

Literature Review

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Smoothed Particle Hydrodynamics (SPH) is a Lagrangian simulation method first proposed independently by L.B. Lucy and R.A. Gingold and J.J. Monaghan to simulate stars[4][8]. J.J. Monaghan later extended the method to free surface flows[9]. Refer to Ting Ye, et al. for a modern review of various advances in the method.

Mathieu Desbrun and Marie-Paule Gascuel applied the Courant-Friedrichs-Lewy criterion to SPH, providing an upper bound on the time step based on the kernel support size and the maximum particle velocity[3]. This means that in practice the time step must often be very small in order for the simulation to remain stable. Predictive Corrective Incompressible SPH (PCISPH) attempts to address this problem for incompressible fluids such as water, where the problem is exacerbated by the high stiffness required in the equation of state (EOS)[11].

Another approach is to avoid a global time-step altogether. Prashant Goswami and Christopher Batty propose segmenting the time-step by spatial chunks.[5]. Asynchronous SPH allows every particle to have its own time frame[10][2][3].

Much research has been done to bring SPH to the GPU. Much of the difficulty lies in efficiently searching a fixed distance neighborhood of each particle, since a brute force search of every particle pair is infeasible. The work of Ihmsen et al. provided much of the groundwork with an early parallel implementation.[7] For this search they used a Z-index sort. Amada et al. present a partial GPU implementation which relies on the CPU for the neighborhood search, providing the information to the GPU as a texture.[1] Harada et al. present an early GPU implementation[6].

References

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