Introduction to information security (IY2760/DC2760): Introduction to key establishment

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Introduction to information security (IY2760/DC2760): Introdu

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Security protocols
Authenticated key establishment
Key agreement

Symmetric cryptosystems and key establishment

- Symmetric cryptosystems (private key cryptosystems):
 - Encryption and decryption keys are identical.
 - Parties must agree a key before communication.
 - Compromise of key compromises system.
- Properties of keys:
 - Large enough for security.
 - Easy enough to handle.
- Major issue in symmetric cryptography.

Public key cryptosystems and key establishment

- ▶ PKC: no need of secure channel for key exchange.
- ▶ Issue 1: authenticity of Bob's public key in the presence of active adversary.
- ▶ Issue 2: Most PKC are slower than symmetric key systems.

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Long-term and short-term keys

- ▶ Users (or pairs of users) may have *long-term keys*:
 - Precomputed and stored securely;
 - Or computed from securely stored secret information (key pre-distribution).
 - Often used to transmit session keys.
- Session keys:
 - Short-term key for a particular session only.
 - ► Can be updated frequently to limit amount of ciphertext (encrypted with one key) available to cryptanalyst, and to limit exposure if session key is compromised.

Security protocols

- ► A protocol is a set of rules for exchanging messages between two or more principals/participants over a network.
- Rules cover:
 - Message formats.
 - How to handle the messages on receipt.
 - How messages are interpreted.
- Here we will see how basic cryptographic primitives (encryption, MACs, signatures) can be used to provide security services (authenticated key establishment) over insecure networks.
- ▶ Build on ISO 7498 OSI generic security architecture.

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A secure protocol

In a secure protocol:

- ▶ When acting honestly, principals/participants achieve the stated *aim* of the protocol.
 - Example 1: A authenticates B.
 - Example 2: A and B sets up a fresh session key (with certain assurances).
- Neither a passive eavesdropper nor an active adversary can defeat this objective.
 - ▶ In Example 1: Oscar cannot successfully impersonate B to A.
 - In Example 2: Oscar cannot persuade A and B to reuse an old session key.

The legitimate principals/participants

- Legitimate participants: conventionally called Alice, Bob, Carol, etc.
- In more complex protocols there may be a Trusted Third Party (TTP) who is trusted by the legitimate participants.
 - Depending on the application they may be called Trusted Third Party, Trusted Authority, Trusted Server, Certification Authority, etc.
 - There may be varying levels of trust, for example, trusted to relay messages correctly, trusted to generate keys, trusted to verify identities, etc

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The adversaries: Eve, Mallory, Oscar

There are two kinds of adversaries:

- Eve, a passive adversary, an eavesdropper.
 - Eve can only read sent messages.
- ► *Mallory/Oscar*, an active adversary, who can:
 - view, alter, delete, replay message.
 - inject messages into the network.
 - initiate protocol runs.
 - impersonate a principal in a protocol run.

The adversaries: What Mallory/Oscar can't do (I)

We assume that the underlying cryptographic primitives are secure:

- ► The (pseudo)random number generation is secure:
 - Mallory cannot guess a random number chosen by another principal if it is selected from a sufficiently large space.
- The hash function is secure:
 - Mallory cannot easily find preimages or collisions.

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The adversaries: What Mallory/Oscar can't do (II)

We assume that the underlying cryptographic primitives are secure:

- ▶ The encryption algorithm is secure.
- For example,
 - In a symmetric key cryptosystem, Mallory cannot deduce the key from observing plaintext-ciphertext pairs.
 - In a public key cryptosystem, Mallory cannot deduce the private key from a public key.
- The signature scheme is secure: Mallory cannot deduce the signing key from the public verification key and from observing message-signature pairs.

Summary of assumptions

- ▶ We equip legitimate participants with idealised cryptographic mechanisms.
- Legitimate participants exchange messages over an untrusted communication network.
- ► How then do we use these cryptographic mechanisms to design secure protocols?

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Key establishment

From Handbook of Applied Cryptography:

- Key establishment: process by which a shared secret key becomes available to two or more parties for subsequent cryptographic use.
 - Key distribution: one party chooses a key and transmits it securely to others.
 - Key agreement: the secret key is derived by all parties as a function of inputs by all parties.

Key management

From Handbook of Applied Cryptography:

key

- ► Key management: set of processes and mechanisms which support key establishment and the maintenance of ongoing keying relationships between parties.
 - ► Eg. key generation, distribution, storage, update, destruction etc.

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Entity authentication and key establishment

- Entity authentication can only be achieved for an instant in time.
 - Typically this is established at the start of a connection/session.
- If we want security (confidentiality/integrity) for a whole session we need to establish a session key.
- A session key can be agreed as part of an authentication protocol.
 - ▶ The session key can be bound to that protocol run.
 - This can be done in an authenticated key establishment protocol.

Participants in a key establishment protocol

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- Legitimate participants: Alice, Bob, Carol, etc.
- Trusted parties: Trusted Third Party, Trusted Authority, Trusted Server, Certification Authority, etc.
 - TTP can be online or offline.
 - Can be certification authority, vouching for authenticity of public keys or key generator or key escrow agent etc.
 - Varying levels of trust.
- Adversaries:
 - Can be passive or active, outsider or insider.

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Key establishment protocols

- ► Many different scenarios and methods and models:
 - ► Key pre-distribution: TTP distributes keying information ahead of time securely. Pairs of users can derive secret keys later on.
 - Key transport/distribution: One party creates and transfers the key to other parties.
 - ► Key agreement: Users agree on session key using interactive protocols, maybe based on symmetric-key or public-key schemes. Usually do not require on-line TTP.

Security goals of key establishment protocols

Implicit key authentication:

key

- No one other than specified party may gain access to a key
- Key confirmation:
 - Assurance that second party (possibly unspecified) has actual possession of a key
- Explicit key authentication: both implicit key authentication and key confirmation
- Entity authentication:
 - Assurance of identity and liveness of communicating party

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Other assurances and considerations (I)

- Other assurrances:
 - Key freshness: guarantee that new key is used.
 - Key control: neither party can control/predict key value.
- Other considerations:
 - Efficiency: number of passes and bandwidth, complexity of computations.
 - ► TTP requirement: on-line, off-line, or none; degree of trust.

Other assurances and considerations (II)

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- Security under different attack models:
 - Security if a session key is known?
 - Security if long-term key is known?
- ▶ Perfect forward secrecy: compromise of long-term keys does not affect security of short-term keys before the compromise.

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- Oscar may be a passive adversary and restrict action to eavesdropping.
- Oscar may be an active adversary, and can
 - alter messages, replay recorded messages, masquerade as other users.
- Oscar's objectives?

Example: Session keys

Two parties, Alice and Bob, share a secret long-term key k. Session key establishment:

 \triangleright Alice sends Bob k' in the clear.

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► Session key is $k \oplus k'$.

Weaknesses?

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Example: Key hierarchies

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Two parites, Alice and Bob, share a master key k_M . Session key establishment:

- ▶ Alice sends Bob session key as $e_{k_M}(k_S)$.
- ▶ Bob decrypts and obtain session key k_S .
- Many level hierarchies are possible.
- Weaknesses?

Example: Using TTP

TTP is an agency trusted by all parties.

key

- ► TTP can generate and convey keys.
- Each user has secret key agreed with TTP.
 - ightharpoonup Alice shares secret key k_A with TTP.
 - \triangleright Bob shares secret key k_B with TTP.
- ▶ When Alice and Bob wish to communicate:
 - ightharpoonup TTP generates session key k_S .
 - ▶ TTP sends Alice $e_{k_A}(k_S)$ and Bob $e_{k_B}(k_S)$.
- Weaknesses?

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ISO/IEC 9798 standards (NON-EXAMINABLE)

ISO/IEC 9798, a multi-part standard, specifies a variety of authentication protocol and related key distribution protocols:

- ► ISO/IEC 9798-1: 1997 (2nd edition) General.
- ► ISO/IEC 9798-2: 1999 (2nd edition) Mechanisms using symmetric encipherment algorithms.
- ► ISO/IEC 9798-3: 1998 (2nd edition) Mechanisms using digital signature techniques.
- ▶ ISO/IEC 9798-4: 1999 (2nd edition) Mechanisms using a cryptographic check function.
- ► ISO/IEC 9798-5: 1999 Mechanisms using using zero knowledge techniques.

Key pre-distribution

- TTP distribute keying information securely ahead of time.
 - Preload keys/keying material on to devices in controlled environment before deployment.
- Pairs of users later determine key from keying information.
- Evaluation criteria:
 - How much information to be transmitted securely,
 - How much information to be stored securely,
 - Others: how much information to be published or broadcast, how much computation to be performed by TTP and users.

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Examples of key pre-distribution

- A trivial example: for each pair of users U, V, TTP chooses random key K_{UV} and transmit it securely to U and V.
 - Strength and weaknesses?
- Example: Preloaded keys in SIMs on mobile phones.
- Example: Set top boxes for digital TV services.
- Issues:
 - Keeping track of device ownerships.
 - Post deployment key management.

Key distribution protocols

key

- One party (could be TTP) chooses a session key and securely transfers it to the others.
- Many different scenario possible:
 - Using symmetric key cryptosystems only, or PKC only, or a hybrid.
 - ▶ Different levels of involvement of TTP and trust in TTP.
 - Different levels of input to the session key.

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Authenticated key establishment: symmetric key techniques

- Simple example using symmetric key cryptosystems and time-stamps:
 - \triangleright A and B share a long-term key K.
 - ightharpoonup A
 ightarrow B: $e_K(t||i_B||K_s)$
 - ightharpoonup t is a time stamp, i_B is an identifier for B, and K_s is a session key.
 - A is authenticated to B and they now share a secret session key K_s .
- Implicit key authentication: No one other than B (and A) may gain access to K_s .

Authenticated key establishment: public key techniques

- \triangleright A checks the authenticity of B's public key PK_B .
- ightharpoonup A
 ightharpoonup B: $e_{PK_R}(K_s)$.

key

 \triangleright Subsequent messages are encrypted or authenticated using K_s (or keys derived from K_s):

$$B o A$$
: data, $MAC_{K_s}(data)$

- Assurances?
 - A is not authenticated to B.
 - B is authenticated to A if subsequent messages are correctly encrypted/authenticated using K_s .
 - Explicit key authentication if subsequent messages are correct: only B (and A) could have K_s and B does actually have K_s .

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Key pre-distribution **Key distribution**

Key transport protocol using TTP

- ► The "wide-mouthed frog protocol":
- ightharpoonup Alice shares a key K_{AT} with TTP.
- ▶ Bob shares a key K_{BT} with TTP.
- If Alice and Bob wish to communicate, then Alice chooses session key K_{AB} and TTP transfers it to Bob securely.
 - Alice o TTP $e_{K_{AT}}(t_A|ID_B|K_{AB})$ $\mathsf{TTP} o \mathsf{Bob} \quad e_{\mathsf{K}_{\mathsf{RT}}}(t_T|\mathit{ID}_{\mathsf{A}}|\mathsf{K}_{\mathsf{AB}})$
- Security?

Kerberos

- ► Kerberos is a TTP-aided authentication protocol.
 - ► Can achieve mutual authentication and key establishment.
- ► The name also refers to software implementing that protocol, currently Kerberos V5 Release 1.2.
- ▶ Also the name of a project at MIT which devised the protocols (properly called Project Athena).
- ▶ Standardised in RFC 1510 Kerberos V5 (1992).
- Version of Kerberos incorporated in Windows and used in many versions of Unix

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Kerberos: Principals

- Authentication of Client (C) to Server (S) done as a two-stage process.
- Authentication Server (AS)

- Mutual authentication with Client at login based on a shared long-term secret.
- Gives client ticket granting ticket and a short-term key for use between Ticket Granting Server and Client.
- ► Ticket Granting Server (TGS)
 - Performs mutual authentication with Client based on the short-term key and ticket granting ticket.
 - ► The TGS then issues tickets giving Client access to further Servers that demand authentication.

Kerberos: Motivation

- ► Two TTPs: Authentication Server (AS) and Ticket Granting Server (TGS)
 - ➤ A user only needs to load their long-term secret key (shared with AS) into the client host for the minimum time.
 - Once the short-term key is established (with TGS) this long-term secret key can be erased from the client host.
- ▶ All further client interactions are with TGS and servers.
- ► This minimises the risk of exposure of the long-term secret key.

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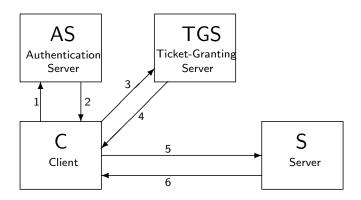
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Kerberos: Information flow I



Kerberos: Information flow II

key

- Messages 1 and 2 are exchanged between the client C and the authentication server AS.
 - ► They derive a short term key to use with the TGS in messages 3 and 4.
- Messages 3 and 4 are exchanged between the client C and the ticket-granting server TGS (using the short-term key provided by the AS).
 - ► They derive a short term key to use with the server in messages 5 and 6.
 - ▶ This can be repeated without repeating messages 1 and 2.
- Messages 5 and 6 are exchanged between the client C and server S (using a key provided by the TGS).
 - ► This can be repeated without repeating messages 3 and 4.

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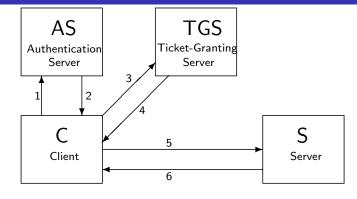
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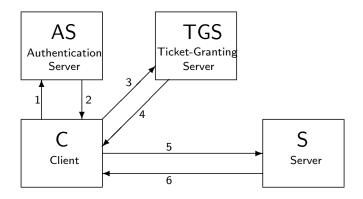
Kerberos: Messages 1 and 2



- ► C and AS share long-term key $K_{AS,C}$ derived from C's password.
- \triangleright C and AS use $K_{AS,C}$ to mutually authenticate one another.
- ▶ C and AS derive a short-term key $K_{C,TGS}$ and a ticket-granting ticket to be used with TGS in messages 3, 4.

Kerberos: Messages 3 and 4

key



- C presents the ticket-granting ticket from AS to TGS.
- ▶ They mutually authenticate each other using $K_{C,TGS}$.
- ▶ They derive a session key $K_{C,S}$ and a (session-granting) ticket to be used with the Server S in messages 5, 6.

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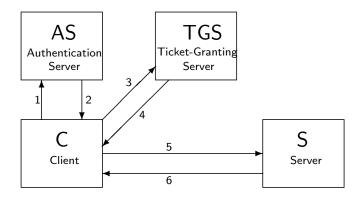
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Kerberos: Messages 5 and 6



- C presents the session granting ticket to S.
- \triangleright S authenticates C using $K_{C,S}$.
- Optionally, S can send C another message to authenticate itself to C.

Kerberos: Notation

ix	Identifier of principal X.
N_C, N'_C	Nonces generated by the client C.
$K_{AS,C}$	Long term secret key shared by AS and C.
$K_{AS,TGS}$	Long term secret key shared by AS and TGS.
$K_{TGS,S}$	Long term secret key shared by TGS and S.
$K_{C,TGS}$	Short term secret key shared by C and TGS.
$K_{C,S}$	Short term secret key shared by the C and S.
T_1 , T_2	Time-stamps.
L, L'	Life time, specifying validity period of a key.
$e_K()$	Encryption using symmetric cryptosystem with key K .

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Kerberos simplified message format: Messages 1, 2

1. $C \rightarrow AS$: $i_C ||i_{TGS}||L||N_C$

key

2. AS \rightarrow C: $i_C || \underbrace{e_{\mathcal{K}_{AS,TGS}}(\mathcal{K}_{C,TGS}||i_C||L)}_{||e_{\mathcal{K}_{AS,C}}(\mathcal{K}_{C,TGS}||\mathcal{N}_C||L||i_{TGS})}$

Ticket-granting ticket

- ightharpoonup C and AS use $K_{AS,C}$ derived from client password to authenticate one another.
- ▶ They derive a short-term key $K_{C,TGS}$, and a ticket-granting ticket to allow C to talk to TGS in messages 3 and 4.
- ▶ The ticket includes $K_{C,TGS}$ and ticket lifetime L encrypted under longterm key $K_{AS,TGS}$.

Kerberos simplified message format: Messages 3, 4

3.
$$C \to TGS$$
: $i_S||L||N'_C||e_{K_{AS,TGS}}(K_{C,TGS}||i_C||L)||e_{K_{C,TGS}}(i_C||T_1)$
4. $TGS \to C$: $i_C||\underbrace{e_{K_{TGS,S}}(K_{C,S}||i_C||L')}_{Session-granting ticket for S}||e_{K_{C,TGS}}(K_{C,S}||N'_C||L'||i_S)$

- ▶ C presents request for access to server S along with ticket granting ticket and a message authenticating C to TGS (Message 3).
- ▶ TGS checks validity and lifetime of ticket granting ticket and extracts $K_{C,TGS}$. TGS can now authenticate the Client.
- ▶ If all OK, TGS issues session key $K_{C,S}$ and session-granting ticket to C. (Default validity is 5 minutes.)
- ► TGS also authenticates itself to C (Message 4).

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Kerberos simplified message format: Messages 5, 6

- 5. $C \rightarrow S$: $e_{K_{TGS,S}}(K_{C,S}||i_C||L')||e_{K_{C,S}}(i_C||T_2)$
- 6. $S \rightarrow C$: $e_{K_{C,S}}(T_2)$
- ► C presents session-granting ticket along with a message authenticating C to S (Message 5).
- ▶ S checks validity and lifetime of session-granting ticket and extracts session key $K_{C,S}$. S can now authenticate C.
- ▶ If all OK, S grants access to C.

key

Optionally, S sends C a message authenticating S to C (Message 6).

Kerberos: Use of cryptography

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- Kerberos uses symmetric encryption and Manipulation Detection Codes (MDC).
- ► The MDC is computed on the data to be encrypted, and then the concatenation of the MDC with the data is encrypted.
- Specifically, Kerberos version 5 (as originally in RFC 1510) uses DES and MD4 or MD5.
- Release 1.2 of Kerberos Version 5 implements triple DES (3DES).

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Kerberos issues I

- Revocation: ticket granting tickets valid until they expire, typically 10 hours.
- Within realms (domains): long-term keys need to be established between AS and TGS, TGS and Servers and AS and clients.
- Synchronous clocks are needed, and must be protected against attacks.
- Cache of recent messages to protect against replay.

Kerberos issues II

- ► AS and TGS must be trusted by clients not to eavesdrop.
 - Can be extended to include keying material to establish additional secret not chosen by AS or TGS.
- Client-AS long-term key often still based on password entry vulnerable to guessing.
- ► Short-term keys and ticket granting tickets located on largely unprotected client hosts.
- Denial of service possible? E.g. on the clock service or on the TGS.

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Kerberos and Windows network authentication

- Microsoft has adopted and extended Kerberos to provide network authentication in Windows.
- One extension: support for public key encryption to protect client/AS messages (rather than password-based long-term key).
- Second extension: use Kerberos (normally empty) data authorisation field to transmit access privileges.
- Message formats proprietary to Microsoft.
- ► Non-standard extension to Kerberos makes it hard to interoperate Microsoft & non-Microsoft implementations.

Key agreement protocols

- ► Key agreement: secret key derived by all parties as a function of inputs by all parties.
 - May or may not involve a TTP.
- Diffie-Hellman key exchange:
 - Allow two parties who have not met in advance or shared keying material to establish shared secret by public exchange of message.
 - First practical solution.

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Diffie-Hellman key exchange STS protocol

Diffie-Hellman key exchange

- Public information: prime p and primitive element α .
- ▶ Alice chooses secret x_A at random $(0 \le x_A \le p 2)$.
 - Alice sends $y_A = \alpha^{x_A} \mod p$ to Bob.
- ▶ Bob chooses secret x_B at random $(0 \le x_B \le p 2)$.
 - ▶ Bob sends $y_B = \alpha^{x_B} \mod p$ to Alice.
- ▶ Alice calculates $k = y_B^{x_A} = \alpha^{x_A x_B} \mod p$.
- ▶ Bob calculates $k = y_A^{x_B} = \alpha^{x_A x_B} \mod p$.

Example: Diffie-Hellman key exchange

Public information: prime p = 59, primitive element $\alpha = 2$.

Alice chooses secret key	Bob chooses secret key
$x_{A} = 13$	$x_B = 41$
Alice calculates y_A :	Bob calculates <i>y_B</i> :
$y_A = 2^{13} = 50 \mod 59$	$y_B = 2^{41} = 34 \mod 59$
	$\xrightarrow{\mathcal{Y}A}$
	$\stackrel{y_B}{\leftarrow}$
Alice calculates $y_B^{x_A}$	Bob calculates $y_A^{x_B}$
$y_B^{x_A} = 34^{13} = 42 \mod 59$	$y_A^{x_B} = 50^{41} = 42 \mod 59$

Agreed secret value k = 42.

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The Diffie-Hellman problem

- Outsider knows p and α , $y_A = \alpha^{X_A} \mod p$, $y_B = \alpha^{X_B} \mod p$.
 - ▶ Determine $k = \alpha^{X_A X_B} \mod p$ from this information.
- ▶ Diffie-Hellman problem: Given prime p, primitive element α :
 - Given α^{x_A} mod p and α^{x_B} mod p.
 - Find $\alpha^{x_A x_B} \mod p$.
- **Example:** Prime p = 59, primitive element $\alpha = 2$
 - Given $2^{x_A} = 47 \mod 59$, $2^{x_B} = 33 \mod 59$, find $2^{x_A x_B} \mod 59$
- ▶ Diffie-Hellman problem believed to be hard.

The Diffie-Hellman problem and the discrete log problem

- ► The discrete log problem:
 - Prime p and primitive element α .
 - ▶ Given $\beta \in \mathbb{Z}_p$, find integer a ($0 \le a \le p-2$) such that $\beta = \alpha^a \mod p$.
- Can try to calculate x_A from α^{x_A} mod p the discrete log problem.
 - Solution to discrete logarithm gives solution to Diffie-Hellman problem.

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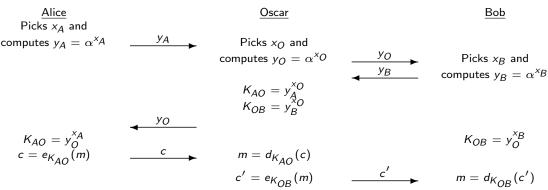
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Authentication in Diffie-Hellman key exchange

- ▶ Diffie-Hellman key exchange does not provide entity or key authentication.
 - subject to intruder-in-the-middle attacks:



Station-to-station (STS) protocol

- Public information: prime p, primitive element α .
- ▶ User U: signature generation function S_U , signature verification algorithm V_U certified by TTP.
 - 1 Alice \rightarrow Bob $y_A = \alpha^{x_A} \mod p$
 - 2 Bob \rightarrow Alice $y_B = \alpha^{x_B} \mod p$, $e_K(S_A(y_B||y_A))$
 - 3 Alice o Bob $e_K(S_B(y_A||y_B))$
- $K = \alpha^{X_A X_B} \mod p$ can be calculated by Bob after the first message, and Alice after the second message.
- Achieves key agreement, mutual entity authentication, explicit key authentication.