



BAYESIAN REGRESSION MODELING WITH RSTANARM

Visualizing a Bayesian Model

Jake Thompson

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Saving model coefficients

```
stan_model <- stan_glm(kid_score ~ mom_iq, data = kidiq)
```

```
tidy(stan_model)
```

```
#> # A tibble: 2 x 3
```

```
#>   term          estimate std.error
```

```
#>   <chr>         <dbl>      <dbl>
```

```
#> 1 (Intercept)    25.7        5.92
```

```
#> 2 mom_iq         0.611       0.0590
```

```
tidy_coef <- tidy(stan_model)
```

```
model_intercept <- tidy_coef$estimate[1]
```

```
model_intercept
```

```
#> [1] 25.67857
```

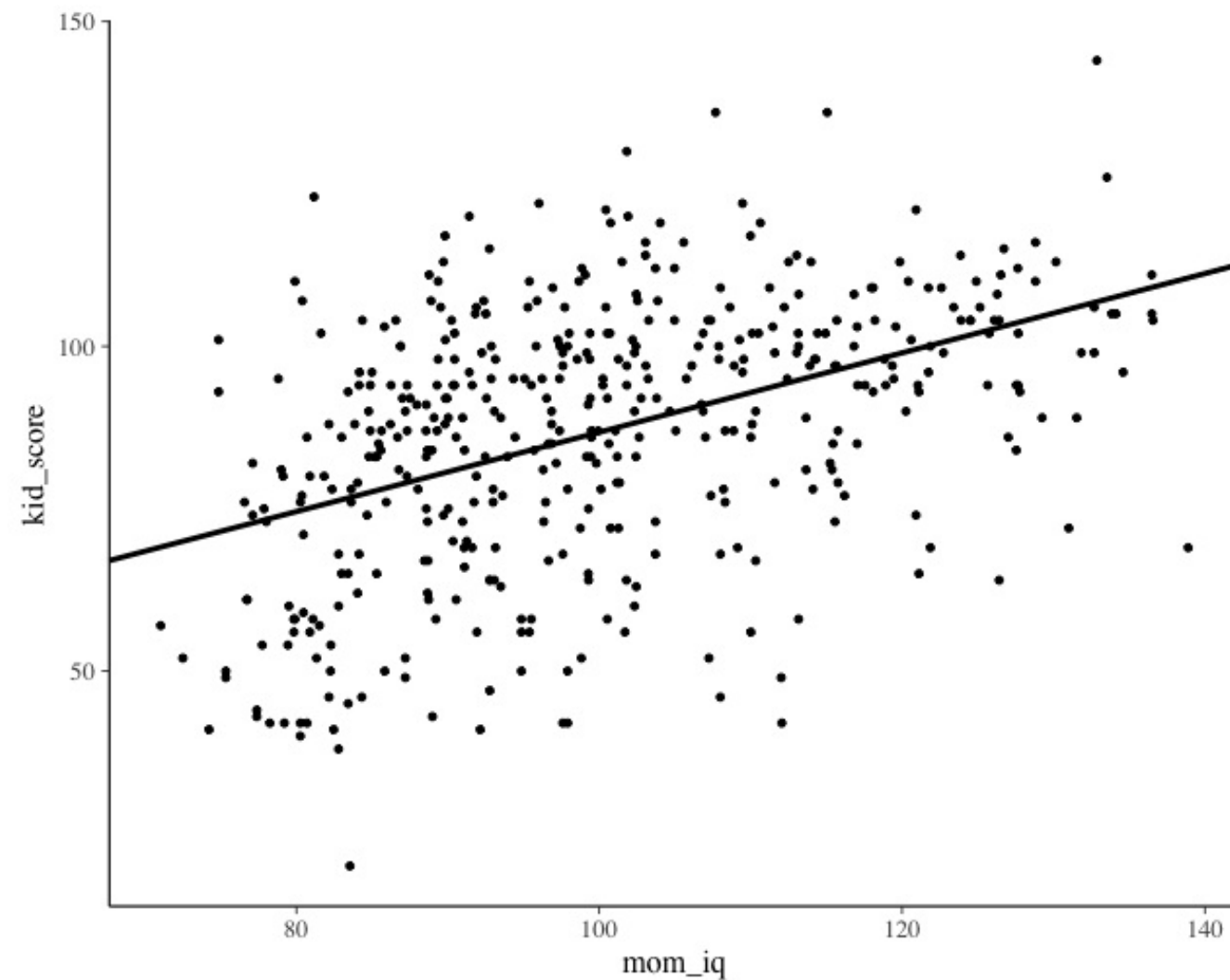
```
model_slope <- tidy_coef$estimate[2]
```

```
model_slope
```

```
#> [1] 0.6110473
```

Creating a plot

```
ggplot(kidiq, aes(x = mom_iq, y = kid_score)) +  
  geom_point() +  
  geom_abline(intercept = model_intercept, slope = model_slope,)
```



Plotting uncertainty

```
draws <- spread_draws(stan_model, `(Intercept)`, mom_iq)
```

```
draws
```

```
#> # A tibble: 4,000 x 5
```

```
#>   .chain .iteration .draw `(Intercept)` mom_iq
```

```
#>   <int>      <int> <int>      <dbl>  <dbl>
```

```
#> 1         1         1         28.2  0.586
```

```
#> 2         1         2         28.7  0.593
```

```
#> 3         1         3         13.5  0.735
```

```
#> 4         1         4         30.3  0.564
```

```
#> 5         1         5         34.5  0.522
```

```
#> 6         1         6         19.2  0.669
```

```
#> 7         1         7         34.8  0.523
```

```
#> 8         1         8         16.3  0.707
```

```
#> 9         1         9         35.8  0.511
```

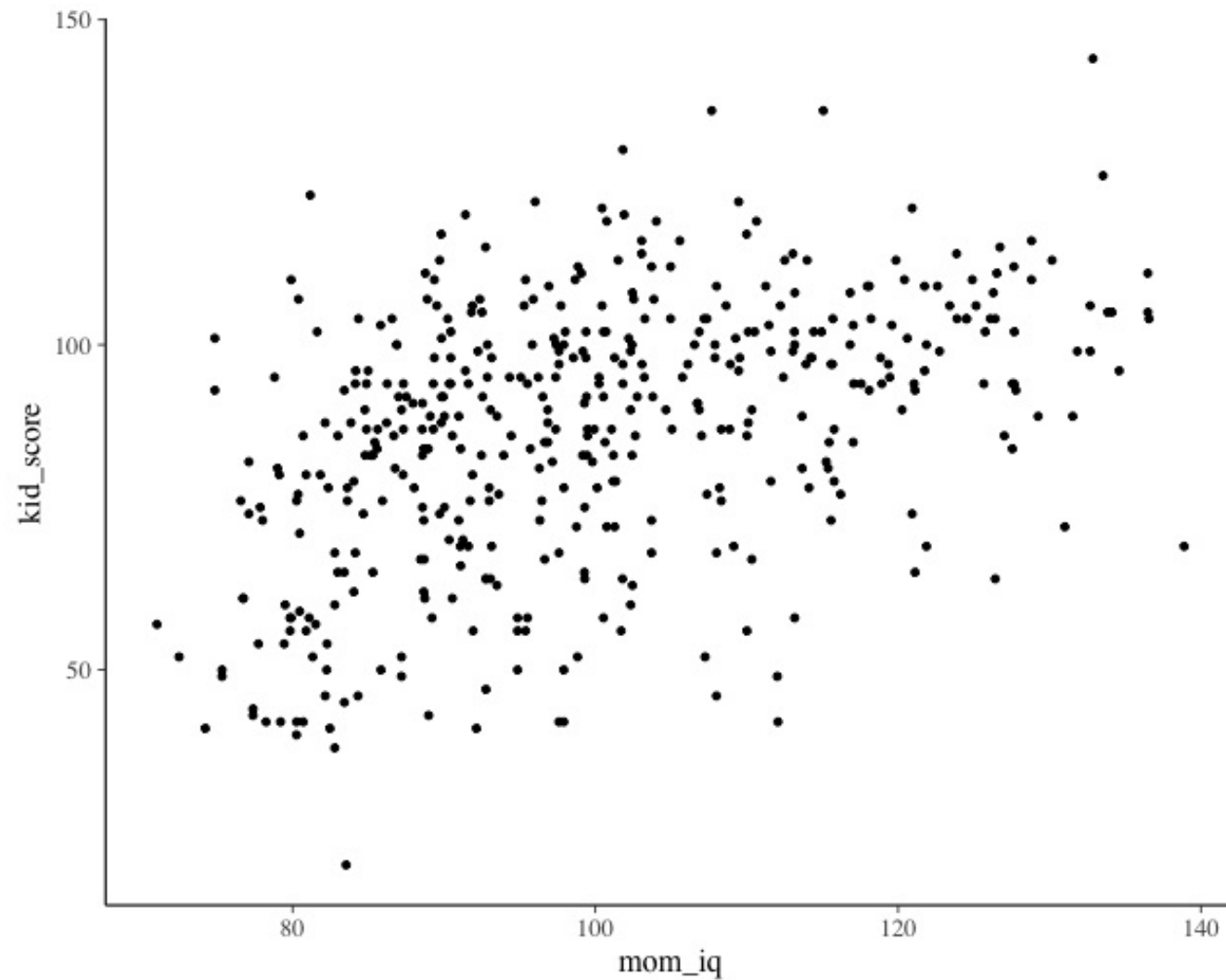
```
#> 10        1        10         14.5  0.734
```

```
#> # ... with 3,990 more rows
```



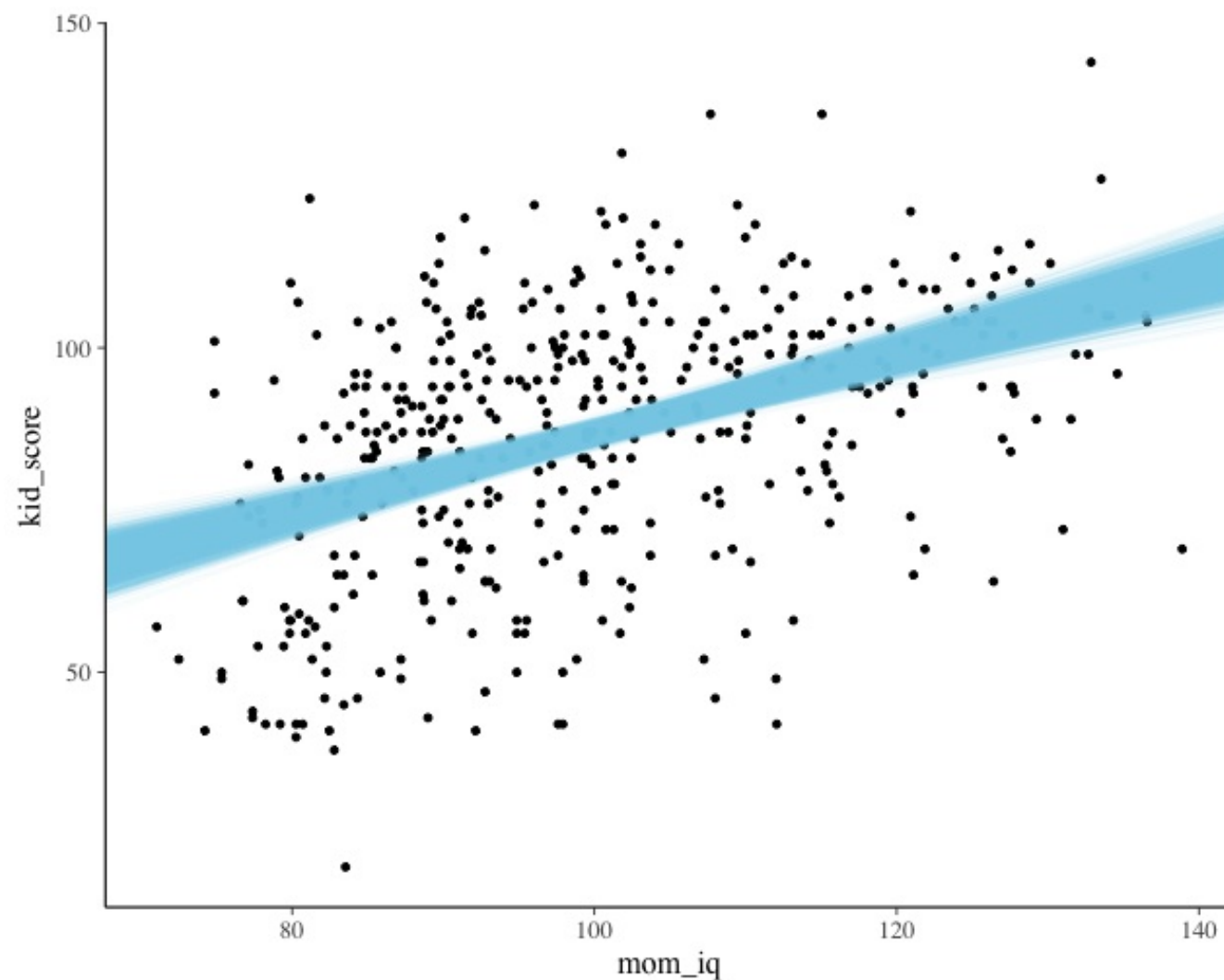
Plotting uncertainty

```
ggplot(kidiq, aes(x = mom_iq, y = kid_score)) +  
  geom_point()
```



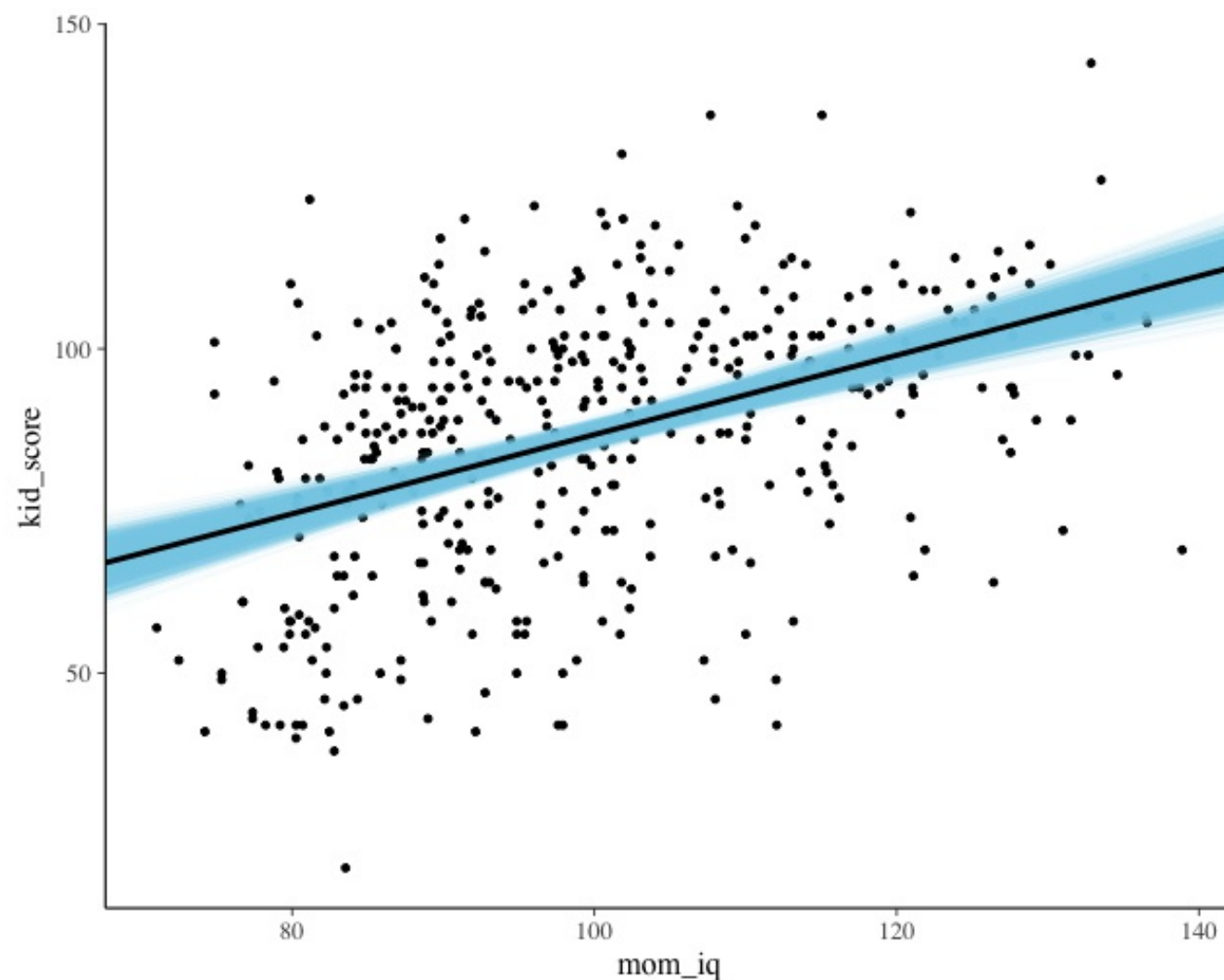
Plotting uncertainty

```
ggplot(kidiq, aes(x = mom_iq, y = kid_score)) +  
  geom_point()  
  geom_abline(data = draws, aes(intercept = `(Intercept)`, slope = mom_iq),  
             size = 0.2, alpha = 0.1, color = "skyblue")
```



Plotting uncertainty

```
ggplot(kidiq, aes(x = mom_iq, y = kid_score)) +  
  geom_point()  
  geom_abline(data = draws, aes(intercept = `(Intercept)`, slope = mom_iq),  
    size = 0.2, alpha = 0.1, color = "skyblue") +  
  geom_abline(intercept = model_intercept, slope = model_slope)
```





BAYESIAN REGRESSION MODELING WITH RSTANARM

Let's practice



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Making Predictions

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Making predictions for observed data

```
stan_model <- stan_glm(kid_score ~ mom_iq + mom_hs, data = kidiq)
```

```
posteriors <- posterior_predict(stan_model)
```

```
posteriors[1:10, 1:5]
```

```
#>           1           2           3           4           5
#> [1,]  61.08989  58.57298  80.68946 101.00810  76.37946
#> [2,] 111.52704  49.92284  99.09657  97.33291  72.98906
#> [3,]  83.36793  81.35768  94.16414 101.73570  64.69375
#> [4,] 118.15092  74.00476 107.28852  75.75912  91.93991
#> [5,] 103.95042  58.98491 128.40312 121.42753  62.70008
#> [6,] 102.29874 127.74050  84.10661  67.94056  82.02546
#> [7,]  91.39445  88.49029  75.05702  94.48594 102.50331
#> [8,]  93.33446  84.99589 101.49261  66.74698  68.26968
#> [9,] 101.85065  91.46998 123.43011  76.53226  74.93288
#> [10,]  79.61489 101.29745 105.97636  97.48332  99.80582
```



Making predictions for new data

```
predict_data <- data.frame(  
  mom_iq = 110,  
  mom_hs = c(0, 1)  
)
```

```
predict_data  
#>   mom_iq mom_hs  
#> 1    110     0  
#> 2    110     1
```



Making predictions for new data

```
new_predictions <- posterior_predict(stan_model, newdata = predict_data)
```

```
new_predictions[1:10,]
```

```
#>           1           2
#> [1,]  90.90581 107.75710
#> [2,]  78.72466 139.86677
#> [3,]  80.67743  88.81523
#> [4,]  83.47852  74.06063
#> [5,]  69.07708  87.81177
#> [6,]  40.46229  85.45969
#> [7,]  79.41597  64.19011
#> [8,] 107.93867 117.49345
#> [9,]  95.31493  82.51476
#> [10,] 91.18056  94.22732
```

```
summary(new_predictions[, 1])
```

```
#>   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
#>  20.90   75.26   87.64   87.68  100.02  156.00
```

```
summary(new_predictions[, 2])
```

```
#>   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
#>  34.78   81.32   93.49   93.66  105.62  159.82
```



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Visualizing Predictions

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Plotting new predictions

```
stan_model <- stan_glm(kid_score ~ mom_iq + mom_hs, data = kidiq)

predict_data <- data.frame(
  mom_iq = 110,
  mom_hs = c(0, 1)
)

posterior <- posterior_predict(stan_model, newdata = predict_data)

posterior[1:10,]
#>           1           2
#> [1,] 76.75484 96.26407
#> [2,] 74.39001 100.38898
#> [3,] 90.90370 70.00591
#> [4,] 70.43835 120.82787
#> [5,] 113.98411 82.40497
#> [6,] 56.15829 121.84269
#> [7,] 90.46640 92.77966
#> [8,] 98.56337 110.17948
#> [9,] 108.86147 123.67762
#> [10,] 94.29429 83.77102
```



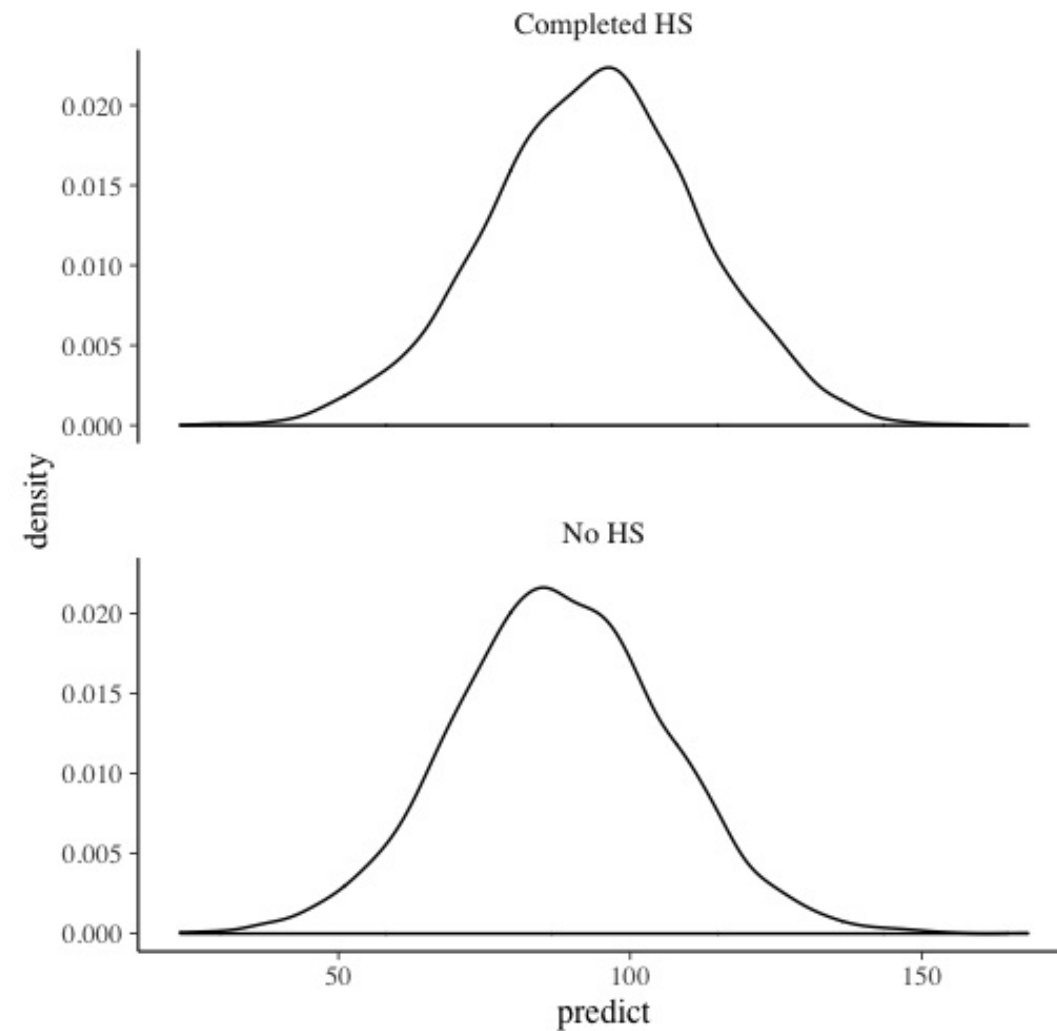
Formatting the data

```
posterior <- as.data.frame(posterior)
colnames(posterior) <- c("No HS", "Completed HS")
plot_posterior <- gather(posterior, key = "HS", value = "predict")

head(plot_posterior)
#>      HS    predict
#> 1 No HS  76.75484
#> 2 No HS  74.39001
#> 3 No HS  90.90370
#> 4 No HS  70.43835
#> 5 No HS 113.98411
#> 6 No HS  56.15829
```


Creating the plot

```
ggplot(plot_posterior, aes(x = predict)) +  
  facet_wrap(~ HS, ncol = 1) +  
  geom_density()
```





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Conclusion

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What we've learned

- How to estimate a Bayesian regression model
 - Differences between frequentist and Bayesian approaches
 - Importance of making correct inferences
- Modifying a Bayesian model
 - Size of the posterior distribution
 - Prior distributions
 - Estimation algorithm



What we've learned

- Evaluate model fit
 - R-squared
 - Posterior predictive model checks
 - Model comparisons
- Using the model
 - Model visualizations
 - Predictions



What we've missed

- Math behind posterior calculations and LOO approximation
- Choosing a prior distribution
- Causes of estimation errors



What comes next?

- More DataCamp courses
 - Bayesian Modeling with RJAGS
- **rstanarm** documentation
 - mc-stan.org/rstanarm
- *Bayesian Data Analysis*, Gelman et al., (2013)



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Thank you!