

In [43]: **using** Gadfly  
**using** Interact

In [2]: set\_default\_plot\_size(15cm, 15cm)

$$U_A = x_1^A x_2^A \quad U_B = x_1^B x_2^B$$

In [3]: U\_A(x1, x2) = x1\*x2  
U\_B(x1, x2) = (ω1-x1)\*(ω2-x2);

In [4]: plot\_U\_A(x,x1,x2) = U\_A(x1, x2)/x  
plot\_U\_B(x,x1,x2) = U\_B(x1, x2)/(x-ω1)+ω2;

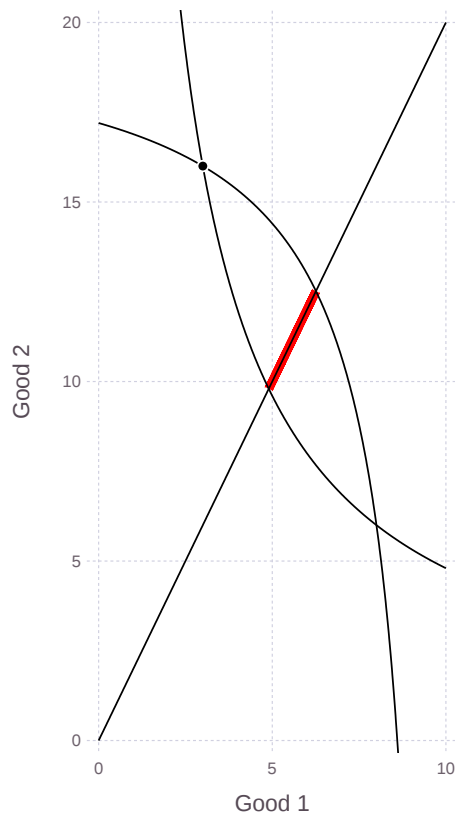
In [41]: ω1 = 10  
ω2 = 20

```
@manipulate for x1 in 1:ω1-1, x2 in 1:ω2-1
  domain = linspace(0, ω1, 1000)
  lower_intercept = (U_A(x1, x2)/2)^(1/2)
  upper_intercept = (2ω1+ω2-((2ω1+ω2)^2-8*(ω1*ω2-U_B(x1,x2)))^(1/2))/4
  plot(
    # Initial State
    layer(x=[x1], y=[x2], Geom.point, Theme(default_color=colorant"black")),
    layer(x=domain, y=plot_U_A(domain, x1, x2), Geom.line, Theme(default_color=colorant"black")),
    layer(x=domain, y=plot_U_B(domain, x1, x2), Geom.line, Theme(default_color=colorant"black")),
    layer(x=domain, y=2*domain, Geom.line, Theme(default_color=colorant"black")),
    # Core
    layer(x=linspace(lower_intercept, upper_intercept, 1000), y=2*linspace(lower_intercept, upper_int
    # Setup
    Coord.Cartesian(xmin=0,xmax=ω1,ymin=0,ymax=ω2,fixed=true),
    Guide.xlabel("Good 1"),
    Guide.ylabel("Good 2")
  )
end
```

x1  3

x2  16

Out[41]:



# Add Prices

```
In [6]: B_x1(ω1_A, ω2_A, P1, P2) = (P1*ω1_A+P2*ω2_A)/(2P1)
B_x2(ω1_A, ω2_A, P1, P2) = (P1*ω1_A+P2*ω2_A)/(2P2)
B_line(x, ω1_A, ω2_A, P1, P2) = -(P1/P2)*x+(P1*ω1_A+P2*ω2_A)/P2;
```

```
In [42]: ω1_A = 210
ω2_A = 210

manipulate for ω1_A in 0:10:ω1-1, ω2_A in 0:10:ω2-1, P1 in 1:10, P2 in 1:10
    domain = linspace(0, ω1, 1000)
    lower_intercept = (U_A(ω1_A, ω2_A))^(1/2)
    upper_intercept = (ω1+ω2-((ω1+ω2)^2-4*(ω1*ω2-U_B(ω1_A, ω2_A)))^(1/2))/2
    plot(
        # Initial State
        layer(x=[ω1_A], y=[ω2_A], Geom.point),
        layer(x=domain, y=plot_U_A(domain, ω1_A, ω2_A), Geom.line),
        layer(x=domain, y=plot_U_B(domain, ω1_A, ω2_A), Geom.line),
        layer(x=domain, y=domain, Geom.line, Theme(default_color=colorant"black")),
        # Core
        layer(x=linspace(lower_intercept, upper_intercept, 1000), y=linspace(lower_intercept, upper_intercept, 1000), Geom.line),
        # Exchange
        layer(x=[B_x1(ω1_A, ω2_A, P1, P2)], y=[B_x2(ω1_A, ω2_A, P1, P2)], Geom.point, Theme(default_color=colorant"red")),
        layer(x=[ω1-B_x1(ω1-ω1_A, ω2-ω2_A, P1, P2)], y=[ω2-B_x2(ω1-ω1_A, ω2-ω2_A, P1, P2)], Geom.point, Theme(default_color=colorant"red")),
        layer(x=domain, y=B_line(domain, ω1_A, ω2_A, P1, P2), Geom.line, Theme(default_color=colorant"black")),
        layer(x=domain, y=plot_U_A(domain, B_x1(ω1_A, ω2_A, P1, P2), B_x2(ω1_A, ω2_A, P1, P2)), Geom.line, Theme(default_color=colorant"red")),
        layer(x=domain, y=plot_U_B(domain, ω1-B_x1(ω1-ω1_A, ω2-ω2_A, P1, P2), ω2-B_x2(ω1-ω1_A, ω2-ω2_A, P1, P2)), Geom.line, Theme(default_color=colorant"red")),
        # Setup
        Coord.Cartesian(xmin=0,xmax=ω1,ymin=0,ymax=ω2,fixed=true),
        Guide.xlabel("Good 1"),
        Guide.ylabel("Good 2")
    )
```

id

ω1\_A  30

ω2\_A  170

P1  8

P2  5

Out[42]:

