

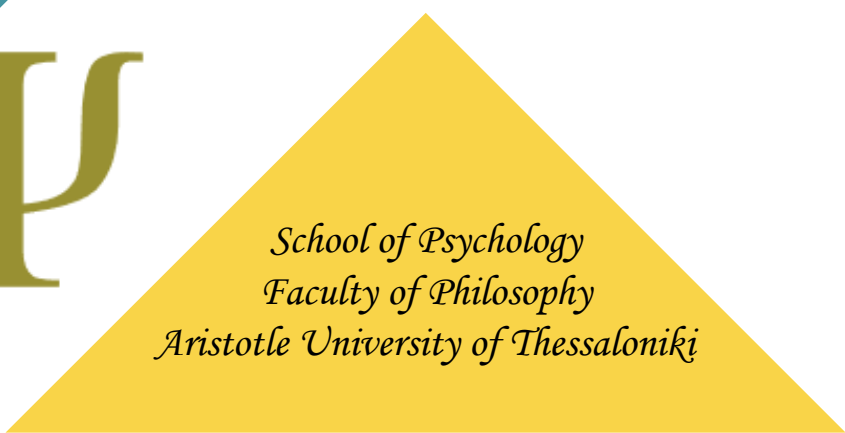


# **One-way Analysis of Variance (ANOVA)**

***Within-subjects designs***

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# Έλεγχος υποθέσεων-Βήματα

1. Καθορίζεται η **μηδενική υπόθεση**  $H_0$  ( = ) και **εναλλακτική υπόθεση**  $H_1$  ( ≠ ) .
2. Ορίζεται το **επίπεδο σημαντικότητας**  $\alpha$  (συνήθως  $\alpha=0.05$ ).
3. Επιλέγεται μια κατάλληλη **στατιστική δοκιμασία** και υπολογίζεται η τιμή του στατιστικού με βάση τα δεδομένα του δείγματος.
4. Σύγκριση της **πιθανότητας**  $p$  να έχουμε την συγκεκριμένη τιμή του στατιστικού (ή κάτι πιο ακραίο) θεωρώντας ότι ισχύει η  $H_0$ , με το **επίπεδο σημαντικότητας**  $\alpha$  (0.05). Στατιστικά σημαντικό αποτέλεσμα ( $p < 0.05$ ).
5. **Ερμηνεία** αποτελεσμάτων.

# One-way within-subjects ANOVA

ANOVA: Y = numeric variable → **Dependent**

X = categorical (factor) variable (>2 levels) → **Independent**

Each subject is exposed to all levels of the independent variable.

**NOTE:** If categorical variable has only 2 related samples: paired t-test

## EXAMPLE

A study investigated the effect of a drug on symptom intensity in a specific disease, assessing eight patients before (two pre-test baseline measures) and after treatment (three post-test measures). The primary question is whether the mean symptom intensity score changed over time.

Y: Symptom intensity in a specific disease (0-12)

X: Follow-up time (five time points: 1 month and 1 week before treatment, 1 week, 1 month, 1 year after treatment)

# One-way within-subjects ANOVA: hypotheses

$H_0$ : The means of all the **related** groups are equal ( $\mu_1 = \mu_2 = \mu_3 = \mu_4 = \mu_5$ ).

$H_1$ : At least one mean differs from the other

- doesn't say how or which ones differ.
- Can follow up with “post-hoc tests”

# Assumptions of one-way within-subjects ANOVA

- **Within-subjects design** (each participant is exposed to all levels of the independent variable)
- **Normality:** The outcome variable (symptom intensity in our example) must be normally distributed in each group (here five time points: 2 baseline and 3 after treatment measurements).

Check this by looking at histograms, Q-Q plots, and Shapiro-Wilk test:

If  $P > 0.05$  then normal distribution

If  $P < 0.05$  then non-normal distribution

- **Sphericity assumption:** The variances of the differences between all possible pairs of within-subject conditions are equal.

Check sphericity with the Mauchly's sphericity test

If  $P > 0.05$  then ANOVA

If  $P < 0.05$  then ANOVA with corrected df (Greenhouse-Geisser (GGe), or Huynh-Feldt (HFe))

# DATA

Factor levels →	Follow-up time					Sum
	1 month before	1 week before	1 week after	1 month after	1 year after	
S1	12	10	5	5	5	41
S2	9	10	6	5	5	35
S3	9	10	5	6	6	35
S4	8	10	4	4	4	28
S5	8	10	4	5	5	32
S6	9	10	6	7	7	40
S7	12	10	7	5	4	38
S8	6	7	5	7	5	30
Sum	73	72	51	42	41	
Mean	9.13	9.00	6.38	5.25	5.13	

symptom  
intensity  
scores

# DATA

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Between  
subjects  
(residuals)

## DATA

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Mean	9.13	9.00	6.38	5.25	5.13	

Within subjects: time  
Treatment effect



## DATA

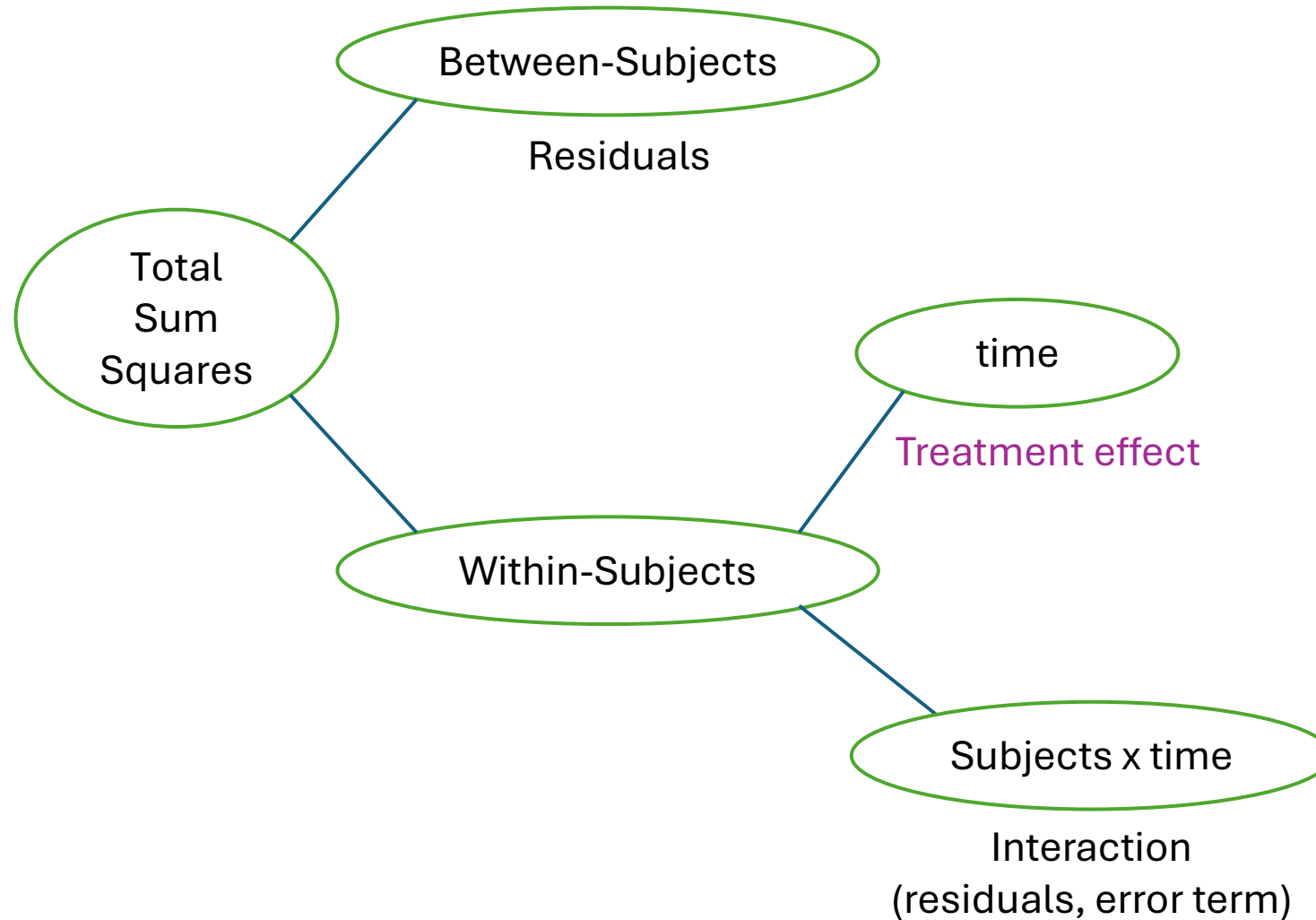
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Within subjects: subjects x time

Interaction  
(residuals, error term)

# One-way within- subjects ANOVA

## Partitioning the total variance into its sources



# Repeated ANOVA table

## Within Subjects Effects

	Sphericity Correction	Sum of Squares	df	Mean Square	F	p	$\eta^2$	$\eta^2_p$
time	Greenhouse-Geisser	123.850	1.951	63.483	18.624	< .001	0.616	0.727
Residual	Greenhouse-Geisser	46.550	13.657	3.409				

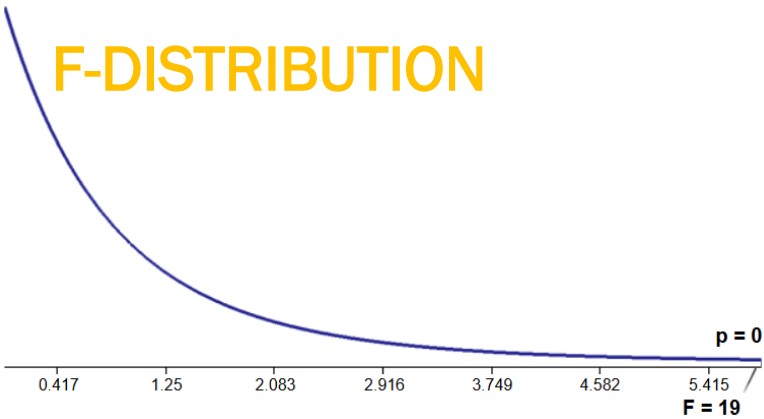
Note. Type 3 Sums of Squares

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## Between Subjects Effects

	Sum of Squares	df	Mean Square	F	p	$\eta^2$	$\eta^2_p$
Residual	30.575	7	4.368				

Note. Type 3 Sums of Squares



# Post hoc Tests

- Bonferroni Procedure
- Tukey's Test
- Scheffe
- Holm

