

Dependencies

```
In [7]: using Interact
        using Gadfly
        using CSV
```

```
In [2]: set_default_plot_size(20cm, 20cm)
```

Functions

```
In [3]: function Plot_estimates(x, y, xaxis, yaxis)
        X = [ones(x) x]
        β = inv(transpose(X)*X)*transpose(X)*y
        SST = sum(transpose(y-mean(y))*(y-mean(y)))
        SSE = sum(transpose(X*β-mean(y))*(X*β-mean(y)))
        SSR = sum(transpose(y-X*β)*(y-X*β))
        R_squared = SSE/SST
        p = plot(
            layer(x = x, y = y, Geom.point),
            layer(x = x, y = X*β, Geom.line),
            Guide.xlabel(xaxis),
            Guide.ylabel(yaxis),
            Guide.title(join(["β₀, β₁ = (", string(round(β[1], 2)), ", ", string(round(β[2], 2))
        )
        return p
    end
```

Out[3]: Plot_estimates (generic function with 1 method)

```
In [4]: function Model_Regression(x_values, y_values)

        # Plots
        plot_linlin = Plot_estimates(x_values, y_values, "x", "y")
        plot_linlog = Plot_estimates(x_values, log.(y_values), "x", "log(y)")
        plot_loglin = Plot_estimates(log.(x_values), y_values, "log(x)", "y")
        plot_loglog = Plot_estimates(log.(x_values), log.(y_values), "log(x)", "log(y)")

        title(gridstack([plot_linlin plot_linlog; plot_loglin plot_loglog]), "Regression Plots")

    end
```

Out[4]: Model_Regression (generic function with 1 method)

Engel Example

```
In [5]: # y
        dairy = [8.87, 6.59, 11.46, 15.07, 15.6, 6.71, 10.02, 7.41, 11.52, 7.47, 6.73, 8.05, 11.03, 16.05, 10.05, 10.05, 10.05, 10.05, 10.05, 10.05]
        # x
        inc_per_capita = [1250, 985, 2175, 1025, 1690, 670, 1600, 940, 1730, 640, 860, 960, 1575, 1236, 1236, 1236, 1236, 1236, 1236, 1236]
```

Problem:

$$\hat{\mathbf{y}} = \hat{\beta}_0 + \hat{\beta}_1 \cdot x = \mathbf{X}\hat{\beta}$$

With:

$$\hat{\beta} = (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{y}$$

Where:

$$\mathbf{X} = \begin{bmatrix} 1 & incpercapita_1 \\ \dots & \dots \\ 1 & incpercapita_n \end{bmatrix}$$

```
In [6]: Model_Regression(inc_per_capita, dairy)
```

Out[6]:

