

$$W := \text{Matrix}([[-1, 0, -1], [-1, -1, 0], [0, 1, 1]])$$

$$W := \begin{bmatrix} -1 & 0 & -1 \\ -1 & -1 & 0 \\ 0 & 1 & 1 \end{bmatrix} \quad (1)$$

$$T := \text{Matrix}([[x2 - x1, x3 - x1, x4 - x1], [y2 - y1, y3 - y1, y4 - y1], [z2 - z1, z3 - z1, z4 - z1]])$$

$$T := \begin{bmatrix} x2 - x1 & x3 - x1 & x4 - x1 \\ y2 - y1 & y3 - y1 & y4 - y1 \\ z2 - z1 & z3 - z1 & z4 - z1 \end{bmatrix} \quad (2)$$

$$F := \text{Matrix}([[1, 1, 1], [-1, 0, 0], [0, -1, 0]])$$

$$F := \begin{bmatrix} 1 & 1 & 1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{bmatrix} \quad (3)$$

$$A := T \cdot (W^{-1})$$

$$A := \left[\left[\begin{aligned} &-\frac{x2}{2} + \frac{x1}{2} + \frac{x3}{2} - \frac{x4}{2}, & -\frac{x2}{2} + \frac{x1}{2} \\ &-\frac{x3}{2} + \frac{x4}{2}, & -\frac{x2}{2} - \frac{x1}{2} + \frac{x3}{2} + \frac{x4}{2} \end{aligned} \right], \right. \\ \left[\begin{aligned} &-\frac{y2}{2} + \frac{y1}{2} + \frac{y3}{2} - \frac{y4}{2}, & -\frac{y2}{2} + \frac{y1}{2} - \frac{y3}{2} \\ &+ \frac{y4}{2}, & -\frac{y2}{2} - \frac{y1}{2} + \frac{y3}{2} + \frac{y4}{2} \end{aligned} \right], \\ \left[\begin{aligned} &-\frac{z2}{2} + \frac{z1}{2} + \frac{z3}{2} - \frac{z4}{2}, & -\frac{z2}{2} + \frac{z1}{2} - \frac{z3}{2} \\ &+ \frac{z4}{2}, & -\frac{z2}{2} - \frac{z1}{2} + \frac{z3}{2} + \frac{z4}{2} \end{aligned} \right] \right] \quad (4)$$

$$X := \text{Vector}([x], [y], [z])$$

$$X := \begin{bmatrix} x \\ y \\ z \end{bmatrix} \quad (5)$$

$$f := A \cdot X$$

$$f := \left[\left(-\frac{x2}{2} + \frac{x1}{2} + \frac{x3}{2} - \frac{x4}{2} \right) x + \left(-\frac{x2}{2} \right. \right. \quad (6)$$

$$\begin{aligned}
& + \frac{x1}{2} - \frac{x3}{2} + \frac{x4}{2} \Big) y + \Big(-\frac{x2}{2} - \frac{x1}{2} + \frac{x3}{2} \\
& + \frac{x4}{2} \Big) z \Big], \\
& \Big[\Big(-\frac{y2}{2} + \frac{y1}{2} + \frac{y3}{2} - \frac{y4}{2} \Big) x + \Big(-\frac{y2}{2} + \frac{y1}{2} \\
& - \frac{y3}{2} + \frac{y4}{2} \Big) y + \Big(-\frac{y2}{2} - \frac{y1}{2} + \frac{y3}{2} \\
& + \frac{y4}{2} \Big) z \Big], \\
& \Big[\Big(-\frac{z2}{2} + \frac{z1}{2} + \frac{z3}{2} - \frac{z4}{2} \Big) x + \Big(-\frac{z2}{2} + \frac{z1}{2} \\
& - \frac{z3}{2} + \frac{z4}{2} \Big) y + \Big(-\frac{z2}{2} - \frac{z1}{2} + \frac{z3}{2} \\
& + \frac{z4}{2} \Big) z \Big] \Big]
\end{aligned}$$

$$J := \text{VectorCalculus}[\text{Jacobian}](f, [x, y, z])$$

$$J := \left[\left[-\frac{x2}{2} + \frac{x1}{2} + \frac{x3}{2} - \frac{x4}{2}, -\frac{x2}{2} + \frac{x1}{2} \right. \right. \quad (7)$$

$$\begin{aligned}
& -\frac{x_3}{2} + \frac{x_4}{2}, -\frac{x_2}{2} - \frac{x_1}{2} + \frac{x_3}{2} + \frac{x_4}{2} \Big], \\
& \left[-\frac{y_2}{2} + \frac{y_1}{2} + \frac{y_3}{2} - \frac{y_4}{2}, -\frac{y_2}{2} + \frac{y_1}{2} - \frac{y_3}{2} \right. \\
& \left. + \frac{y_4}{2}, -\frac{y_2}{2} - \frac{y_1}{2} + \frac{y_3}{2} + \frac{y_4}{2} \right], \\
& \left[-\frac{z_2}{2} + \frac{z_1}{2} + \frac{z_3}{2} - \frac{z_4}{2}, -\frac{z_2}{2} + \frac{z_1}{2} - \frac{z_3}{2} \right. \\
& \left. + \frac{z_4}{2}, -\frac{z_2}{2} - \frac{z_1}{2} + \frac{z_3}{2} + \frac{z_4}{2} \right] \Big]
\end{aligned}$$