

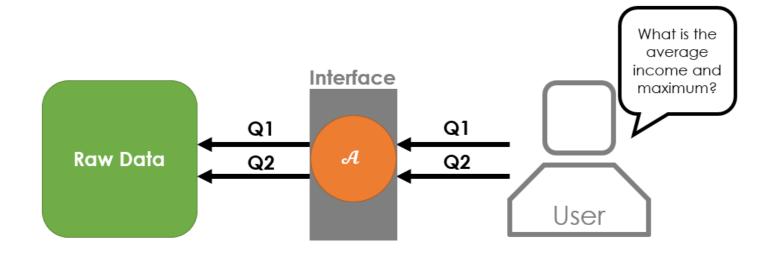


Sequential Composition

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Sequential Composition



• The privacy budget must be divided by two.



Male Fertility Data: Correction on Hours Sitting

```
# Mean and Variance of Hours Sitting
fertility %>%
    summarise_at(vars(Hours_Sitting), funs(mean, var))

# Apply the Laplace mechanism
set.seed(42)
rdoublex(1, 0.41, gs.mean / 0.1)
rdoublex(1, 0.19, gs.var / 0.1)
```

Male Fertility Data: Applying the Laplace mechanism

```
# Set Value of Epsilon
> eps <- 0.1 / 2

# GS of Mean and Variance
> gs.mean <- 0.01
> gs.var <- 0.01

# Apply the Laplace mechanism
> set.seed(42)
> rdoublex(1, 0.41, gs.mean / eps)
[1] 0.4496674

> rdoublex(1, 0.19, gs.var / eps)
[1] 0.2466982
```

For Hours Sitting in the Feritlity Data:

- GS Mean = 0.01
- GS Variance = 0.01
- Mean = 0.41
- Variance = 0.19





Let's practice!



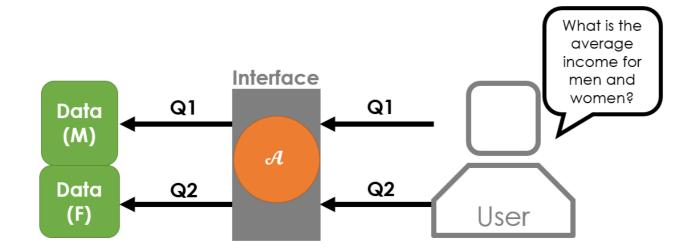


Parallel Composition

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Parallel Composition



- The privacy budget does not need to be divided.
- The query with the most epsilon is the budget for the data.



Male Fertility Data: Prepping Data

```
# High Fevers and Mean of Hours Sitting
> fertility %>%
    filter(High Fevers >= 0) %>%
    summarise at (vars (Hours Sitting), mean)
# A tibble: 1 x 1
  Hours Sitting
       <dbl>
     0.3932967
# No High Fevers and Mean of Hours Sitting
> fertility %>%
    filter(High Fevers == -1) %>%
    summarise at (vars (Hours Sitting), mean)
# A tibble: 1 x 1
  Hours Sitting
       <dbl>
     0.5433333
```



Male Fertility Data: Applying Laplace mechanism

```
# Set Value of Epsilon
> eps <- 0.1

> # GS of mean for Hours_Sitting
> gs.mean <- 1 / 100

# Apply the Laplace mechanism
> set.seed(42)
> rdoublex(1, 0.39, gs.mean / eps)
[1] 0.4098337

> rdoublex(1, 0.54, gs.mean / eps)
[1] 0.5683491
```





Let's practice!





Post-processing

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Male Fertility Data: Prepping Data



Male Fertility Data: Applying the Laplace mechanism

```
# Apply the Laplace mechanism
> set.seed(42)
> smoking1 <- rdoublex(1, 56, gs.count / eps / 2) %>%
    round()
> smoking2 <- rdoublex(1, 23, gs.count / eps / 2) %>%
    round()
# Post-process based on previous queries
> smoking3 <- nrow(fertility) - smoking1 - smoking2
# Checking the noisy answers
> smoking1
[1] 60
> smoking2
[1] 29
> smoking3
[1] 11
```





Let's practice!





Impossible and Inconsistent Answers

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Negative Counts: Prepping Data



Negative Counts: Applying the Laplace mechanism

```
# Apply the Laplace mechanism and set.seed(22)
> set.seed(22)
> rdoublex(1, 12, gs.count / eps) %>%
    round()
[1] -79
# Apply the Laplace mechanism and set.seed(22)
> set.seed(22)
> rdoublex(1, 12, qs.count / eps) %>%
    round() %>%
    max(0)
[1] 0
# Suppose we set a different seed
> set.seed(12)
> noisy answer <- rdoublex(1, 12, gs.count / eps) %>%
    round() %>%
    max(0)
> n <- nrow(fertility)
# ifelse example
> ifelse(noisy answer > n, n, noisy answer)
[1] 100
```



Normalizing Noise: Prepping Data



Normalizing Noise: Applying the Laplace mechanism

```
# Apply the Laplace mechanism and set.seed(42)
> set.seed(42)
> smoking1 <- rdoublex(1, 56, gs.count / eps / 2) %>%
    max(0)
> smoking2 <- rdoublex(1, 23, gs.count / eps / 2) %>%
    max(0)
> smoking3 <- rdoublex(1, 21, gs.count / eps / 2) %>%
    max(0)

# Checking the noisy answers
> smoking <- c(smoking1, smoking2, smoking3)
> smoking
[1] 65.91684 37.17455 0.00000
```



Normalizing Noise: Constraining Results

```
# Normalize smoking
> normalized <- (smoking/sum(smoking)) * (nrow(fertility))
# Round the values
> round(normalized)
[1] 64 36 0
```





Let's practice!