



BAYESIAN REGRESSION MODELING WITH RSTANARM

What's in a Bayesian Model?

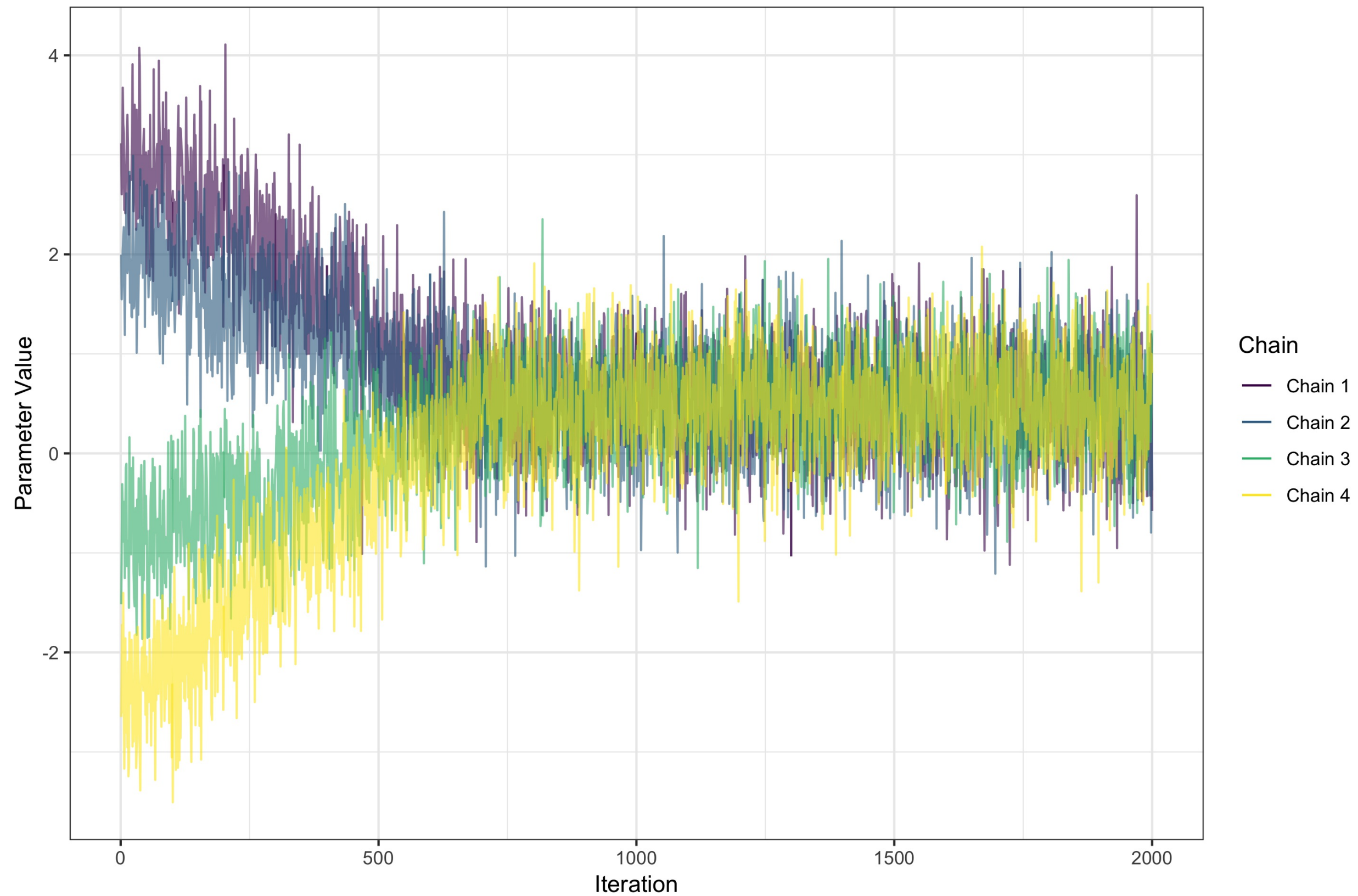
Jake Thompson

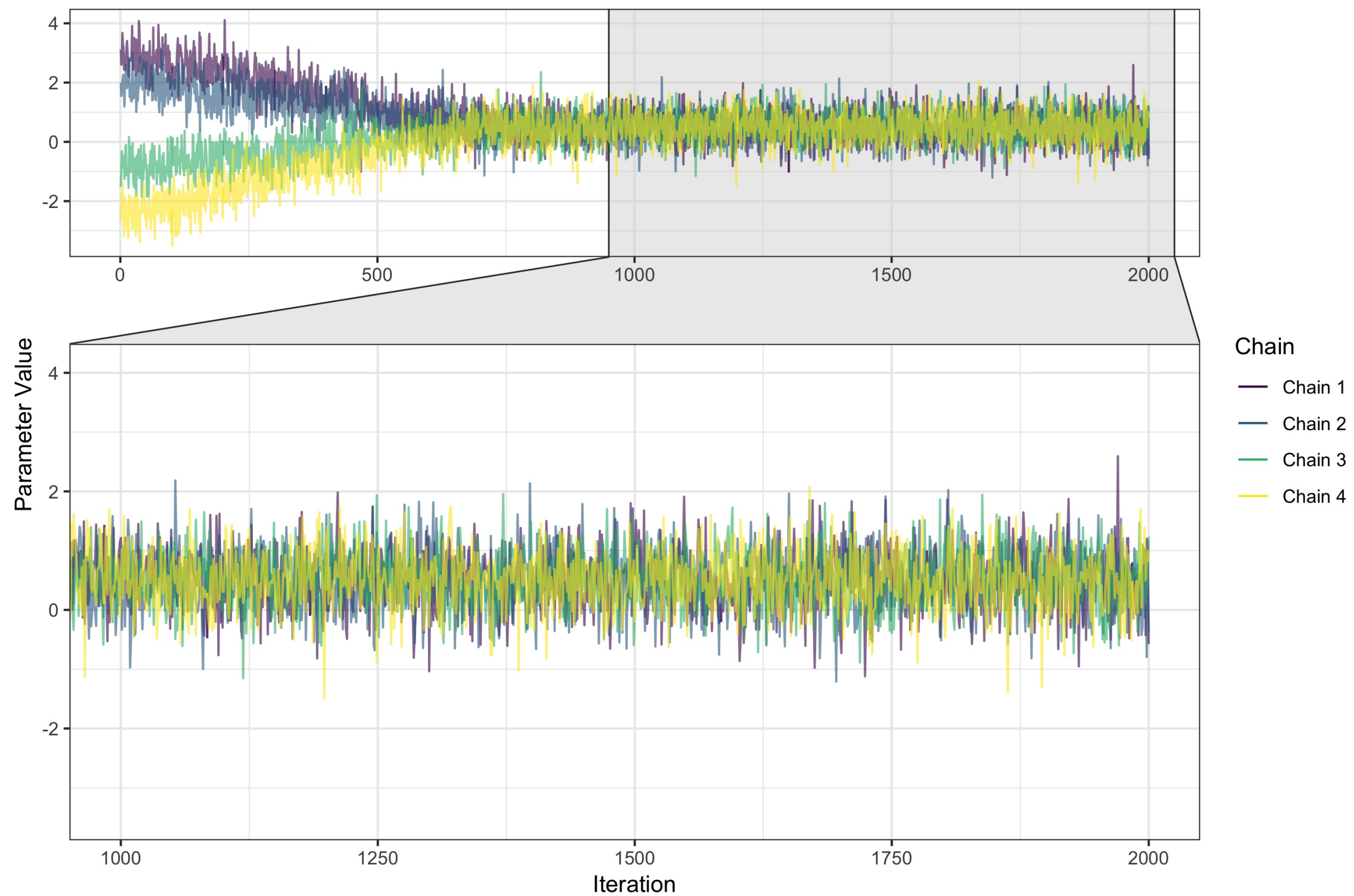
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Posterior Distributions

- Posterior distributions sampled in groups called chains
- Each sample in a chain is an iteration





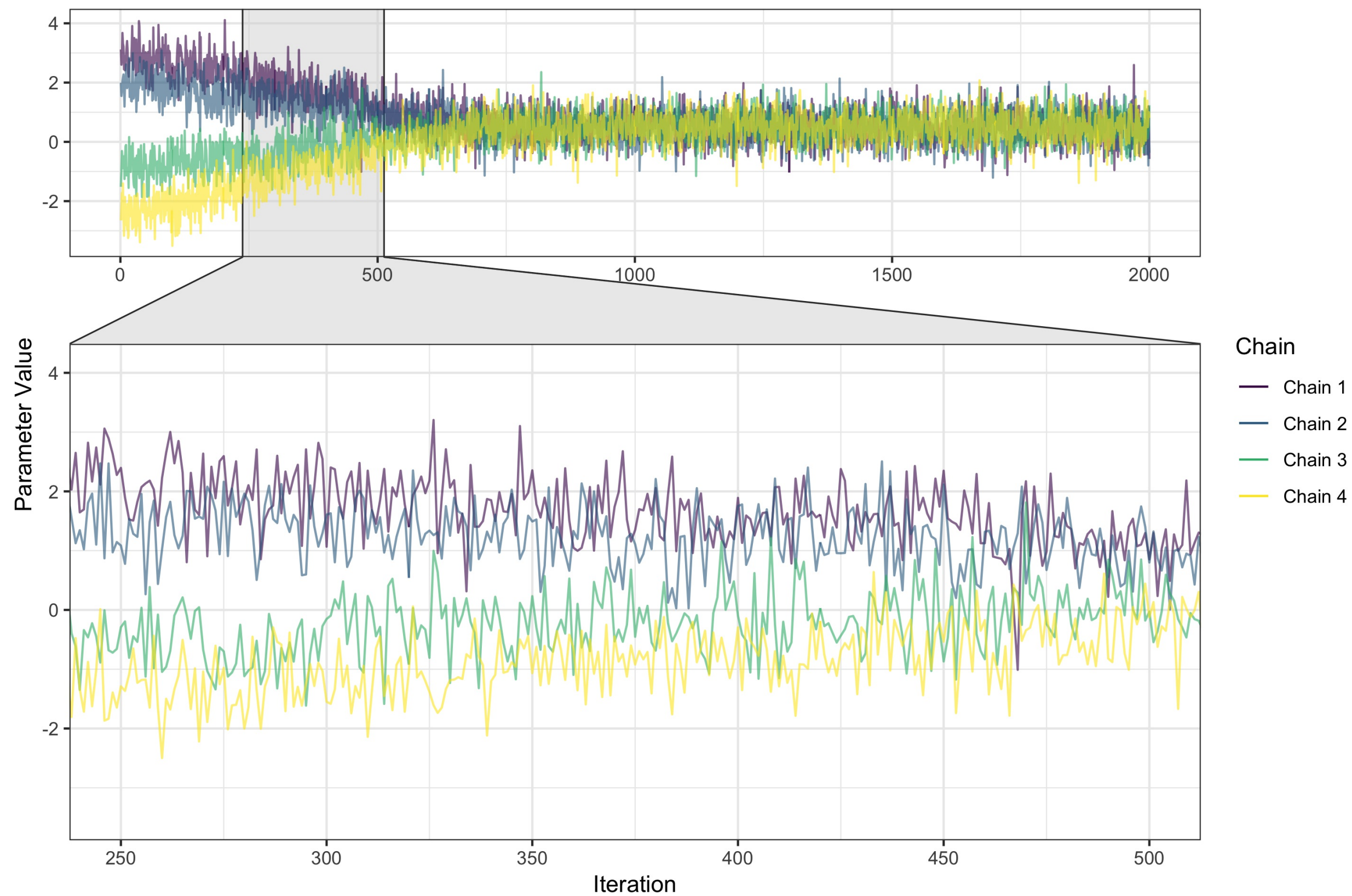


Changing the Number and Length of Chains

```
stan_model <- stan_glm(kid_score ~ mom_iq, data = kidiq,  
  chains = 3, iter = 1000, warmup = 500)
```

Changing the Number and Length of Chains

```
summary(stan_model)
#> Model Info:
#>
#> function:      stan_glm
#> family:        gaussian [identity]
#> formula:       kid_score ~ mom_iq
#> algorithm:     sampling
#> priors:         see help('prior_summary')
#> sample:        1500 (posterior sample size)
#> observations:  434
#> predictors:    2
#>
#> Estimates:
#>           mean      sd    2.5%    25%    50%    75%    97.5%
#> (Intercept)  25.8    6.0    14.1    21.7    25.6    29.9    37.5
#> mom_iq       0.6    0.1     0.5     0.6     0.6     0.7     0.7
#> sigma       18.3    0.6    17.2    17.9    18.3    18.7    19.6
#> mean_PPD     86.9    1.3    84.5    86.0    86.9    87.7    89.2
#> log-posterior -1885.4  1.2 -1888.4 -1885.9 -1885.1 -1884.5 -1884.0
#>
#> Diagnostics:
#>           mcse  Rhat  n_eff
#> (Intercept)  0.2   1.0  1500
#> mom_iq       0.0   1.0  1500
#> sigma        0.0   1.0  1500
```



How many iterations?

- Fewer iterations = shorter estimation time
- Not enough iteration = convergence problems



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Prior Distributions

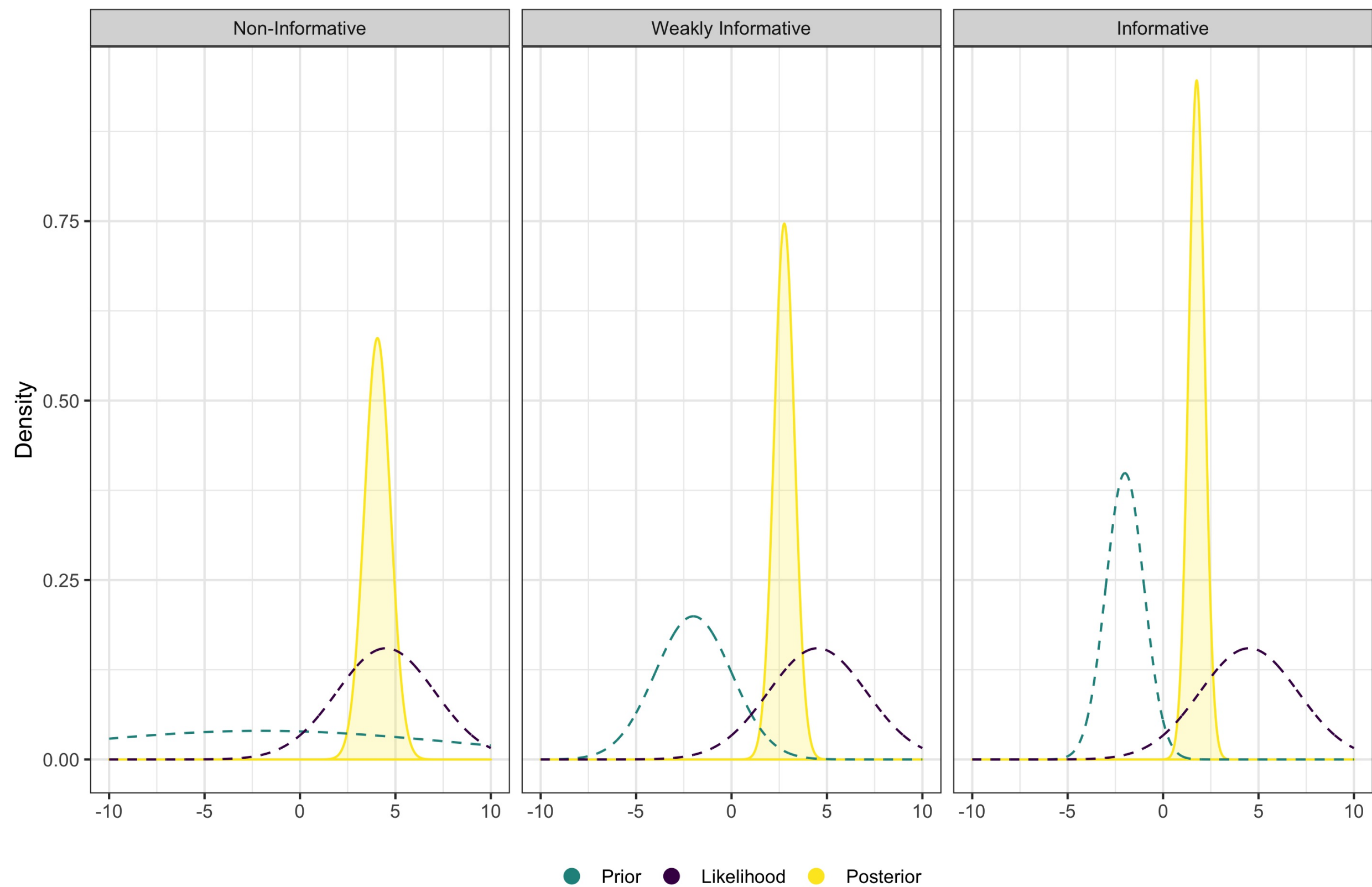
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What's a prior distribution?

- Information that we bring to the model
- Likelihood + prior = posterior





Prior Distributions in rstanarm

```
stan_model <- stan_glm(kid_score ~ mom_iq, data = kidiq)

prior_summary(stan_model){1}
#> Priors for model 'stan_model'
#> -----
#> Intercept (after predictors centered)
#> ~ normal(location = 0, scale = 10)
#> **adjusted scale = 204.11
#>
#> Coefficients
#> ~ normal(location = 0, scale = 2.5)
#> **adjusted scale = 3.40
#>
#> Auxiliary (sigma)
#> ~ exponential(rate = 1)
#> **adjusted scale = 20.41 (adjusted rate = 1/adjusted scale)
#> -----
#> See help('prior_summary.stanreg') for more details
```



Calculating Adjusted Scales

- Intercept: $10 * sd(y)$
- Coefficients: $(2.5 / sd(x)) * sd(y)$

```
prior_summary(stan_model)
#> Priors for model 'stan_model'
#> -----
#> Intercept (after predictors centered)
#> ~ normal(location = 0, scale = 10)
#> **adjusted scale = 204.11
#>
#> Coefficients
#> ~ normal(location = 0, scale = 2.5)
#> **adjusted scale = 3.40
```

```
10 * sd(kidiq$kid_score)
#> [1] 204.1069
```

```
(2.5 / sd(kidiq$mom_iq)) * sd(kidiq$kid_score)
#> [1] 3.401781
```




Unadjusted Priors

```
no_scale <- stan_glm(kid_score ~ mom_iq, data = kidiq,  
  prior_intercept = normal(autoscale = FALSE),  
  prior = normal(autoscale = FALSE),  
  prior_aux = exponential(autoscale = FALSE)  
)
```

```
prior_summary(no_scale)  
#> Priors for model 'no_scale'  
#> -----  
#> Intercept (after predictors centered)  
#> ~ normal(location = 0, scale = 10)  
#>  
#> Coefficients  
#> ~ normal(location = 0, scale = 2.5)  
#>  
#> Auxiliary (sigma)  
#> ~ exponential(rate = 1)  
#> -----  
#> See help('prior_summary.stanreg') for more details
```



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User Specified Priors

Jake Thompson

Psychometrician, ATLAS, University of Kansas



Why change the default prior?

- Good reason to believe the parameter will take a given value
- Constraints on parameter



Specify a prior

```
stan_model <- stan_glm(kid_score ~ mom_iq, data = kidiq,  
  prior_intercept = normal(location = 0, scale = 10),  
  prior = normal(location = 0, scale = 2.5),  
  prior_aux = exponential(rate = 1)  
)
```



Specify a prior

```
stan_model <- stan_glm(kid_score ~ mom_iq, data = kidiq,  
  prior_intercept = normal(location = 0, scale = 10, autoscale = FALSE),  
  prior = normal(location = 0, scale = 2.5, autoscale = FALSE),  
  prior_aux = exponential(rate = 1, autoscale = FALSE)  
)
```




Specify a prior

```
stan_model <- stan_glm(kid_score ~ mom_iq, data = kidiq,  
  prior_intercept = normal(location = 3, scale = 2),  
  prior = cauchy(location = 0, scale = 1),  
)
```

- Many different priors
 - normal()
 - exponential()
 - student_t()
 - cauchy()
- ?priors



Flat priors

```
stan_model <- stan_glm(kid_score ~ mom_iq, data = kidiq,  
  prior_intercept = NULL,  
  prior = NULL,  
  prior_aux = NULL  
)
```

```
prior_summary(stan_model)  
#> Priors for model 'stan_model'  
#> -----  
#> Intercept (after predictors centered)  
#> ~ flat  
#>  
#> Coefficients  
#> ~ flat  
#>  
#> Auxiliary (sigma)  
#> ~ flat  
#> -----  
#> See help('prior_summary.stanreg') for more details
```



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Altering the Estimation Process

Jake Thompson

Psychometrician, ATLAS, University of Kansas

Divergent Transitions

1: There were 15 divergent transitions after warmup. Increasing `adapt_delta` above 0.8 may help.

- Too big of steps in the estimator
- Adjust step size

```
stan_model <- stan_glm(popularity ~ song_age, data = songs,  
  control = list(adapt_delta = 0.95))
```

```
stan_model <- stan_glm(popularity ~ song_age, data = songs,  
  control = list(adapt_delta = 0.99))
```

Exceeding the Maximum Treedepth

Chain 1 reached the maximum tree depth

- Sample evaluates branches and looks for a good place to "U-Turn"
- Max tree depth indicates poor efficiency

```
stan_model <- stan_glm(popularity ~ song_age, data = songs,  
  control = list(max_treedepth = 10))
```

```
stan_model <- stan_glm(popularity ~ song_age, data = songs,  
  control = list(max_treedepth = 15))
```




Tuning the Estimation

- Estimation errors are threats to the validity of the model
- Although complicated, these errors can be addressed easily



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