```
In [13]: set_default_plot_size(15cm, 15cm)
                                                                      U_A = x_1^A x_2^A \qquad U_B = x_1^B x_2^B
In [14]: U_A(x1, x2) = x1*x2
              U_B(x1, x2) = (\omega 1-x1)*(\omega 2-x2);
In [15]: plot_U_A(x,x1,x2) = U_A(x1, x2)/x
              plot_U_B(x,x_1,x_2) = U_B(x_1, x_2)/(x-\omega_1)+\omega_2;
In [19]:
              \omega 1 = 10
              \omega 2 = 20
              @manipulate for x1 in 1:\omega1-1, x2 in 1:\omega2-1
                    domain = linspace(0, \omega1, 1000)
                    plot(
                           layer(x=[x1], y=[x2], Geom.point, Theme(default_color=colorant"black")),
                          layer(x=domain, y=plot_U_A(domain, x1, x2), Geom.line, Theme(default_color=colorant"blacklayer(x=domain, y=plot_U_B(domain, x1, x2), Geom.line, Theme(default_color=colorant"blacklayer(x=domain, y=2*domain, Geom.line, Theme(default_color=colorant"blacklayer(x=domain, y=2*domain, Geom.line, Theme(default_color=colorant"black")),
                           # Setup
                          Coord.Cartesian(xmin=0,xmax=ω1,ymin=0,ymax=ω2,fixed=true),
                           Guide.xlabel("Good 1"),
                           Guide.ylabel("Good 2")
              end
```

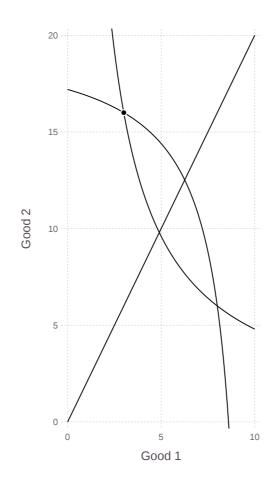
Out[19]:

In [10]: **using** Gadfly

using Interact

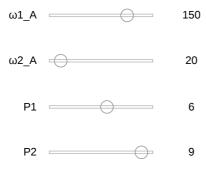
x1 —

x2



Add Prices

```
B_{\text{line}}(x, \omega_1A, \omega_2A, P_1, P_2) = -(P_1/P_2)*x + (P_1*\omega_1A + P_2*\omega_2A)/P_2;
In [20]:
                 \omega 1 = 210
                  \omega 2 = 210
                  @manipulate for \omega1_A in 0:10:\omega1-1, \omega2_A in 0:10:\omega2-1, P1 in 1:10, P2 in 1:10
                          domain = linspace(0, \omega1, 1000)
                          plot(
                                  # Initial State
                                  layer(x=[\omega1_A], y=[\omega2_A], Geom.point),
                                  layer(x=domain, y=plot_U_A(domain, ω1_A, ω2_A), Geom.line),
                                  layer(x=domain, y=plot_U_B(domain, ω1_A, ω2_A), Geom.line),
                                  layer(x=domain, y=domain, Geom.line, Theme(default color=colorant"black")),
                                  # Exchange
                                  layer(x=[B_x1(\omega_1_A, \omega_2_A, P1, P2)], y=[B_x2(\omega_1_A, \omega_2_A, P1, P2)], Geom.point, Theme(default)
                                  \label{eq:layer} \begin{split} &\text{layer}(\text{x=}[\omega\text{1-B}\_\text{x1}(\omega\text{1-}\omega\text{1}\_\text{A},\ \omega\text{2-}\omega\text{2}\_\text{A},\ \text{P1},\ \text{P2})],\ \text{y=}\omega\text{2-}[\text{B}\_\text{x2}(\omega\text{1-}\omega\text{1}\_\text{A},\ \omega\text{2-}\omega\text{2}\_\text{A},\ \text{P1},\ \text{P2})],\ \text{Geom.} \\ &\text{layer}(\text{x=}\text{domain},\ \text{y=}\text{B}\_\text{line}(\text{domain},\ \omega\text{1}\_\text{A},\ \omega\text{2}\_\text{A},\ \text{P1},\ \text{P2}),\ \text{Geom.} \\ &\text{line},\ \text{Theme}(\text{default}\_\text{color=color}) \end{split}
                                  layer(x=domain, y=plot_U_A(domain, B_x1(\omega1_A, \omega2_A, P1, P2), B_x2(\omega1_A, \omega2_A, P1, P2)), (layer(x=domain, y=plot_U_B(domain, \omega1-B_x1(\omega1-\omega1_A, \omega2-\omega2_A, P1, P2), \omega2-B_x2(\omega1-\omega1_A, \omega2
                                  # Setup
                                  Coord.Cartesian(xmin=0,xmax=ω1,ymin=0,ymax=ω2,fixed=true),
                                  Guide.xlabel("Good 1"),
                                  Guide.ylabel("Good 2")
                  end
                 4
```



In [17]: $B_x1(\omega_1A, \omega_2A, P1, P2) = (P1*\omega_1A+P2*\omega_2A)/(2P1)$

 $B_x^2(\omega_1^A, \omega_2^A, P_1, P_2) = (P_1^*\omega_1^A + P_2^*\omega_2^A)/(2P_2)$

Out[20]:

