week2_assessment

October 12, 2020

0.1 Creating confidence intervals in python

In this assessment, you will look at data from a study on toddler sleep habits.

The confidence intervals you create and the questions you answer in this Jupyter notebook will be used to answer questions in the following graded assignment.

```
In [42]: import numpy as np
    import pandas as pd
    from scipy.stats import t
    import statsmodels.api as sm
    pd.set_option('display.max_columns', 30) # set so can see all columns of the DataFram
```

Your goal is to analyse data which is the result of a study that examined differences in a number of sleep variables between napping and non-napping toddlers. Some of these sleep variables included: Bedtime (lights-off time in decimalized time), Night Sleep Onset Time (in decimalized time), Wake Time (sleep end time in decimalized time), Night Sleep Duration (interval between sleep onset and sleep end in minutes), and Total 24-Hour Sleep Duration (in minutes). Note: Decimalized time is the representation of the time of day using units which are decimally related.

The 20 study participants were healthy, normally developing toddlers with no sleep or behavioral problems. These children were categorized as napping or non-napping based upon parental report of children's habitual sleep patterns. Researchers then verified napping status with data from actigraphy (a non-invasive method of monitoring human rest/activity cycles by wearing of a sensor on the wrist) and sleep diaries during the 5 days before the study assessments were made.

You are specifically interested in the results for the Bedtime, Night Sleep Duration, and Total 24- Hour Sleep Duration.

Reference: Akacem LD, Simpkin CT, Carskadon MA, Wright KP Jr, Jenni OG, Achermann P, et al. (2015) The Timing of the Circadian Clock and Sleep Differ between Napping and Non-Napping Toddlers. PLoS ONE 10(4): e0125181. https://doi.org/10.1371/journal.pone.0125181

Out[3]:		id	sex	age	(mont		dlmo tir		days	napped	na	apping	\		
	0	1	female		3	3.7	19.2	24		0		0			
	1	2	female		3	1.5	18.2	27		0		0			
	2	3	male		3	1.9	19.3	14		0		0			
	3	4	female		3	1.6	19.6	3 9		0		0			
	4	5	female		3	3.0	19.5	52		0		0			
	5	6	female		30	6.2	18.2	22		4		1			
	6	7	male		30	6.3	19.2	28		1		1			
	7	8	male		30	0.0	21.0	06		5		1			
	8	9	male		33	3.2	19.3	38		2		1			
	9	10	female		3	7.1	19.9	93		3		1			
	10	11	${\tt male}$		3:	2.9	18.7	79		4		1			
	11	12	female		3	5.0	19.6	35		5		1			
	12	13	male		3	5.1	19.8	33		3		1			
	13	14	female		3	5.6	19.8	38		4		1			
	14	15	female		30	6.6	19.9	94		4		1			
	15	16	male		30	6.5	20.2	25		3		1			
	16	17	female		3	3.7	20.3	33		5		1			
	17	18	male		30	6.4	20.3	16		5		1			
	18	19	female		3	3.6	19.6	86		3		1			
	19	20	${\tt male}$		3	3.8	20.5	51		3		1			
		nap	lights	outl		nap	sleep or		na	_	_	nap	sleep		\
	0				NaN			NaN			NaN			NaN	
	1				NaN			NaN			NaN			NaN	
	2				NaN			NaN			NaN			NaN	
	3				NaN			NaN			NaN			NaN	
	4				NaN			NaN			NaN			NaN	
	5				14.00			4.22			.00			15.78	
	6				14.75			5.03			.92			16.80	
	7				13.09			3.43			.44			15.46	
	8				14.41			4.42			.71			17.01	
	9				13.12			3.42			.31			15.19	
	10				13.99			4.03			.85			15.68	
	11				13.18			3.45			.33			15.21	
	12				13.94			4.48			.26			16.03	
	13				12.68			3.08			.92			14.76	
	14				12.71			2.88			.80			14.72	
	15				13.74			4.68			.66			16.64	
	16				13.15			3.87			.49			15.11	
	17				12.47			2.56			.30			14.05	
	18				14.71			4.85			.46			16.07	
	19			1	12.68		13	3.54		14	.30			15.07	
													_		
	_	nap			nap du:		n nap 1	time			ght				
	0			NaN		Na				NaN		20.			
	1			NaN		Na				NaN		19.			
	2]	NaN		Na	ιN			NaN		19.	60		

3	NaN	NaN	1	NaN	19.46	3
4	NaN	NaN	1	NaN	19.21	
5	16.28	93.75	137	.00	19.95	<u>,</u>
6	16.08	106.00	80	.00	20.60)
7	15.82	121.60	163	.80	22.01	
8	16.60	155.50	131	. 25	20.24	Ŀ
9	15.30	106.67	130	. 67	20.78	3
10	16.10	98.75	126	.60	19.45	5
11	15.35	105.80	130	.40	20.18	}
12	15.78	93.33	110	. 20	20.22	2
13	15.00	100.75	139	. 33	20.26	3
14	14.88	110.75	.00	20.28		
15	16.45	117.33	162	.75	20.46	3
16	15.40	74.20	135	.00	20.43	}
17	14.25	89.80	107	.00	20.02	2
18	16.20	73.00	.40	19.50		
19	15.23	91.67	. 67	20.18	3	
	night sleep onset	sleep onset	latency n	ight mid	sleep time	, \
0	20.68		0.23		1.92	2
1	19.48		0.25		1.09)
2	20.05		0.45		1.29)
3	19.50		0.05		1.89)
4	19.65		0.45		1.30)
5	20.25		0.29		1.26	5
6	20.96		0.36		2.12	2
7	22.53		0.51		2.92	2
8	20.37		0.13		1.60)
9	21.63		0.84		2.20)
10	19.88		0.44		1.34	Ŀ
11	20.84		0.66		1.93	3
12	20.89		0.67		1.99)
13	20.80		0.54		1.96	5
14	20.92		0.64		1.49)
15	21.25		0.79		2.19)
16	21.03		0.60		2.44	
17	20.45		0.43		1.23	}
18	19.64		0.14		1.42	
19	21.38		1.19		2.51	-
	night wake time n	ight sleep du	-	ght time		١.
0	7.17		629.40		643.00	
1	6.69		672.40		700.40	
2	6.53		628.80		682.60	
3	8.28		766.60		784.00	
4	6.95		678.00		718.00	
5	6.28		602.20		653.80	
6	7.27		618.40		655.40	

```
7
                7.31
                                      526.80
                                                           582.40
8
                6.82
                                      626.80
                                                           660.33
9
                6.52
                                      549.50
                                                           626.00
10
                6.80
                                      655.20
                                                           694.80
11
                7.03
                                      611.20
                                                           660.40
12
                7.09
                                      611.80
                                                           662.20
13
                7.11
                                      618.80
                                                           671.20
14
                6.33
                                      548.00
                                                           595.00
15
                7.13
                                      593.25
                                                           662.00
16
                7.86
                                      649.80
                                                           708.60
17
                6.01
                                      573.60
                                                           614.60
18
                7.20
                                      693.40
                                                           715.00
19
                                                           692.00
                7.63
                                      615.33
    24 h sleep duration
                           bedtime phase difference
0
                  629.40
                                                -1.21
1
                  672.40
                                                -0.96
2
                  628.80
                                                -0.46
3
                  766.60
                                                 0.23
4
                  678.00
                                                 0.31
5
                  695.95
                                                -1.73
6
                  724.40
                                                -1.32
7
                  648.40
                                                -0.95
8
                  782.30
                                                -0.86
9
                  656.17
                                                -0.76
10
                  753.95
                                                -0.66
                                                -0.53
11
                  717.00
12
                  705.13
                                                -0.39
13
                  719.55
                                                -0.38
14
                  658.75
                                                -0.34
15
                  710.58
                                                -0.21
                  724.00
16
                                                -0.10
17
                  663.40
                                                 0.14
18
                  766.40
                                                 0.18
19
                  707.00
                                                 0.33
    sleep onset phase difference midsleep phase difference \
0
                             -1.44
                                                            6.68
                             -1.21
                                                            6.82
1
2
                             -0.91
                                                            6.15
3
                              0.19
                                                            6.20
4
                             -0.13
                                                            5.78
5
                             -2.03
                                                            7.05
6
                             -1.68
                                                            6.84
7
                             -1.47
                                                            5.86
8
                             -0.99
                                                            6.22
9
                             -1.82
                                                            6.21
10
                             -1.09
                                                            6.55
```

11	-1.19	6.28
12	-1.06	6.16
13	-0.92	6.08
14	-0.90	5.64
15	-1.00	5.94
16	-0.70	6.12
17	-0.29	5.07
18	0.04	5.74
19	-0.87	6.00
	wake time phase difference	
0	11.93	
1	12 42	

12.42 2 11.39 3 12.59 4 11.43 5 12.06 6 11.99 7 10.25 8 11.44 9 10.59 10 12.01 11.38 11 12 11.26 13 11.23 14 10.39 10.88 15 11.53 16 9.85 17 18 11.52 19 11.12

Question: What variable is used in the column 'napping' to indicate a toddler takes a nap? **Question**: What is the sample size n? What is the sample size for toddlers who nap, n_1 , and toddlers who don't nap, n_2 ?

Napping column: 0 = no nap 1 = nap So from above value counts we can see that 5 toddlers did not nap, 15 did take a nap.

```
In [6]: #sample size?
len(df)
```

Out[6]: 20

We can see there are a total of 20 toddlers in the study.

0.1.1 Average bedtime confidence interval for napping and non napping toddlers

Create two 95% confidence intervals for the average bedtime, one for toddler who nap and one for toddlers who don't.

Before any analysis, we will convert 'night bedtime' into decimalized time.

Now, isolate the column 'night bedtime' for those who nap into a new variable, and those who didn't nap into another new variable.

```
In [22]: bedtime_nap = df[['night bedtime', 'napping']][(df['napping']==1)]
         bedtime_nap
Out [22]:
             night bedtime napping
         5
                     1235.0
         6
                                    1
                     1260.0
         7
                     1321.0
         8
                     1224.0
         9
                     1278.0
                                    1
         10
                     1185.0
                                    1
         11
                     1218.0
                                    1
         12
                     1222.0
                                    1
         13
                     1226.0
                                    1
                     1228.0
         14
         15
                     1246.0
         16
                     1243.0
                                    1
                     1202.0
         17
                                    1
         18
                     1190.0
                                    1
                     1218.0
In [24]: bedtime_no_nap = df[['night bedtime', 'napping']][(df['napping']==0)]
         bedtime_no_nap
Out [24]:
            night bedtime napping
         0
                    1245.0
                                   0
         1
                    1163.0
         2
                    1200.0
                                   0
         3
                    1186.0
                                   0
                                   0
                    1161.0
```

Now find the sample mean bedtime for nap and no_nap.

```
Out [29]: 1233.066666666666
In [30]: bedtime_nap.groupby("napping").agg({"night bedtime": [np.mean, np.std, np.size]})
Out [30]:
                 night bedtime
                           mean
                                       std size
         napping
         1
                    1233.066667 34.44554 15.0
In [28]: no_nap_mean_bedtime = bedtime_no_nap['night bedtime'].mean()
         no_nap_mean_bedtime
Out[28]: 1191.0
In [31]: bedtime_no_nap.groupby("napping").agg({"night bedtime": [np.mean, np.std, np.size]})
Out [31]:
                 night bedtime
                                        std size
                           mean
         napping
                         1191.0 34.300146 5.0
   Now find the standard error for \bar{X}_{nap} and \bar{X}_{no\ nap}.
In [32]: nap_se_mean_bedtime = 34.445/np.sqrt(15)
         nap_se_mean_bedtime
Out [32]: 8.893660757340966
In [33]: no_nap_se_mean_bedtime = 34.300/np.sqrt(5)
         no_nap_se_mean_bedtime
Out [33]: 15.339426325648555
```

Question: Given our sample sizes of n_1 and n_2 for napping and non napping toddlers respectively, how many degrees of freedom (df) are there for the associated t distributions?

As an over-simplification, you subtract one degree of freedom for each variable, and since there are 1 variable per group, the degrees of freedom are n-1. Degrees of freedom = n-1 - n1 df = 14 - n2 df = 4

To build a 95% confidence interval, what is the value of t*? You can find this value using the percent point function:

```
from scipy.stats import t
t.ppf(probabiliy, df)
```

This will return the quantile value such that to the left of this value, the tail probability is equal to the input probability (for the specified degrees of freedom).

Example: to find the t^* for a 90% confidence interval, we want t^* such that 90% of the density of the t distribution lies between $-t^*$ and t^* .

Or in other words if $X \sim t(df)$:

```
P(-t^* < X < t^*) = .90
   Which, because the t distribution is symmetric, is equivalent to finding t^* such that:
   P(X < t^*) = .95
   So the t^* for a 90% confidence interval, and lets say df=10, will be:
   t star = t.ppf(.95, df=10)
In [47]: # Find the t_stars for the 95% confidence intervals
         #t star calculation
         from scipy.stats import t
         alpha = 0.025 #95% confidence
         nap_t_star = t.ppf(1 - alpha, df=14)
         print(f'The tstar for napping is:',nap_t_star)
The tstar for napping is: 2.1447866879169273
In [48]: no_nap_t_star = t.ppf(1 - alpha, df=4)
         print(f'The t star for no nap is:',no_nap_t_star)
The t star for no nap is: 2.7764451051977987
   Quesion: What is t^* for nap and no nap?
   Now to create our confidence intervals. For the average bedtime for nap and no nap, find the
upper and lower bounds for the respective confidence intervals.
In [49]: #confidence interval for nap
         lcb = nap_mean_bedtime - nap_t_star * nap_se_mean_bedtime
         ucb = nap_mean_bedtime + nap_t_star * nap_se_mean_bedtime
         (lcb, ucb)
Out [49]: (1213.9916614674726, 1252.1416718658606)
   Another way to do this for napping
In [50]: sm.stats.DescrStatsW(bedtime_nap["night bedtime"]).zconfint_mean()
Out [50]: (1215.635138529232, 1250.498194804101)
In [51]: #confidence interval for no nap
In [52]: lcb2 = no_nap_mean_bedtime - no_nap_t_star * no_nap_se_mean_bedtime
         ucb2 = no_nap_mean_bedtime + no_nap_t_star * no_nap_se_mean_bedtime
         (1cb2, ucb2)
Out [52]: (1148.4109248616107, 1233.5890751383893)
```

another way to do this for no napping:

```
In [53]: sm.stats.DescrStatsW(bedtime_no_nap["night bedtime"]).zconfint_mean()
Out[53]: (1160.9351490855297, 1221.0648509144703)
```

Question: What are the 95% confidence intervals, rounded to the nearest ten, for the average bedtime (in decimalized time) for toddlers who nap and for toddlers who don't nap?

```
CI = \bar{X} \pm t^* \cdot s.e.(\bar{X})
```

Answer: 1. With 95% confidence we can say the average bed time for toddlers who nap is 1233.1 +/- 18.7 (1214 to 1252.1), range of 38. 2. With 95% confidence we can say the average bed time for toddlers who DO NOT NAP is 1191 +/- 42.8 (1148.4 to 1233.6), range of 85. Therefore it appears that toddlers who nap have a smaller margin of error/smaller range of bedtimes but a later average bedtime. Toddlers who do not nap have a larger margin of error/larger range of bedtimes but an earlier bed time.

Challenge problem: Write a function that inputs the column containing the data you want to build your confidence interval from and returns the confidence interval as a list or tuple (i.e. [upper, lowe] or (upper, lower)).