

SOLAR THERMAL COLLECTORS

Dr. Herena Torio



[Wikipedia.org](https://en.wikipedia.org/wiki/Solar_thermal_collector)

Learning outcomes on solar collectors

- Understand the physical principles governing solar thermal collectors
- Understand the main heat transfer mechanisms for solar thermal collectors
- Understand the relationship between the collector efficiency and main variables influencing it
- Get a critical understanding on equations describing collectors' performance
- Get familiar with parameters depicting collectors' performance

Outline

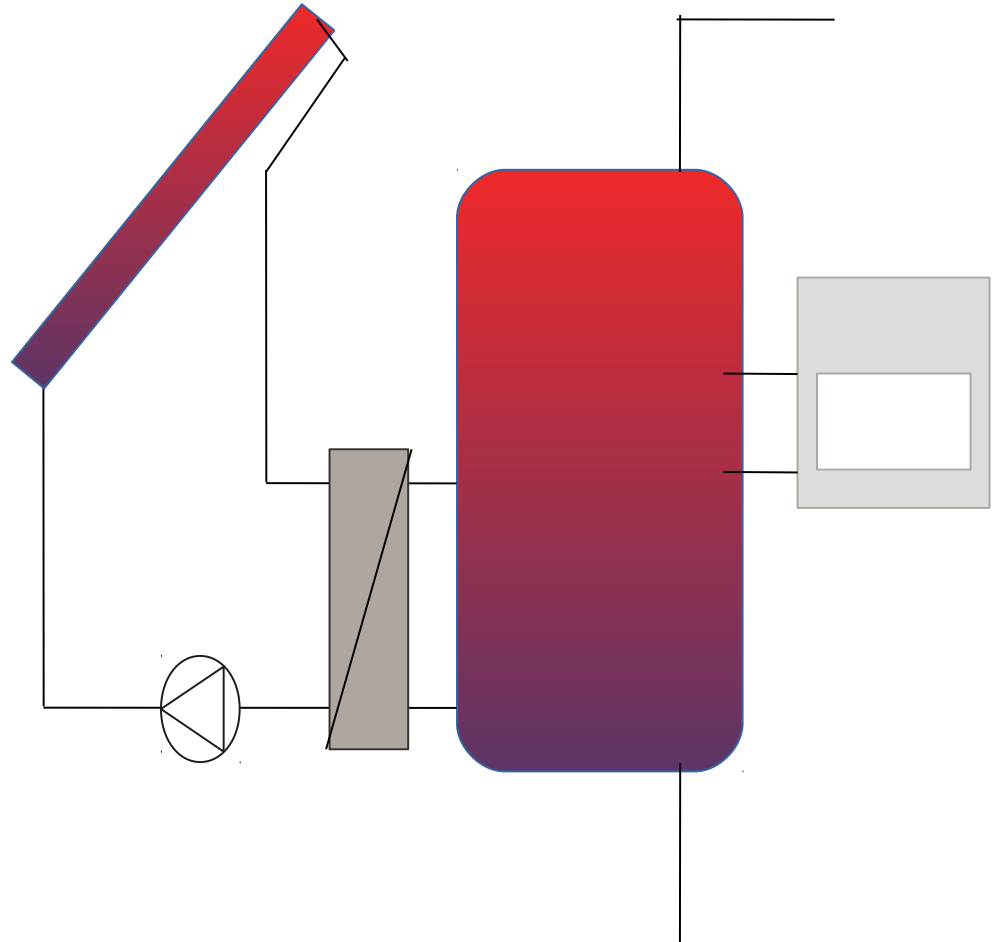
- **Collector types and system outline**
- **Main heat processes involved**
- **Collectors' performance: flat plate collectors**
 - Radiation
 - Mass flow
 - Geometry
 - Materials
 - Capacity effects (thermal inertia)

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Solar thermal systems

First system overview

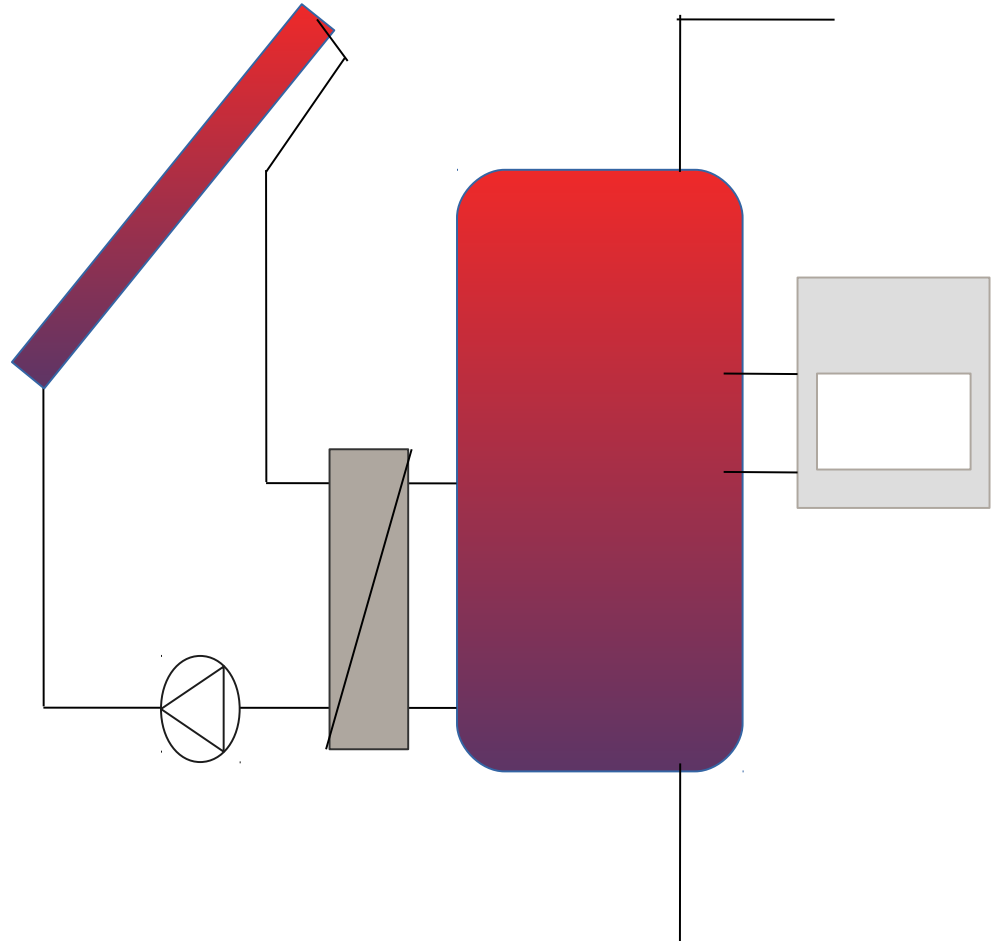


Solar thermal systems

First system overview

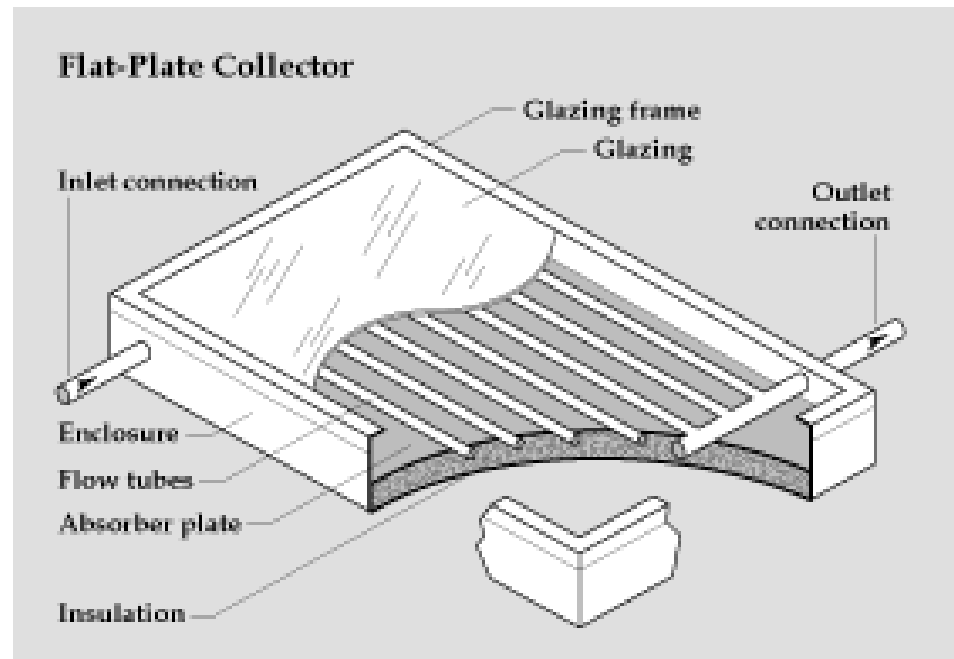
Main solar thermal collector types:

- flat plate
- vacuum tube
- concentrating collectors:
concentrating parabolic
compound (CPC)



Main collector types

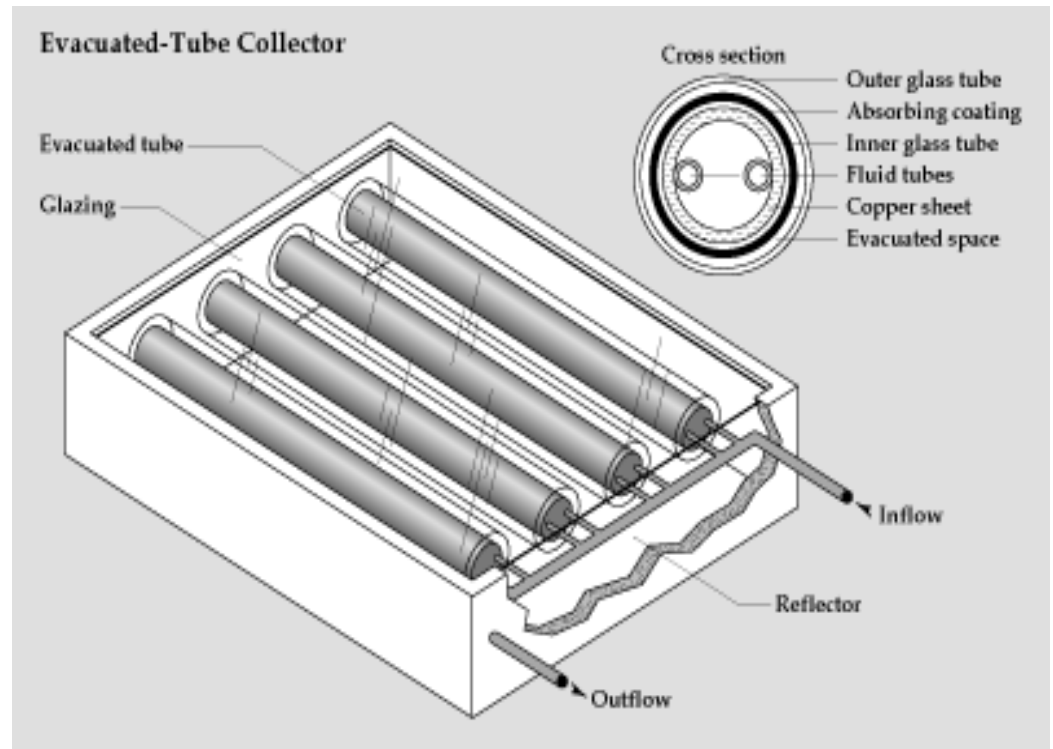
Flat plate collectors



Source: wikipedia.org

Main collector types

Vacuum tube collectors



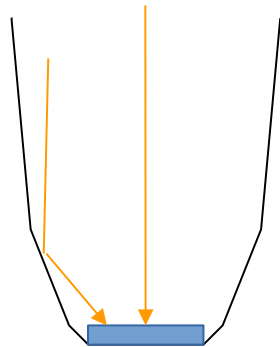
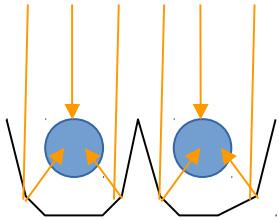
Source: wikipedia.org

Main collector types

Concentrating collectors

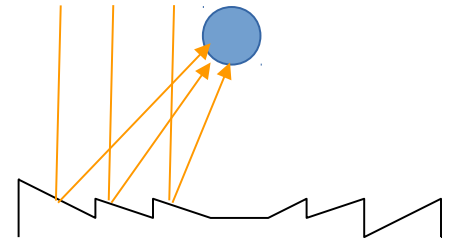
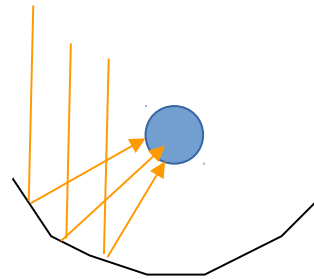
Non imaging: CPC

- lower concentration rates
- lower temperatures
- better use of diffuse radiation



Imaging:

- parabolic through
- solar tower
- parabolic dish
- Fresnel collectors

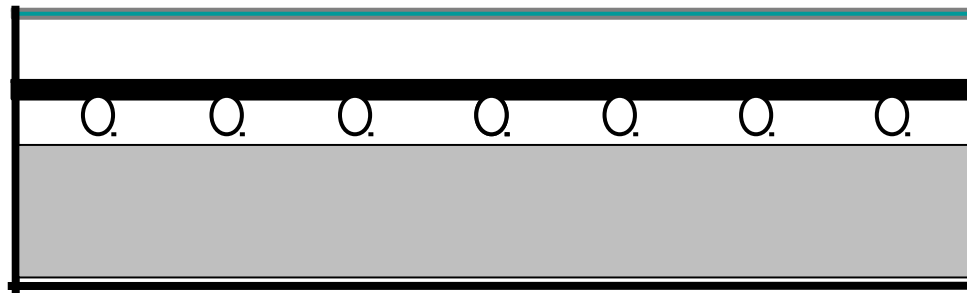


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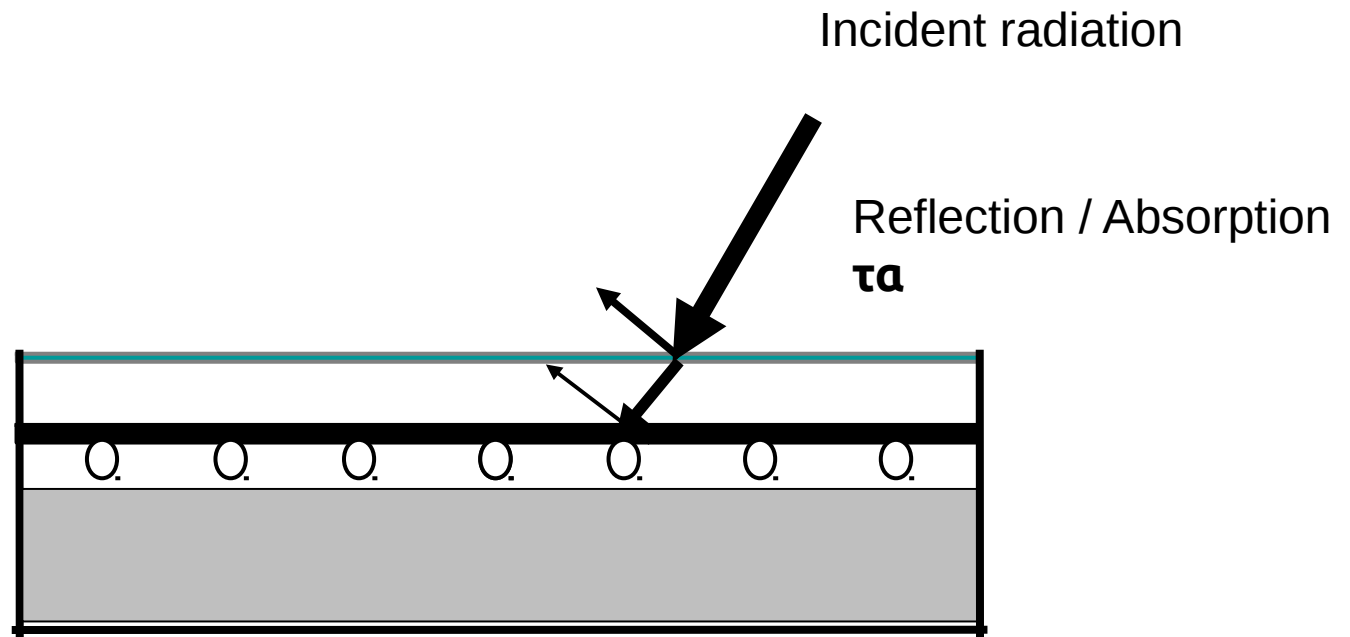
Main heat processes involved

Cross section flat plate collector



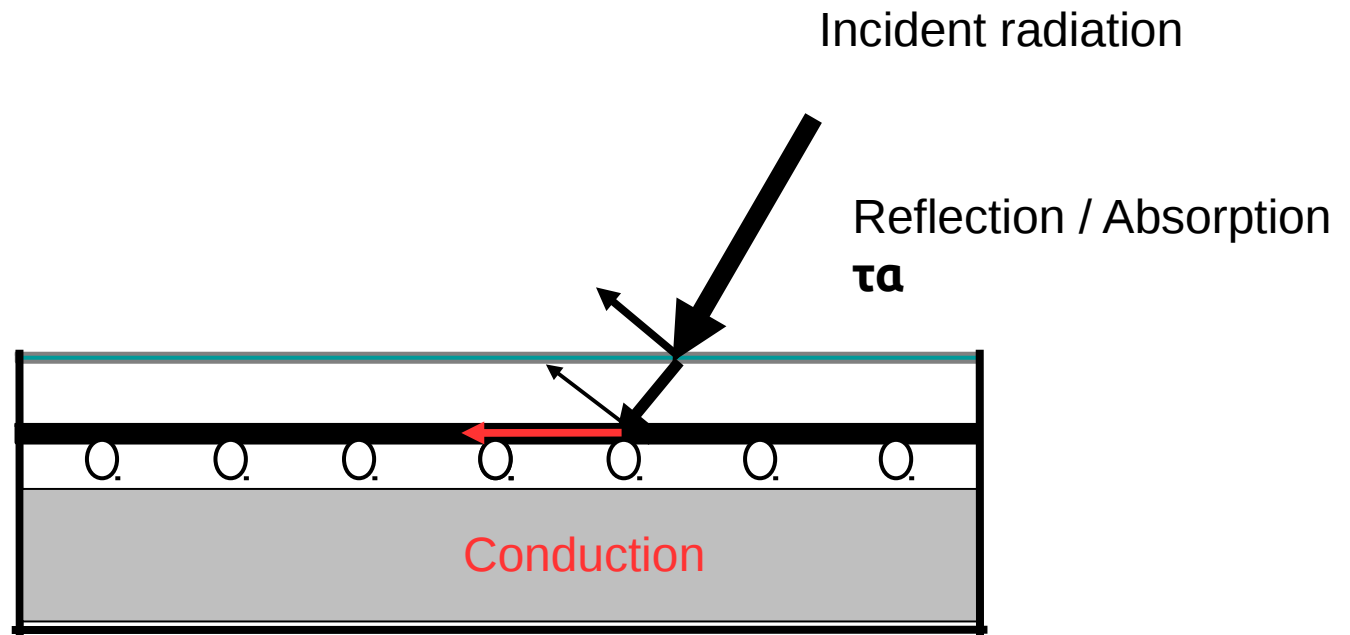
Main heat processes involved

Cross section flat plate collector



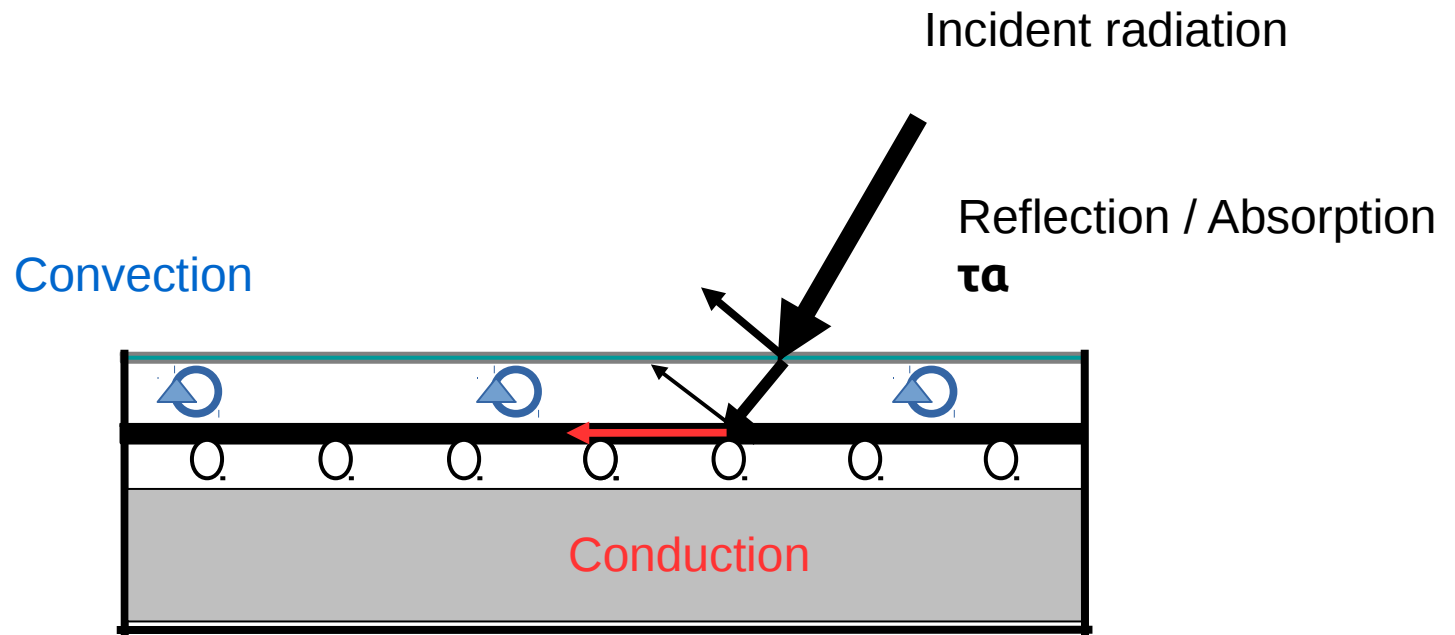
Main heat processes involved

Cross section flat plate collector



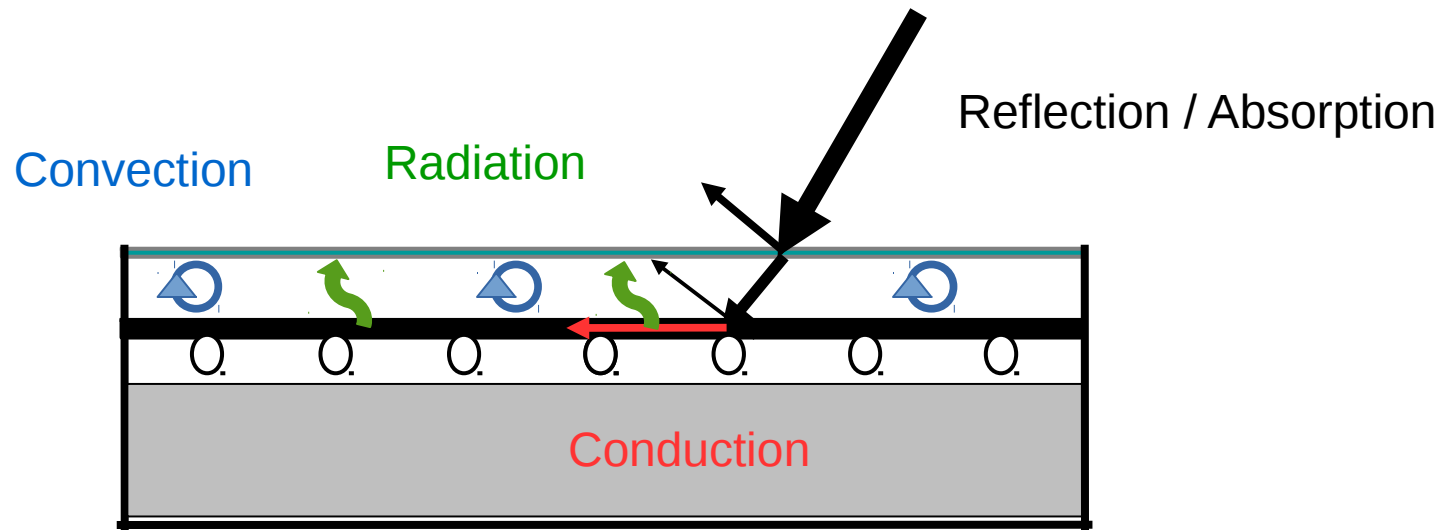
Main heat processes involved

Cross section flat plate collector



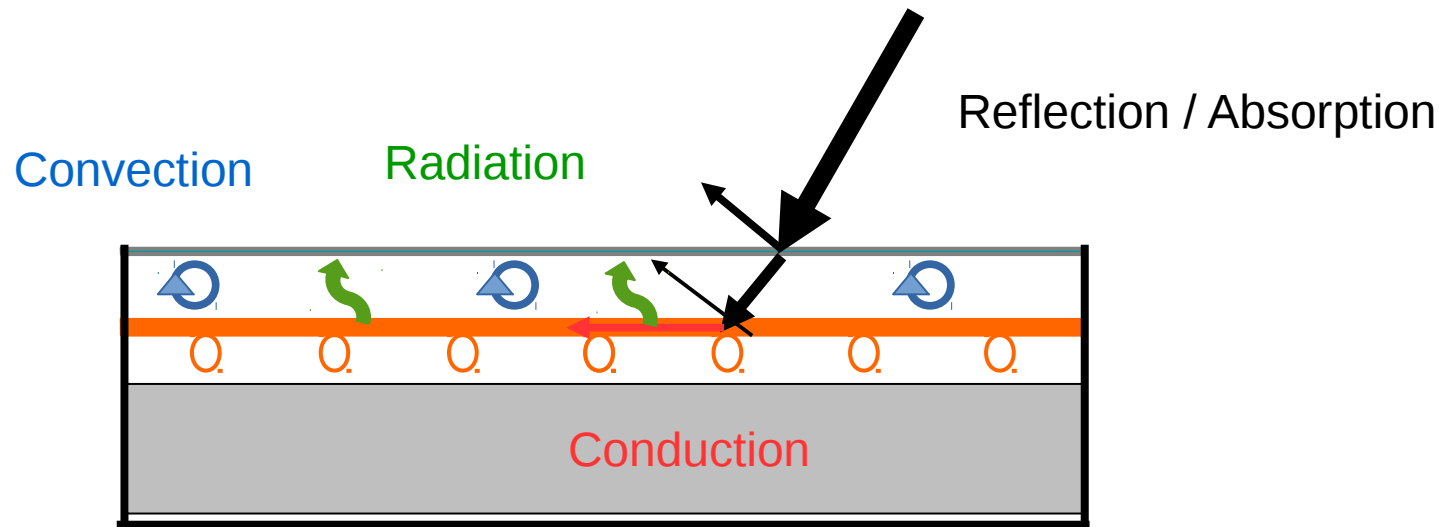
Main heat processes involved

Cross section flat plate collector



Main heat processes involved

Cross section flat plate collector



Capacitance (heat storage) effects

Outline

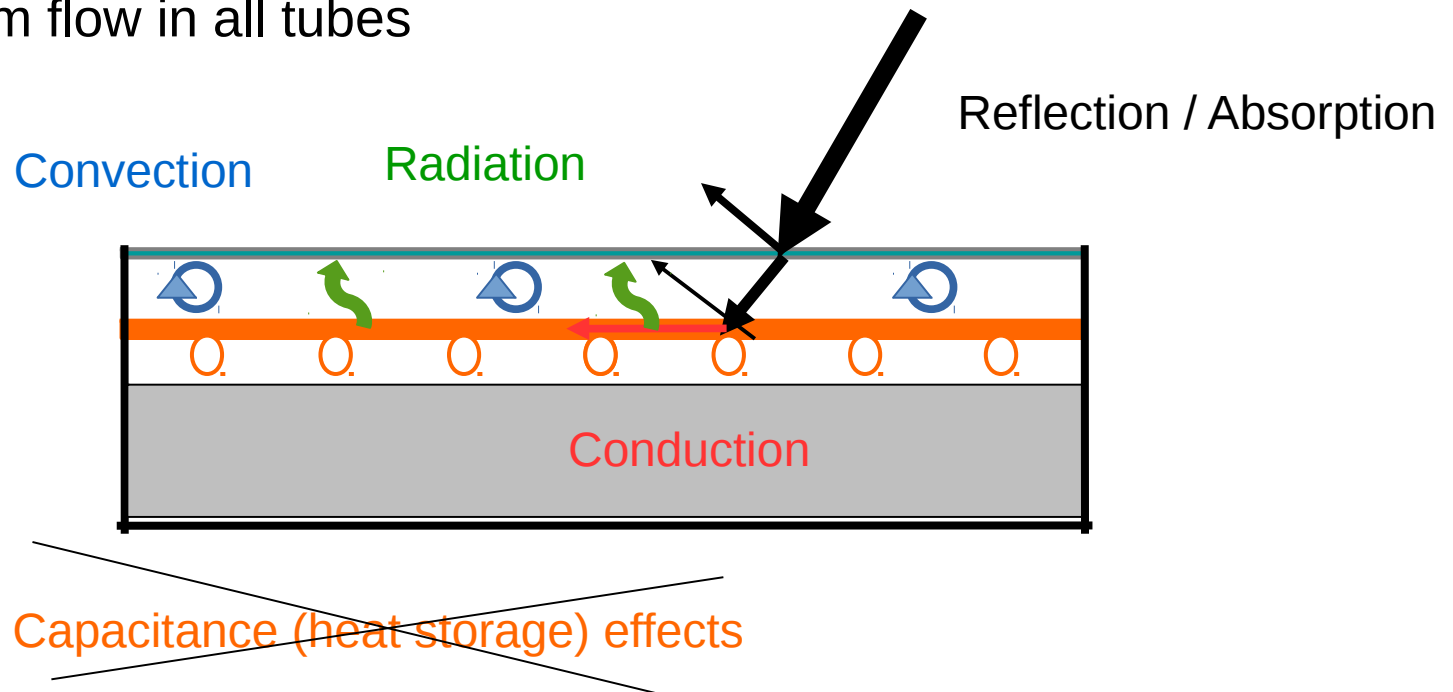
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Main heat processes involved

Cross section flat plate collector: performance assessment

First simplifications:

- Steady state operation
- No absorption from covers affecting thermal losses
- Sheet (absorber) and parallel tubes
- Uniform flow in all tubes



Flat plate collectors: performance

Main heat transfer processes involved

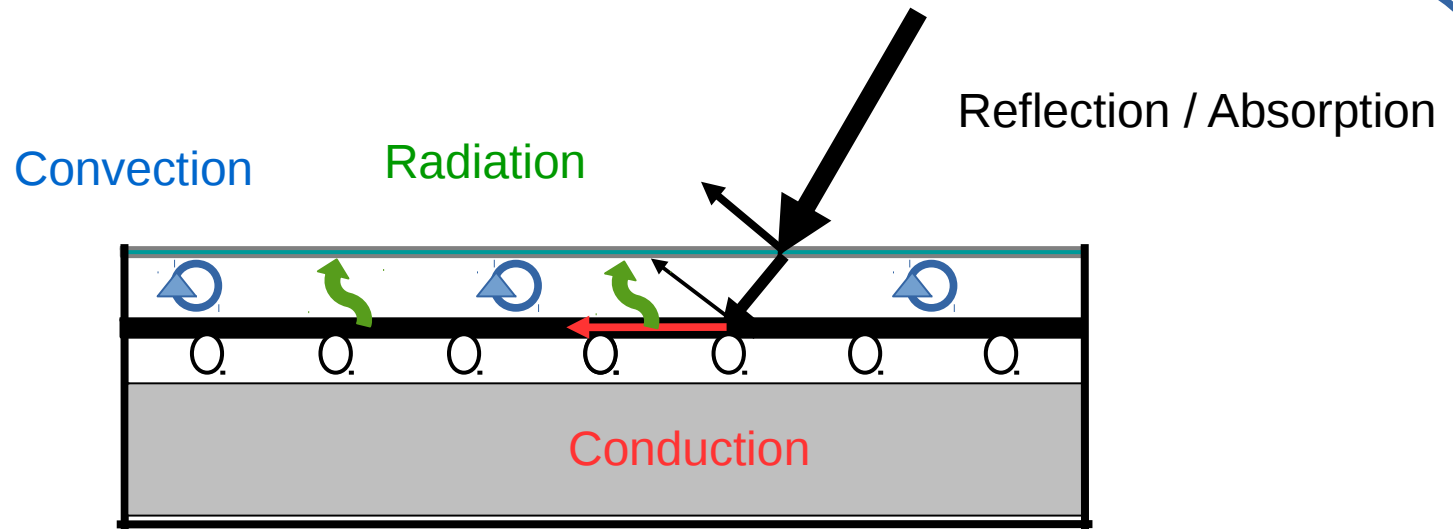
Collectors' performance

$$\eta_{Coll} = \frac{\int \dot{Q}_u dt}{A_{coll} \int G_T dt}$$

\dot{Q}_u : useful energy output [W]

G_T : total incident solar radiation [W/m²]

A_{coll} : total collector area [m²]



Flat plate collectors

Collectors' performance

Defining the useful energy output: \dot{Q}_u

$$\dot{Q}_u = A_{coll} F_R \left[S - U_L (T_i - T_a) \right] \quad [\text{W}]$$

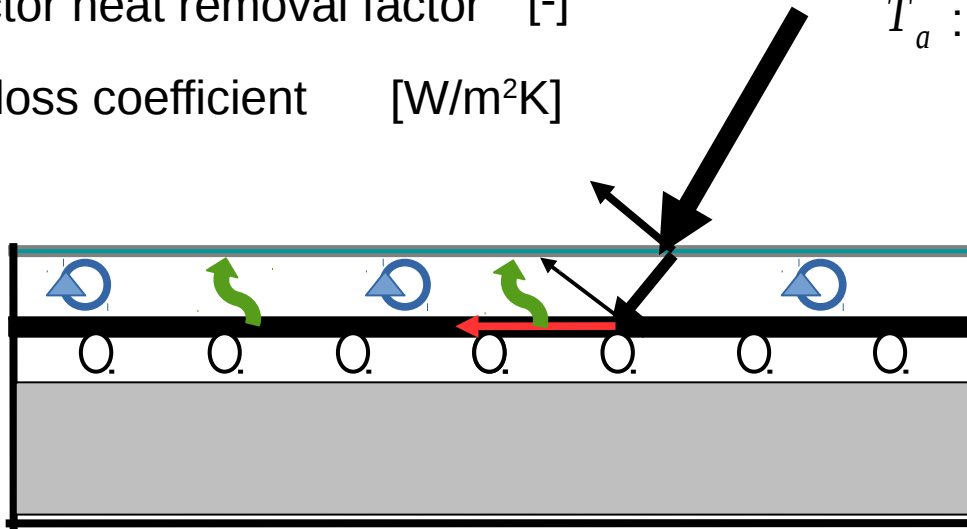
S : **absorbed radiation** $[\text{W}/\text{m}^2]$

F_R : collector heat removal factor $[-]$

U_L : heat loss coefficient $[\text{W}/\text{m}^2\text{K}]$

T_i : inlet fluid temperature $[^\circ\text{C}]$

T_a : ambient temperature $[^\circ\text{C}]$



$$\eta_{Coll} = \frac{\int \dot{Q}_u dt}{A_{coll} \int G_T dt}$$

Flat plate collectors: performance

Absorbed solar radiation:

$$\eta_{Coll} = \frac{\int \dot{Q}_u dt}{A_{coll} \int G_T dt}$$

$$S = G_b R_b (\tau\alpha)_b + G_d (\tau\alpha)_d \underbrace{\frac{(1 + \cos \beta)}{2}}_{\text{view factor sky}} + \rho_g (G_b + G_d) (\tau\alpha)_g \underbrace{\frac{(1 - \cos \beta)}{2}}_{\text{view factor ground}} \quad [\text{W/m}^2]$$

G : radiation [W/m²] β : collector tilt angle [°]

R_b : ratio of beam radiation on the tilted surface to that on a horizontal surface at any time [-] ρ_g : ground reflectivity [-]

$(\tau\alpha)$: transmittance-absorptance product [-]

Subscripts:

b = beam; d = diffuse; g = ground

Flat plate collectors: performance

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Subscripts:

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Flat plate collectors: performance

Absorbed solar radiation:

R_b : ratio of beam radiation on the tilted surface to that on a horizontal surface at any time [-]

$$R_b = \frac{\cos(\theta)}{\cos(\theta)_z}$$

$$\gamma = 0 \longrightarrow R_b = \frac{\cos(\Phi - \beta) \cos \delta \cos \omega + \sin(\Phi - \beta) \sin \delta}{\cos \Phi \cos \delta \cos \omega + \sin \Phi \sin \delta}$$

θ : incidence angle (incident beam to collector normal) [°]

θ_z : incidence angle at zenith [°]

Φ : latitude [°]

ω : Hour angle, sun displacement [°]

β : collector tilt angle (slope) [°]

δ : declination (angular sun position at noon) [°]

γ : azimuth angle (from south, south = 0°) [°]

Flat plate collectors: performance

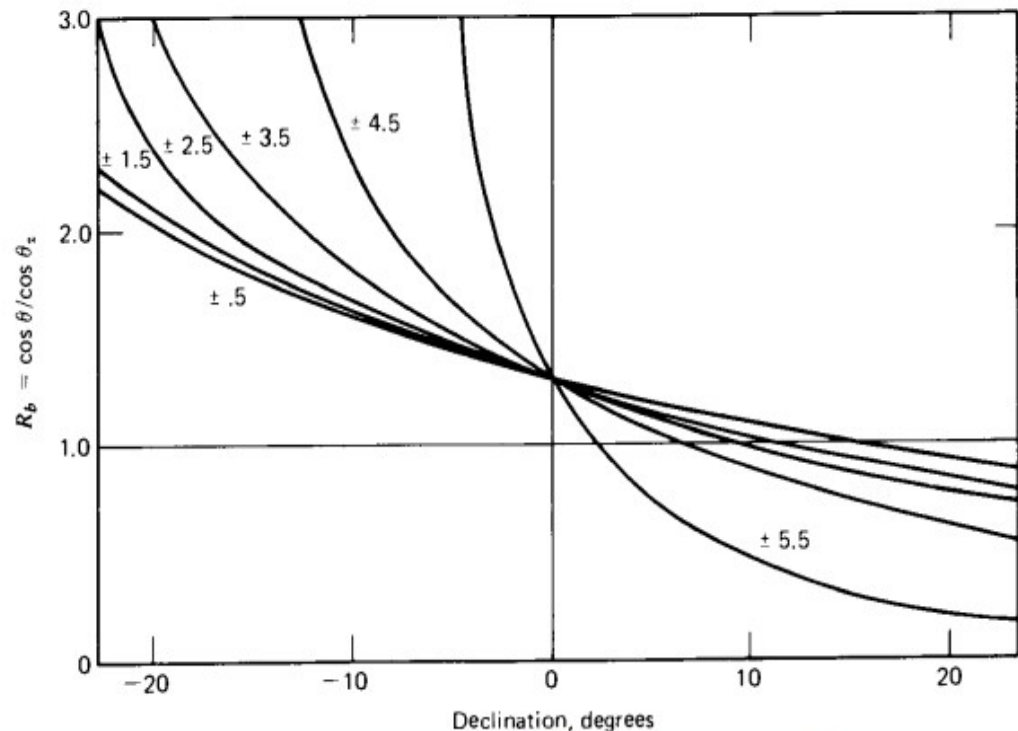
Absorbed solar radiation:

R_b : ratio of beam radiation on the tilted surface to that on a horizontal surface at any time [-]

Example:

$$\beta = 50^\circ$$

$$\Phi = 40^\circ$$

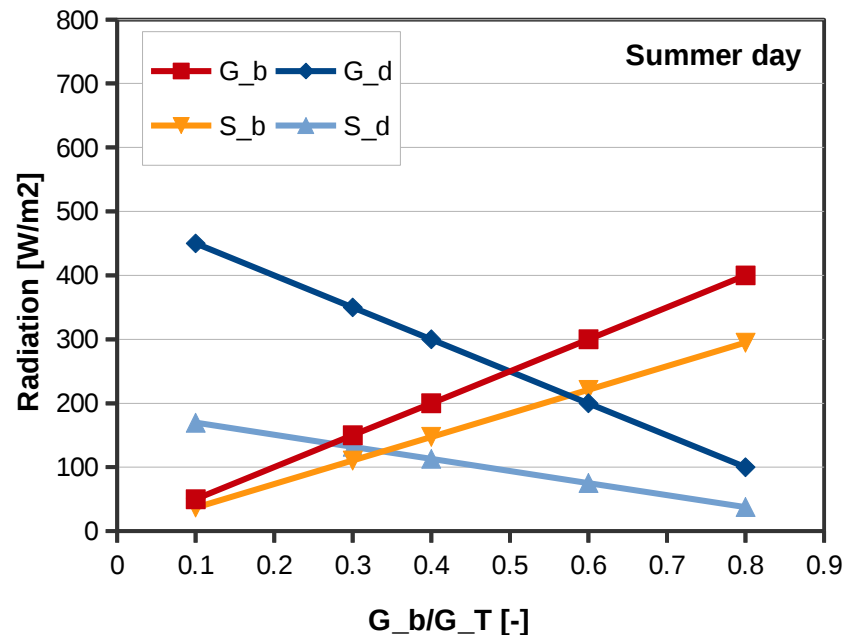
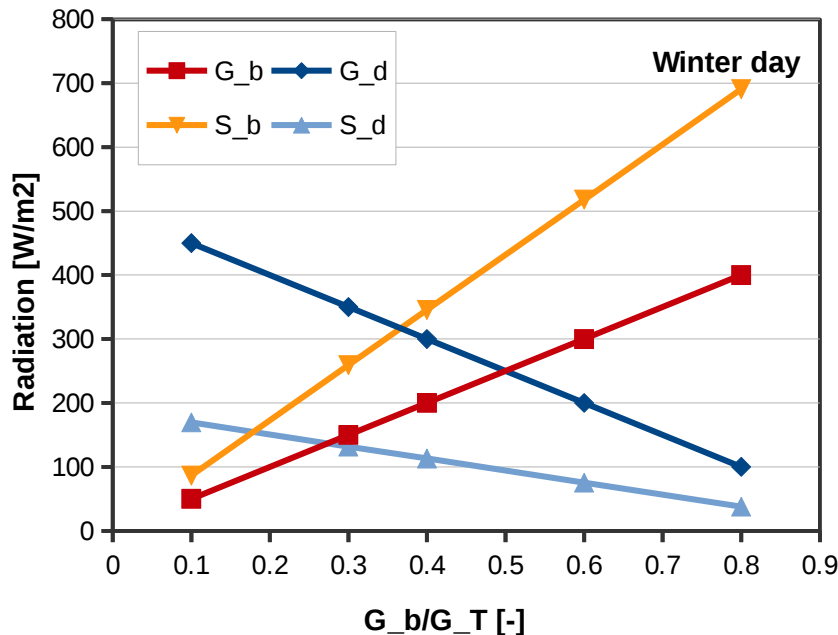


Flat plate collectors: performance

Absorbed solar radiation:

Seasonal contribution of beam and diffuse components

Example: $G = 500 \text{ W/m}^2$; $\beta = 60^\circ$; $\alpha_n = 0.93$ (single cover collector);
 $\rho_g = 0.6$ $\Phi = 40^\circ$



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Flat plate collectors: performance

$$\eta_{Coll} = \frac{\int \dot{Q}_u dt}{A_{coll} \int G_T dt}$$

Defining the useful energy output: \dot{Q}_u

$$\dot{Q}_u = A_{coll} F_R \left[S - U_L (T_i - T_a) \right] \quad [W]$$

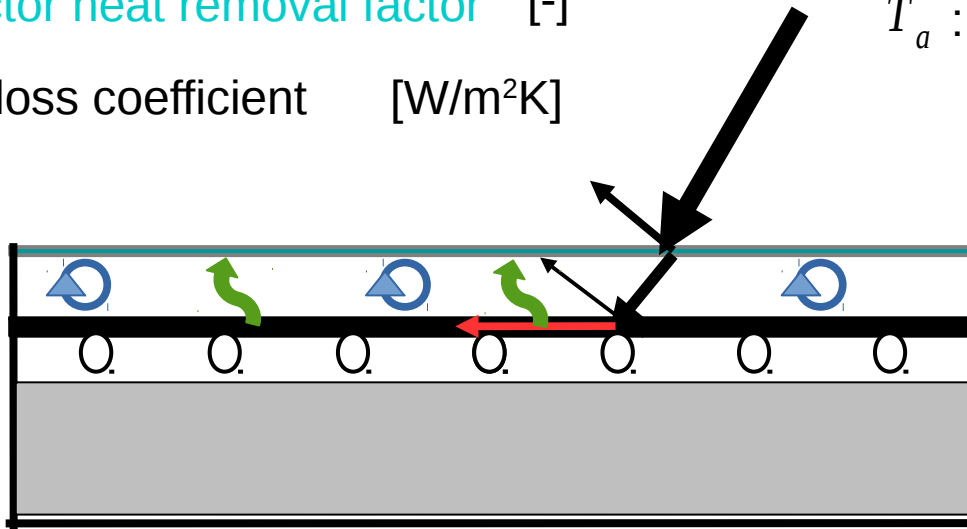
S : absorbed radiation $[W/m^2]$

T_i : inlet fluid temperature $[^\circ C]$

F_R : collector heat removal factor $[-]$

T_a : ambient temperature $[^\circ C]$

U_L : heat loss coefficient $[W/m^2K]$



Flat plate collectors: performance

Heat removal factor: F_R

\approx effectiveness of a heat exchanger: ratio of actual heat exchange to maximum one (with minimum losses, i.e. $T_{\text{fluid}} = T_{\text{in}}$)

$$F_R = \frac{\dot{m} C_p}{A_{\text{coll}} U_L} \left[1 - \exp \left(\frac{-A_{\text{coll}} U_L F'}{\dot{m} C_p} \right) \right]$$

\dot{m} : collector mass flow rate [kg/s]

C_p : specific heat capacity fluid [kJ/KgK]

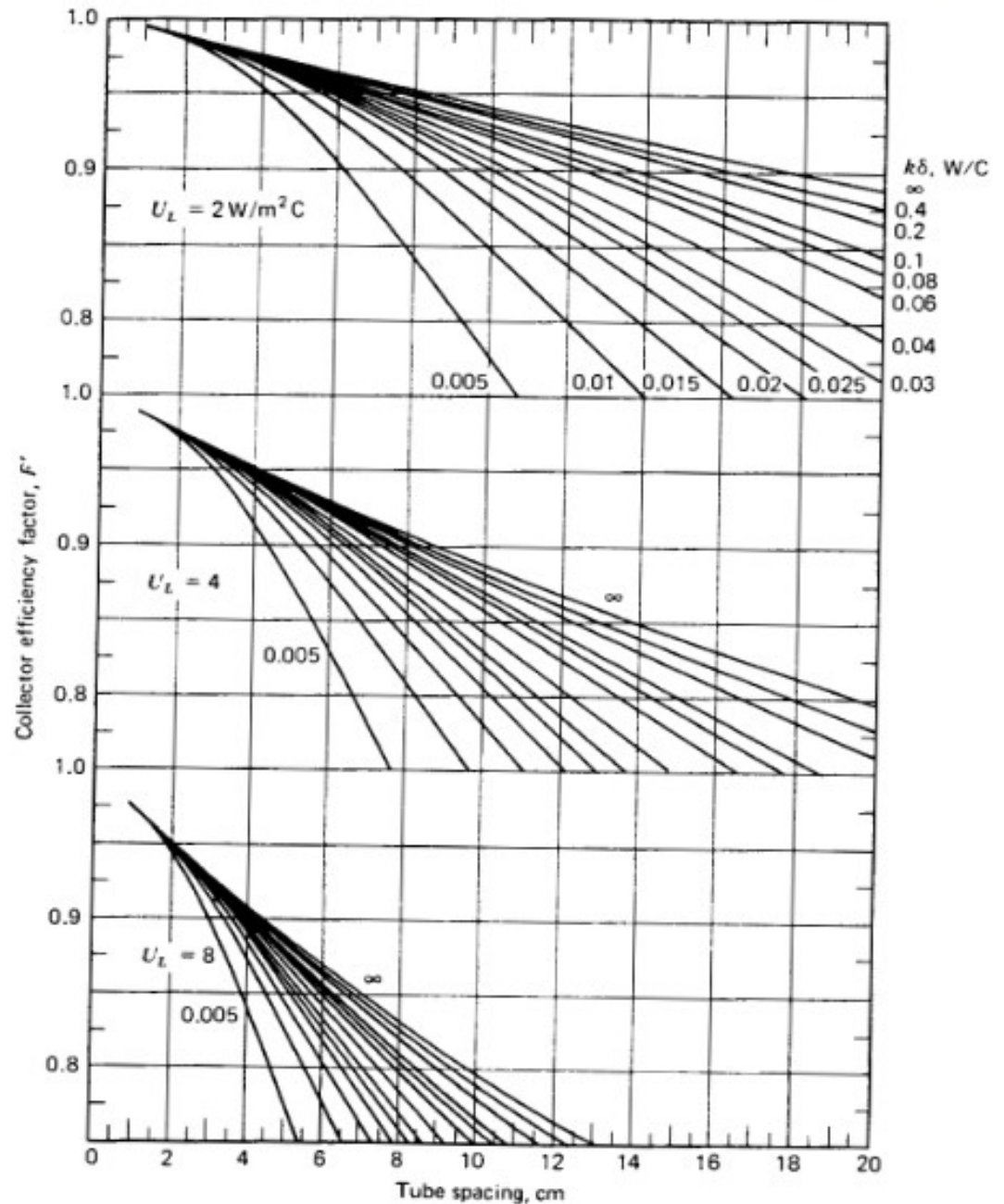
A_{coll} : collector area [m²]

U_L : overall loss coefficient [W/Km²]

F' : collector efficiency factor [-]

Function of geometry (tube spacing, tube diameter, absorber thickness) and materials (loss coefficient, U_L)

Behavior of collector efficiency factor, F'



Flat plate collectors: performance

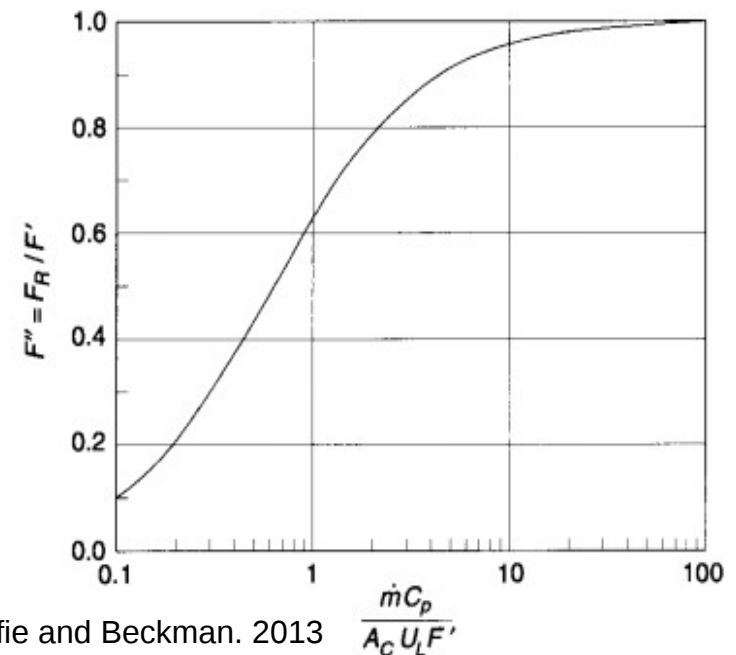
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Collector flow factor [-]: effect of mass flow rate on collectors' performance

$$F'' = \frac{F_R}{F'}$$



Source: Duffie and Beckman. 2013

Flat plate collectors: performance

$$\eta_{Coll} = \frac{\int \dot{Q}_u dt}{A_{coll} \int G_T dt}$$

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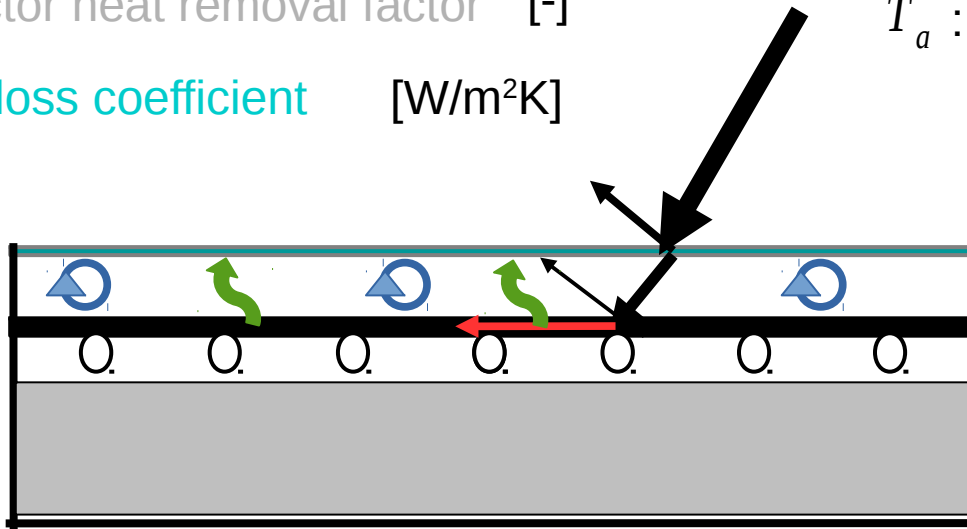
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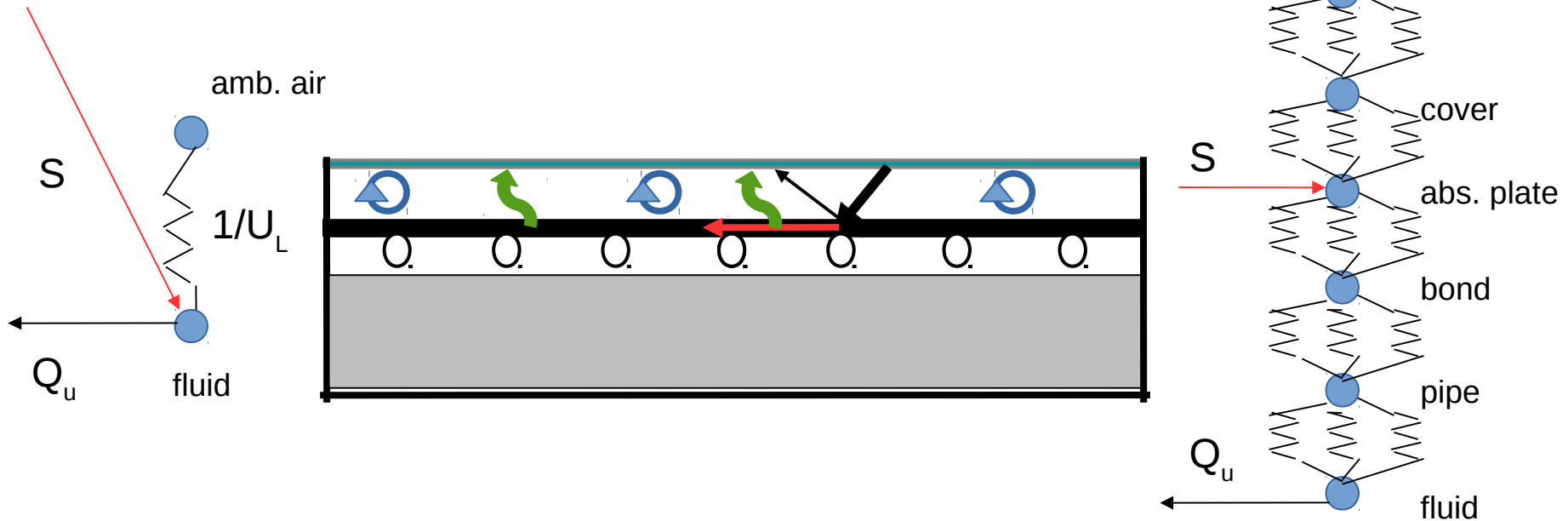
T_a : ambient temperature $[\text{°C}]$

U_L : heat loss coefficient $[\text{W}/\text{m}^2\text{K}]$



Flat plate collectors: performance

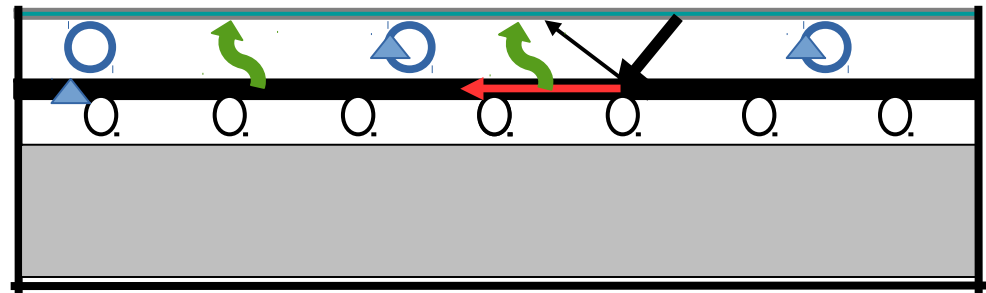
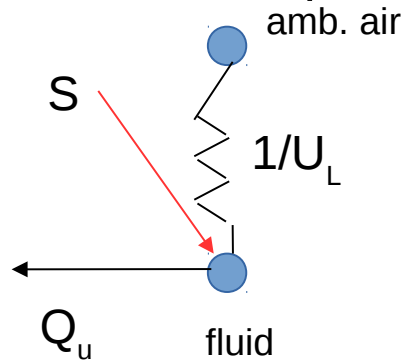
Overall heat loss coefficient: U_L



Flat plate collectors: performance

Overall heat loss coefficient: U_L

Often determined experimentally



Conduction:

$$q_{cond} = \frac{\lambda}{d} (T_1 - T_2)$$

λ : thermal conductivity [W/mK]

d : thickness [m]

Convection:

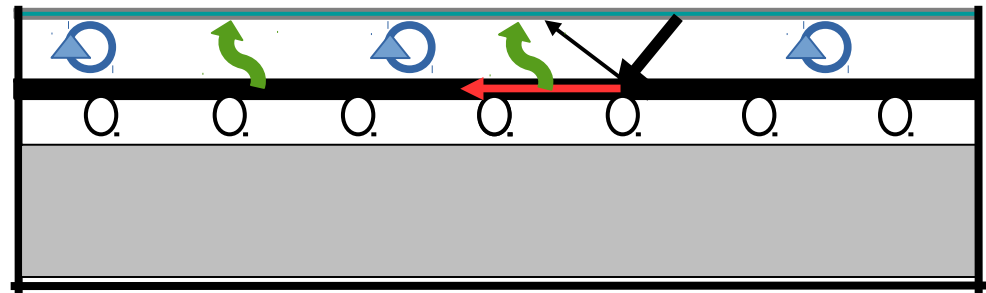
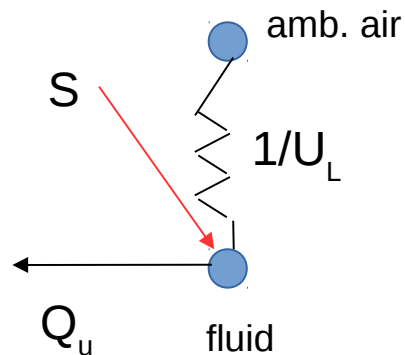
$$q_{conv} = h_i (T_1 - T_2)$$

h_i : convective heat transfer coefficient [W/K]

Flat plate collectors: performance

Overall heat loss coefficient: U_L

Often determined experimentally



Radiation:

$$q_{rad} = \sigma \varepsilon (T_1^4 - T_2^4)$$

σ : Stephan-Boltzmann constant [$\text{W}/\text{m}^2\text{K}^4$]

ε : emissivity [-] \longrightarrow **Selective surface!**

T : absolute temperature [K]

Flat plate collectors: performance

Overall heat loss coefficient: U_L

Often determined experimentally

Radiation:

$$q_{rad} = \sigma \varepsilon (T_1^4 - T_2^4)$$

ε : emissivity [-]

	<u>ε</u>	α
"TINOX" ¹	0.04	0.95
Copper polished ²	0.23-0.52	0.18
Aluminum polished ²	0.09	0.30

¹ http://www.almecogroup.com/uploads/1074-ALMECO_TinoxEnergy_ENG_S402_05_2013_mail.pdf

² www.engineeringtoolbox.com

Flat plate collectors: performance

Defining the useful energy output:

$$\eta_{Coll} = \frac{\int \dot{Q}_u dt}{A_{coll} \int G_T dt}$$

$$\dot{Q}_u = A_{coll} F_R \left[S - U_L (T_i - T_a) \right] \quad [\text{W}]$$

S : absorbed radiation $[\text{W}/\text{m}^2]$

T_i : inlet fluid temperature $[\text{°C}]$

F_R : collector heat removal factor $[-]$

T_a : ambient temperature $[\text{°C}]$

U_L : heat loss coefficient $[\text{W}/\text{m}^2\text{K}]$

- Determining S is not an easy task (requires detailed hourly data of radiation and angles variations)
- Standard (european) collector test procedures often refer to the mean fluid temperature, not the inlet one!

Flat plate collectors: performance

Defining the useful energy output:

$$\eta_{Coll} = \frac{\int \dot{Q}_u dt}{A_{coll} \int G_T dt}$$

$$\dot{Q}_u = A_{coll} F_R \left[S - U_L (T_i - T_a) \right] \quad [\text{W}]$$

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U_L : heat loss coefficient $[\text{W}/\text{m}^2\text{K}]$

$$\dot{Q}_u = A_{coll} F_{av} \left[S - U_L (T_m - T_a) \right] \quad [\text{W}]$$

T_m : average fluid temperature $[\text{°C}]$

$$T_m = \frac{T_i + T_{out}}{2}$$

T_a : ambient temperature $[\text{°C}]$

Flat plate collectors: performance

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T_i : inlet fluid temperature $[^\circ\text{C}]$

F_R : collector heat removal factor $[-]$

T_a : ambient temperature $[^\circ\text{C}]$

U_L : heat loss coefficient $[\text{W}/\text{m}^2\text{K}]$

$$\dot{Q}_u = A_{coll} F_{av} \left[G_T (\tau\alpha)_n K_{\tau\alpha} - U_L (T_m - T_a) \right] \quad [\text{W}]$$

G_T : global incident radiation on coll. plane $[\text{W}/\text{m}^2]$

$(\tau\alpha)_n$: average transmittance-absorptance product for beam (normal) radiation $[-]$

$K_{\tau\alpha}$: incident angle modifier – function of θ (effective incident angle!) $[-]$

Flat plate collectors: performance

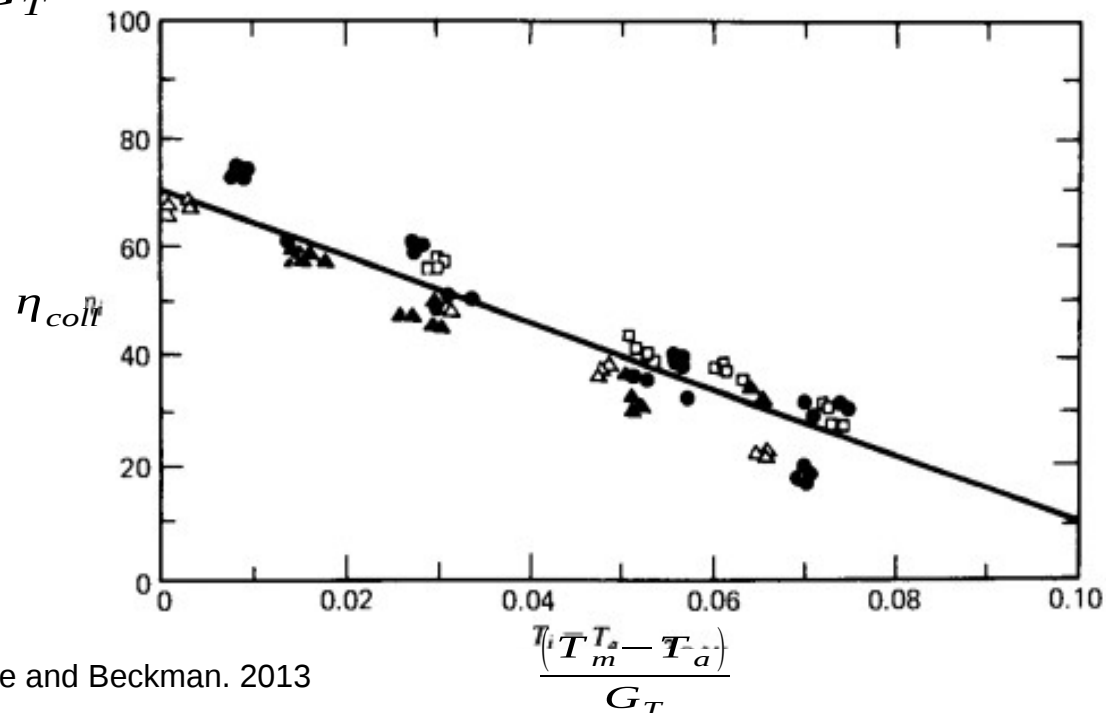
$$\eta_{Coll} = \frac{\int \dot{Q}_u dt}{A_{coll} \int G_T dt}$$

$$\dot{Q}_u = A_{coll} F_{av} \left[G_T (\tau\alpha)_n K_{\tau\alpha} - U_L (T_m - T_a) \right]$$

$$\eta_{coll} = F_{av} (\tau\alpha)_n - \frac{F_{av} U_L (T_m - T_a)}{G_T}$$

Data scatters from linear dependency:

- U_L is a function of temperature
- F_{av} is also weak function of temperature



Source: Duffie and Beckman. 2013

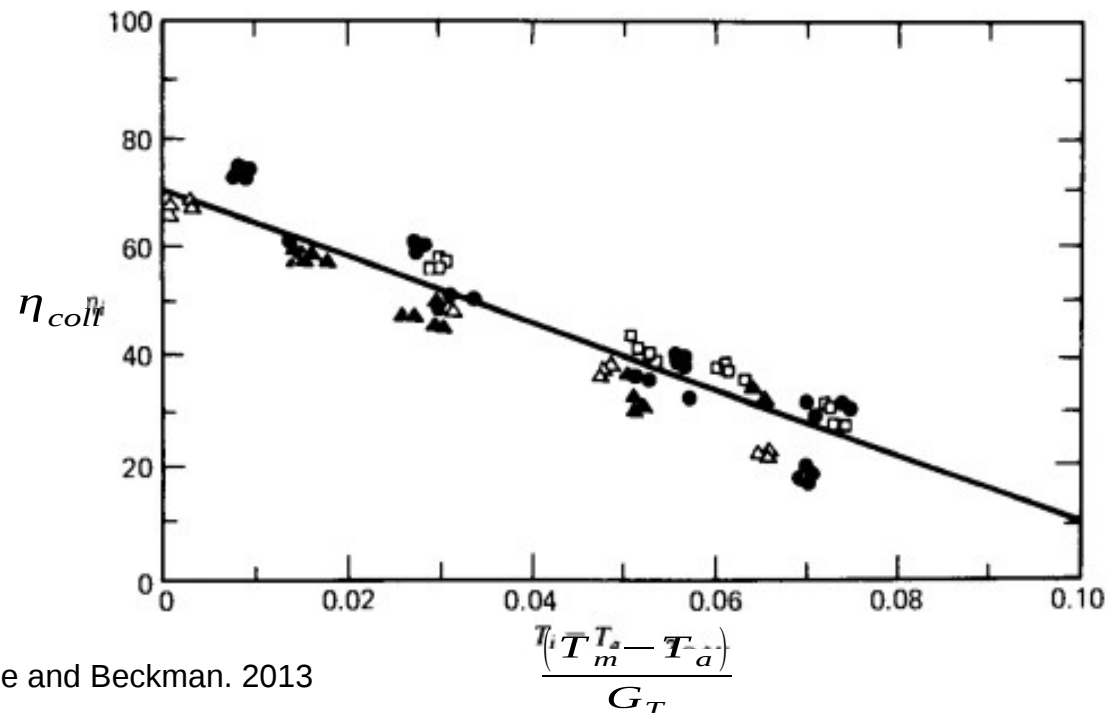
Flat plate collectors: performance

$$F_{av} U_L = c_1 + c_2 (T_m - T_a)$$

$$\eta_{coll} = F_{av} (\tau\alpha)_n - c_1 \frac{(T_m - T_a)}{G_T} - c_2 \frac{(T_m - T_a)^2}{G_T}$$

Data scatters from linear dependency:

- U_L is a function of temperature
- F_{av} is also weak function of temperature



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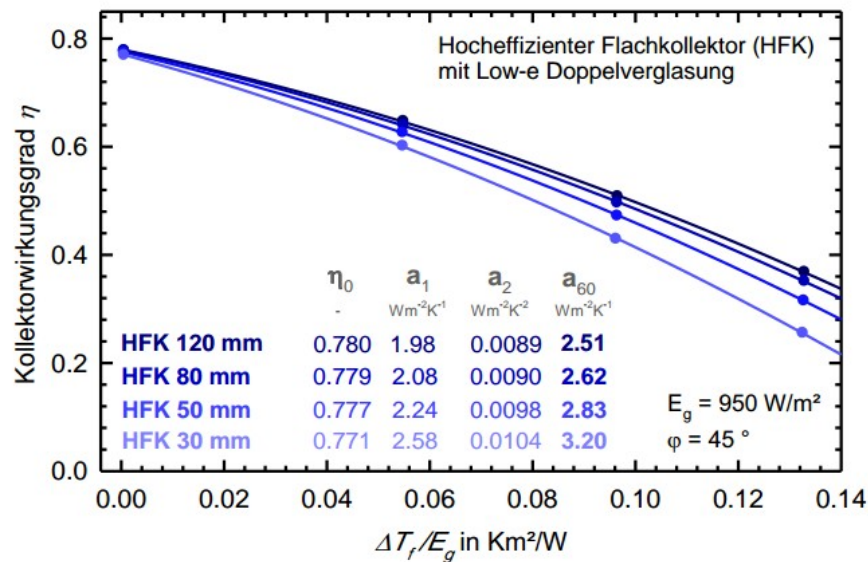
Flat plate collectors: performance

$$F_{av} U_L = c_1 + c_2 (T_m - T_a)$$

$$\eta_{coll} = \boxed{F_{av} (\tau\alpha)_n} - c_1 \frac{(T_m - T_a)}{G_T} - c_2 \frac{(T_m - T_a)^2}{G_T}$$

$$\eta_{coll} = \boxed{\eta_0} - c_1 \frac{(T_m - T_a)}{G_T} - c_2 \frac{(T_m - T_a)^2}{G_T}$$

η_0 : zero loss efficiency [-]
Not optical efficiency!!!!



Source: Föste et al., 2013

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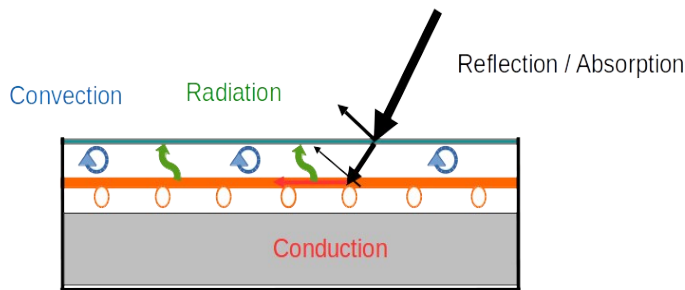
Flat plate collectors: performance

Collectors' **DYNAMIC** performance

European Standard EN 12975-2

Thermal Solar Systems and Components – Solar Collectors CEN2001

$$\dot{Q}_u = \underbrace{F'(\tau\alpha)_{en} K_{\theta b}(\theta) G_b}_{\text{beam}} + \underbrace{F'(\tau\alpha)_{en} K_{\theta d} G_d}_{\text{diffuse}} - \underbrace{c_6 u G - c_1(T_m - T_a) - c_2((T_m - T_a)^2) - c_3 u(T_m - T_a)}_{\text{Wind speed dependence of zero losses}} + \underbrace{c_4 u(E_L - \sigma T_a^4)}_{\text{Wind speed dependence of heat losses}} - \underbrace{c_5 \frac{dT_m}{dt}}_{\text{Long-wave irradiance}}$$



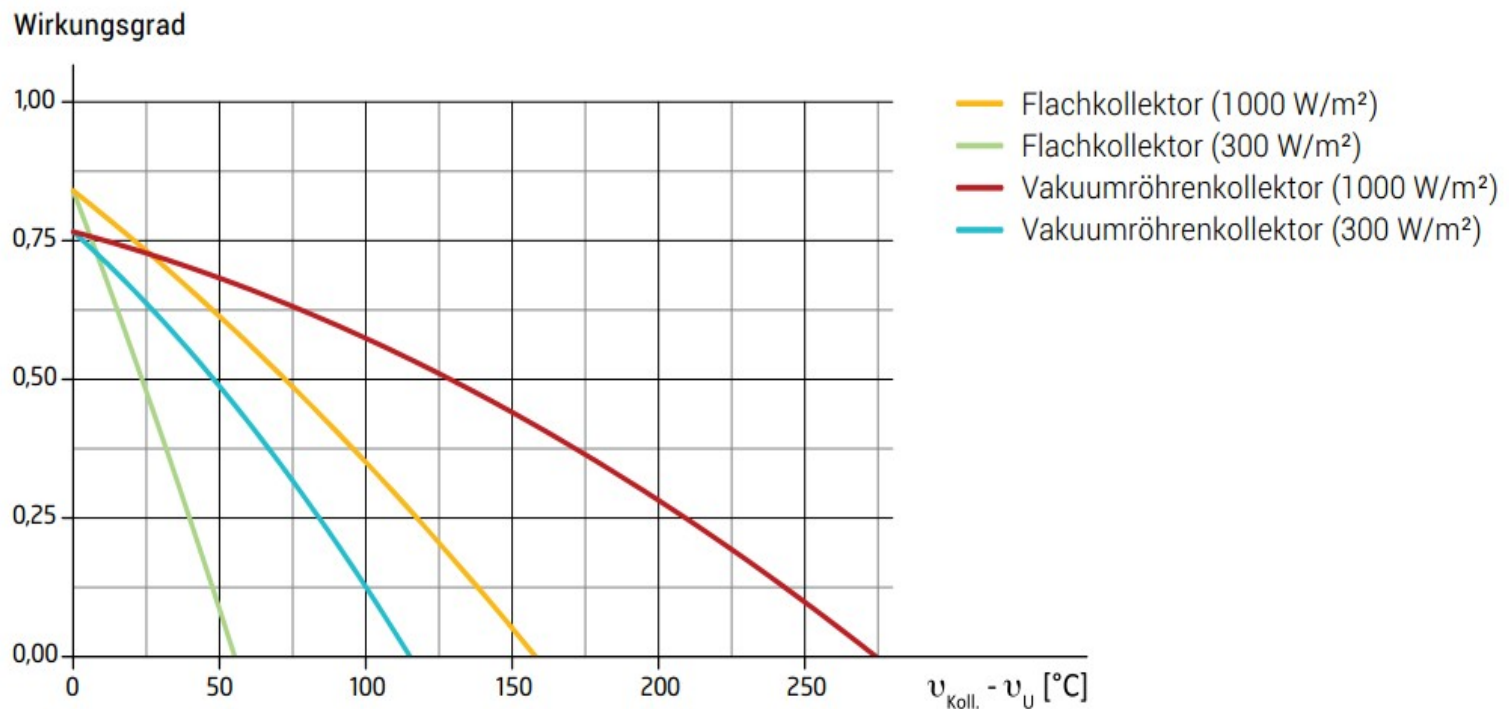
Capacitance (heat storage) effects

Thermal capacitance / Thermal inertia processes

Source: Fischer, Müller-Steinhagen., 2001

Flat plate collectors: performance

$$\eta_{coll} = \eta_0 - c_1 \frac{(T_m - T_a)}{G_T} - c_2 \frac{(T_m - T_a)^2}{G_T}$$



Flat plate collectors: performance

$$\eta_{coll} = \eta_0 - c_1 \frac{(T_m - T_a)}{G_T} - c_2 \frac{(T_m - T_a)^2}{G_T}$$

Collector database: <http://www.solarkeymark.dk/CollectorCertificates>

Collector Type	η_0 [-]	c_1 [W/m ² K]	c_2 [W/m ² K]	C_{eff} [J/m ² K]
Vacuum tube	0.789	1.370	0.005	10.80
Vacuum tube + reflector	0.614	0.285	0.011	17.50
High tech flat plate	0.797	2.833	0.013	4.85
-Low tech flat plate	0.711	4.878	0.044	33.51

References

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