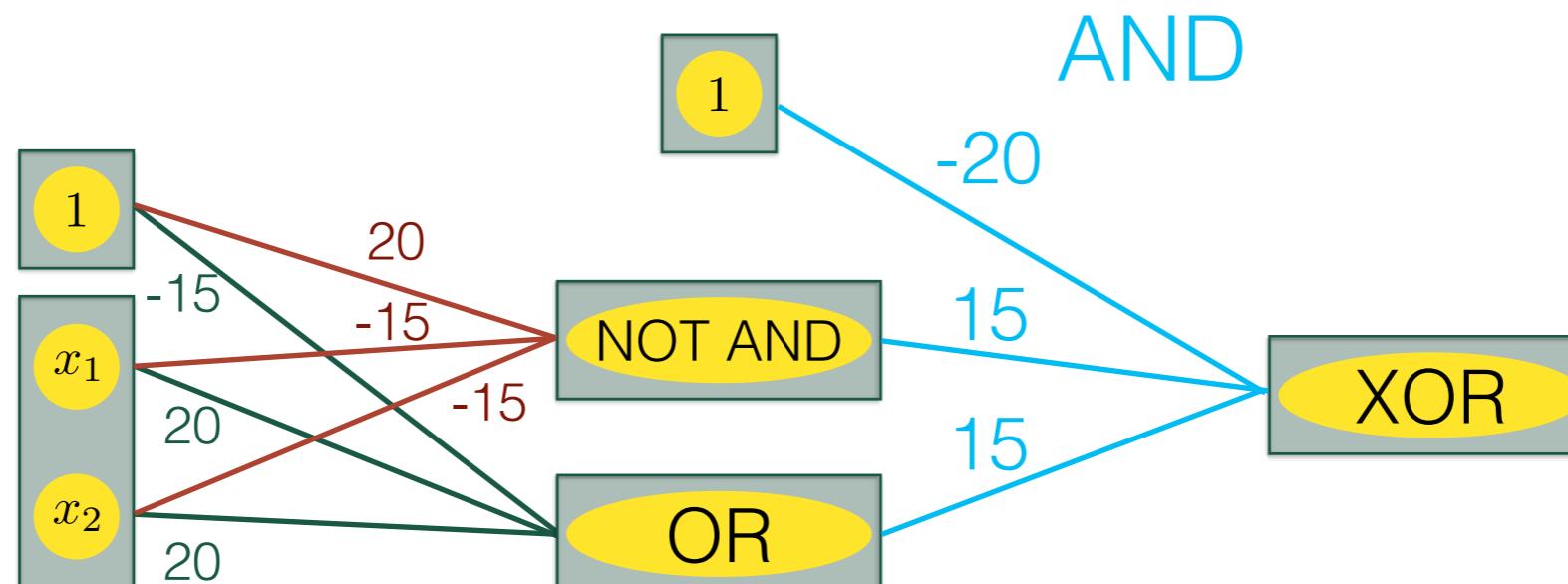
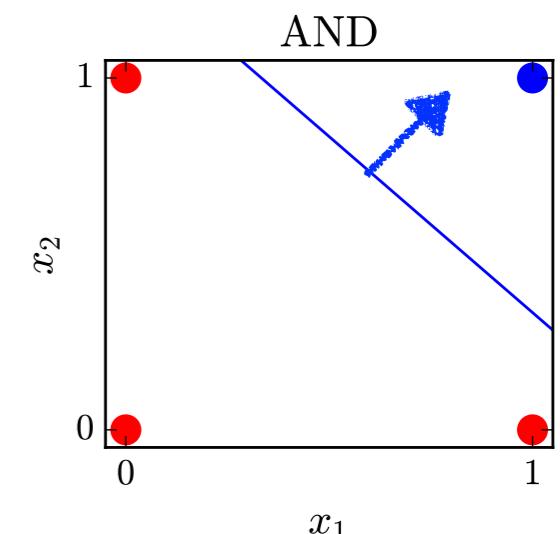
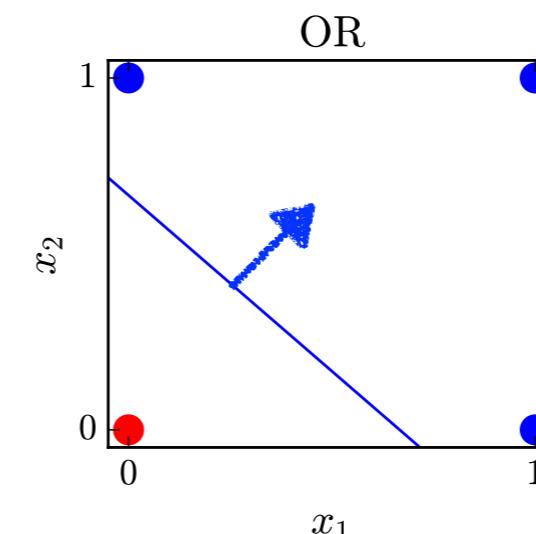
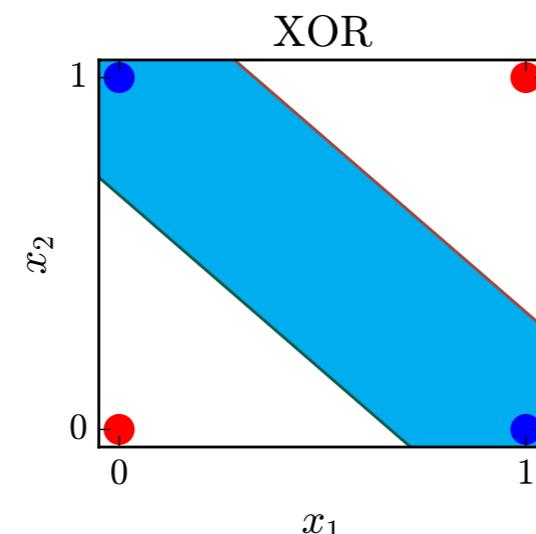
XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



$x_1$	$x_2$	OR	NOT AND	XOR
0	0	0	1	0
0	1	1	1	1
1	0	1	1	1
1	1	1	0	0

# Neural Networks

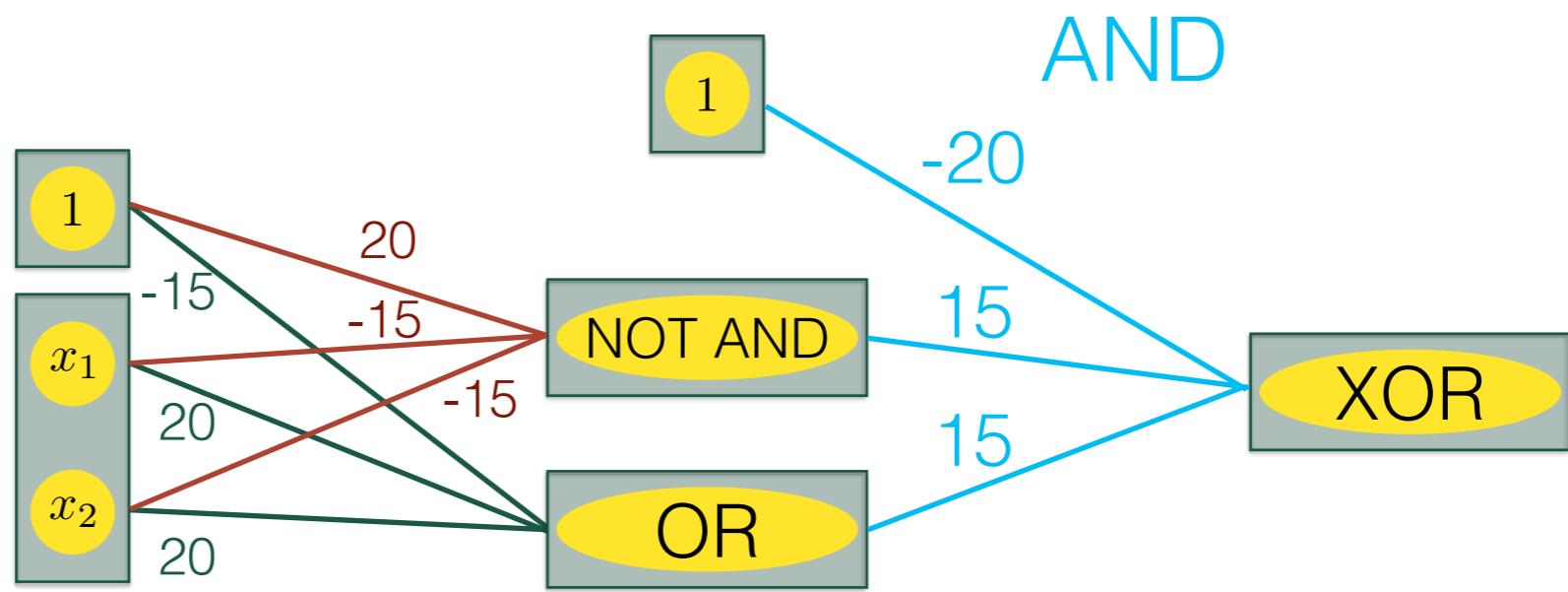
XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



$x_1$	$x_2$	OR	NOT AND	XOR
0	0	0	1	0
0	1	1	1	1
1	0	1	1	1
1	1	1	0	0

# Neural Networks

XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0

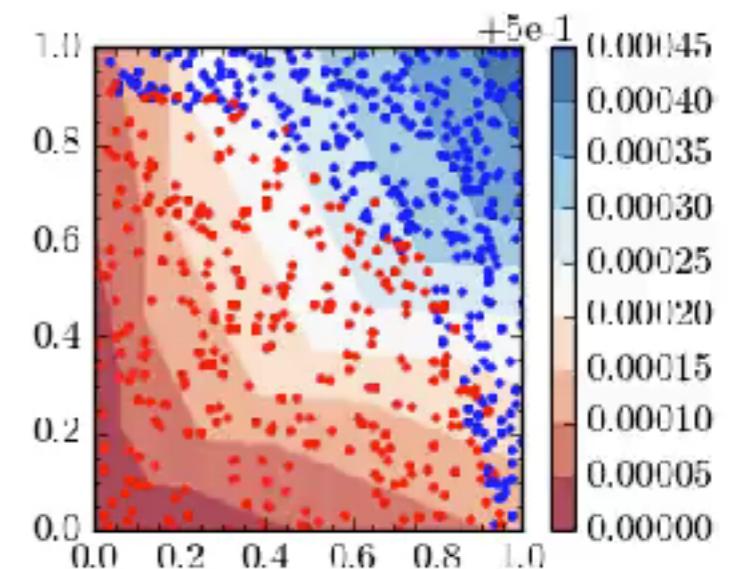
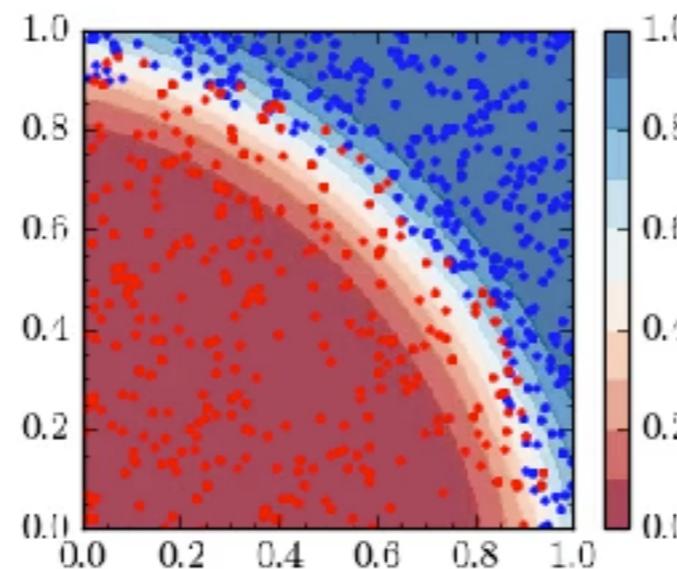
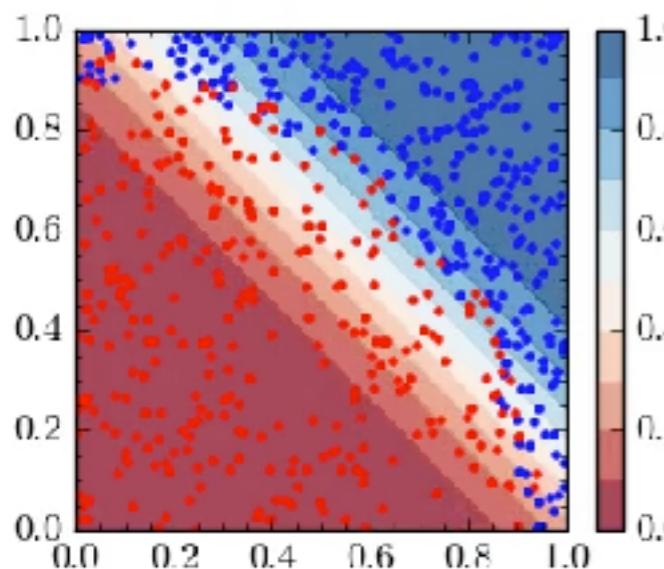
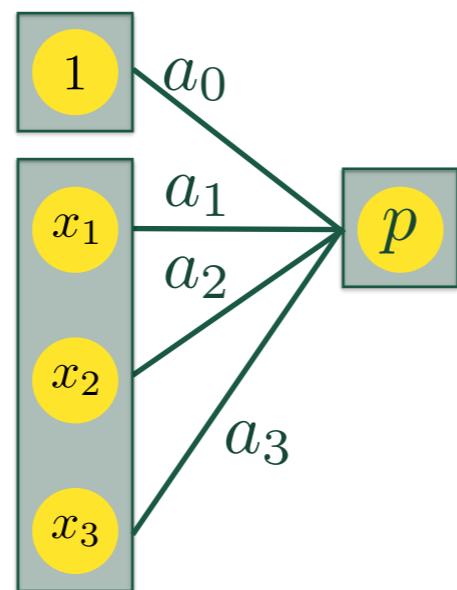


Simple example showing that neural network can access ‘high-level’ functions

To learn weights, need large training set and CPU time

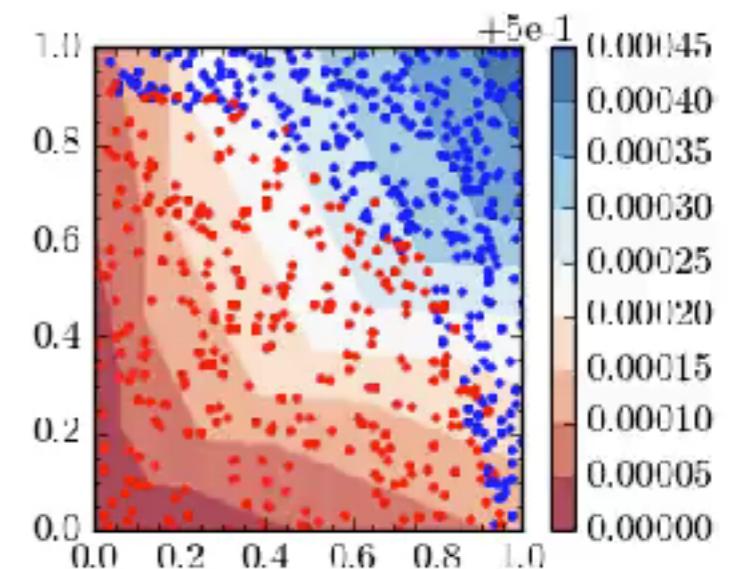
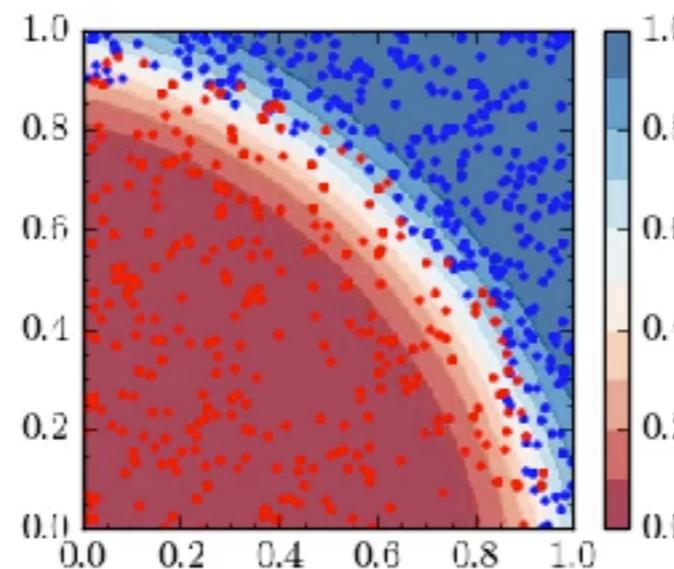
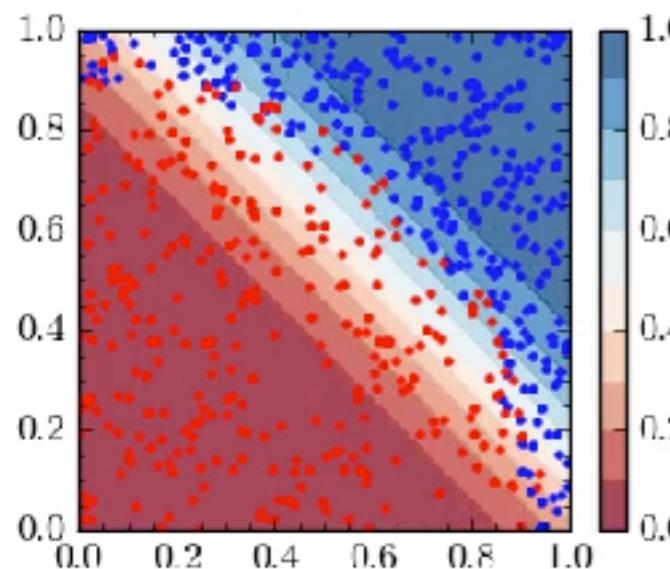
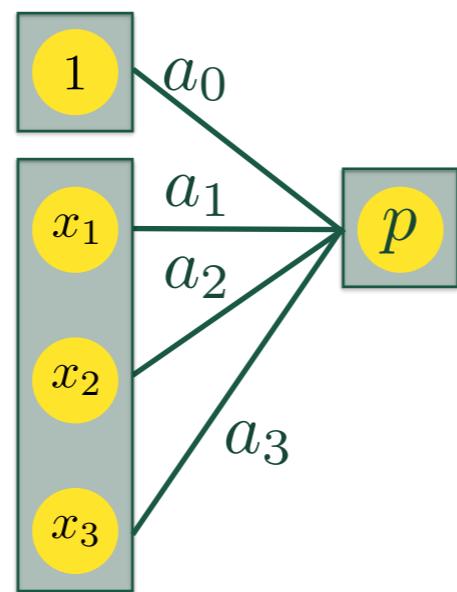
# Neural Networks

- Don't add more inputs, let machine find own shape
- Ability to learn 'any' function
- More nodes/hidden layers allows for more complex features



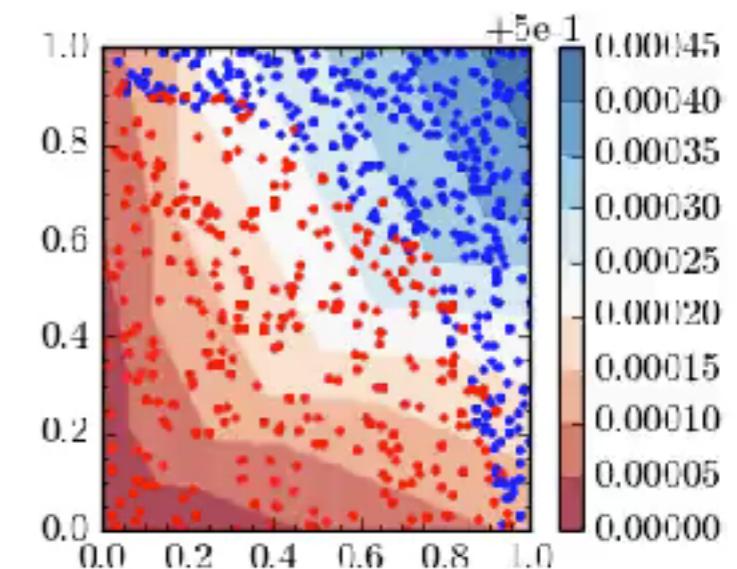
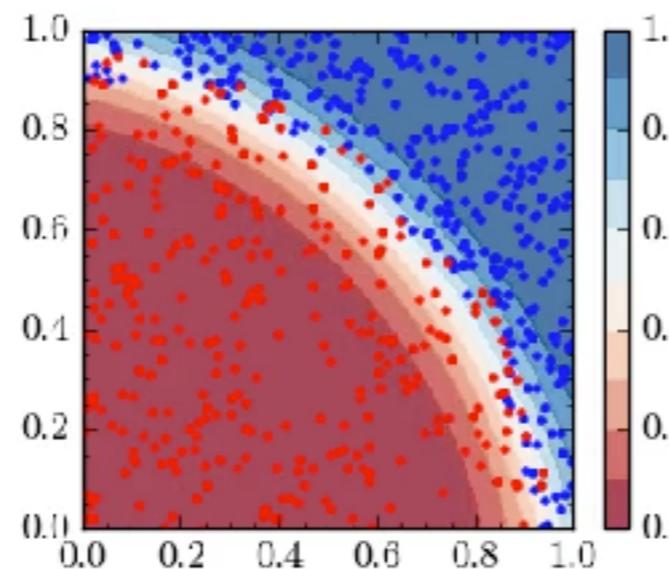
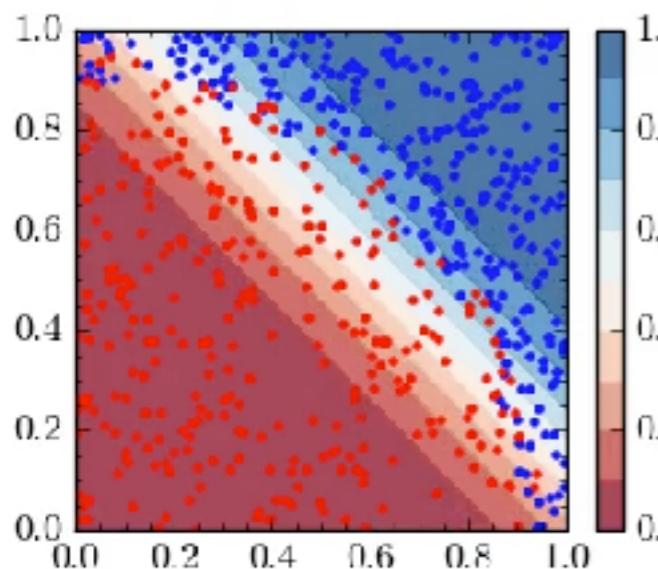
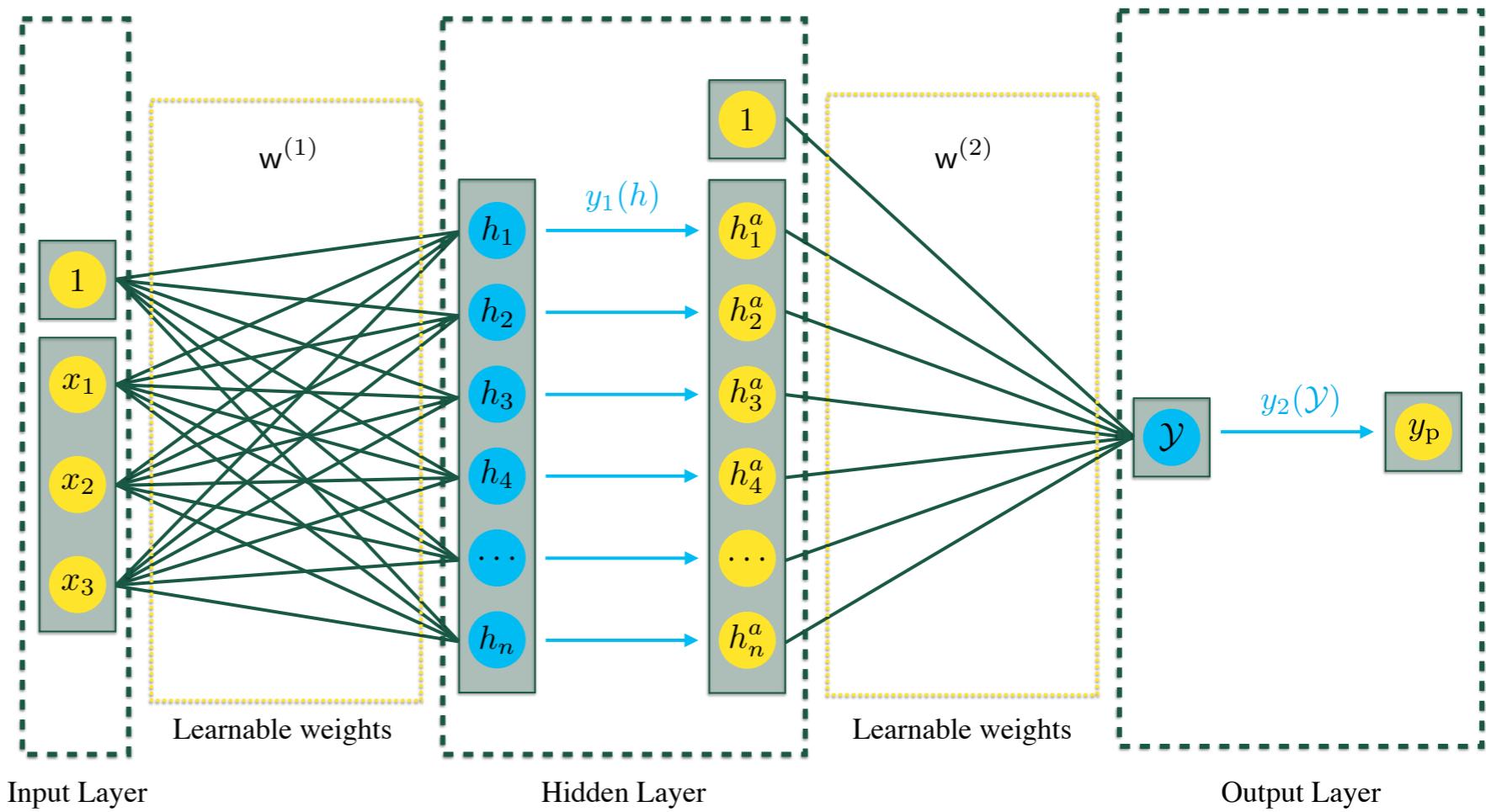
# Neural Networks

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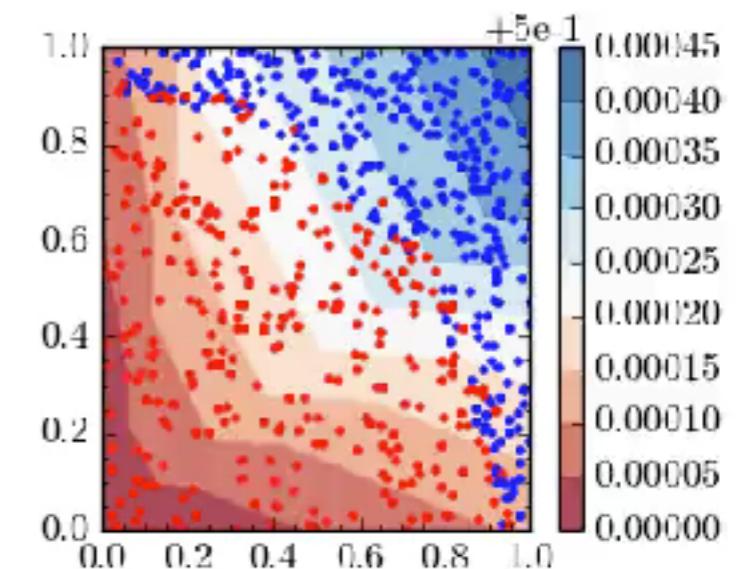
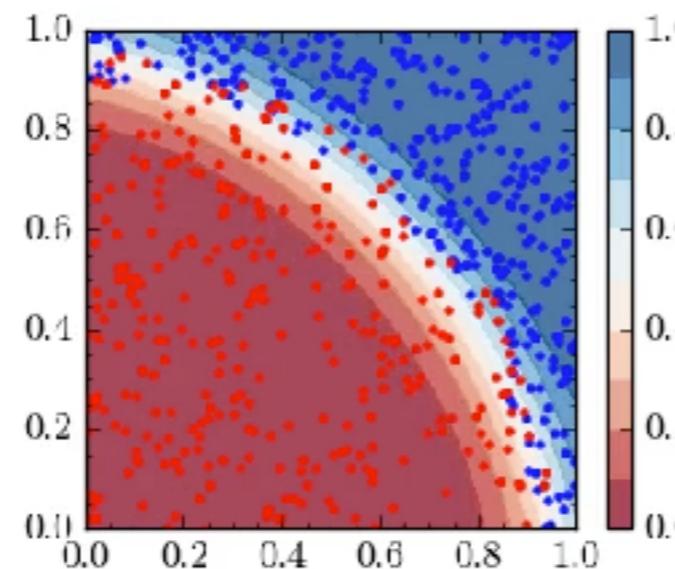
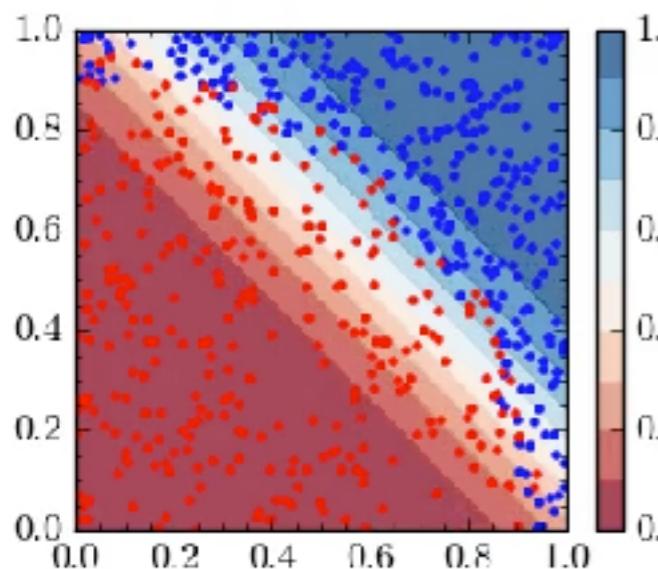
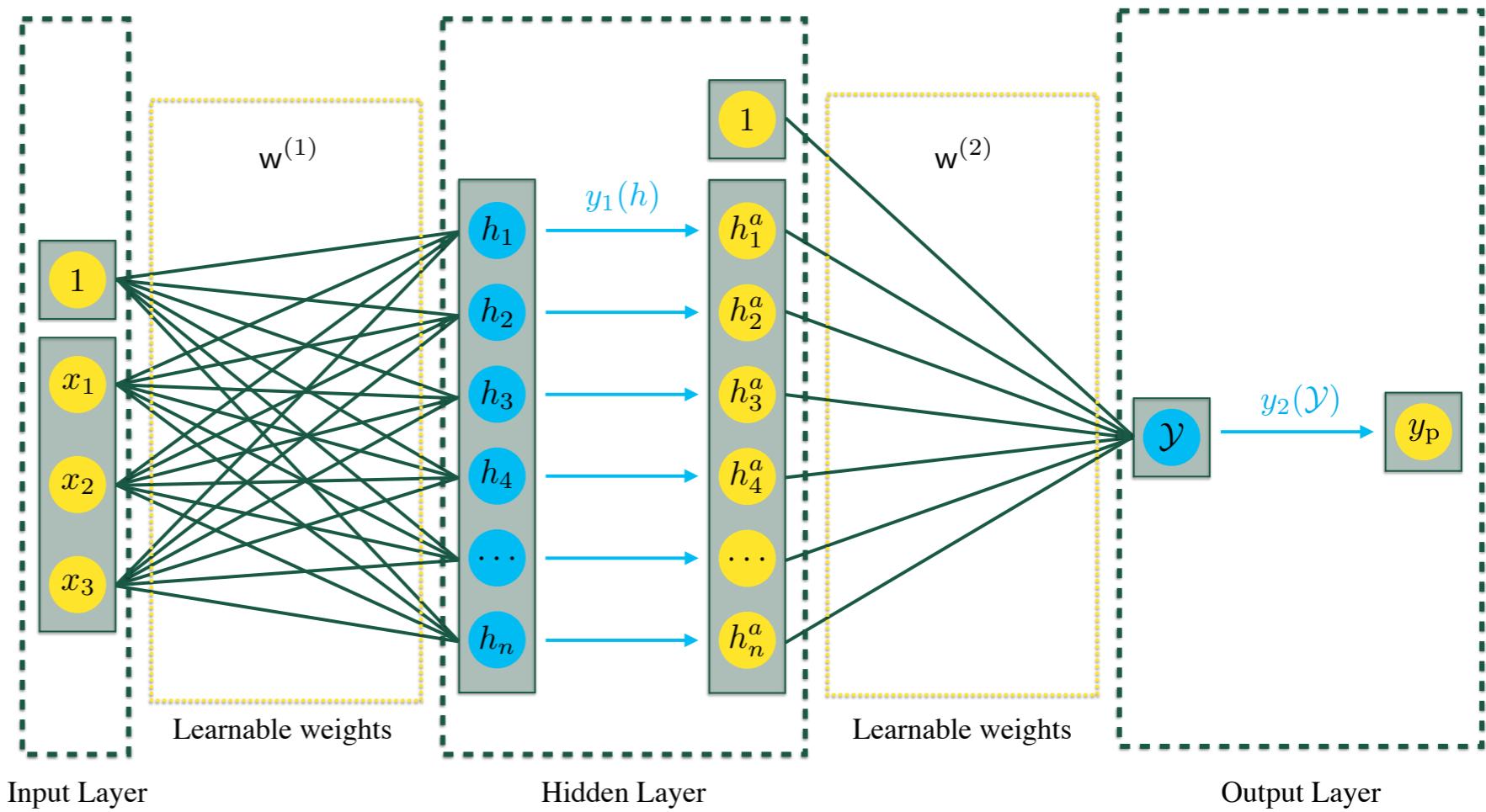
# Neural Networks

- Don't add more inputs, let machine find own shape
- Ability to learn 'any' function
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# Neural Networks

- Don't add more inputs, let machine find own shape
- Ability to learn 'any' function
- More nodes/hidden layers allows for more complex features



# Neural Network Review

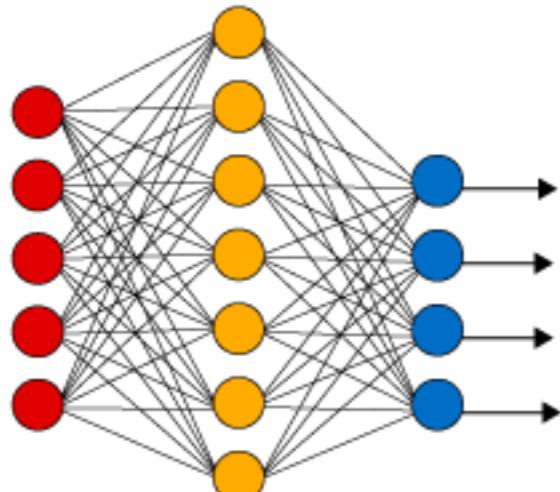
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- Neural networks act as universal function fitter
- Deep networks (many hidden layers) allow the network to pick its own features

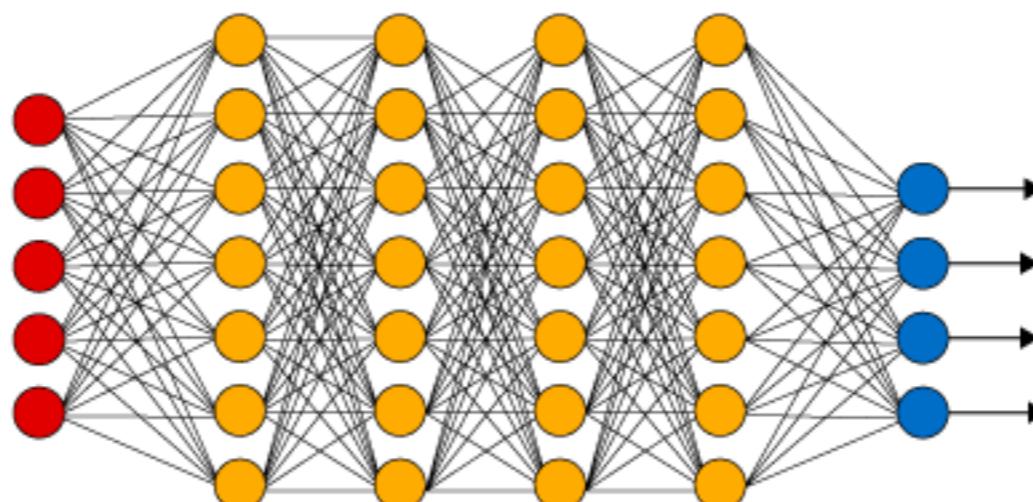


# Deep Learning

**Simple Neural Network**



**Deep Learning Neural Network**



● Input Layer

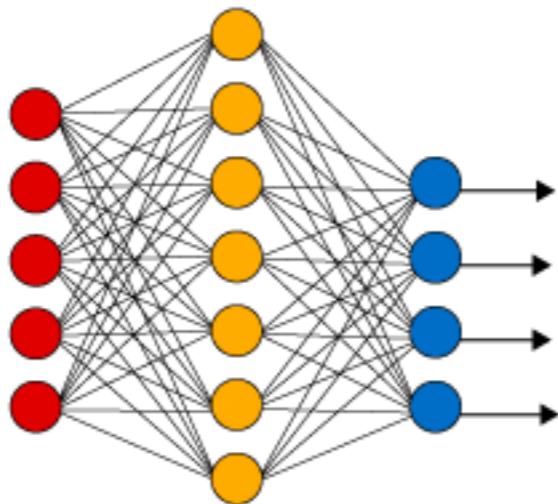
● Hidden Layer

● Output Layer

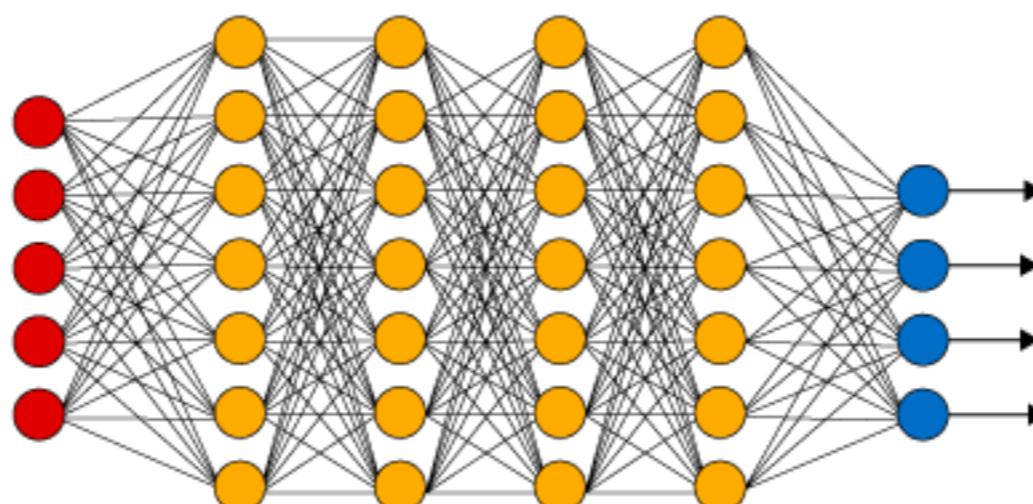
Pic Credit: Xenonstack | Simple Neural Network and Deep Neural Network

# Deep Learning

Simple Neural Network



Deep Learning Neural Network



● Input Layer

● Hidden Layer

● Output Layer

Pic Credit: Xenonstack | Simple Neural Network and Deep Neural Network

Math. Control Signals Systems (1989) 2: 303–314

Mathematics of Control,  
Signals, and Systems

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## Approximation by Superpositions of a Sigmoidal Function\*

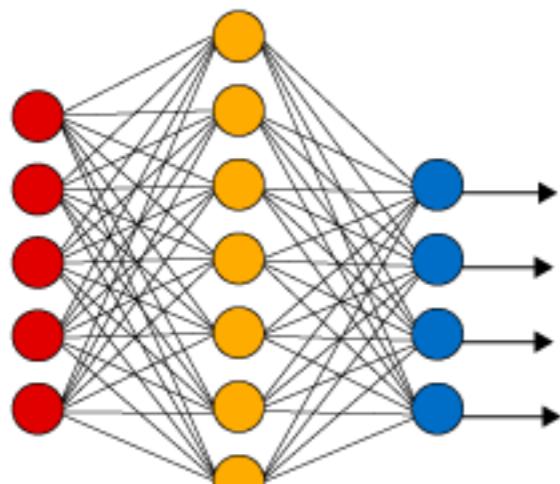
G. Cybenko†

**Abstract.** In this paper we demonstrate that finite linear combinations of compositions of a fixed, univariate function and a set of affine functionals can uniformly approximate any continuous function of  $n$  real variables with support in the unit hypercube; only mild conditions are imposed on the univariate function. Our results settle an open question about representability in the class of single hidden layer neural networks. In particular, we show that arbitrary decision regions can be arbitrarily well approximated by continuous feedforward neural networks with only a single internal, hidden layer and any continuous sigmoidal nonlinearity. The paper discusses approximation properties of other possible types of nonlinearities that might be implemented by artificial neural networks.

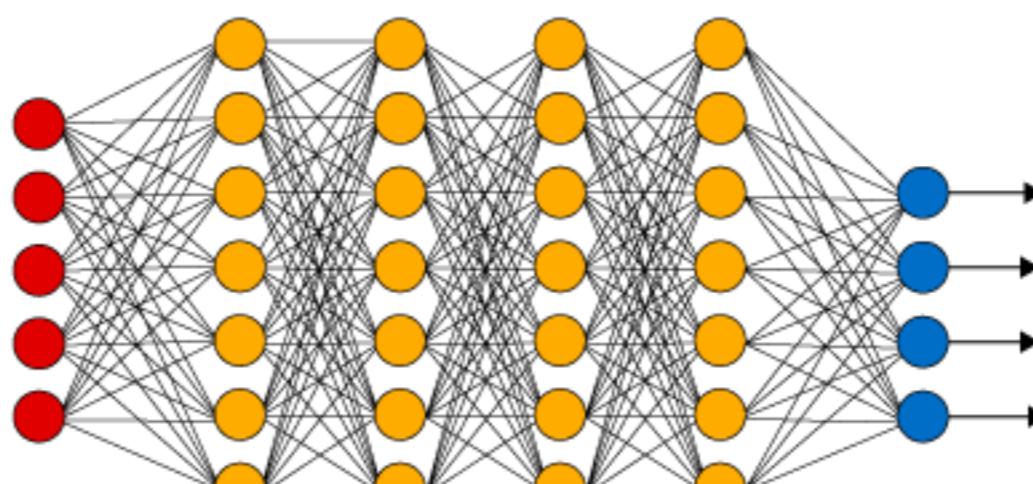
**Key words.** Neural networks, Approximation, Completeness.

# Deep Learning

Simple Neural Network



Deep Learning Neural Network



● Input Layer      ● Hidden Layer      ● Output Layer

Pic Credit: Xenonstack | Simple Neural Network and Deep Neural Network

Can fit any function  
with infinite data  
and infinite nodes  
(1 hidden layer)

Math. Control Signals Systems (1989) 2: 303–314

Mathematics of Control,  
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## Approximation by Superpositions of a Sigmoidal Function\*

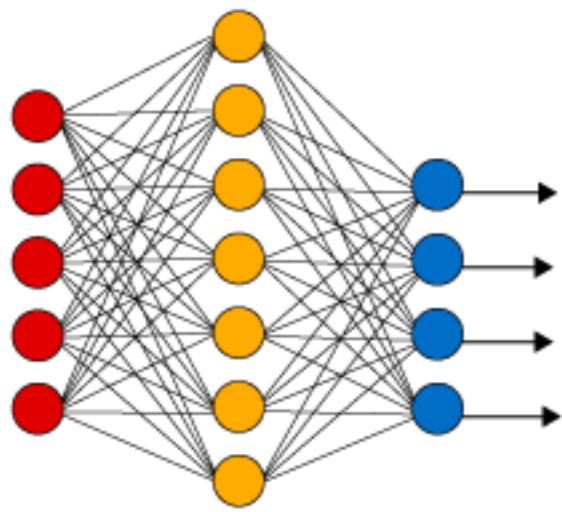
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# Deep Learning

Simple Neural Network

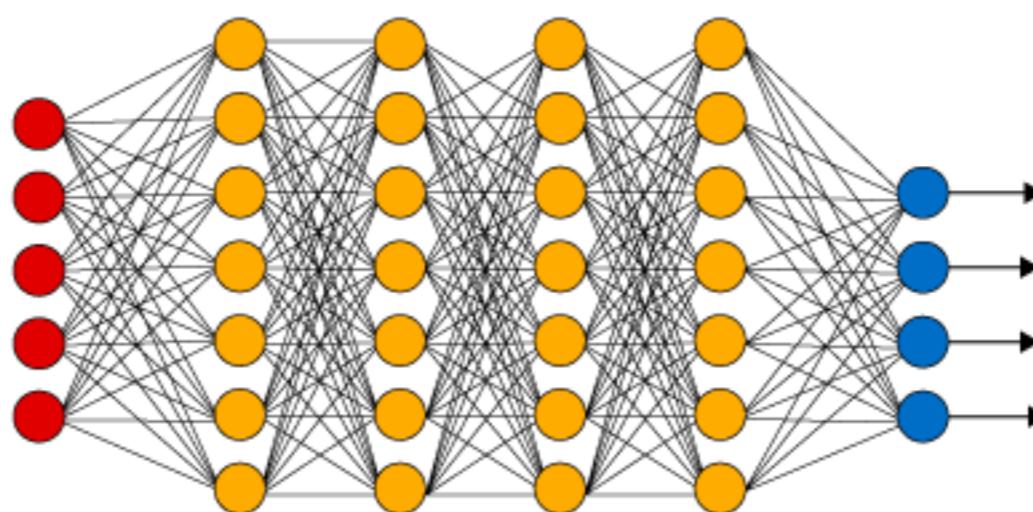


● Input Layer

○ Hidden Layer

● Output Layer

Deep Learning Neural Network



Pic Credit: Xenonstack | Simple Neural Network and Deep Neural Network

Can fit any function  
with infinite data  
and infinite nodes  
(1 hidden layer)

The image shows a white rectangular card with a thin black border. At the top left, it says "Math. Control Signals Systems (1989) 2: 303–314". In the center, it has the title "Mathematics of Control, Signals, and Systems" and the copyright notice "© 1989 Springer-Verlag New York Inc.". Below the title, the abstract begins with "Abstract. In this paper we demonstrate that finite linear combinations of compositions of a fixed, univariate function and a set of affine functionals can uniformly approximate any continuous function of a real variables with support in the unit hypercube; only mild conditions are imposed on the univariate function. Our results settle an open question about representability in the class of single hidden layer neural networks. In particular, we show that arbitrary decision regions can be arbitrarily well approximated by continuous feedforward neural networks with only a single internal, hidden layer and any continuous sigmoidal nonlinearity. The paper discusses approximation properties of other possible types of nonlinearities that might be implemented by artificial neural networks."

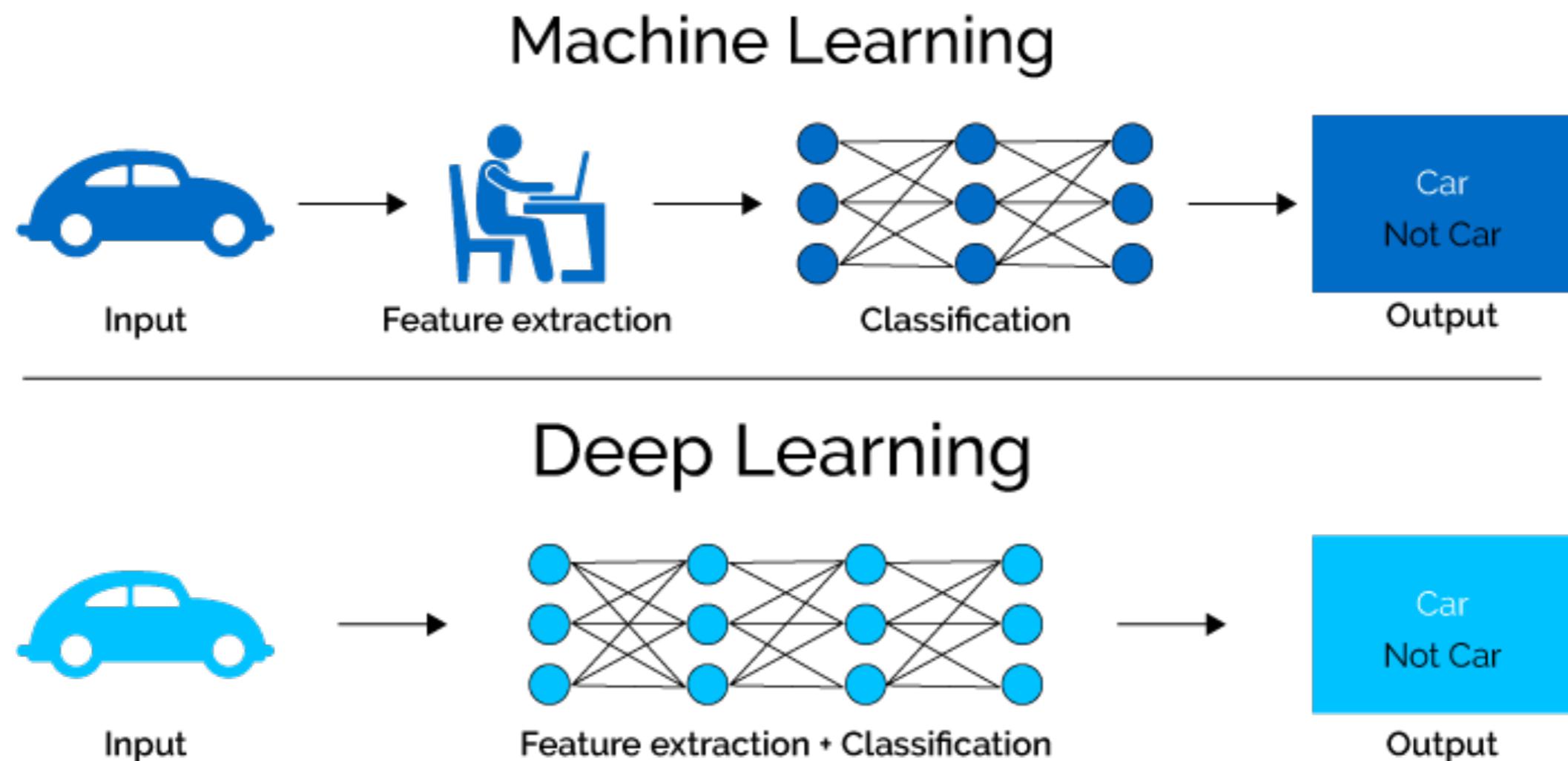
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**Key words.** Neural networks, Approximation, Completeness.

Going deeper rather  
than wider learns non-  
linearities with fewer  
parameters

# Deep Learning

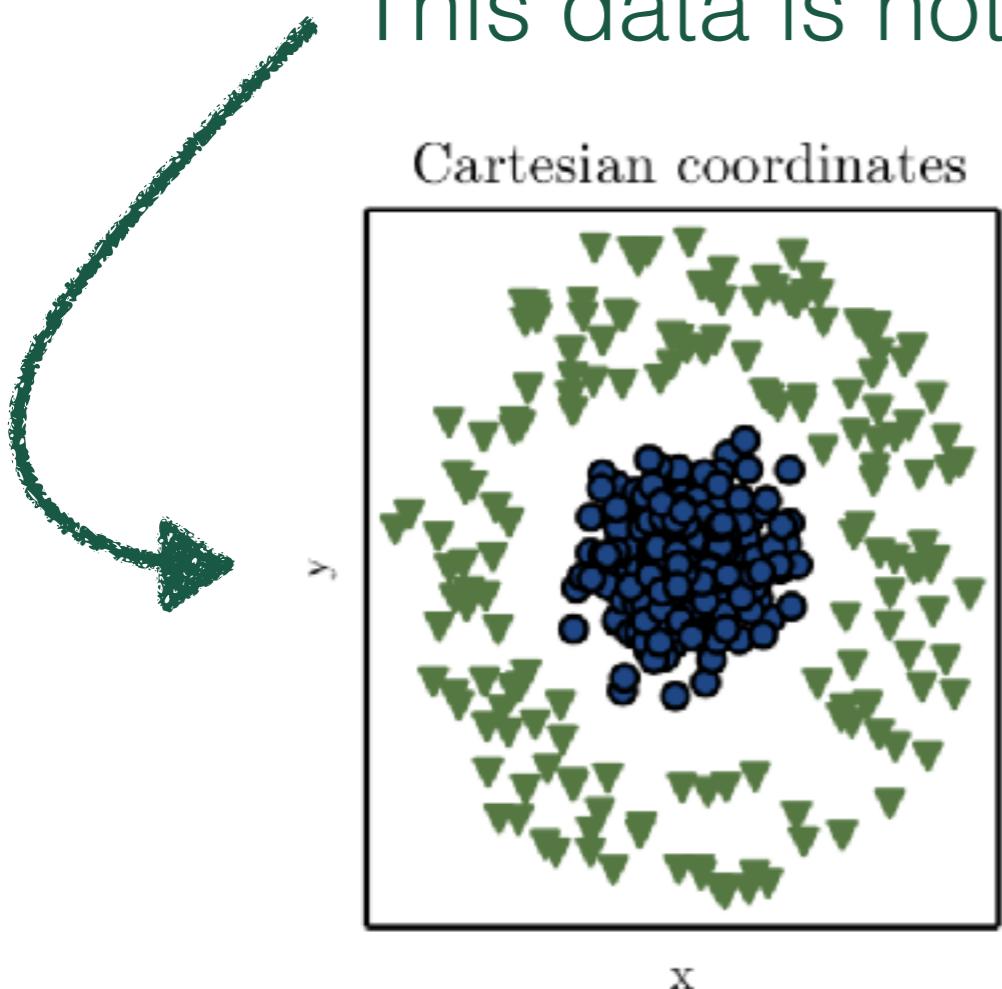
Part of the deep learning revolution is end-to-end learning



Pic Credit: Xenonstack | Machine Learning vs Deep Learning

# End-To-End Learning

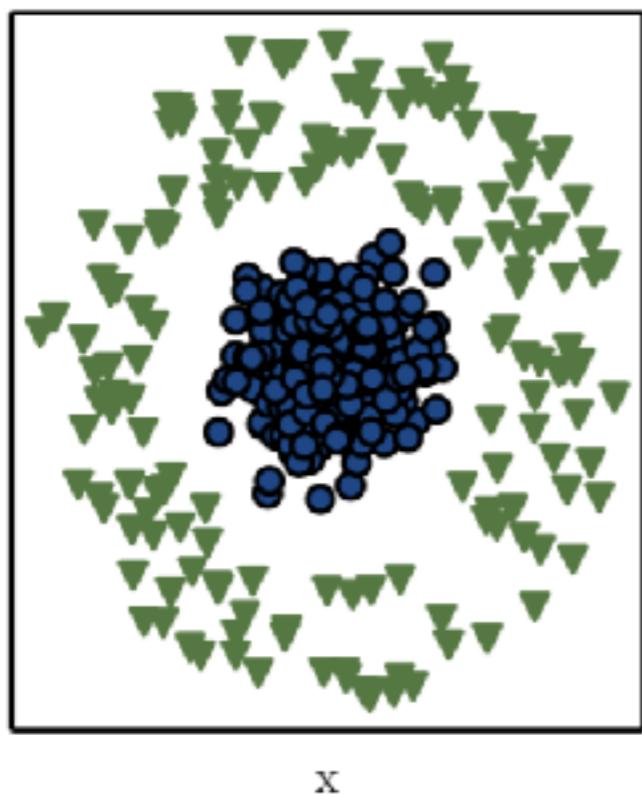
This data is not currently linearly separable



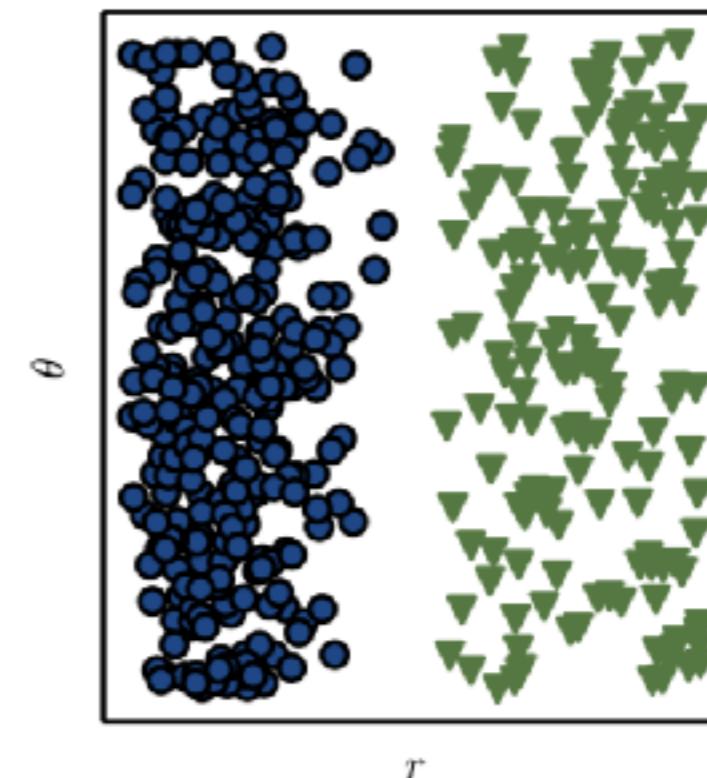
# End-To-End Learning

This data is not currently linearly separable

Cartesian coordinates



Polar coordinates



- A simple coordinate transformation makes this a linear separable problem
- Hard to come up with transformations in high dimensions
- Use physics insights for collider variables

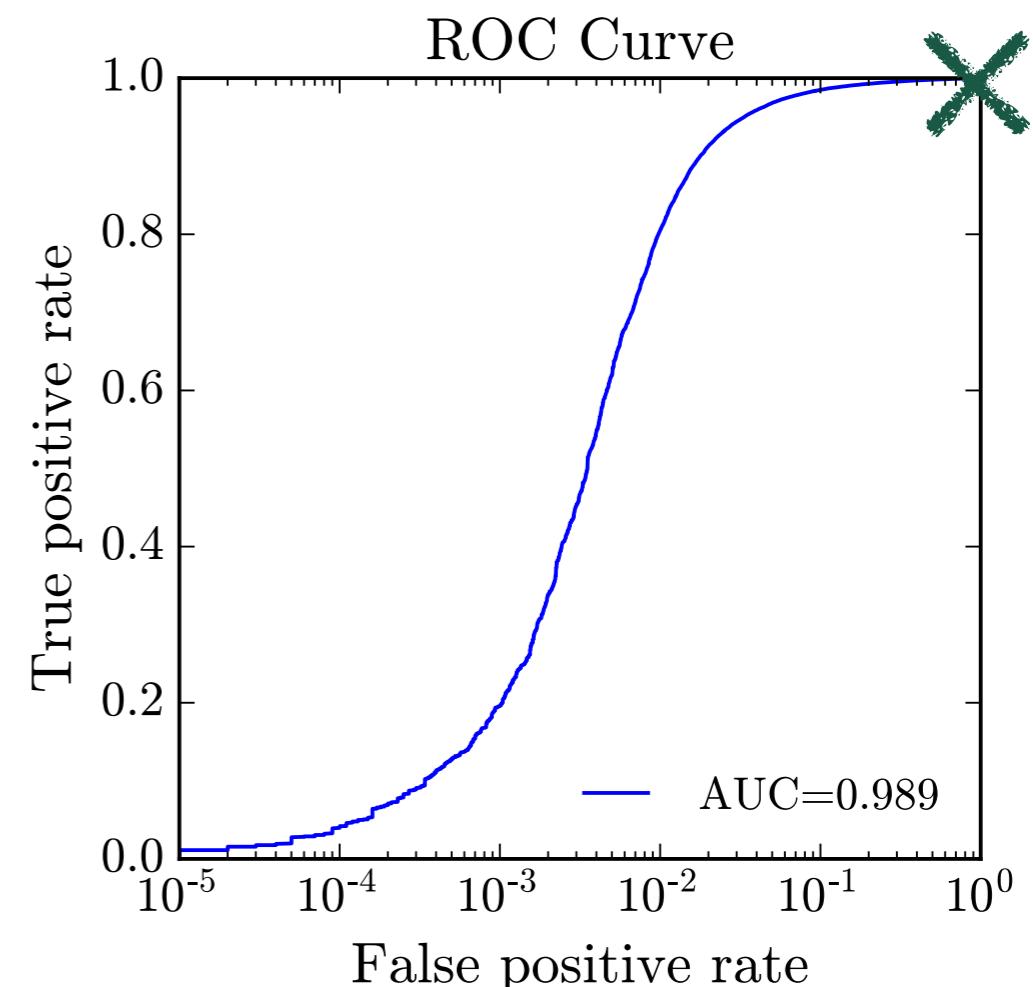
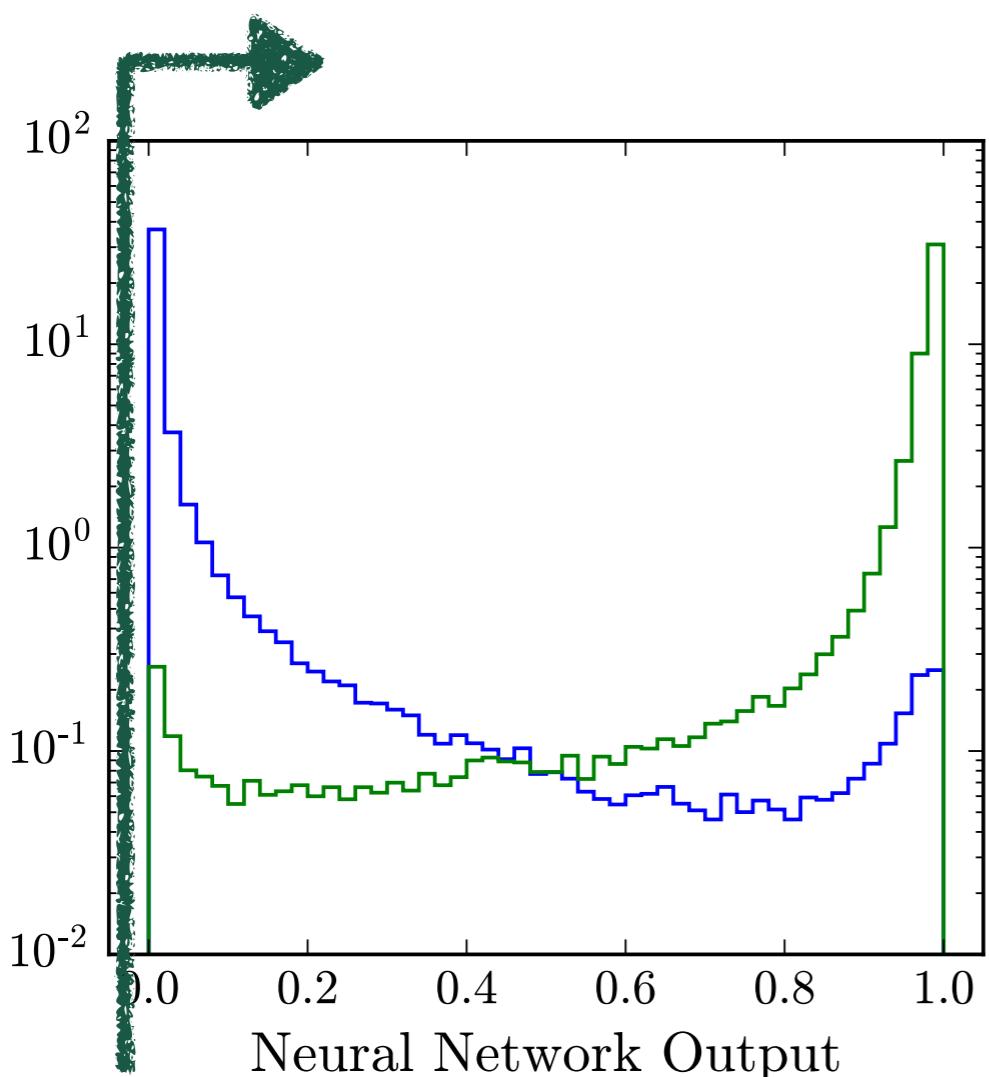
# Quick interlude

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- Going to get into collider machine learning soon
- Any questions so far?
- Examine metric to compare classifiers

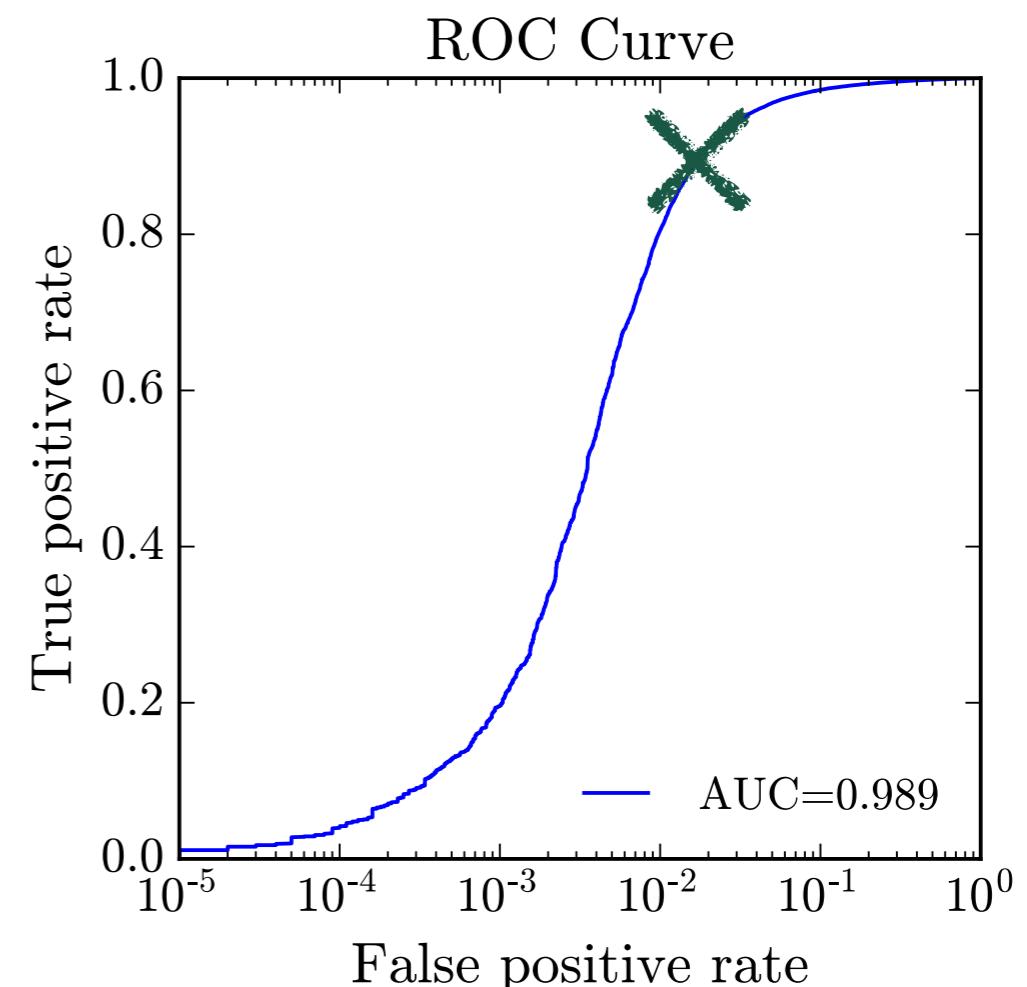
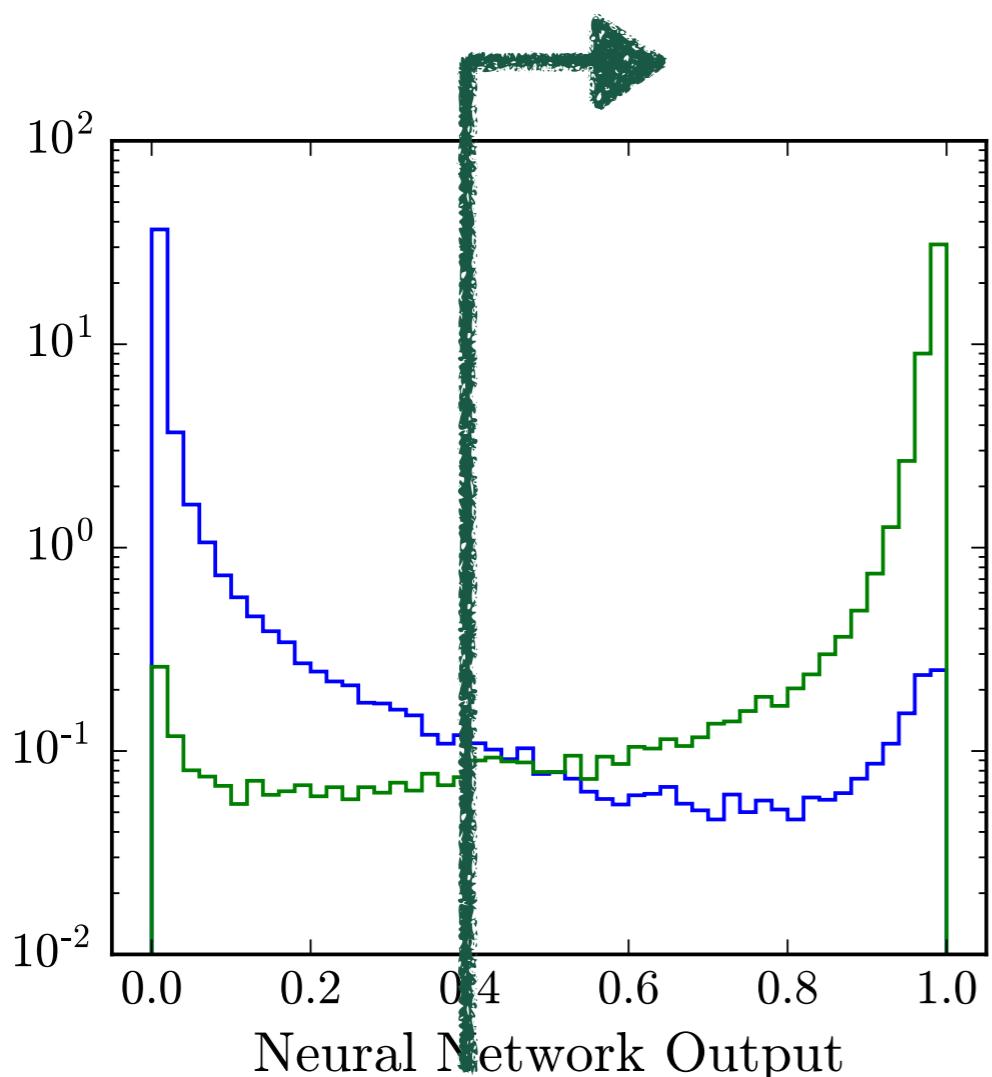
# How to quantify a classifier

If we want to compare the performance of a classifier, one common option is the Receiver Operating Characteristic (ROC) Curve



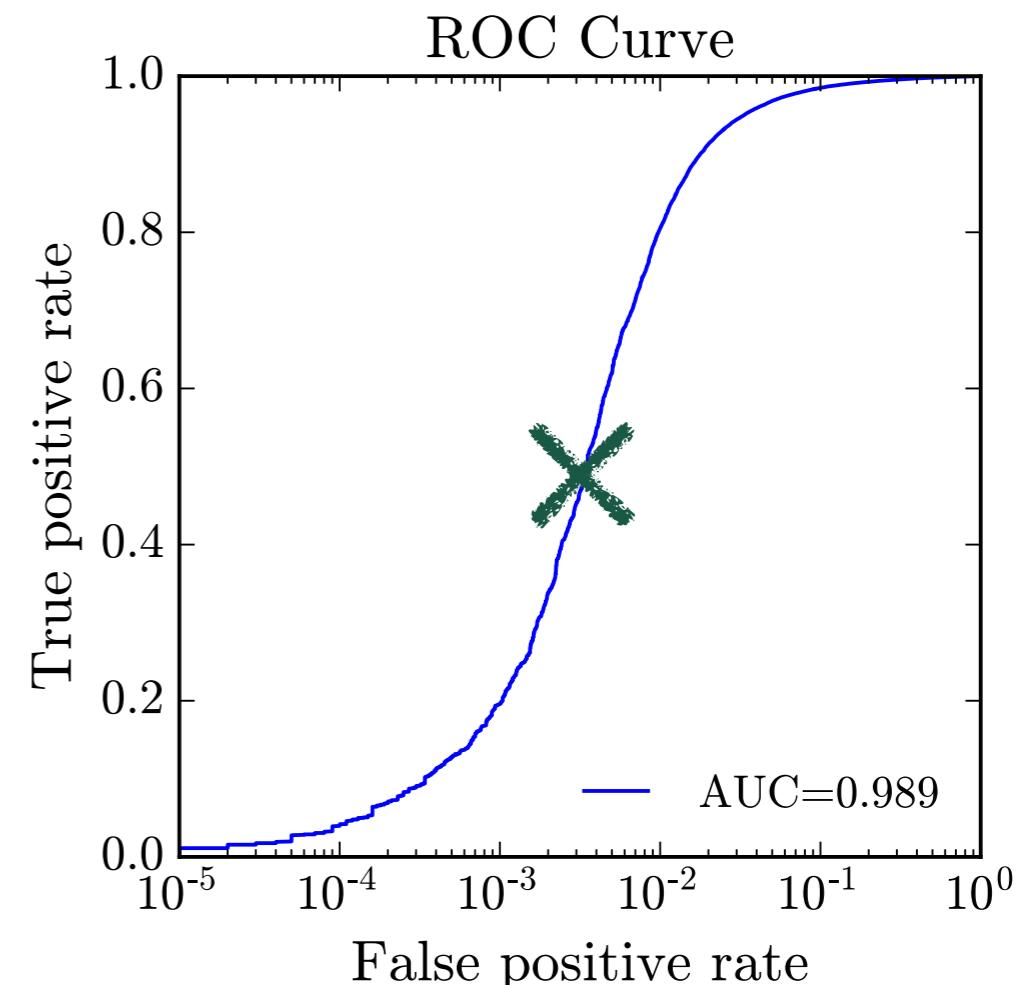
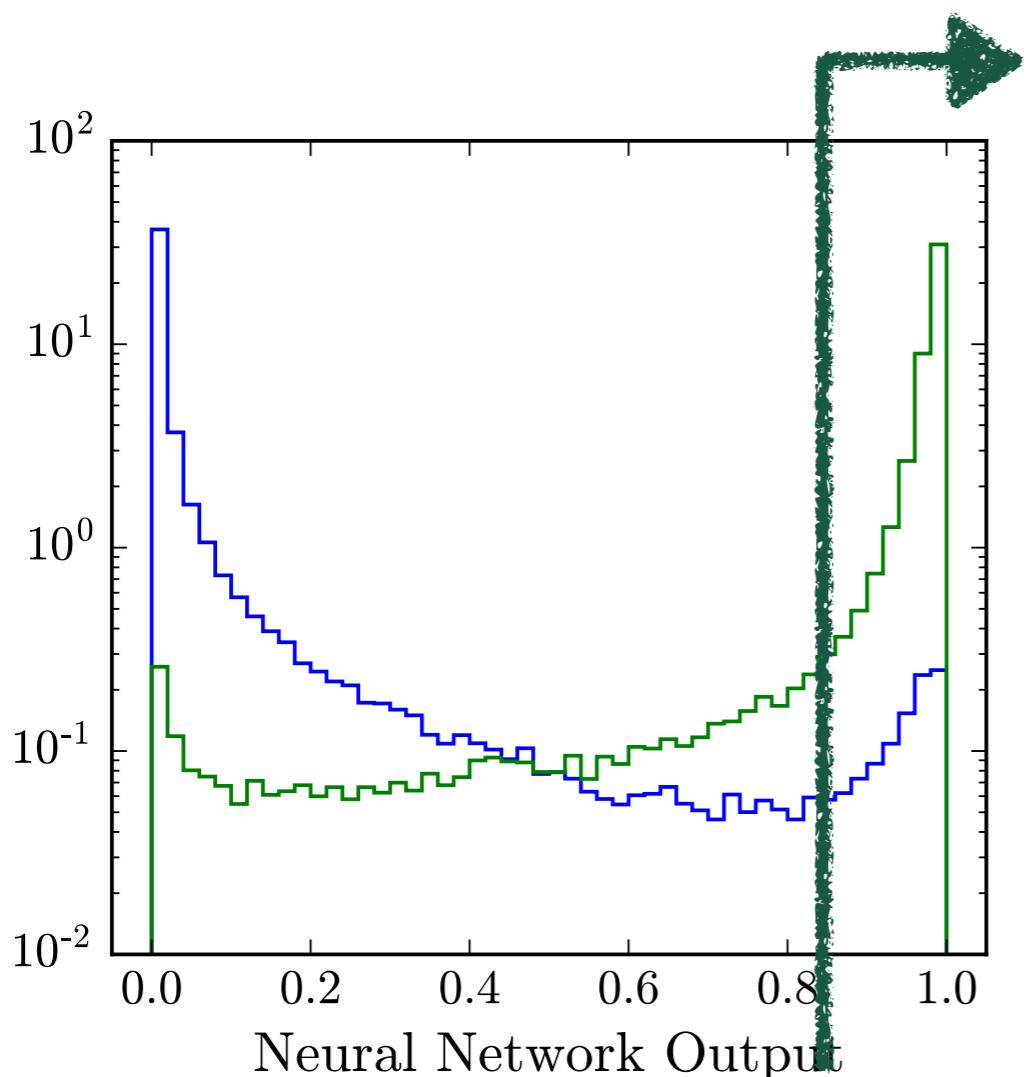
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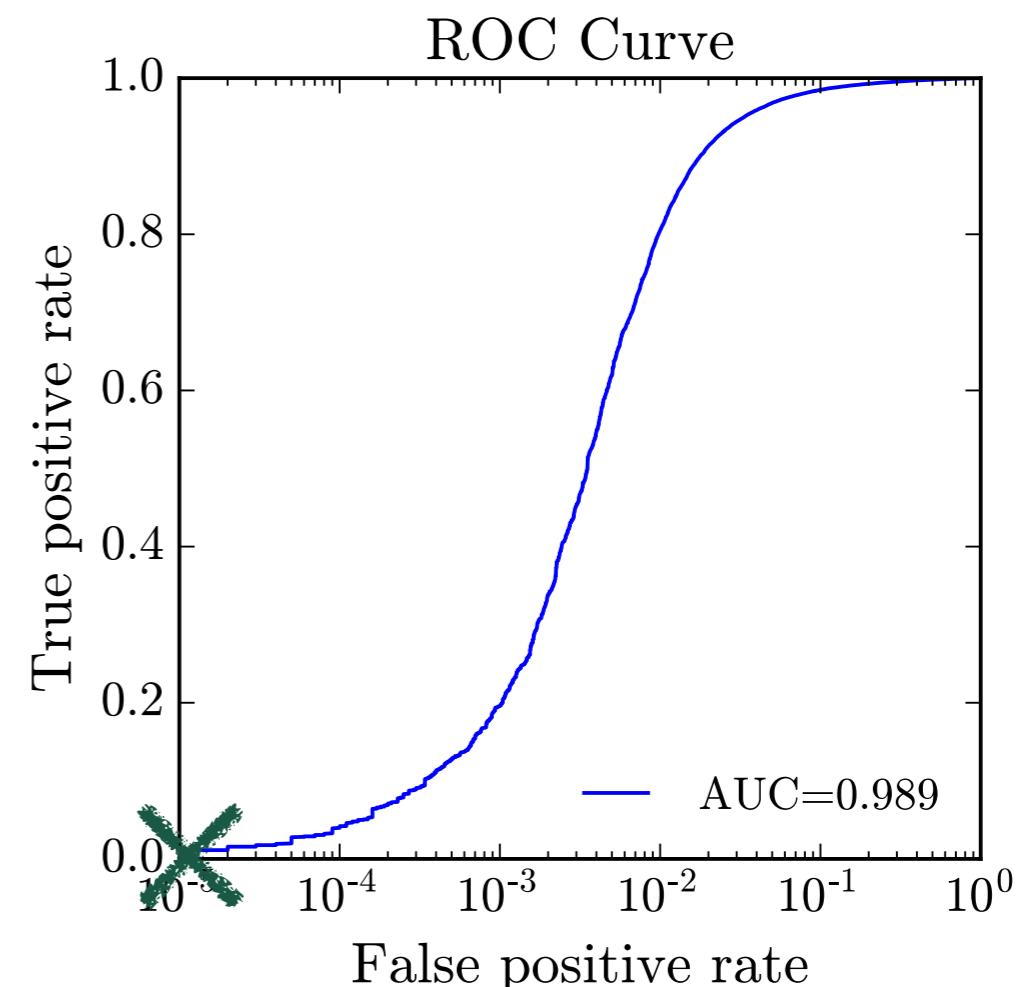
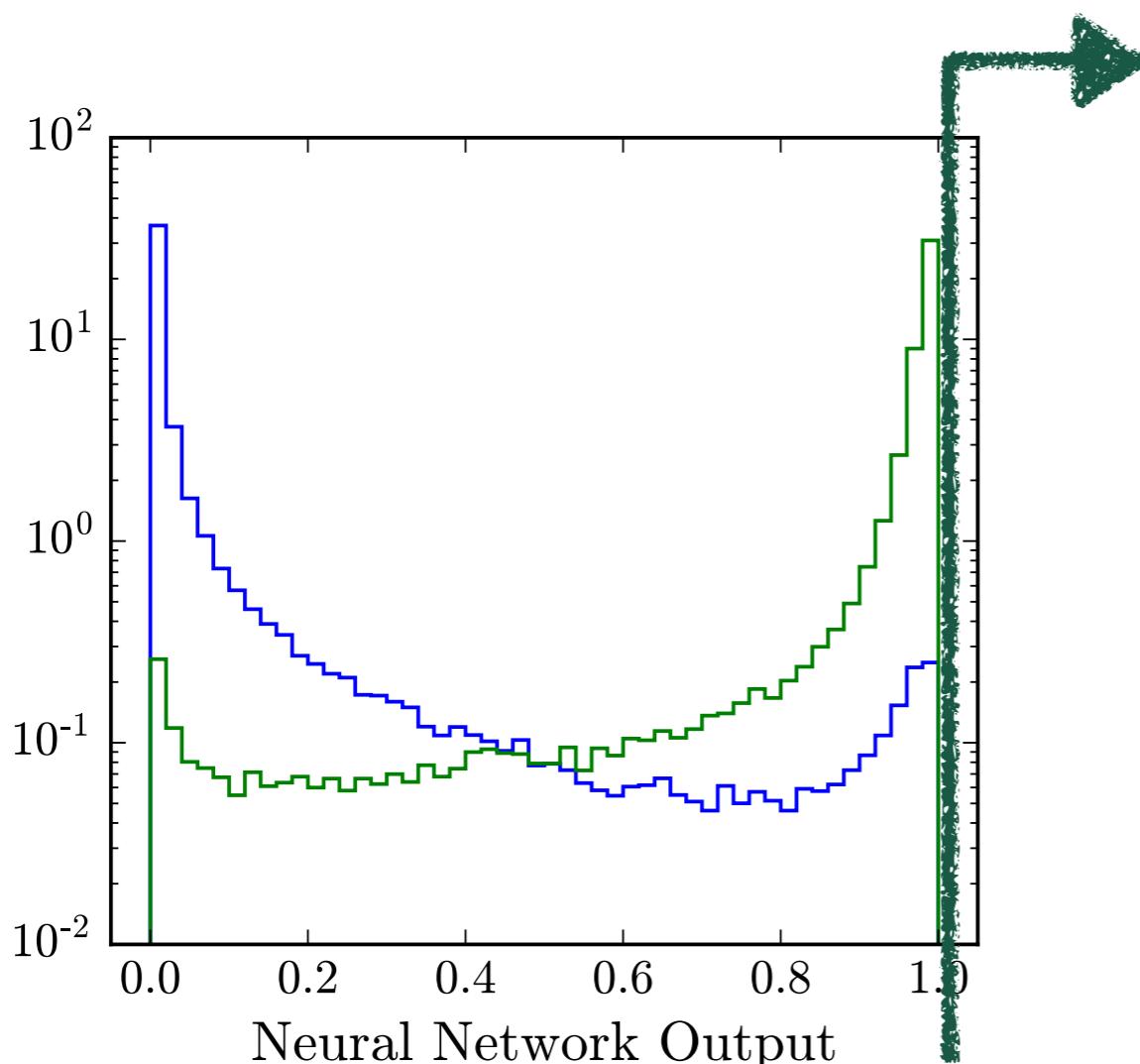
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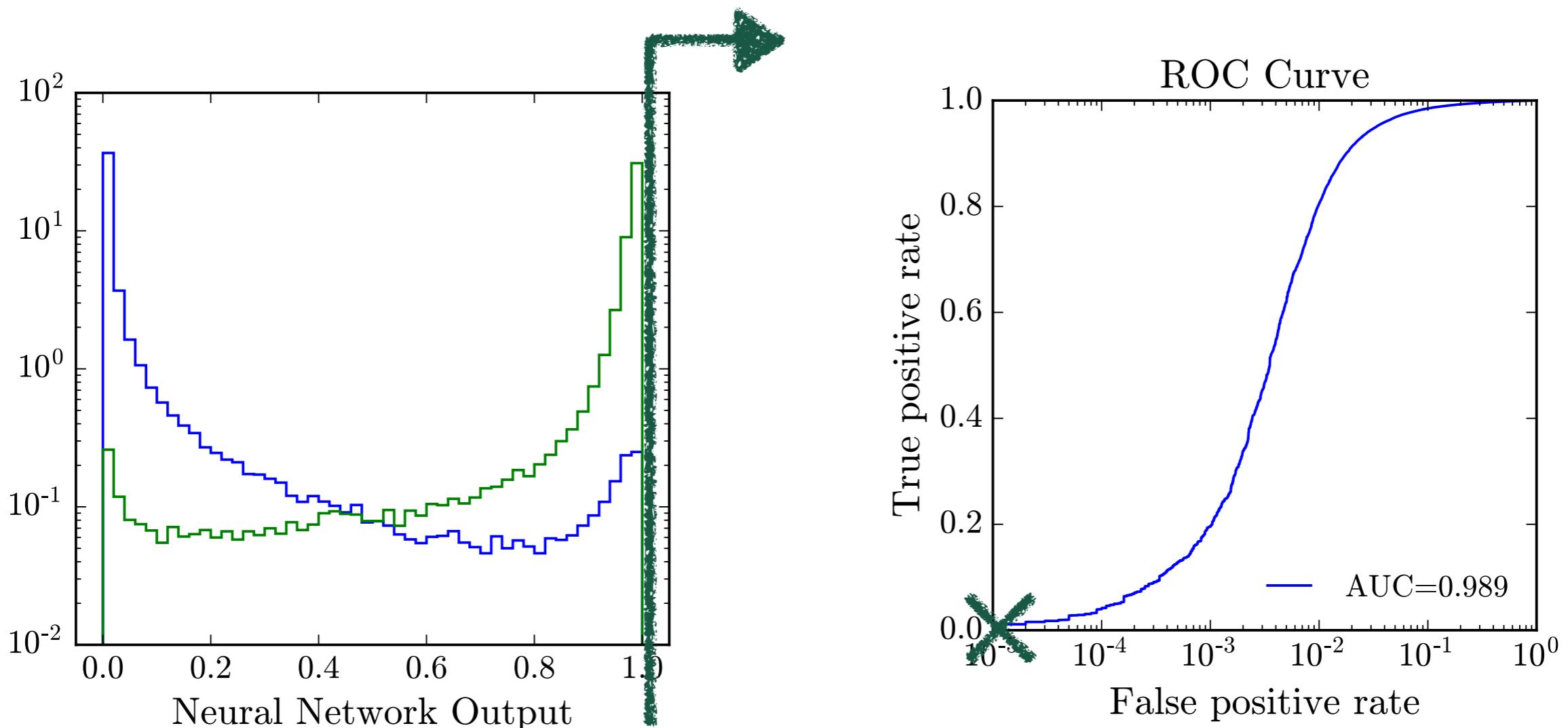
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# How to quantify a classifier

If we want to compare the performance of a classifier, one common option is the Receiver Operating Characteristic (ROC) Curve



AUC = 1.0 is perfect, this is not attainable for most problems

# Machine learning particle physics

## At the LHC

Can identify and measure photons, electrons, muons, and things made of quarks

Neutrinos (and some BSM particles) escape detection

Beams travel in  $\pm z$  direction, no momentum in (x, y) plane

# Machine learning particle physics

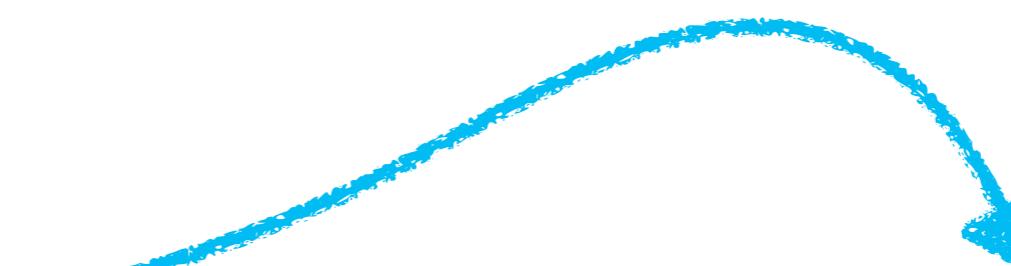
## At the LHC

Can identify and measure photons, electrons, muons, and things made of quarks

Energy and momentum vector

Neutrinos (and some BSM particles) escape detection

Beams travel in  $\pm z$  direction, no momentum in (x, y) plane



# Machine learning particle physics

## At the LHC

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Energy and momentum vector  
jets (b-jets)

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# Machine learning particle physics

## At the LHC

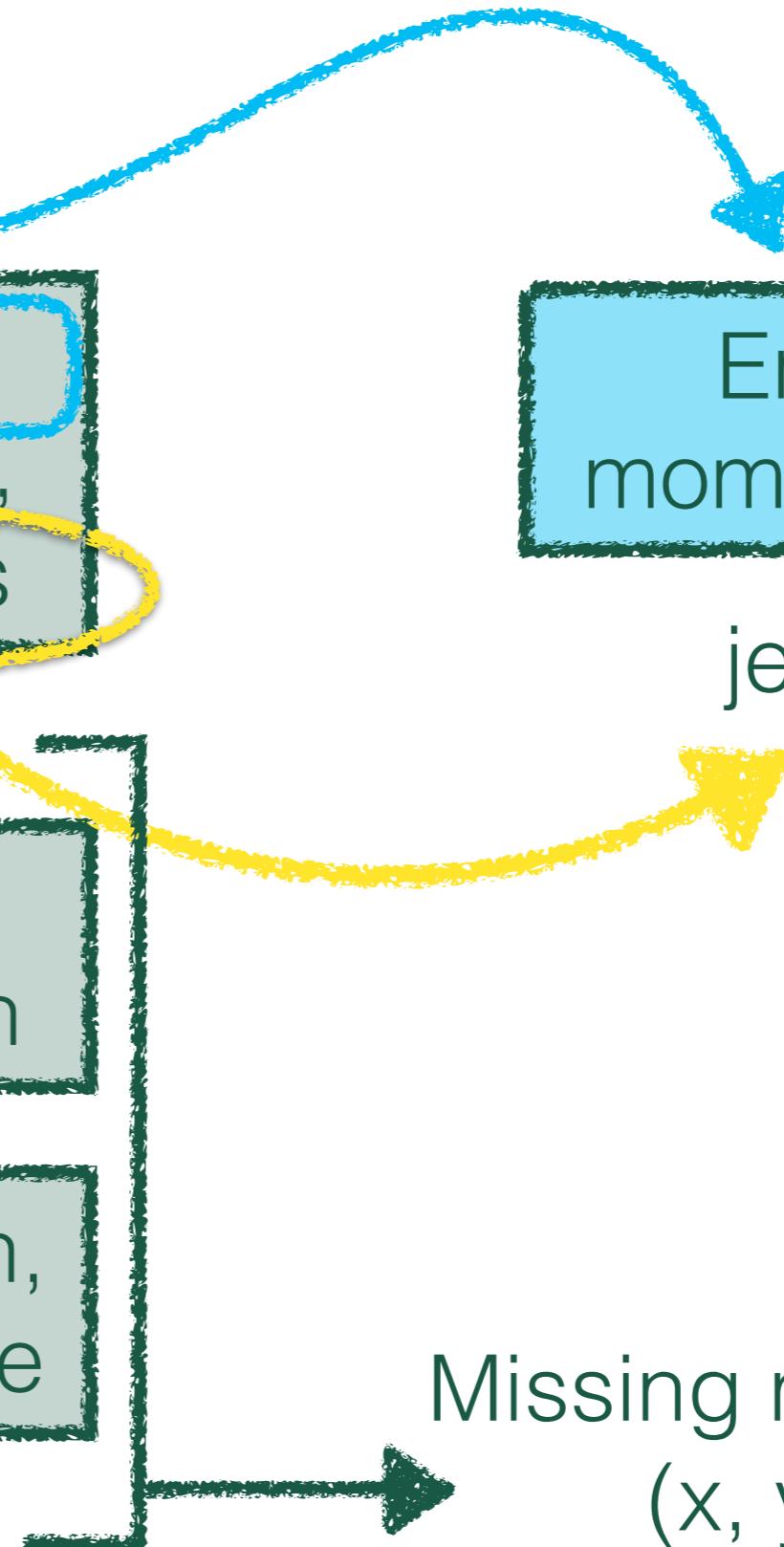
Can identify and measure photons, electrons, muons, and things made of quarks

Neutrinos (and some BSM particles) escape detection

Beams travel in  $\pm z$  direction, no momentum in  $(x, y)$  plane

Energy and momentum vector  
jets (b-jets)

Missing momentum in  $(x, y)$  plane



# Machine learning particle physics

## At the LHC

Can identify and measure photons, electrons, muons, and things made of quarks

Neutrinos (and some BSM particles) escape detection

Beams travel in  $\pm z$  direction, no momentum in (x, y) plane

Energy and momentum vector  
jets (b-jets)

Which heavy particle decayed to the final state particles?

Missing momentum in (x, y) plane

# Deep learning in HEP

## ARTICLE

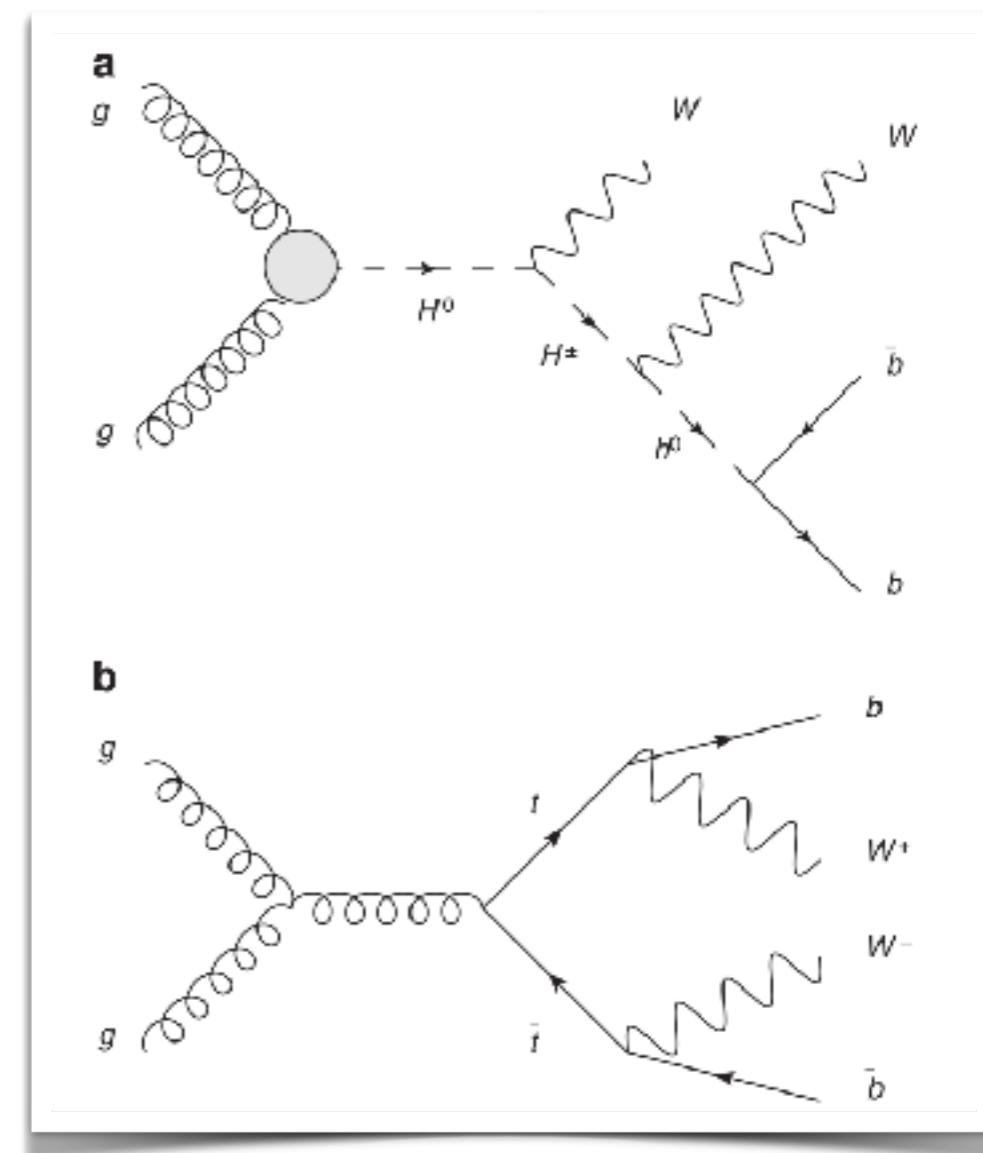
Received 19 Feb 2014 | Accepted 4 Jun 2014 | Published 2 Jul 2014

DOI: 10.1038/ncomms5308

## Searching for exotic particles in high-energy physics with deep learning

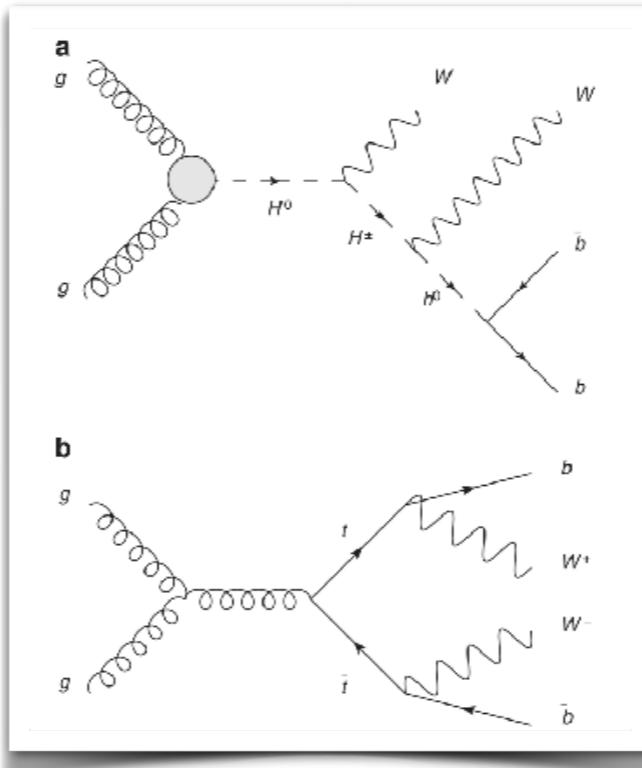
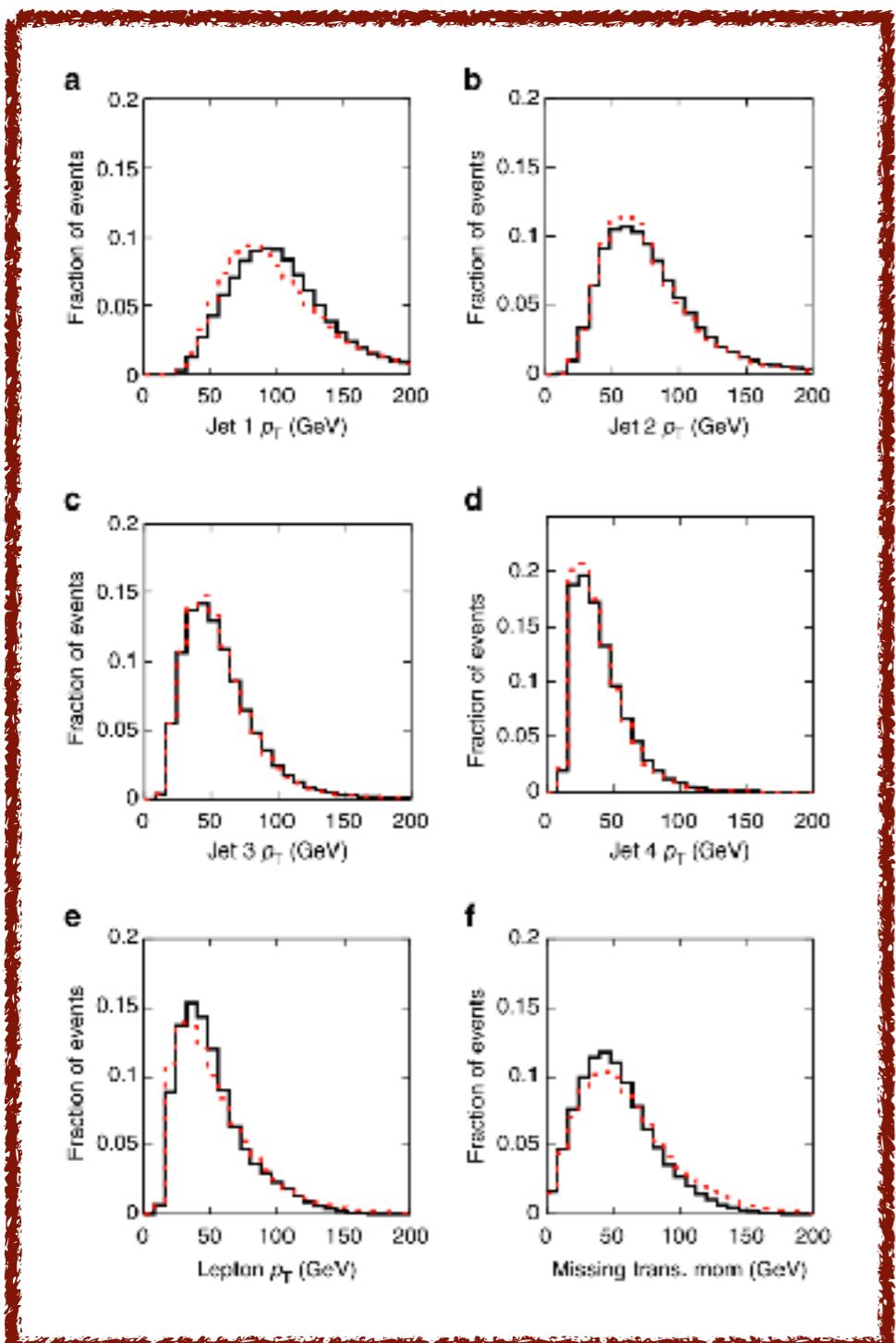
P. Baldi<sup>1</sup>, P. Sadowski<sup>1</sup> & D. Whiteson<sup>2</sup>

[1402.4735]



- One of first papers to show deep learning ***outperforming*** standard techniques in HEP
- Compares shallow and deep networks on raw and high-level features

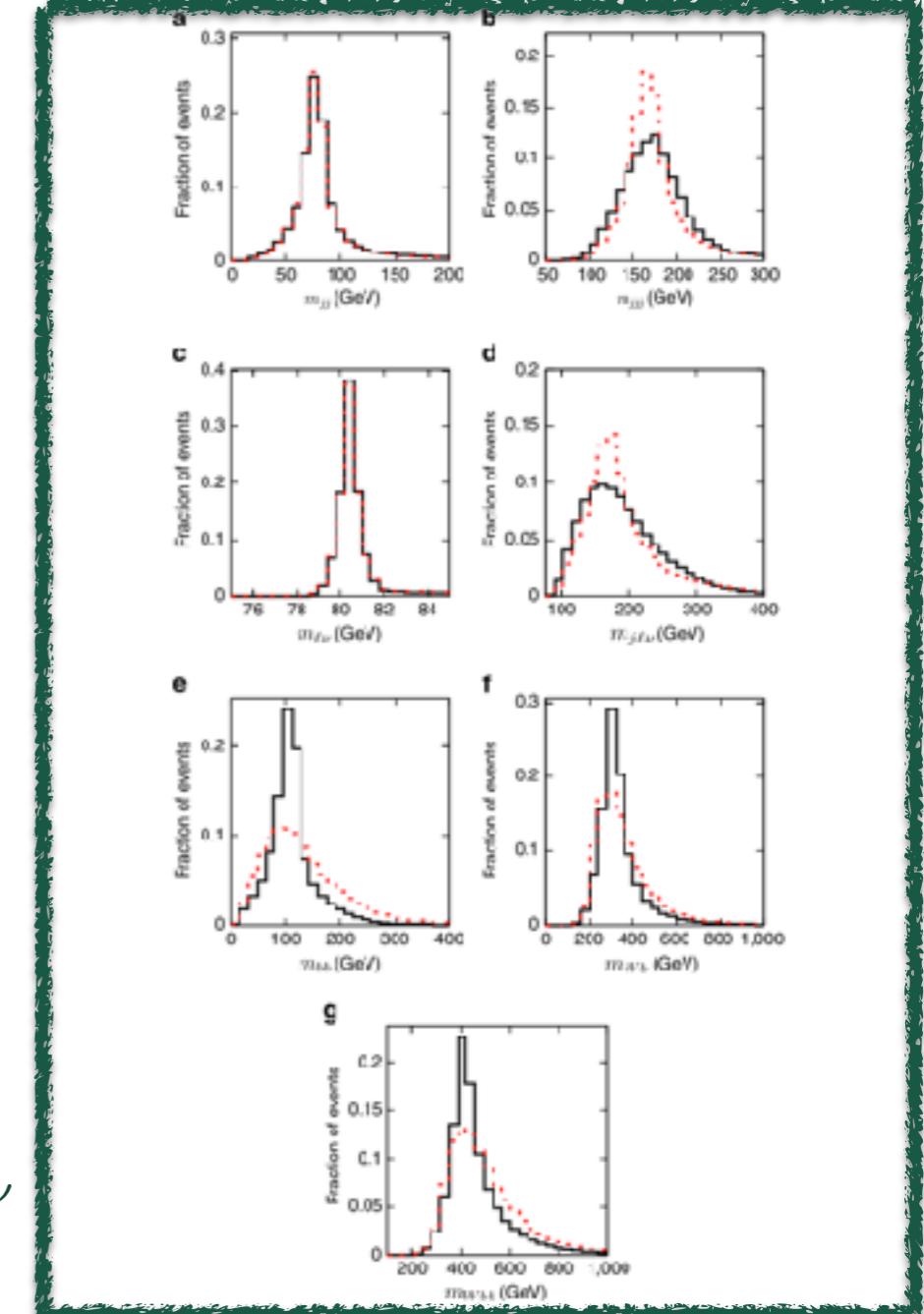
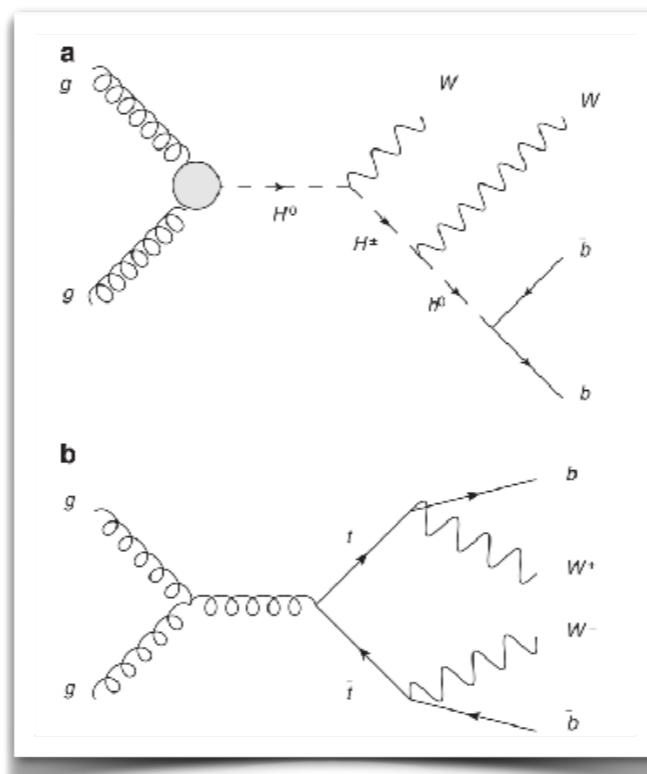
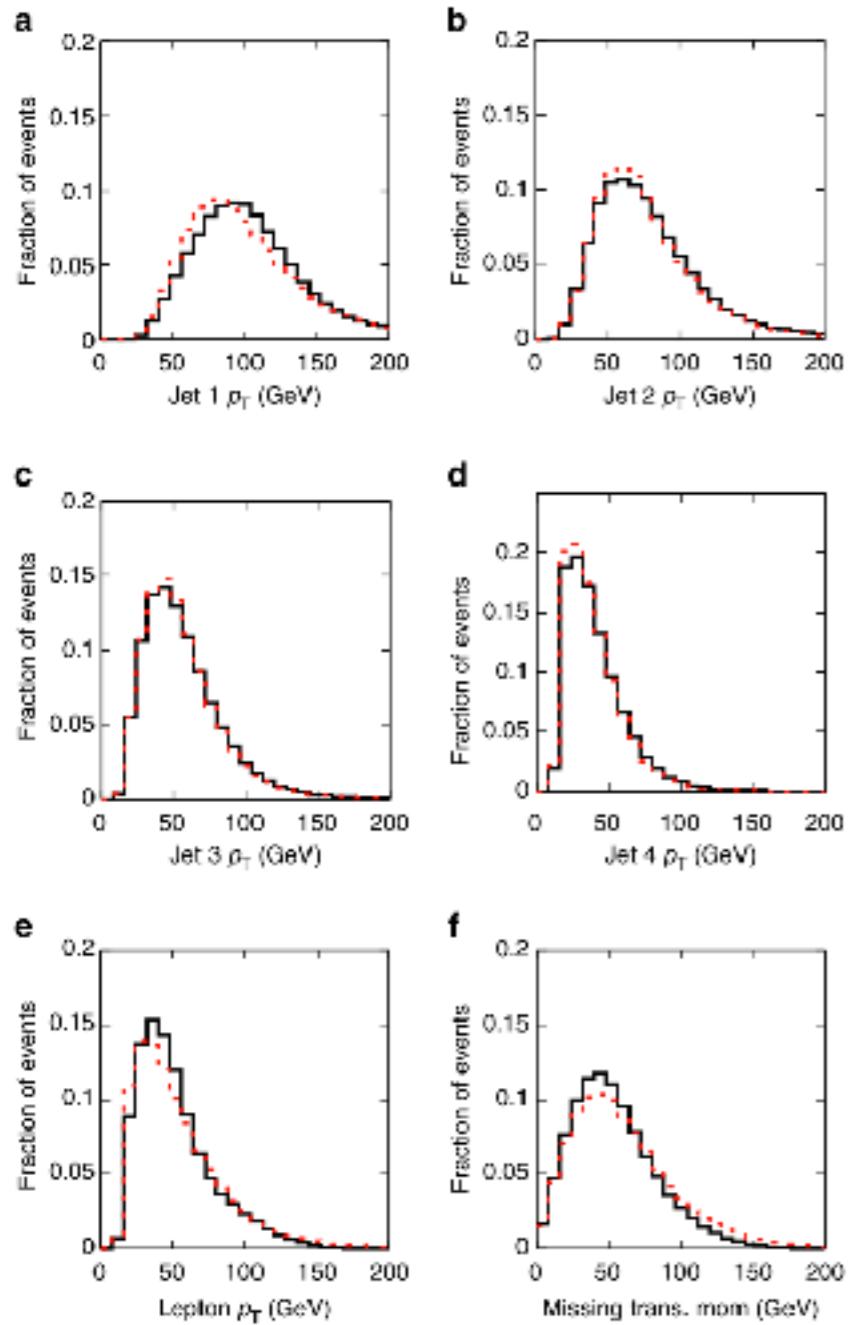
# Deep learning in HEP



21 raw features for  
semi-leptonic channel

Not much separation in  
individual features

# Deep learning in HEP



Invariant masses of  
intermediate states

$m_{jj}$     $m_{jjj}$     $m_{\ell\nu}$     $m_{j\ell\nu}$   
 $m_{bb}$     $m_{Wb}$     $m_{Wbb}$

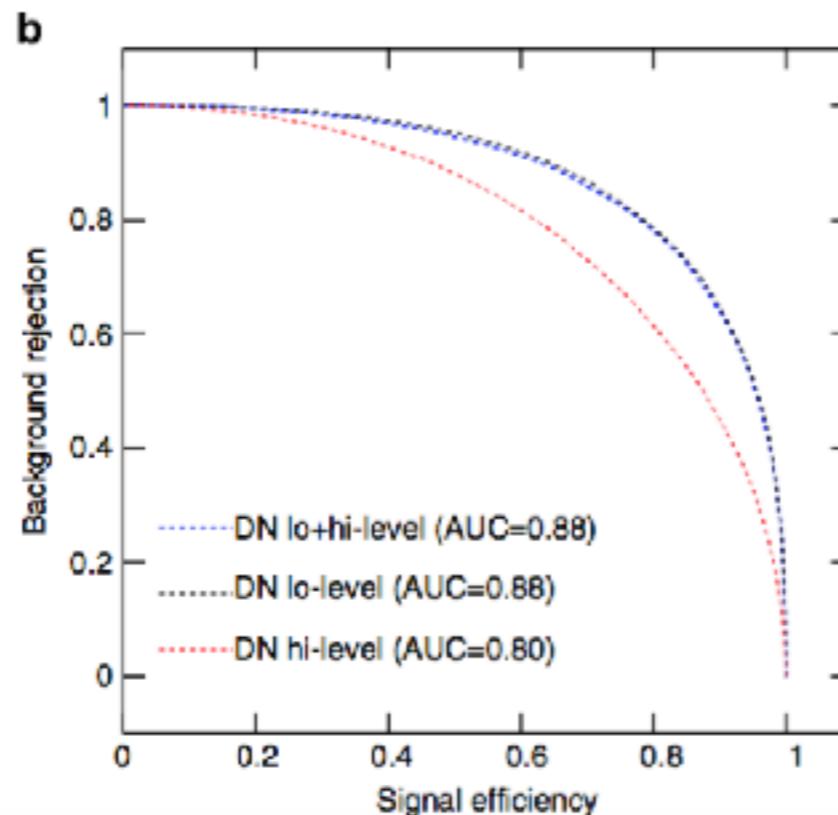
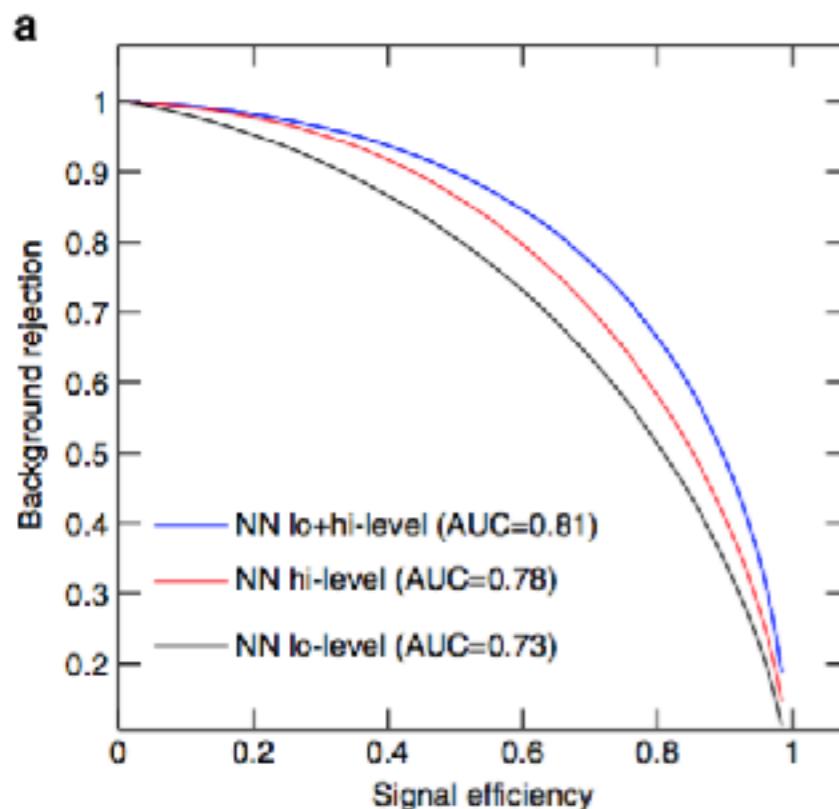
# Deep learning in HEP

11 million training examples  
1 hidden layer shallow network  
5 layer deep network

**Table 1 | Performance for Higgs benchmark.**

Technique	Low-level	High-level	Complete
<b>AUC</b>			
BDT	0.73 (0.01)	0.78 (0.01)	0.81 (0.01)
NN	0.733 (0.007)	0.777 (0.001)	0.816 (0.004)
DN	0.880 (0.001)	0.800 (< 0.001)	0.885 (0.002)
<i>Discovery significance</i>			
NN	$2.5\sigma$	$3.1\sigma$	$3.7\sigma$
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Comparison of the performance of several learning techniques: boosted decision trees (BDT), shallow neural networks (NN), and deep neural networks (DN) for three sets of input features: low-level features, high-level features and the complete set of features. Each neural network was trained five times with different random initializations. The table displays the mean area under the curve (AUC) of the signal-rejection curve in Fig. 7, with s.d. in parentheses as well as the expected significance of a discovery (in units of Gaussian  $\sigma$ ) for 100 signal events and  $1,000 \pm 50$  background events.



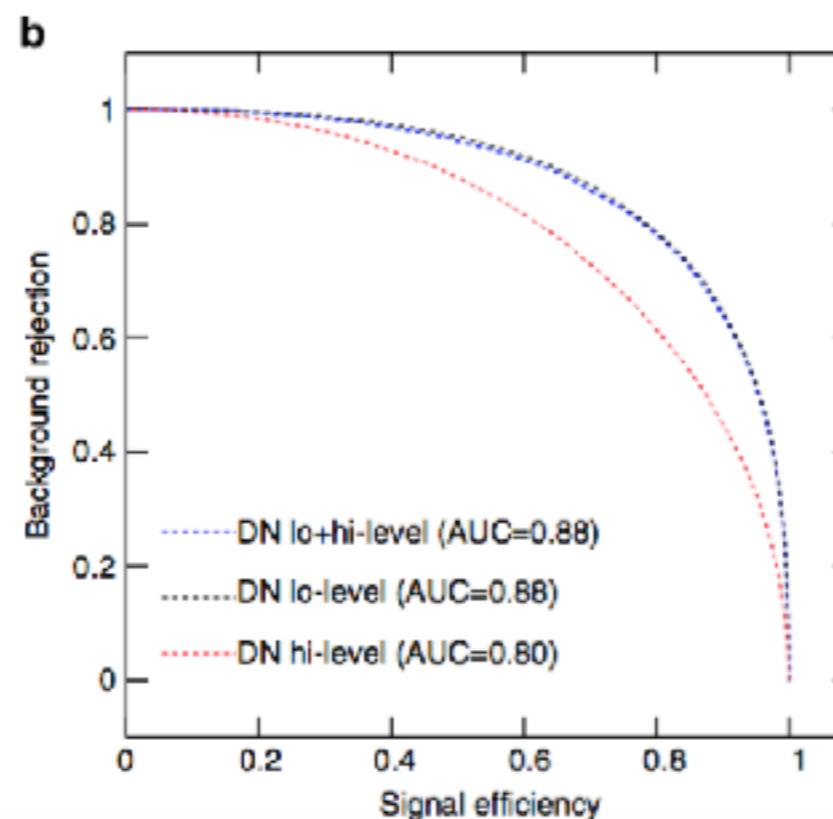
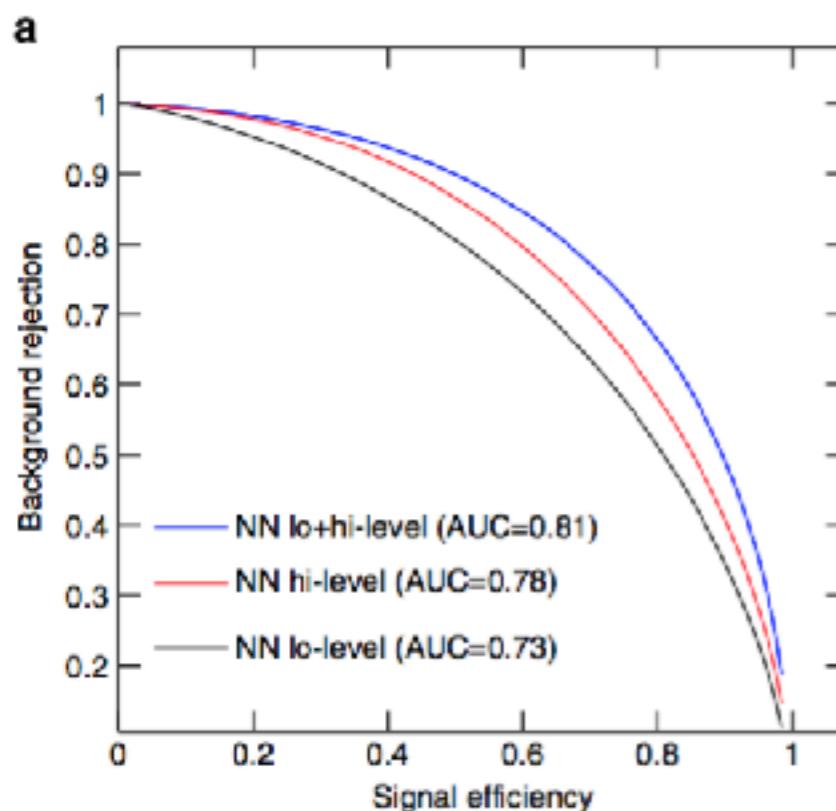
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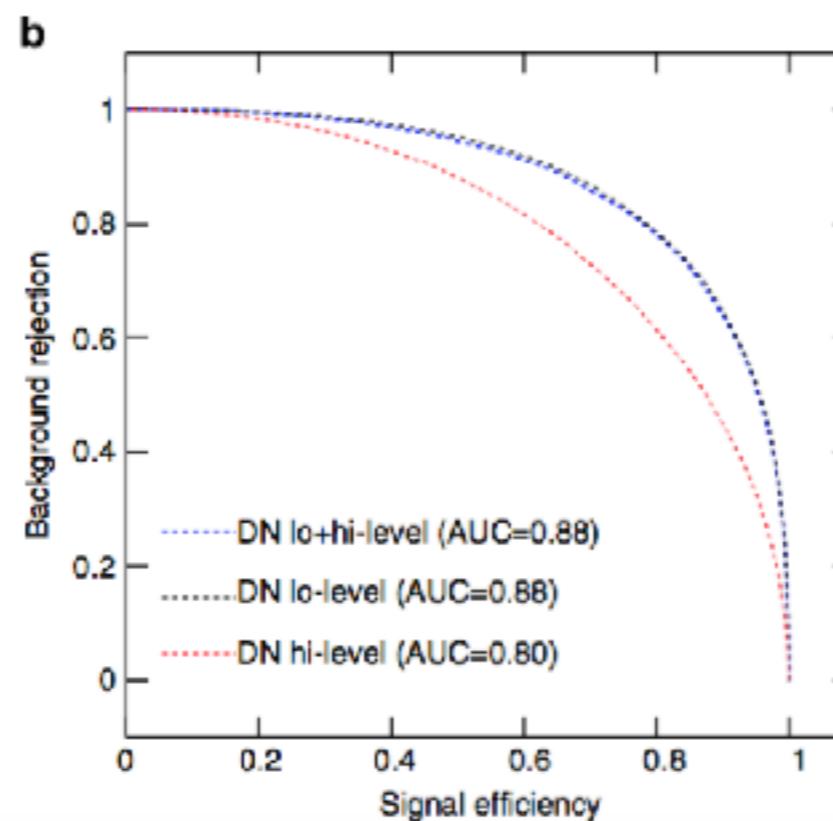
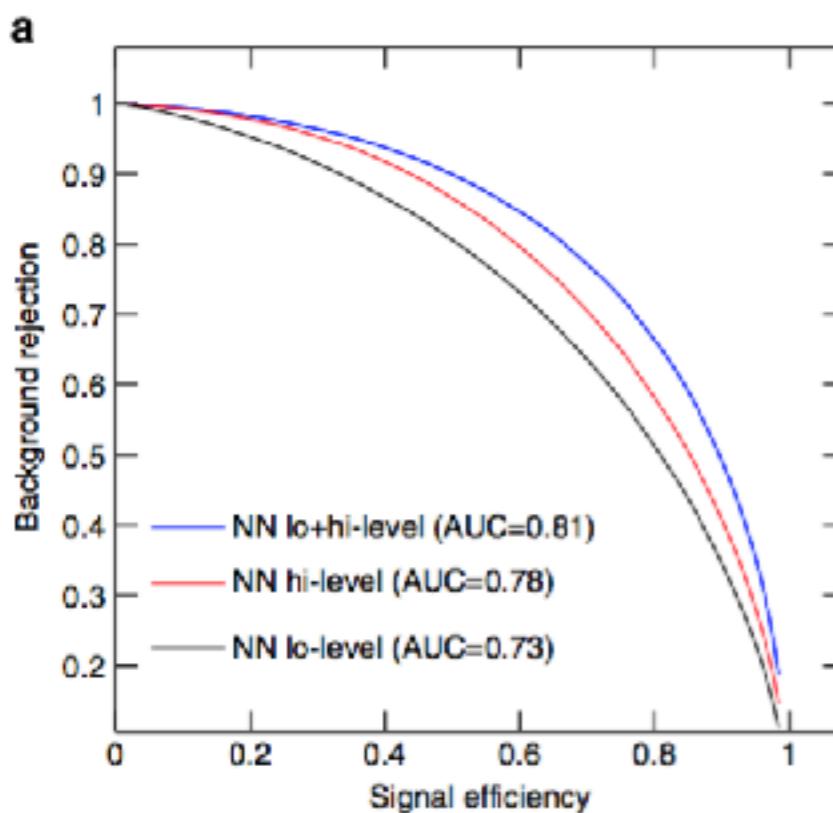
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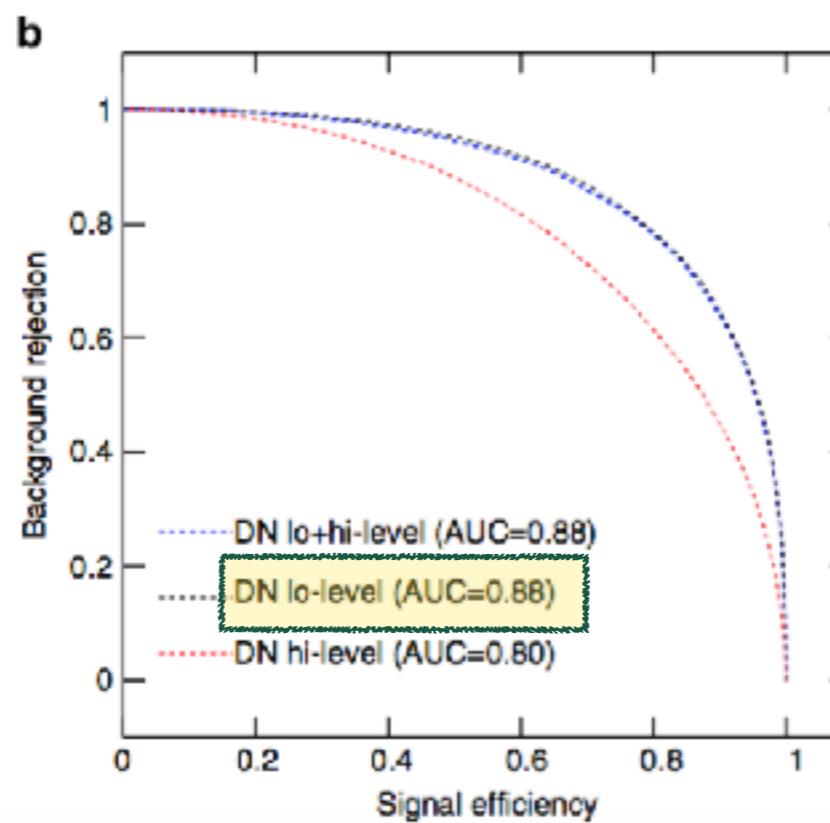
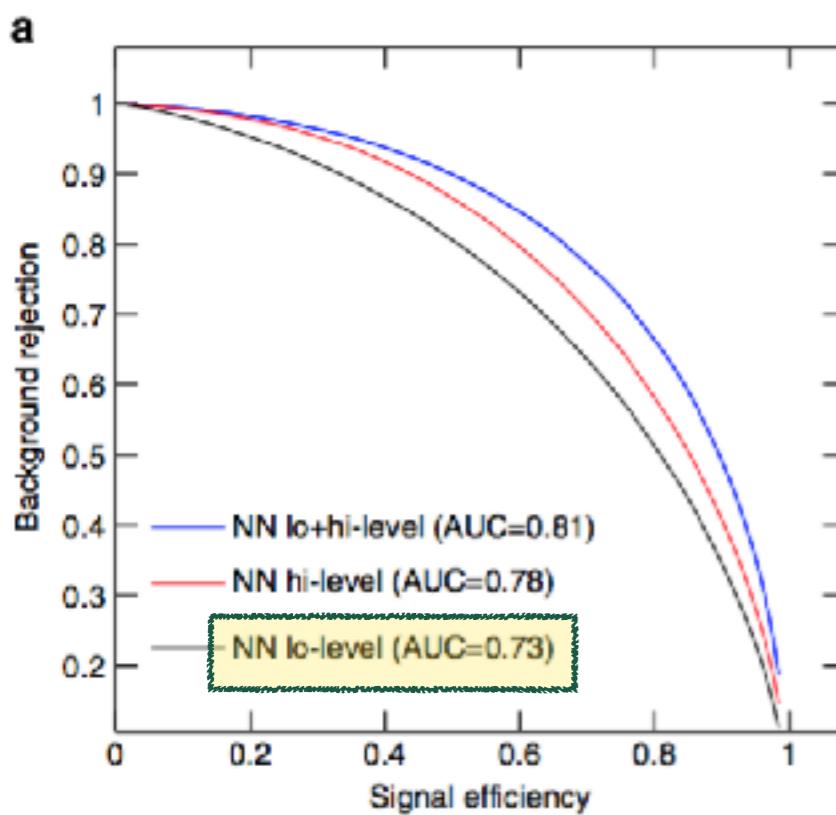
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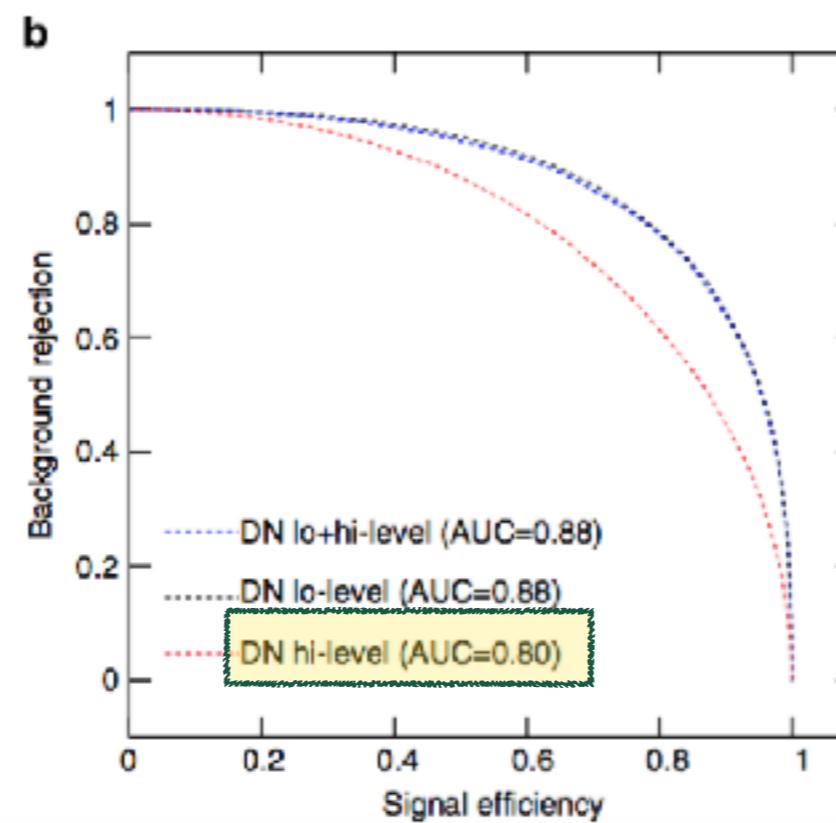
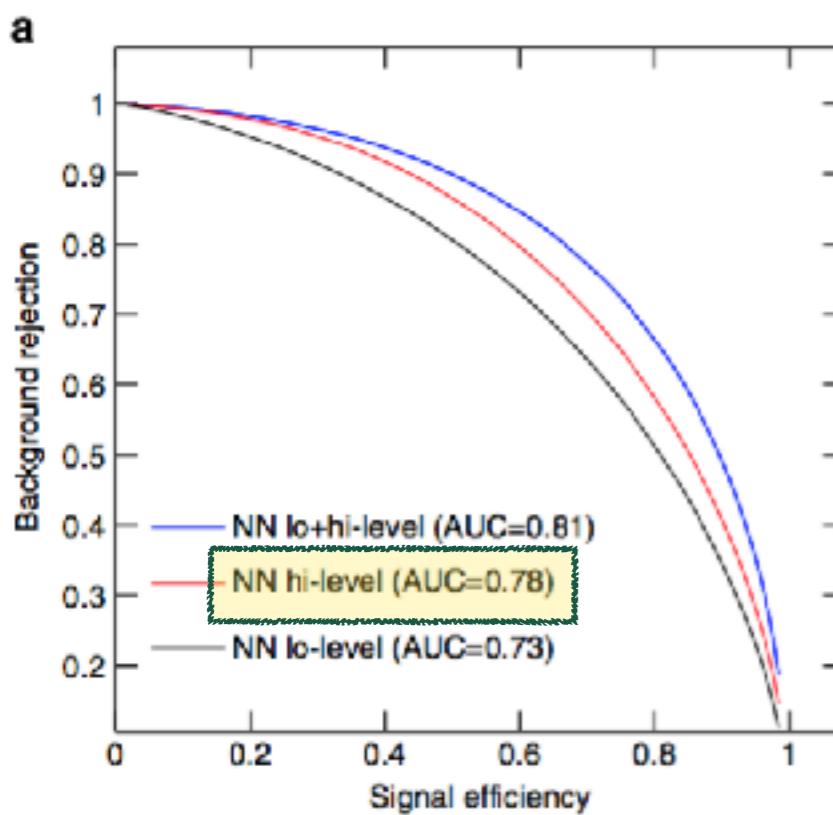
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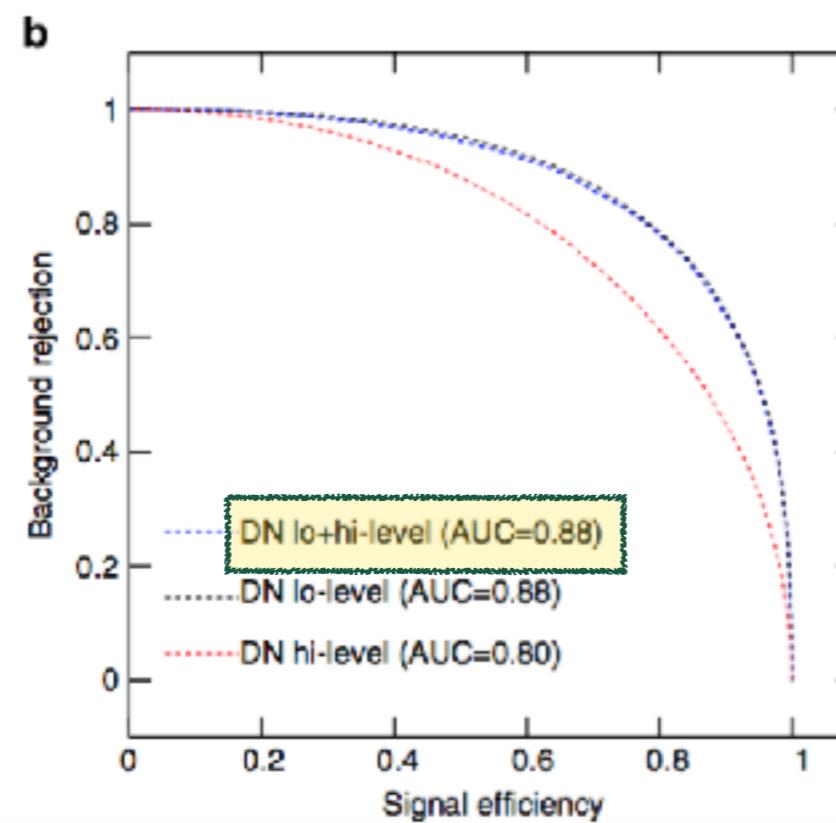
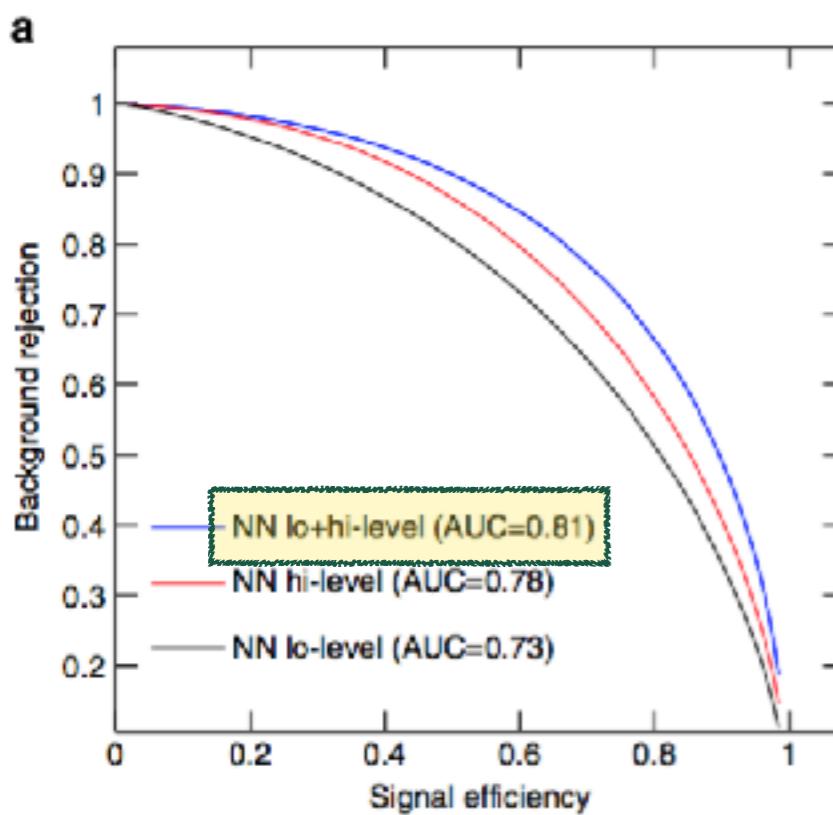
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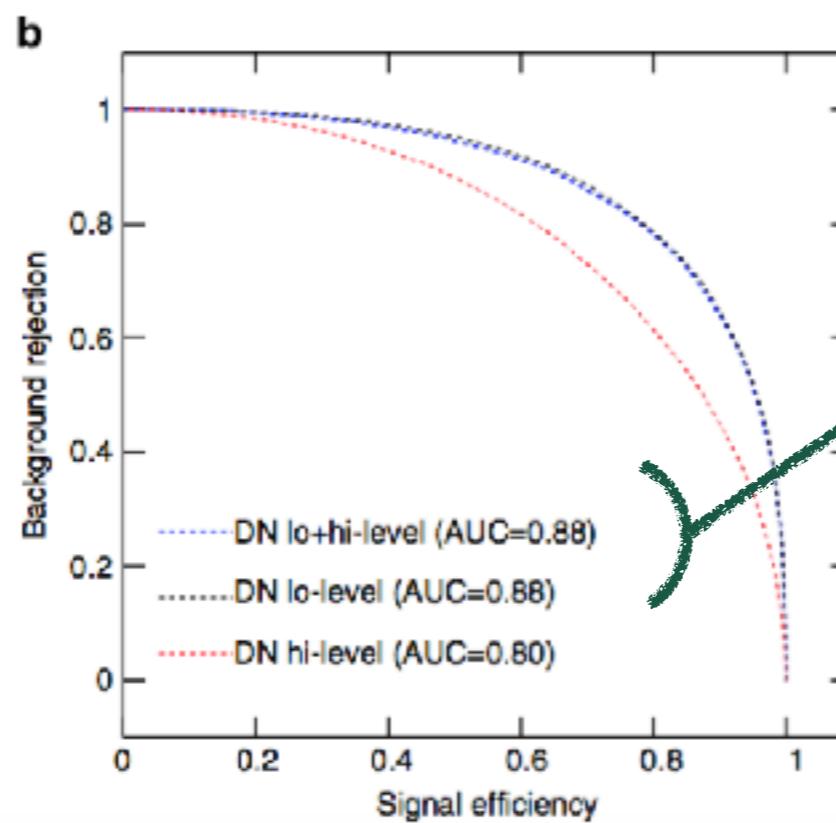
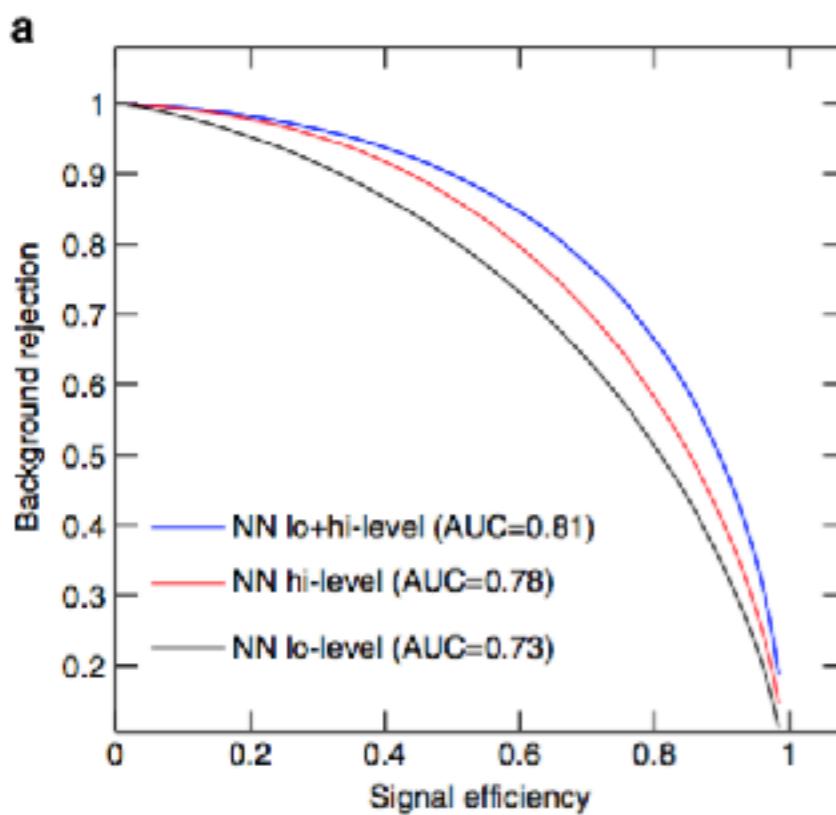
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High-level not helping much

# Deep learning in HEP

---

Deep learning, using raw information, can outperform physics inspired observables.

- Let the machine use *all the information* available

Why isn't every experimental analysis done with machine learning then?

What data should the neural networks be trained on?

What does “raw information” mean?

# Looking forward

- In today's tutorial, you will learn to do linear and logistic regression, from scratch (using linear algebra packages).
- From logistic regression, you will expand to program a neural network from scratch.

- In tomorrow's lecture, we will look at recent machine learning results in HEP.
  - How to represent the data
  - Generalizing from Monte Carlo to real data
  - How to train on unlabelled data (real data)

# Short Break

# Introduction to Machine Learning

## Tutorial 1

- Implement linear regression from scratch
- Implement logistic regression from scratch
- Program your first neural network from scratch

```
git clone https://github.com/bostdiek/KIAS\_Winter\_School.git
cd KIAS_Winter_School
git pull
```

```
docker run -p 8888:8888 -it -v $PWD:$PWD -w $PWD -e
JUPYTER_ENABLE_LAB=yes bostdiek/kias_ws
```