

# Heat pumps I – Thermodynamic processes

Dr. Herena Torio

# Agenda

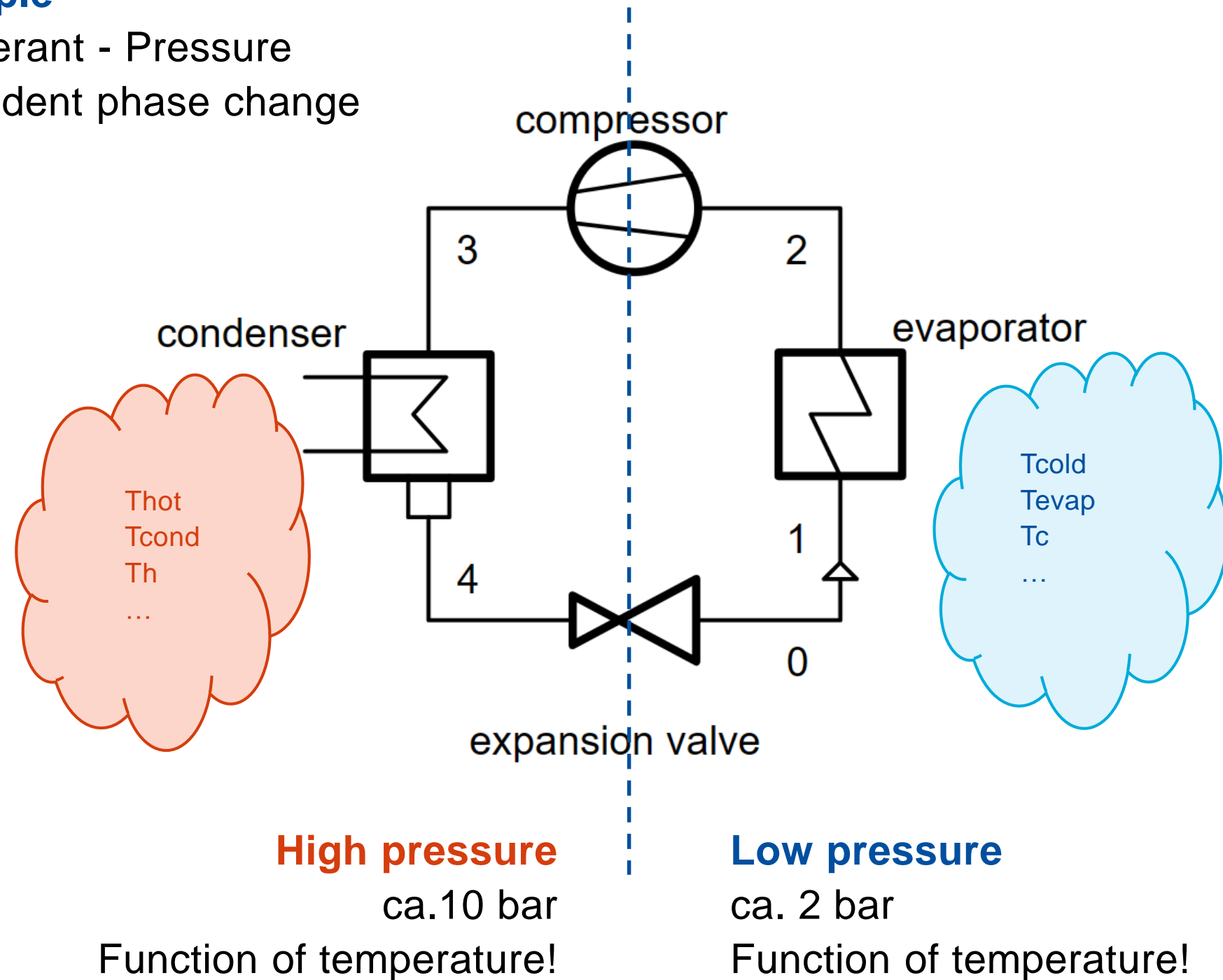
- Heat pump overview
- Re-visiting thermodynamics
- Components and cycles

# Heat pump overview

## The heat pump cycle

### Principle

Refrigerant - Pressure  
dependent phase change  
points



# Heat pump overview

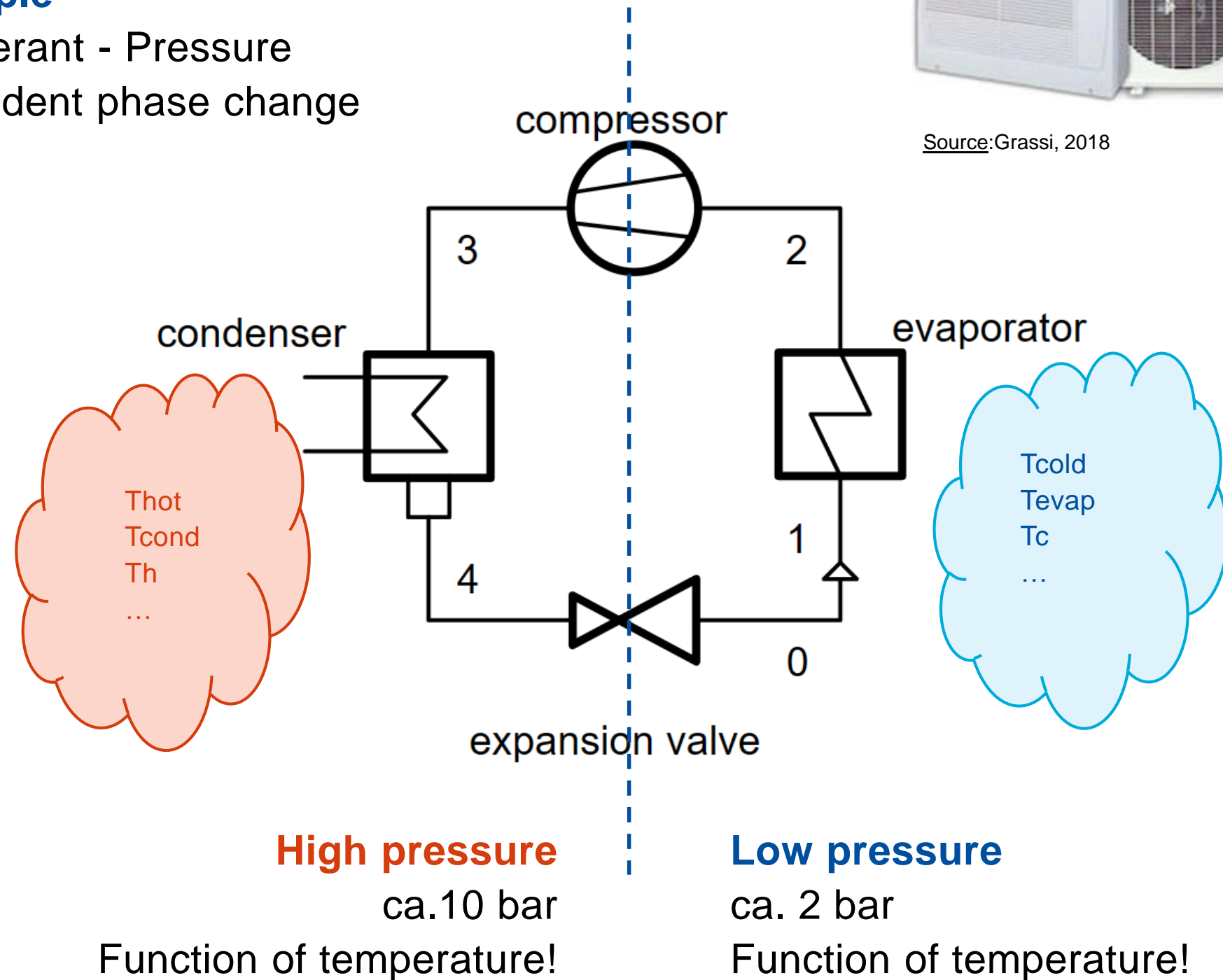
## The heat pump cycle

### Principle

Refrigerant - Pressure  
dependent phase change  
points

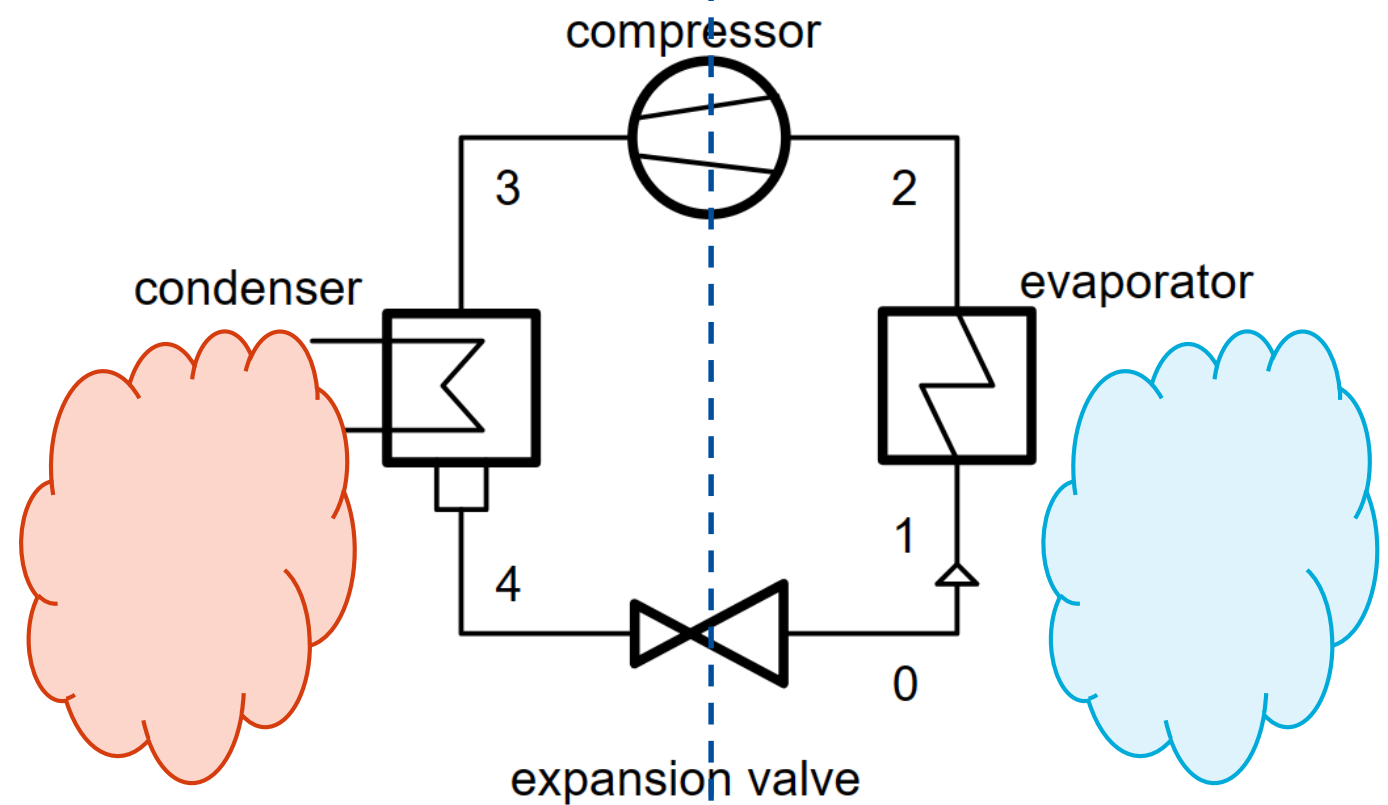


Source:Grassi, 2018

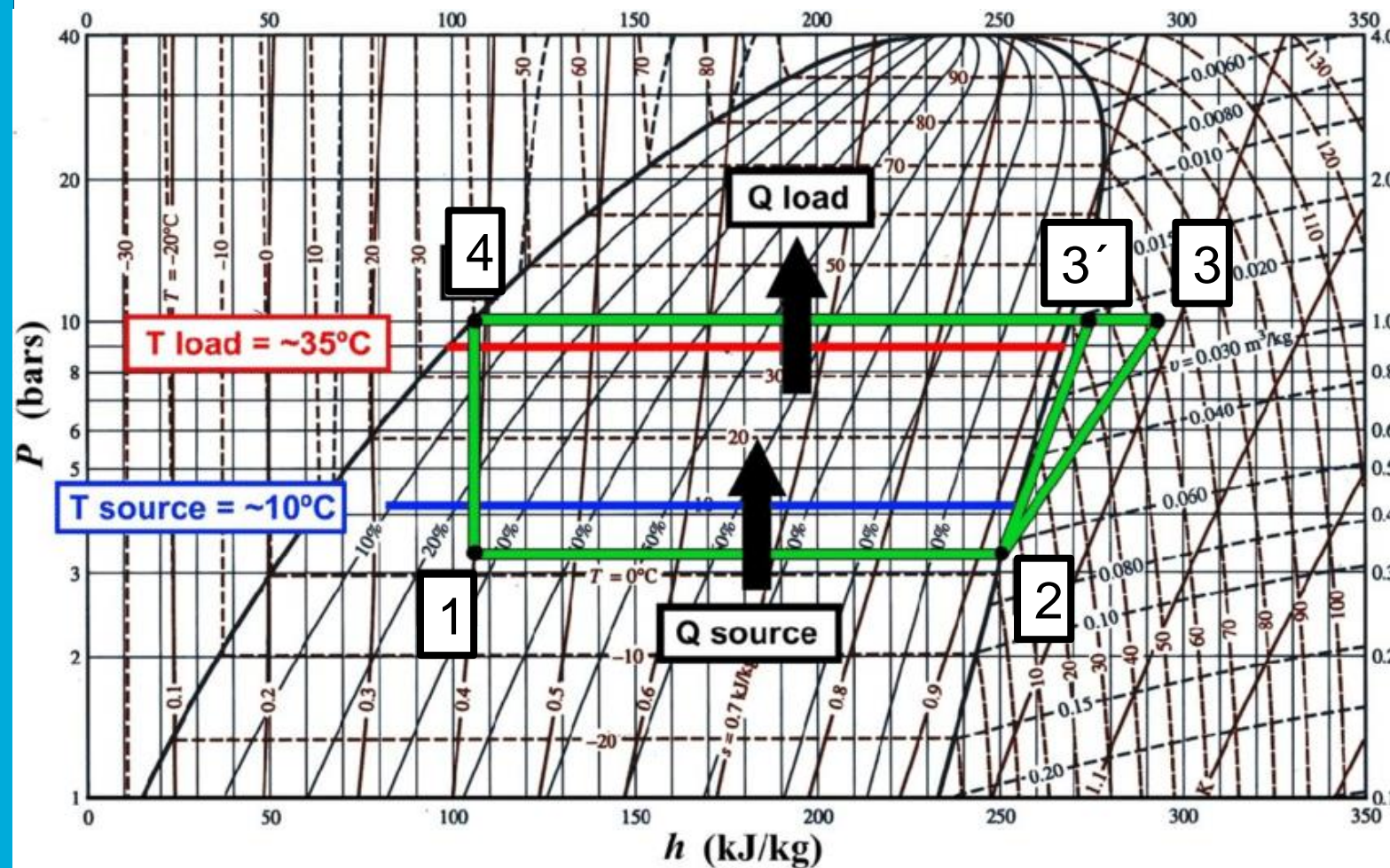


# Heat pump overview

## The heat pump cycle



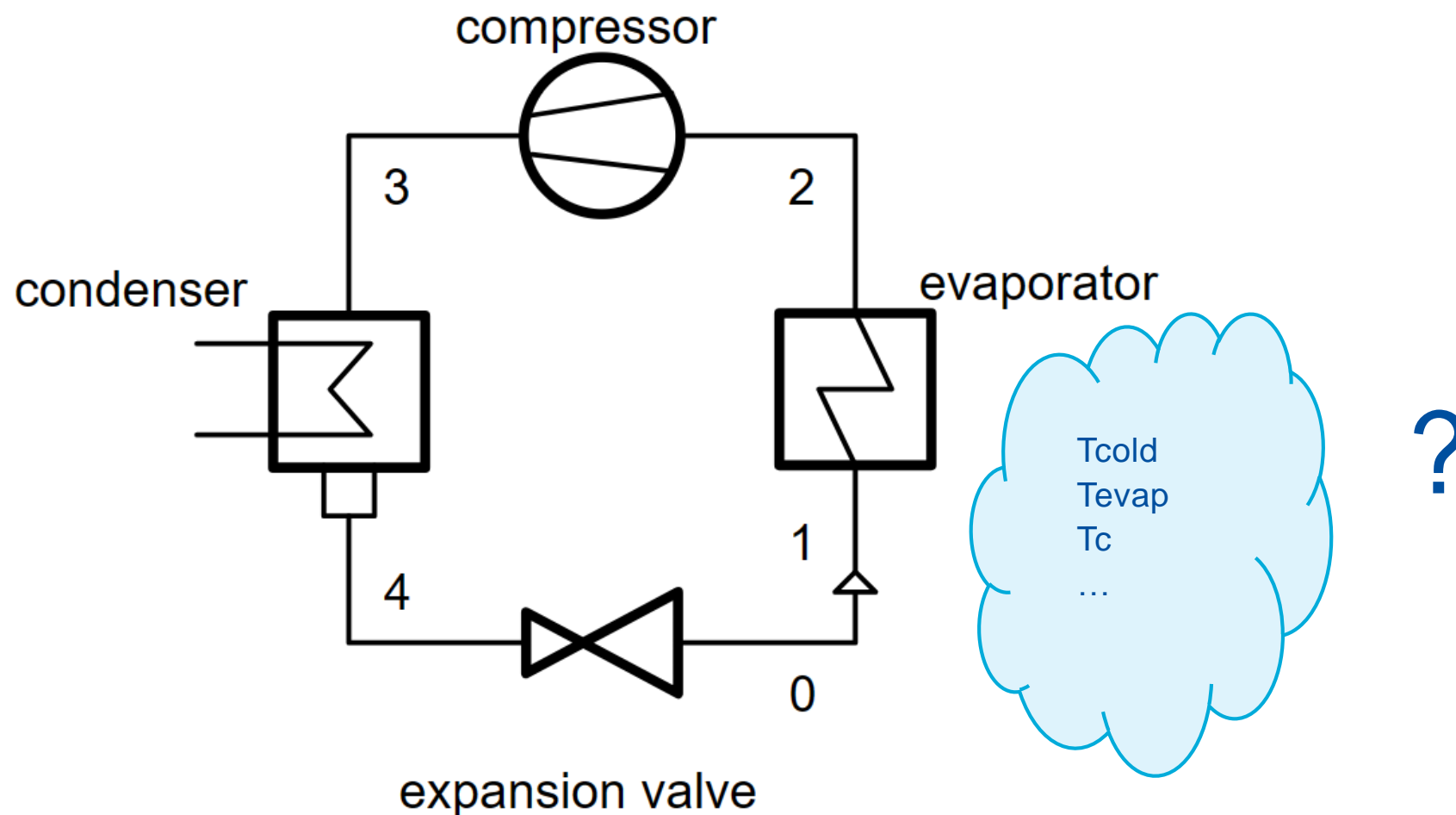
High pressure | Low pressure



# Heat pump overview

## The heat pump cycle

### Typical sources and sinks



**High pressure**

ca. 10 bar

Function of temperature!

**Low pressure**

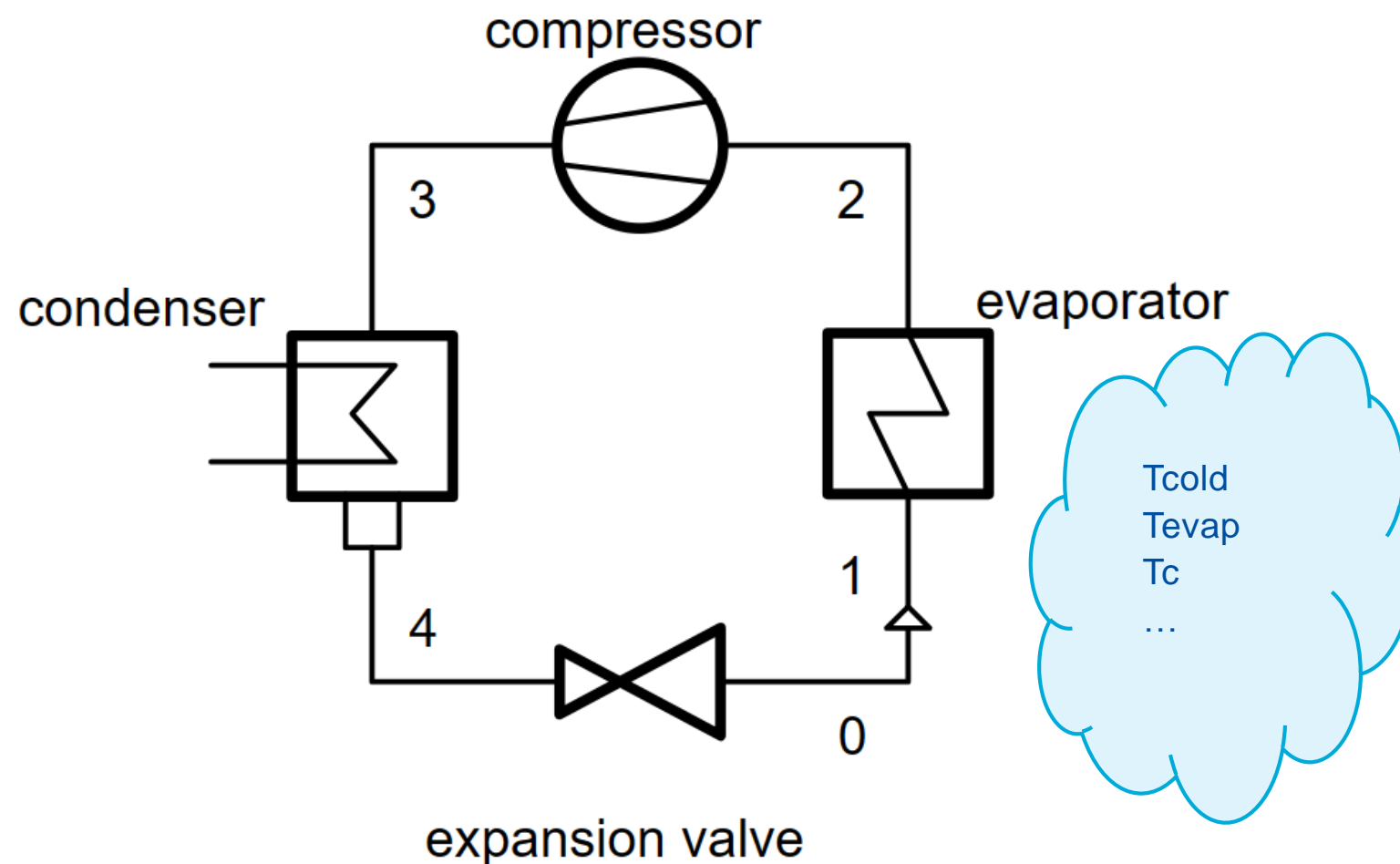
ca. 2 bar

Function of temperature!

# Heat pump overview

## The heat pump cycle

### Typical sources and sinks



Ambient air

Groundwater  
(or any other water  
source)

Waste heat

Solar thermal! ☺

**High pressure**

ca. 10 bar

Function of temperature!

**Low pressure**

ca. 2 bar

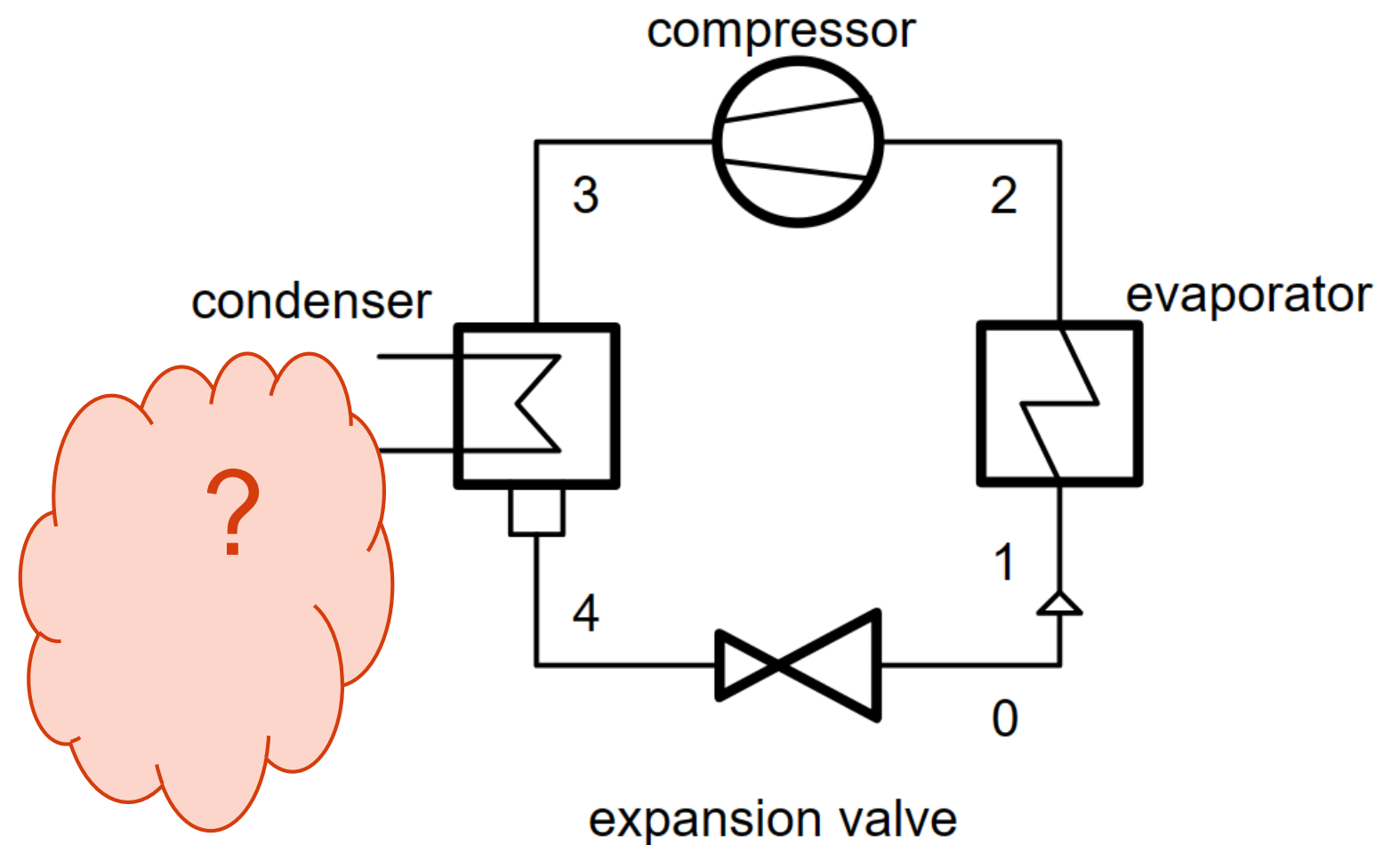
Function of temperature!



# Heat pump overview

## The heat pump cycle

### Typical sources and sinks



**High pressure**

ca. 10 bar

Function of temperature!

**Low pressure**

ca. 2 bar

Function of temperature!



# Heat pump overview

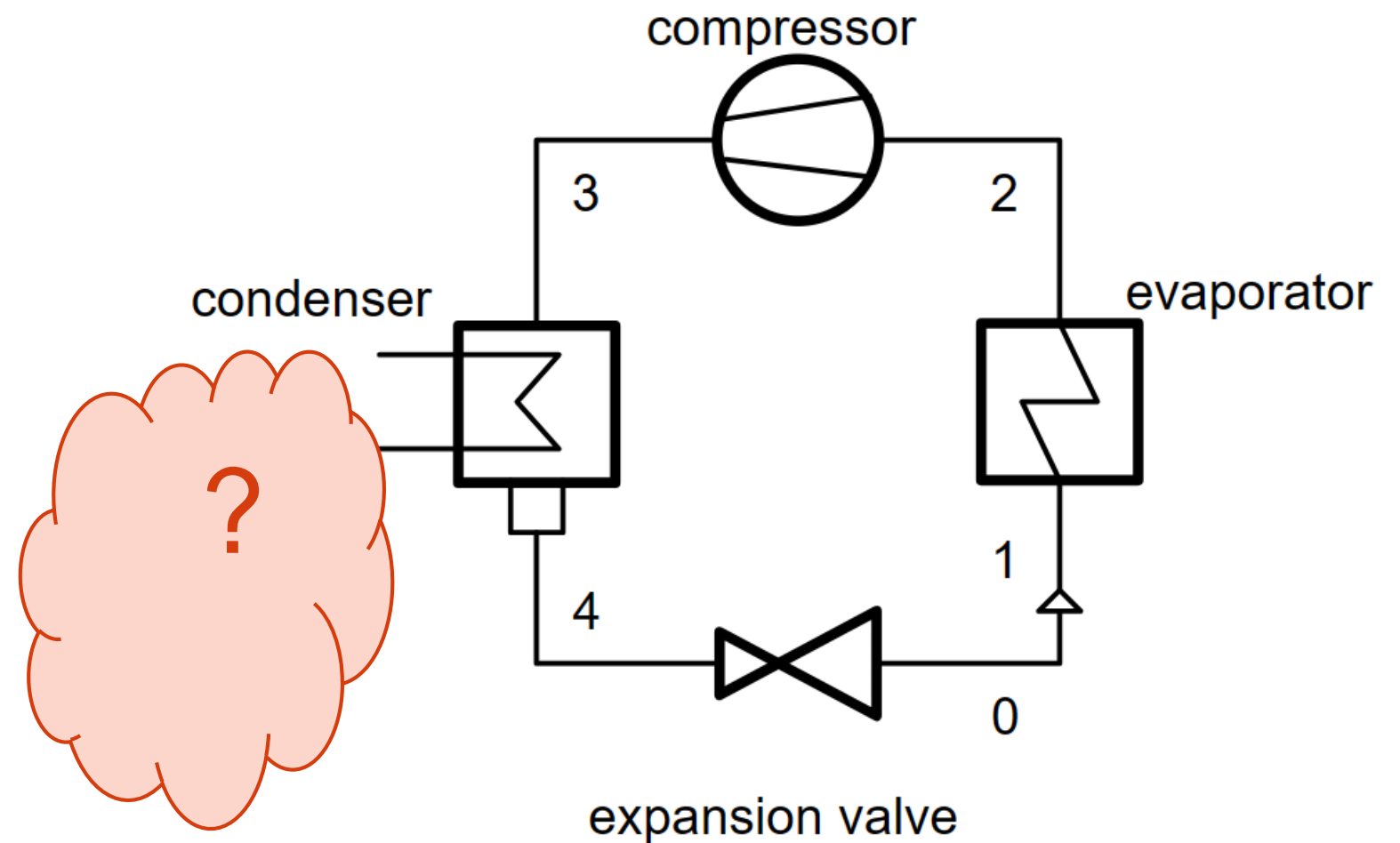
## The heat pump cycle

### Typical sources and sinks

Space heating

DHW

Industrial heat



**High pressure**

ca. 10 bar

Function of temperature!

**Low pressure**

ca. 2 bar

Function of temperature!

# Heat pump overview

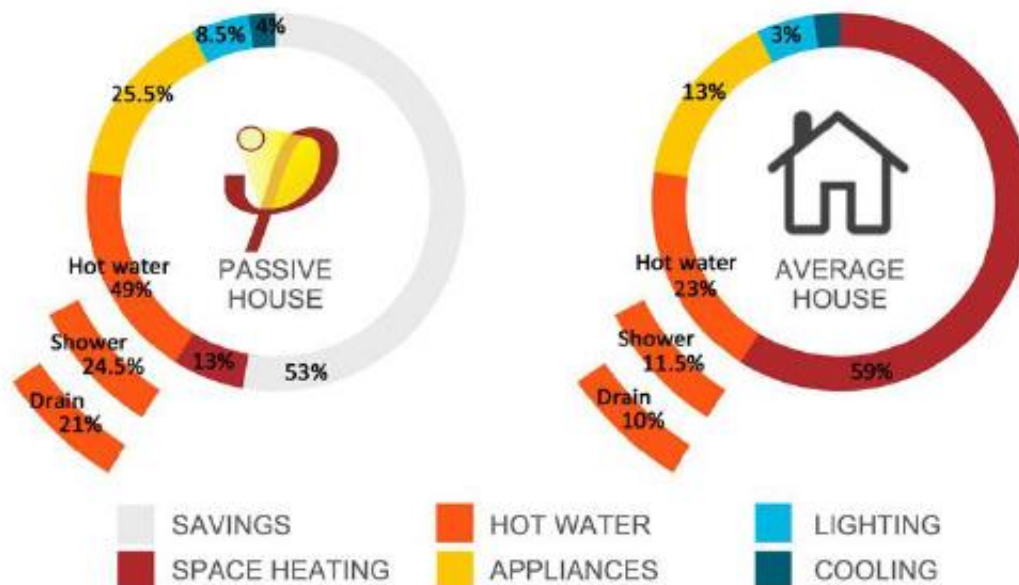
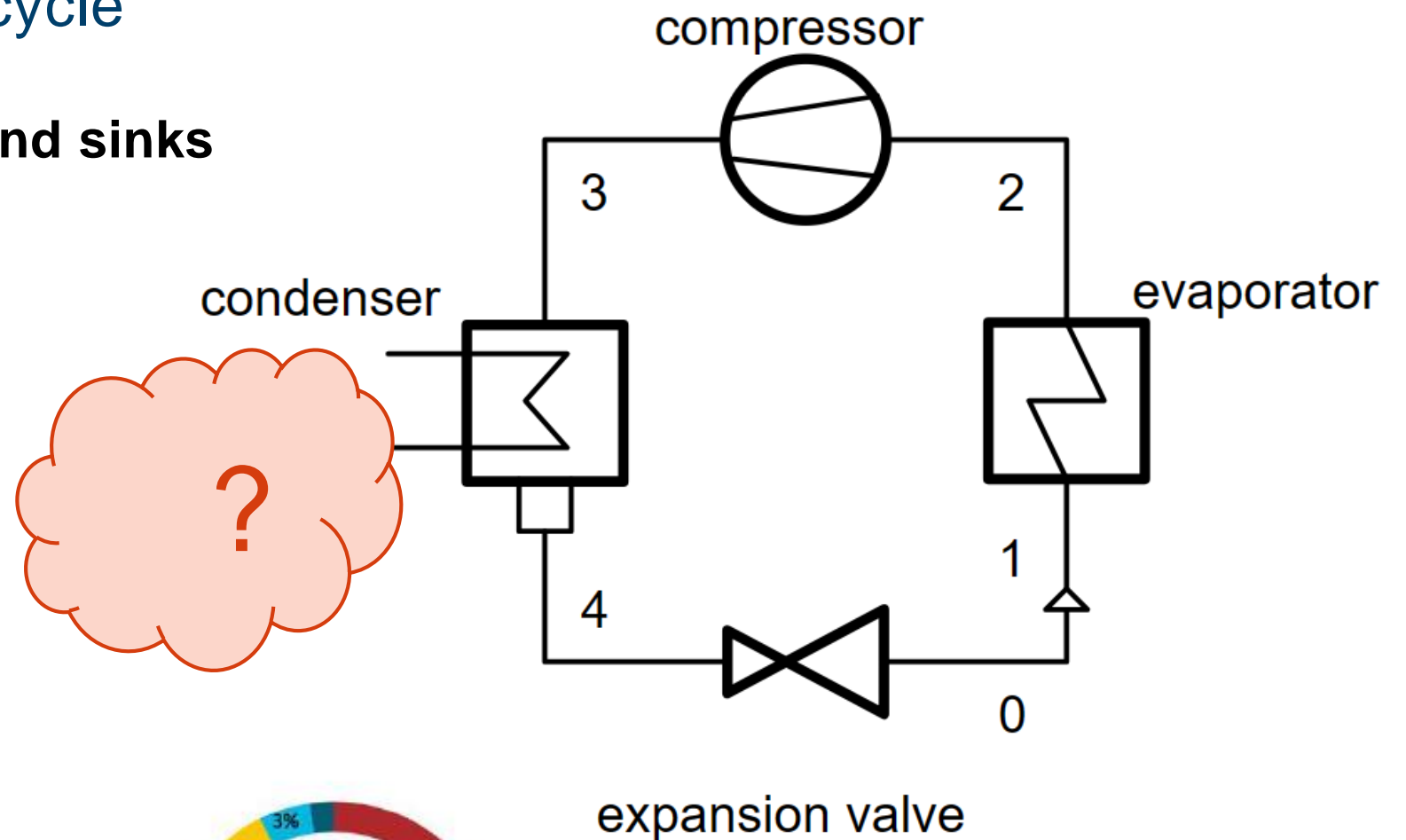
## The heat pump cycle

### Typical sources and sinks

Space heating

DHW

Industrial heat



### Small Excurs:

DHW demands on the rise, in share and importance

Source: Hervas, 2020

# Heat pump overview

## The heat pump cycle

### Typical sources and sinks



Source:Grassi, 2018

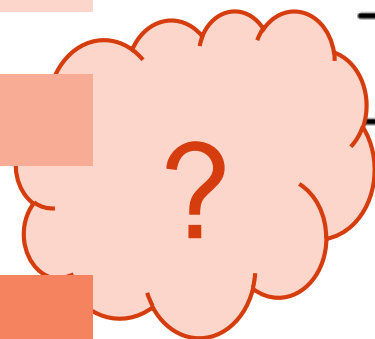
Air- based systems  
(secondary sideS)!!

Source:Grassi, 2018

Space heating

DHW

Industrial heat



Ambient air

Groundwater  
(or any other water  
source)

Waste heat

Solar thermal! ☺

condenser

evaporator

compressor

expansion valve

# Heat pump overview

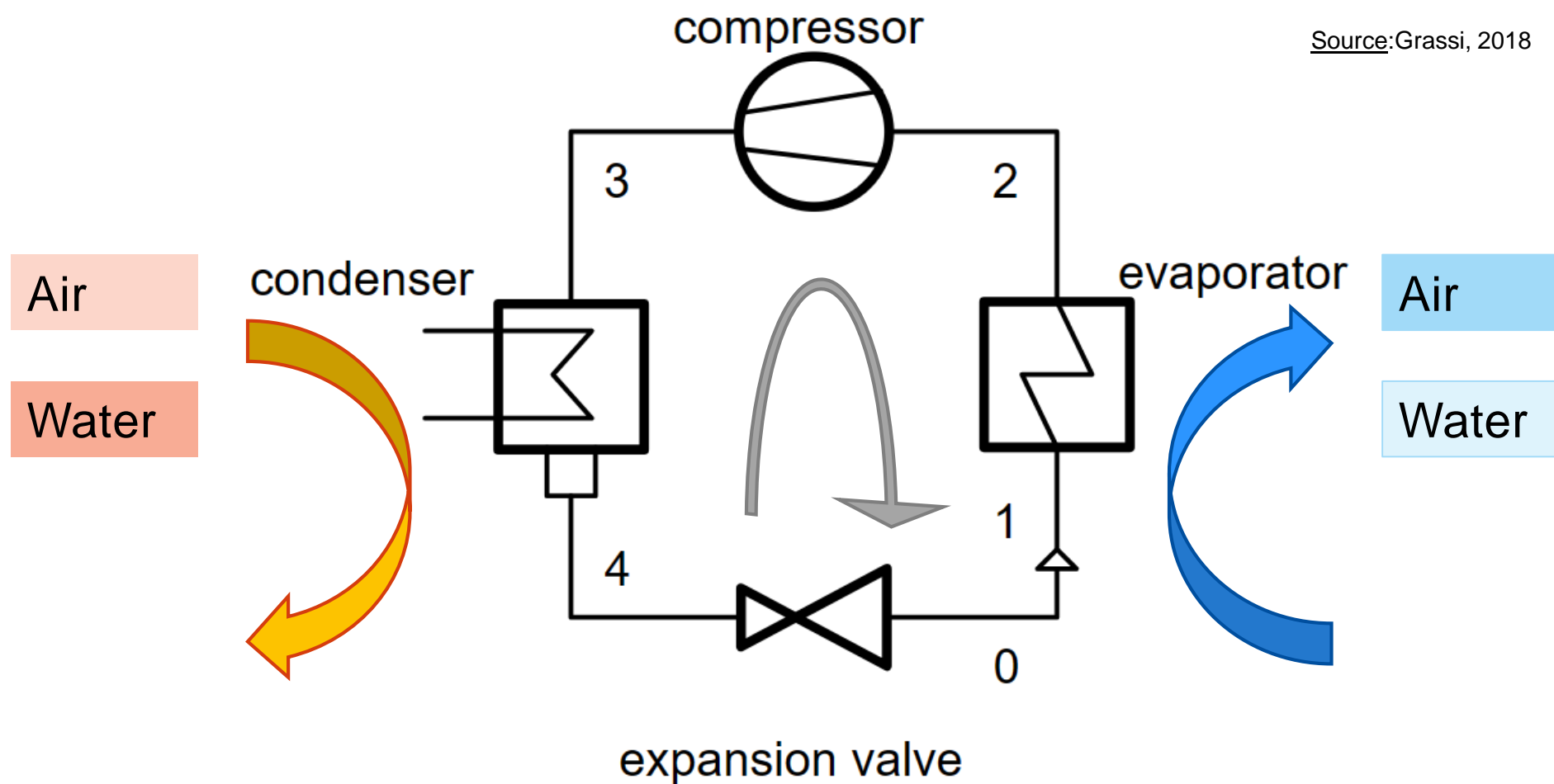
## The heat pump cycle

### Typical sources and sinks

Air- based systems  
(secondary sideS)!!



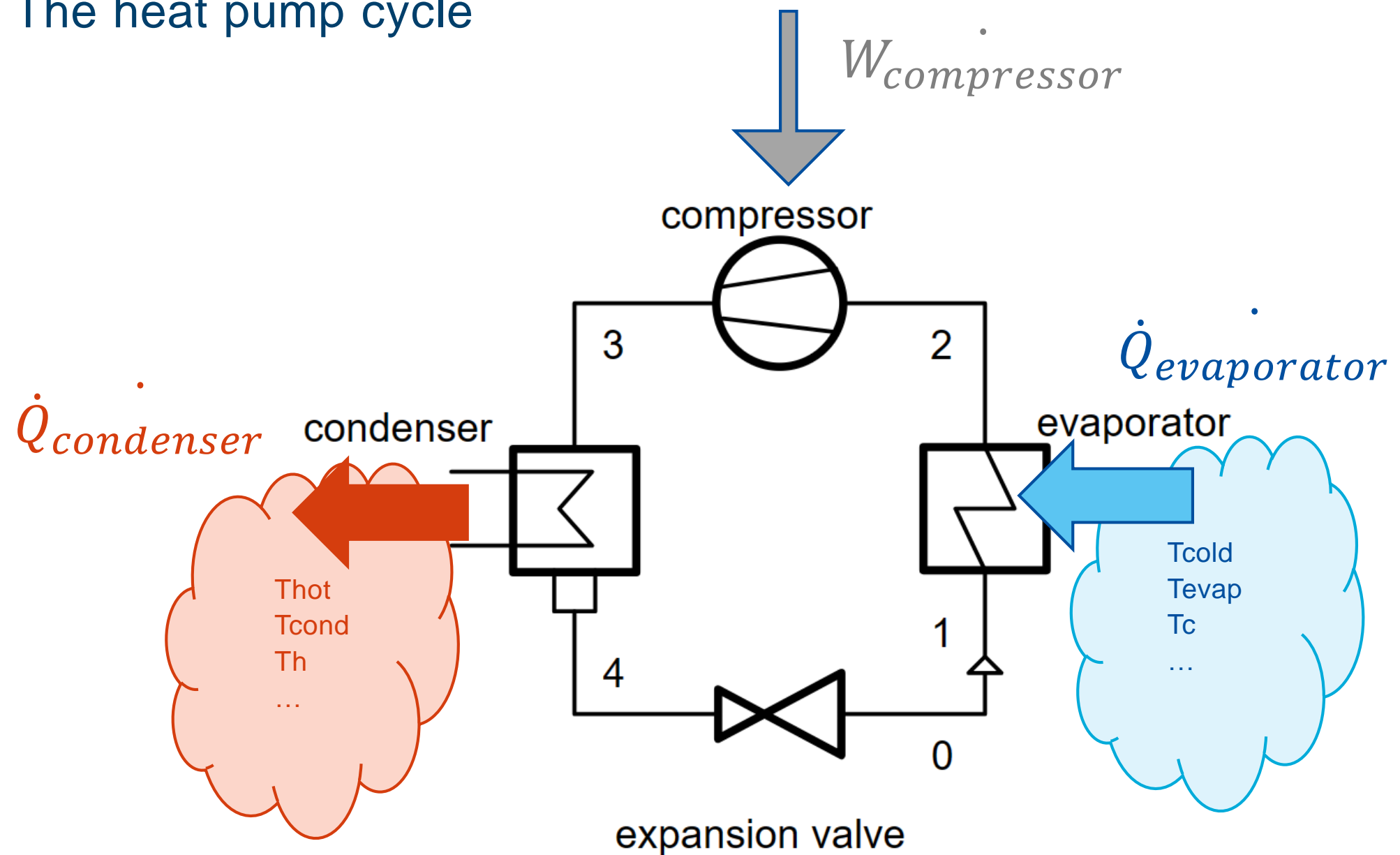
Source:Grassi, 2018



Source:Grassi, 2018

# Heat pump overview

## The heat pump cycle



$$COP = \frac{\dot{Q}_{condenser}}{\dot{W}_{compressor}}$$

# Agenda

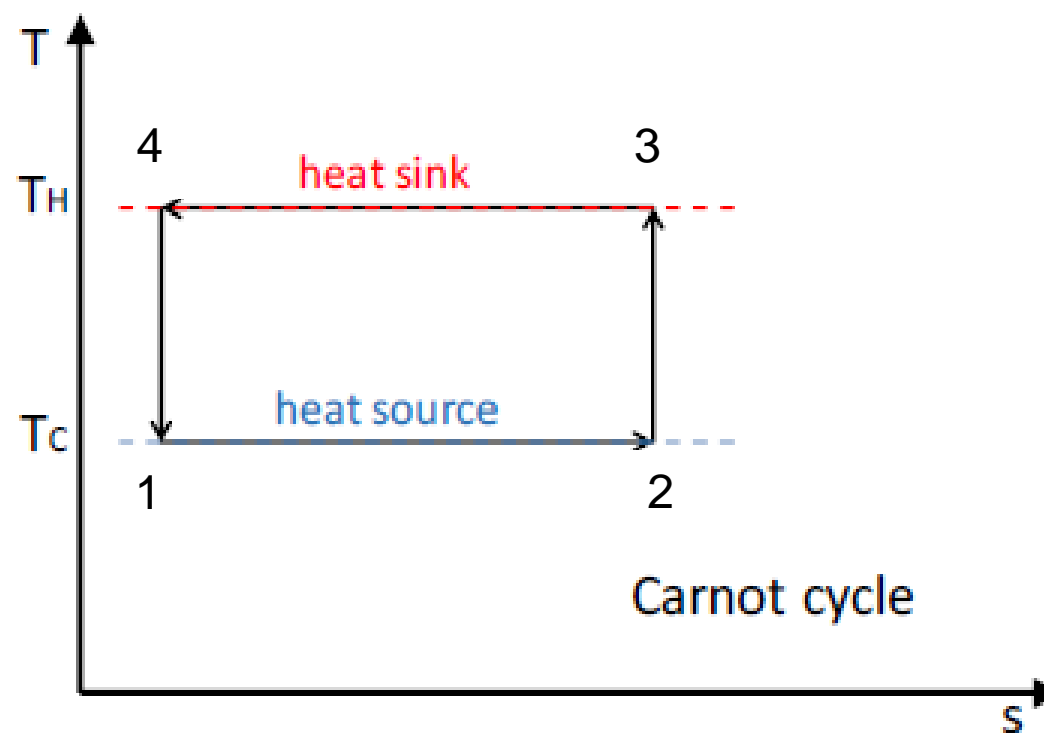
- Heat pump overview
- Re-visiting thermodynamics
- Components and cycles

# Heat pump overview

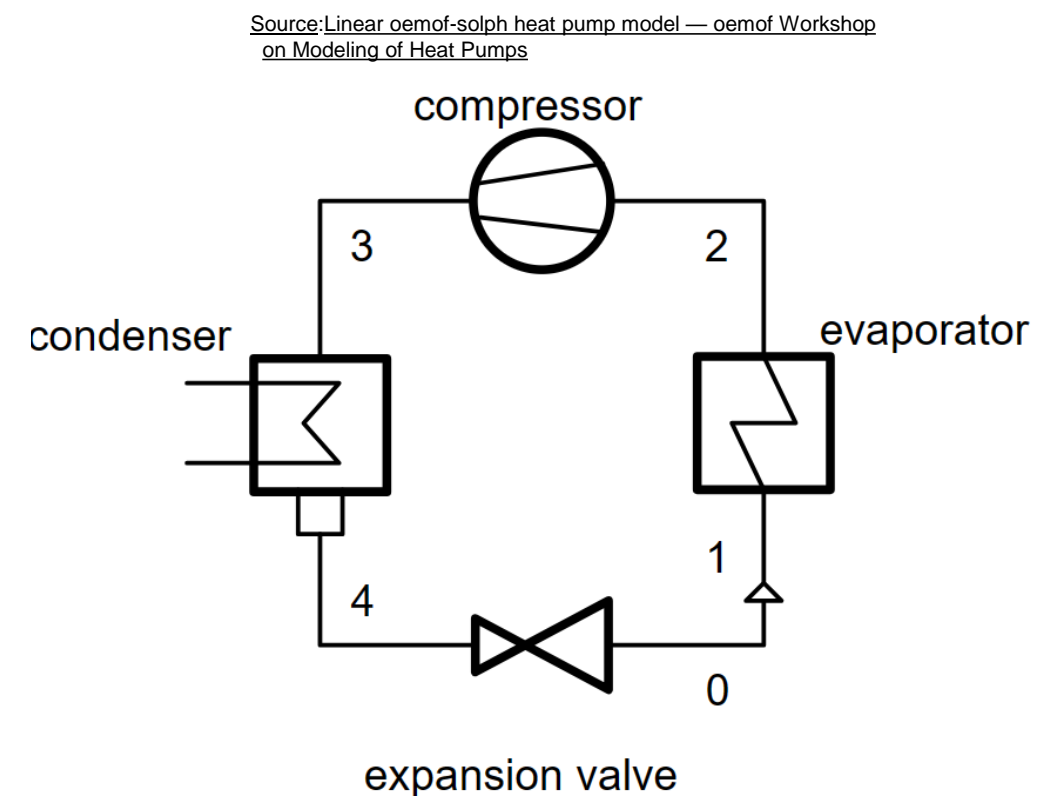
## The heat pump cycle

### Carnot approximation

Assumptions: → isothermal heat transfer at both source and sink  
→ infinite sink and reservoir (source)



$$\text{COP} = \frac{\dot{Q}_{\text{condenser}}}{W_{\text{compressor}}}$$





# Heat pump overview

## The heat pump cycle

### Carnot (ideal) COP

The ideal performance of a heat pump

$$\text{COP} = \frac{\dot{Q}_{\text{condenser}}}{W_{\text{compressor}}}$$

Energy balance

$$\dot{Q}_{\text{cond.}} = W_{\text{compr.}} + \dot{Q}_{\text{evap.}}$$

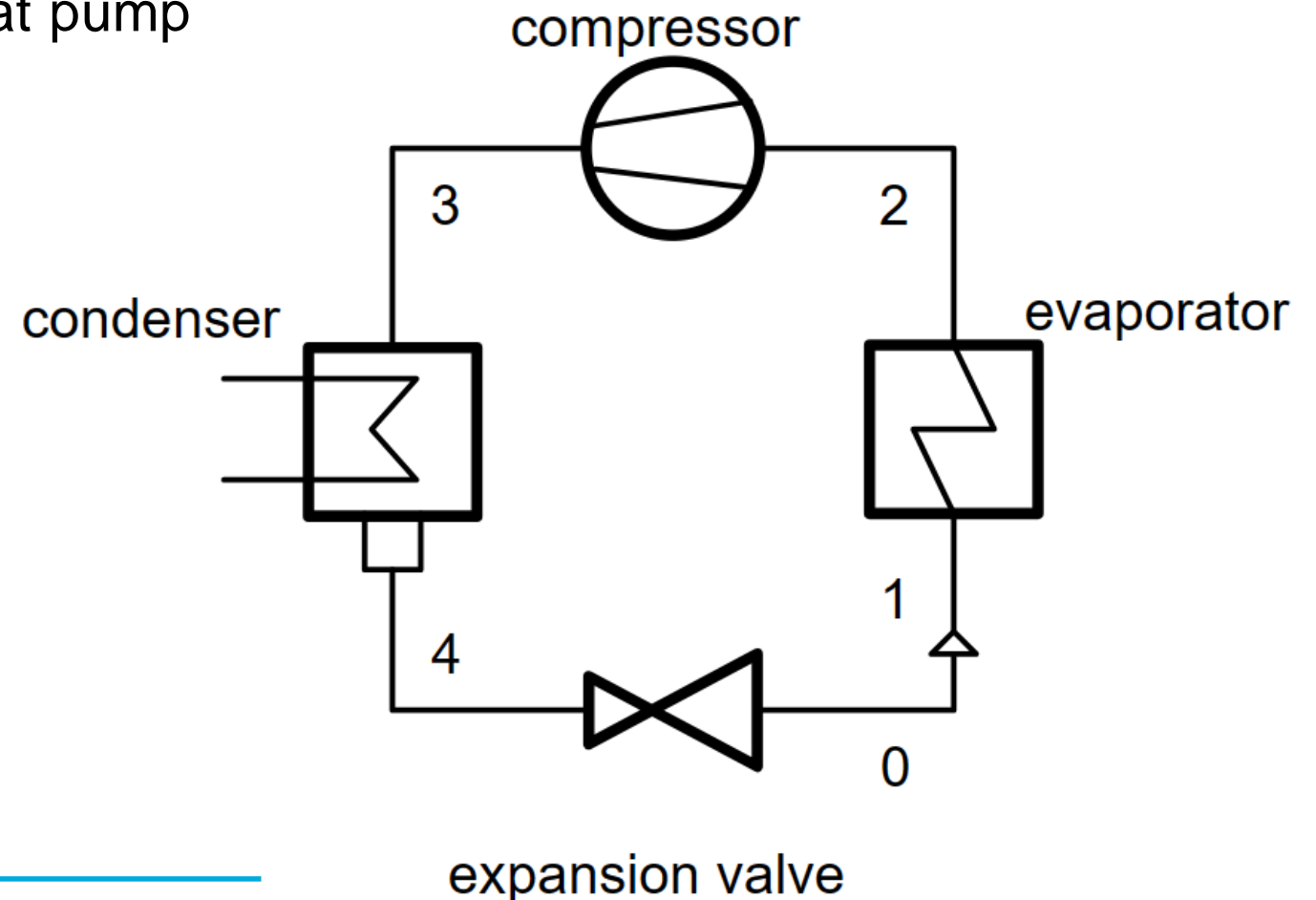
$$\text{COP} = \frac{\dot{Q}_{\text{cond.}}}{\dot{Q}_{\text{cond.}} - \dot{Q}_{\text{evap.}}}$$

Assumption: ideal heat transfer (isothermal),

Temperatures are considered at the „secondary side“ of the cond/evap

$$\text{COP}_{\text{Carnot}} = \frac{T_{\text{cond}}}{T_{\text{cond}} - T_{\text{evap}}} = \frac{T_h}{T_h - T_c} = \frac{T_4}{T_4 - T_2}$$

Source: Linear oemof-solph heat pump model — oemof Workshop  
on Modeling of Heat Pumps

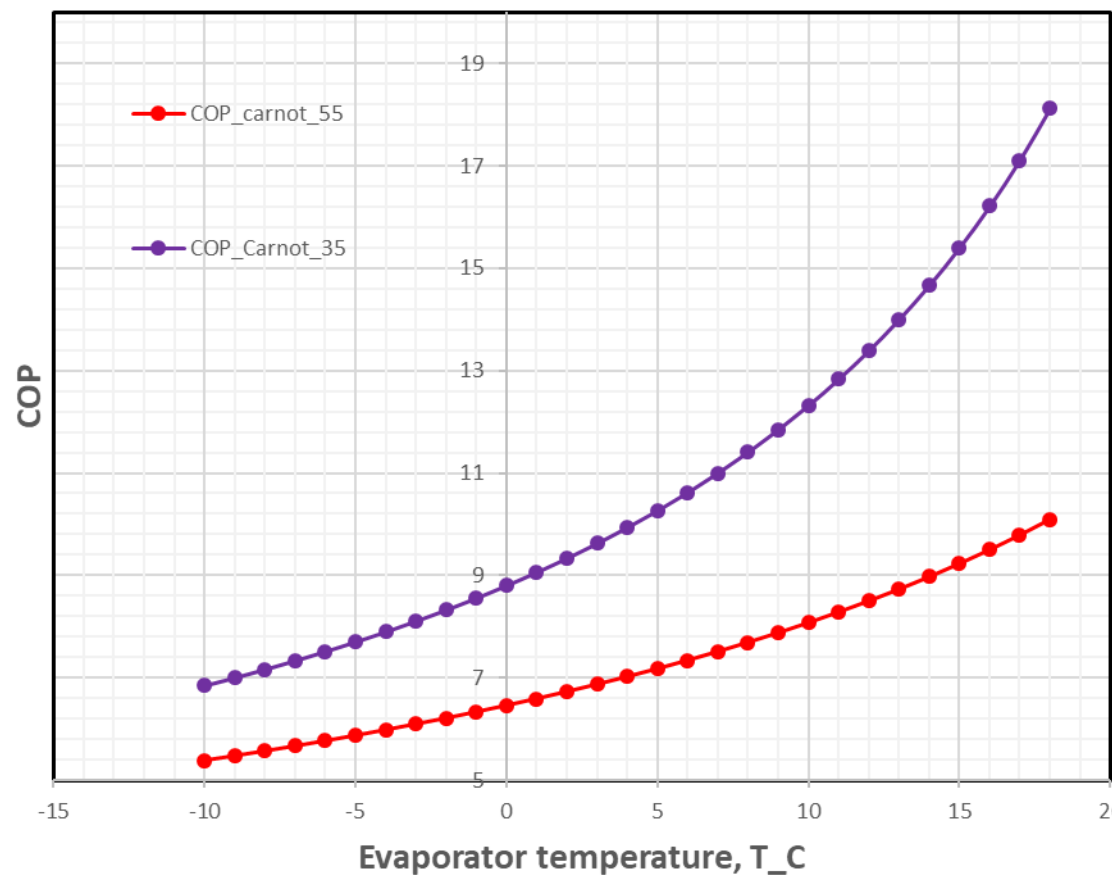


# Heat pump overview

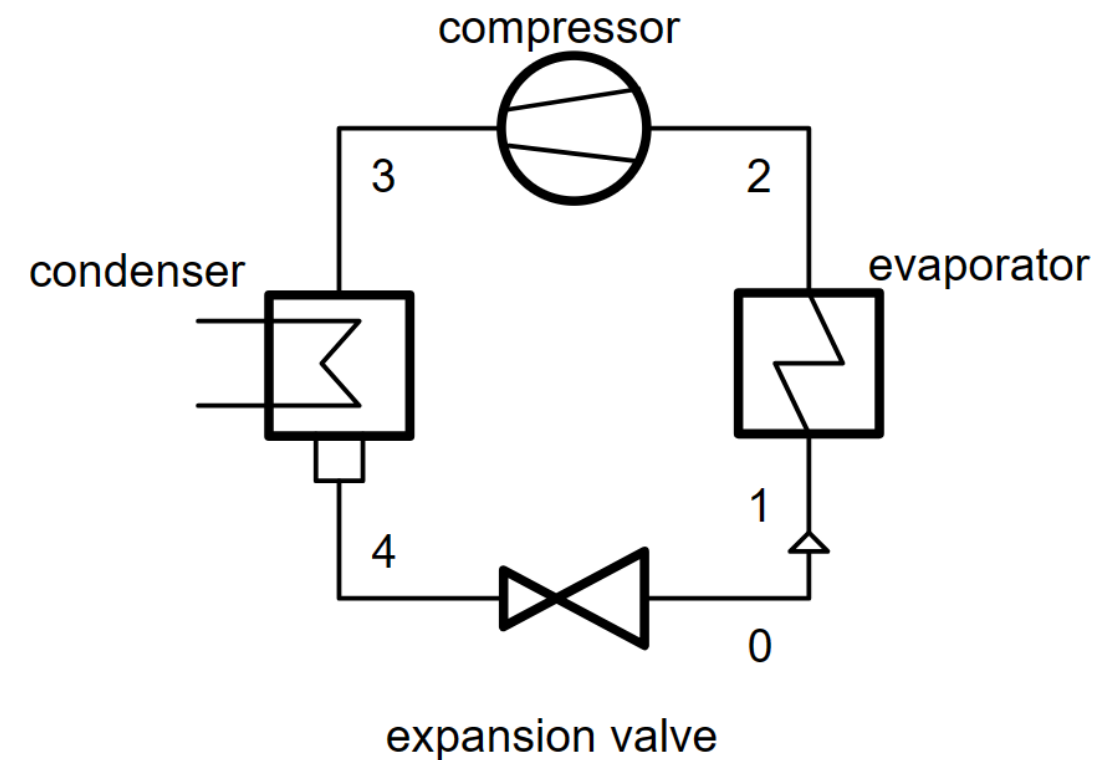
## The heat pump cycle

### Carnot (ideal) COP

The ideal performance of a heat pump



Source: Linear oemof-solph heat pump model — oemof Workshop  
on Modeling of Heat Pumps



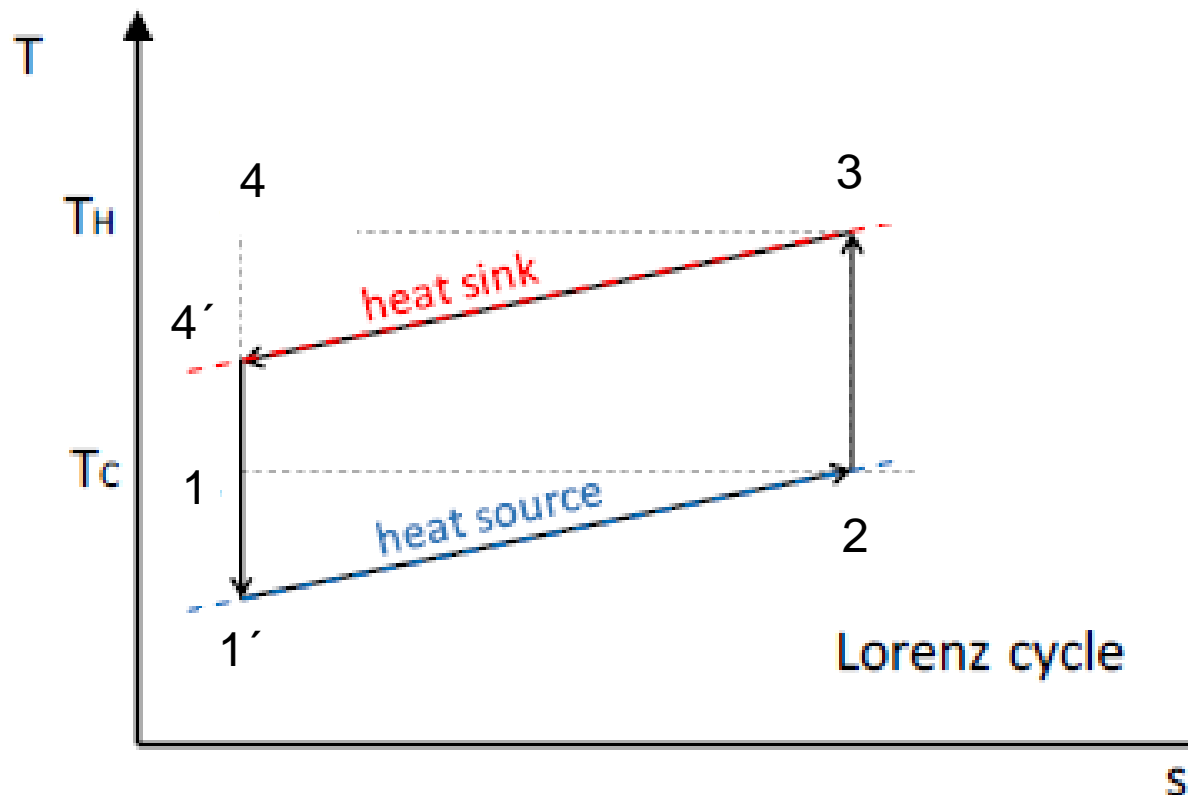
$$\text{COP}_{\text{Carnot}} = \frac{T_{\text{cond}}}{T_{\text{cond}} - T_{\text{evap}}} = \frac{T_h}{T_h - T_c} = \frac{T_4}{T_4 - T_2}$$

# Heat pump overview

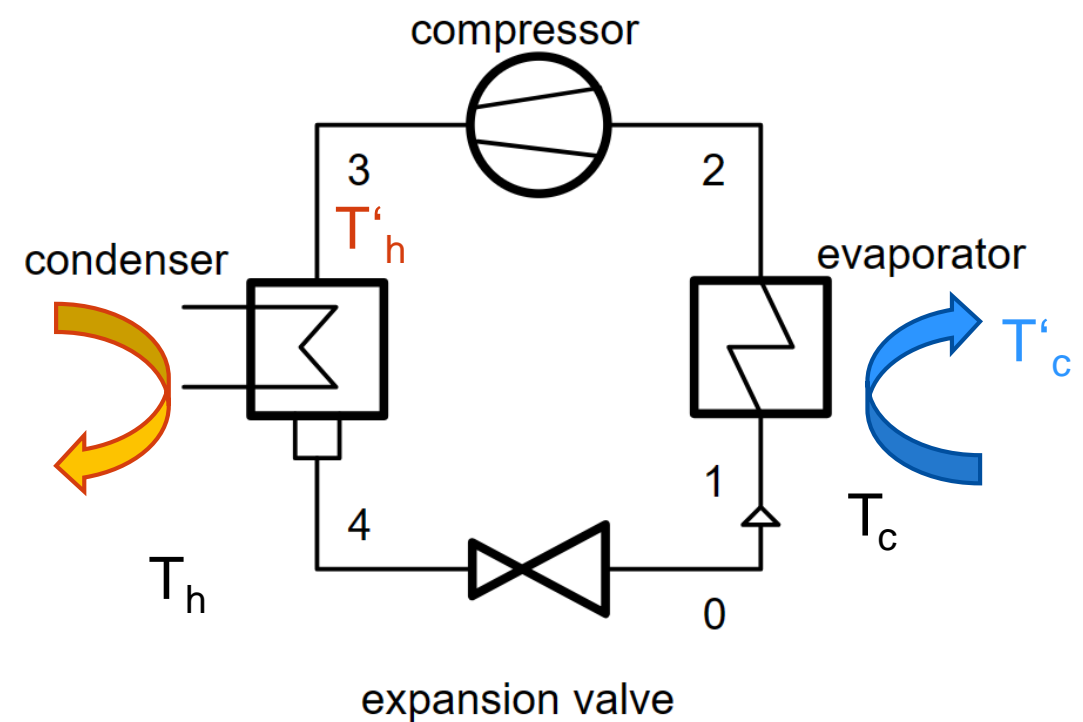
## The heat pump cycle

### Lorenz approximation

Assumptions: → non-isothermal heat transfer at both source and sink  
→ temperature gradients at sink and reservoir (source)



Source: Linear oemof-solph heat pump model —



$$COP = \frac{\dot{Q}_{cond}}{W_{compr}} = \frac{\dot{Q}_{3-4'}}{W_{3-2}}$$

# Heat pump overview

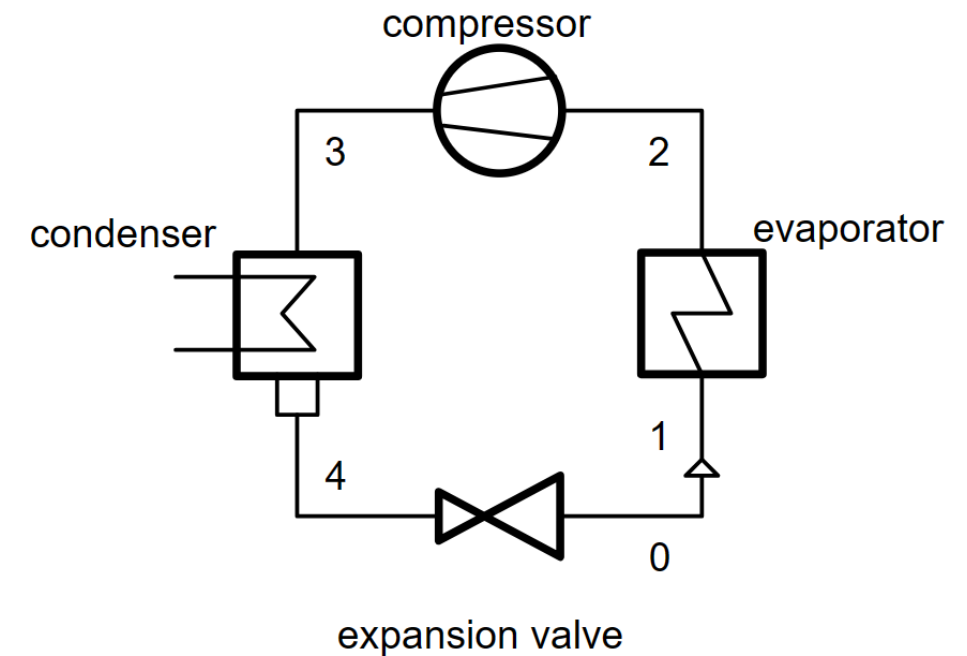
## The heat pump cycle

### Lorenz COP

The ideal performance of a heat pump

$$COP = \frac{\dot{Q}_{cond}}{W_{compr}} = \frac{\dot{Q}_{3-4'}}{W_{3-2}} = \frac{\bar{T}_H (s_2 - s_1)}{(\bar{T}_H - \bar{T}_C) (s_2 - s_1)}$$

$\bar{T}_H, \bar{T}_C$  Entropy-averaged temperatures = avg. Temperature in T-S diagram representing avg. Temperature difference

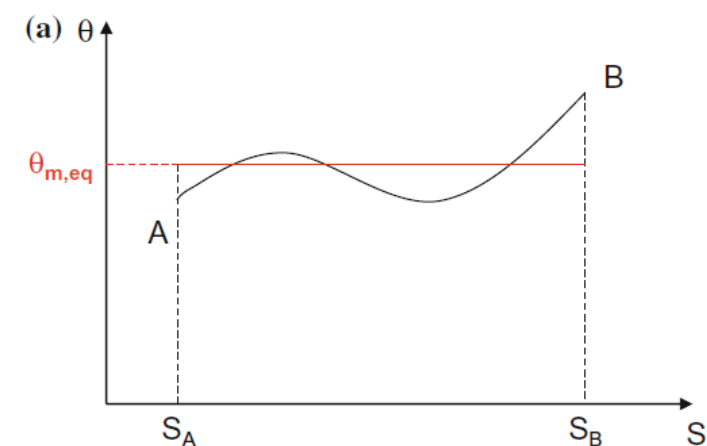
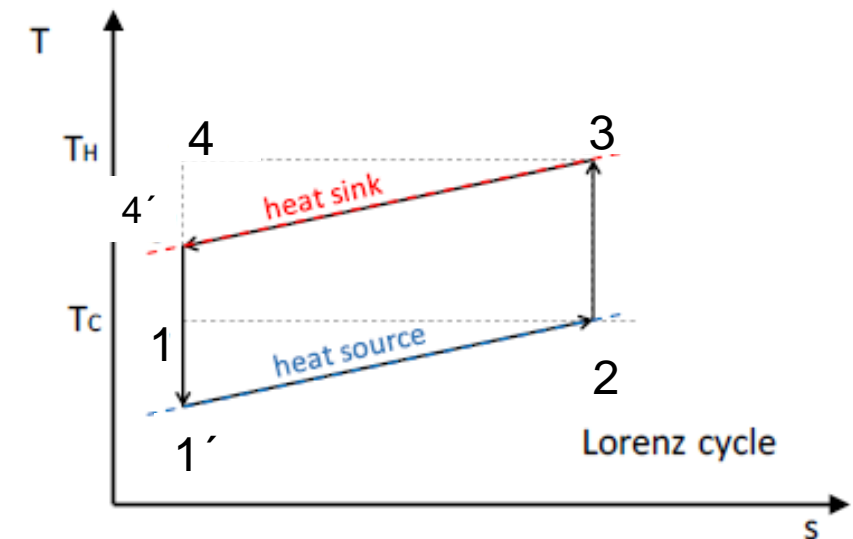


**Assumptions:**  $\dot{m}c_p = \text{constant}$   
pressure,  $p_H, p_C = \text{constant}$

$$\bar{T}_H = \frac{h_3 - h_{4'}}{s_3 - s_{4'}} = \frac{T_3 - T_{4'}}{\ln\left(\frac{T_3}{T_{4'}}\right)}$$

$$\bar{T}_C = \frac{h_2 - h_{1'}}{s_2 - s_{1'}} = \frac{T_2 - T_{1'}}{\ln\left(\frac{T_2}{T_{1'}}\right)}$$

$$COP_{Lorenz} = \frac{\dot{Q}_{cond}}{W_{compr}} = \frac{\bar{T}_H (s_2 - s_1)}{(\bar{T}_H - \bar{T}_C) (s_2 - s_1)} = \frac{1}{1 - \frac{\bar{T}_C}{\bar{T}_H}}$$



# Heat pump overview

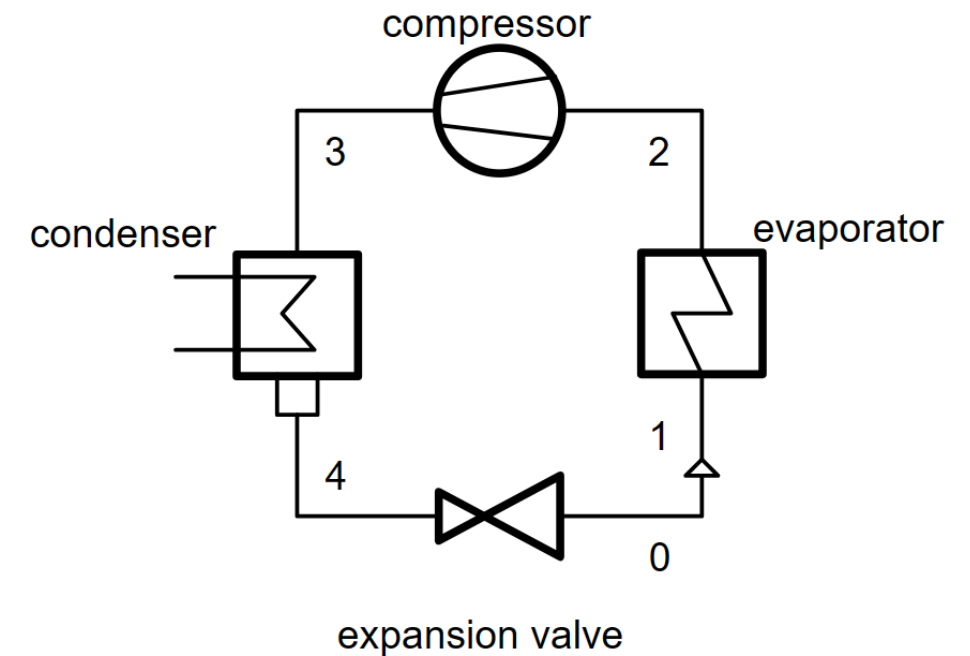
## The heat pump cycle

### Lorenz + Carnot COP

The ideal performance of a heat pump

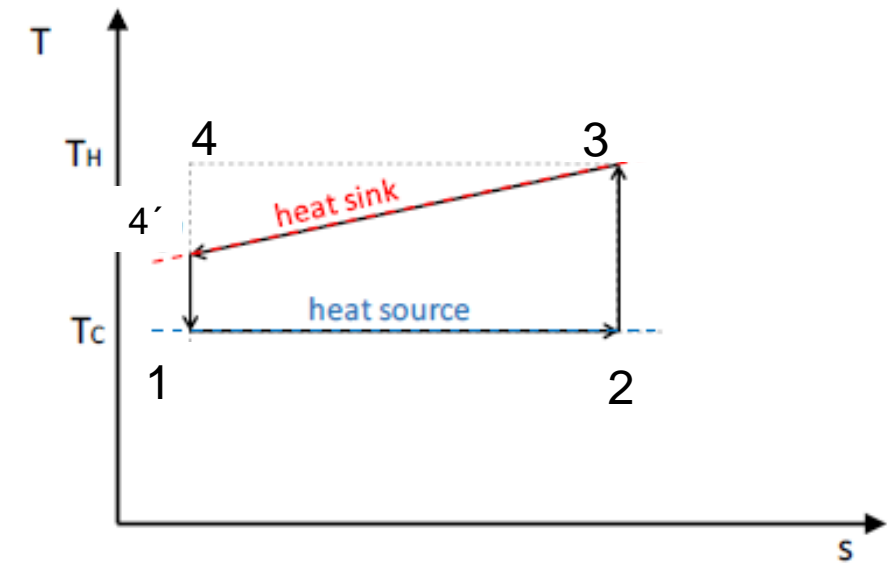
$$COP = \frac{\dot{Q}_{cond}}{W_{compr}} = \frac{\dot{Q}_{3-4'}}{W_{1-2}} = \frac{\bar{T}_H (s_2 - s_1)}{(\bar{T}_H - \bar{T}_C) (s_2 - s_1)}$$

$\bar{T}_H, \bar{T}_C$  Entropy-averaged temperatures = avg. Temperature in T-S diagram representing avg. Temperature difference



**Assumptions:**  $\dot{m}c_p = \text{constant}$   
pressure,  $p_H, p_C = \text{constant}$

$$\bar{T}_H = \frac{h_3 - h_{4'}}{s_3 - s_{4'}} = \frac{T_3 - T_{4'}}{\ln\left(\frac{T_3}{T_{4'}}\right)}$$



$\bar{T}_C = T_C$ , infinite sink/source, constant temperature

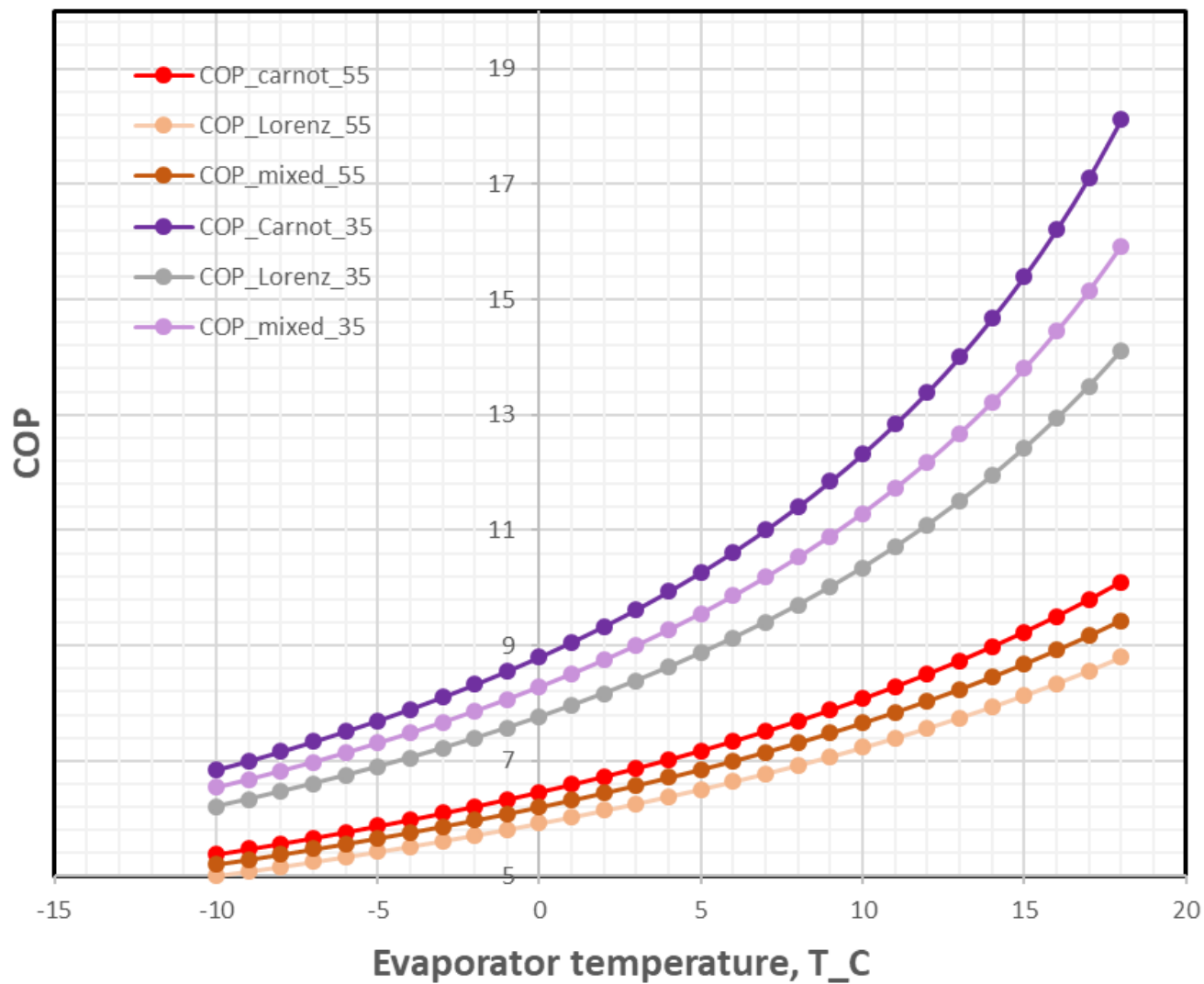
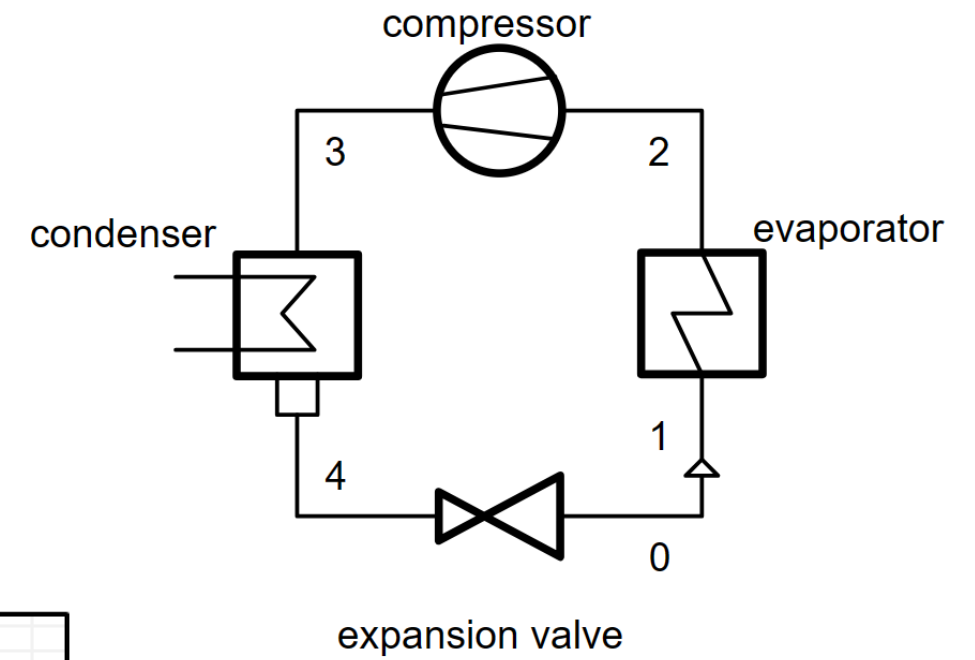
$$COP_{mixed} = \frac{\dot{Q}_{cond}}{W_{compr}} = \frac{\bar{T}_H (s_2 - s_1)}{(\bar{T}_H - \bar{T}_C) (s_2 - s_1)} = \frac{1}{1 - \frac{T_C}{\bar{T}_H}}$$

# Heat pump overview

## The heat pump cycle

### Lorenz + Carnot COP

The ideal performance of a heat pump



# Heat pump overview

## The heat pump cycle

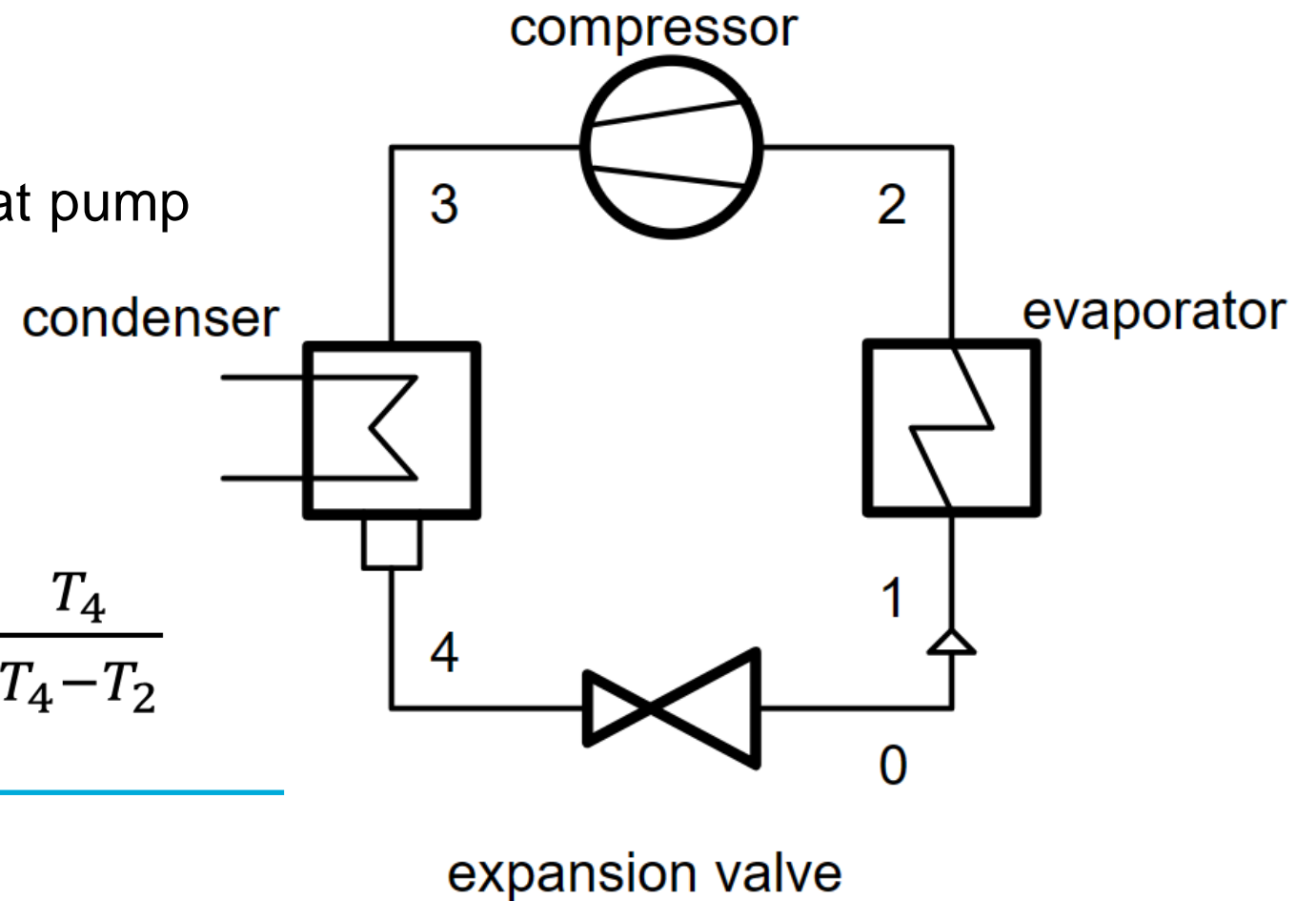
### Real (and ideal) COP

The ideal performance of a heat pump

$$COP = \frac{\dot{Q}_{condenser}}{W_{compressor}}$$

$$COP_{Carnot} = \frac{T_h}{T_h - T_c} = \frac{T_4}{T_4 - T_2}$$

Source: Linear oemof-solph heat pump model — oemof Workshop  
on Modeling of Heat Pumps



$$\eta_{hp} = \frac{COP}{COP_{Carnot}}$$

Characterizes how far the **real performance** deviates from an ideal one.  
Calibration parameter



# Heat pump overview

## The heat pump cycle

### Real (and ideal) COP

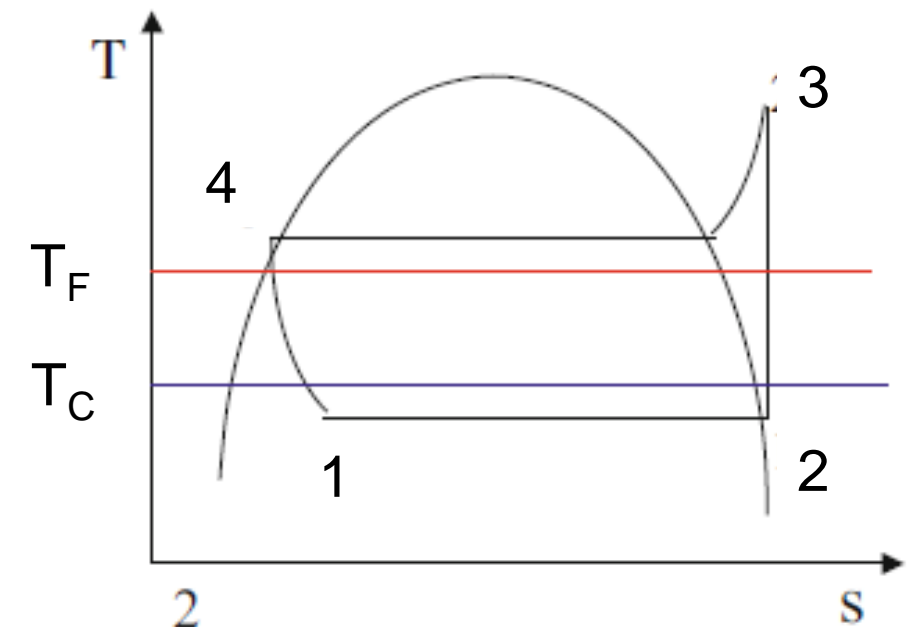
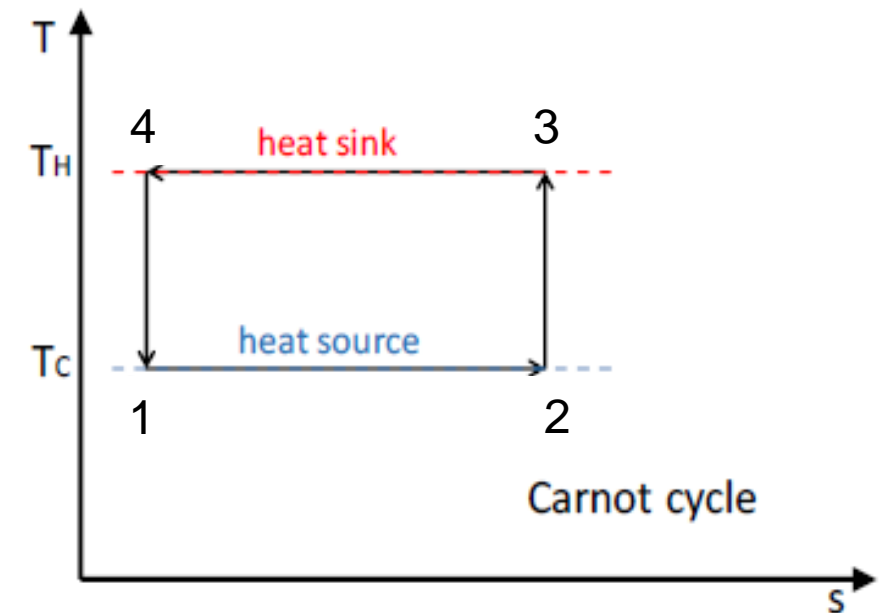
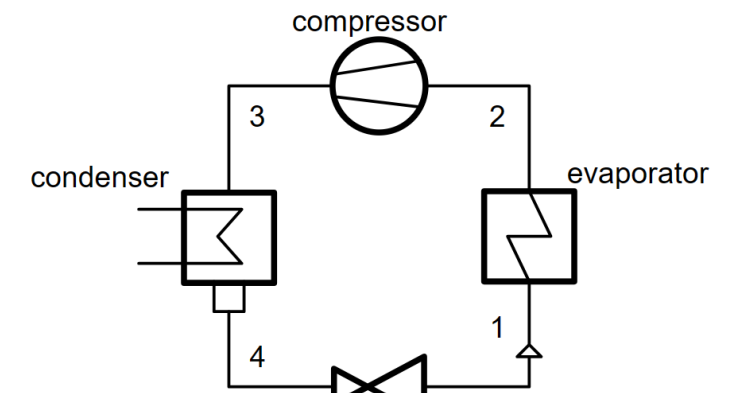
The real performance of a heat pump

$$\text{COP} = \frac{\dot{Q}_{\text{condenser}}}{W_{\text{compressor}}}$$

$$\text{COP}_{\text{Carnot}} = \frac{T_h}{T_h - T_c} = \frac{T_4}{T_4 - T_2}$$

$$\eta_{hp} = \frac{\text{COP}}{\text{COP}_{\text{Carnot}}}$$

Characterizes how far the **real performance** deviates from an ideal one.  
Calibration parameter



# Heat pump overview

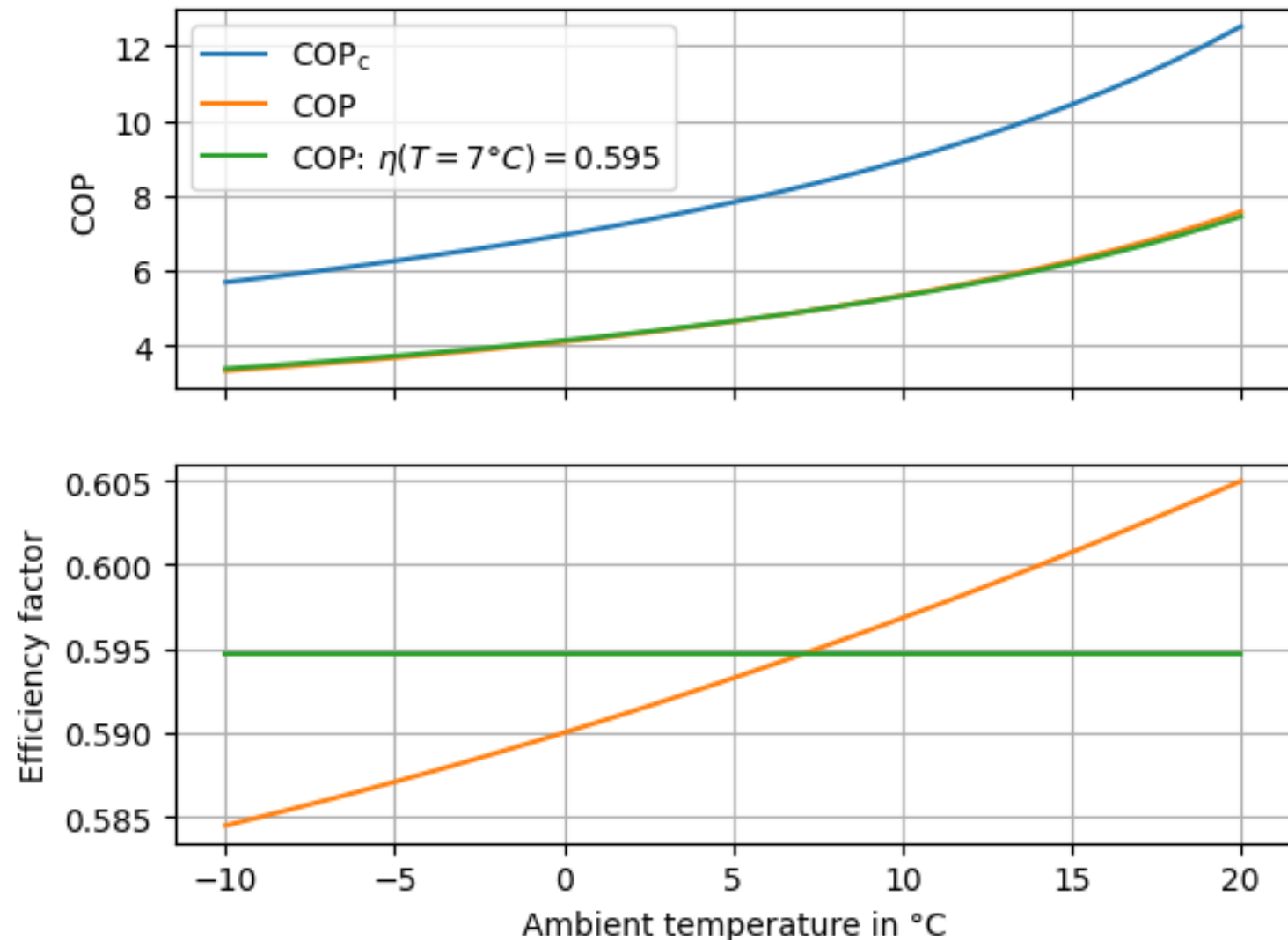
## The heat pump cycle

### Real (and ideal) COP

The real performance of a heat pump

$$\eta_{hp} = \frac{COP}{COP_{Carnot}}$$

- Characterizes how far the real performance deviates from an ideal one.
- Calibration parameter; assumed to be **constant** often!
- Assuming constant compressor efficiency



# Heat pump overview

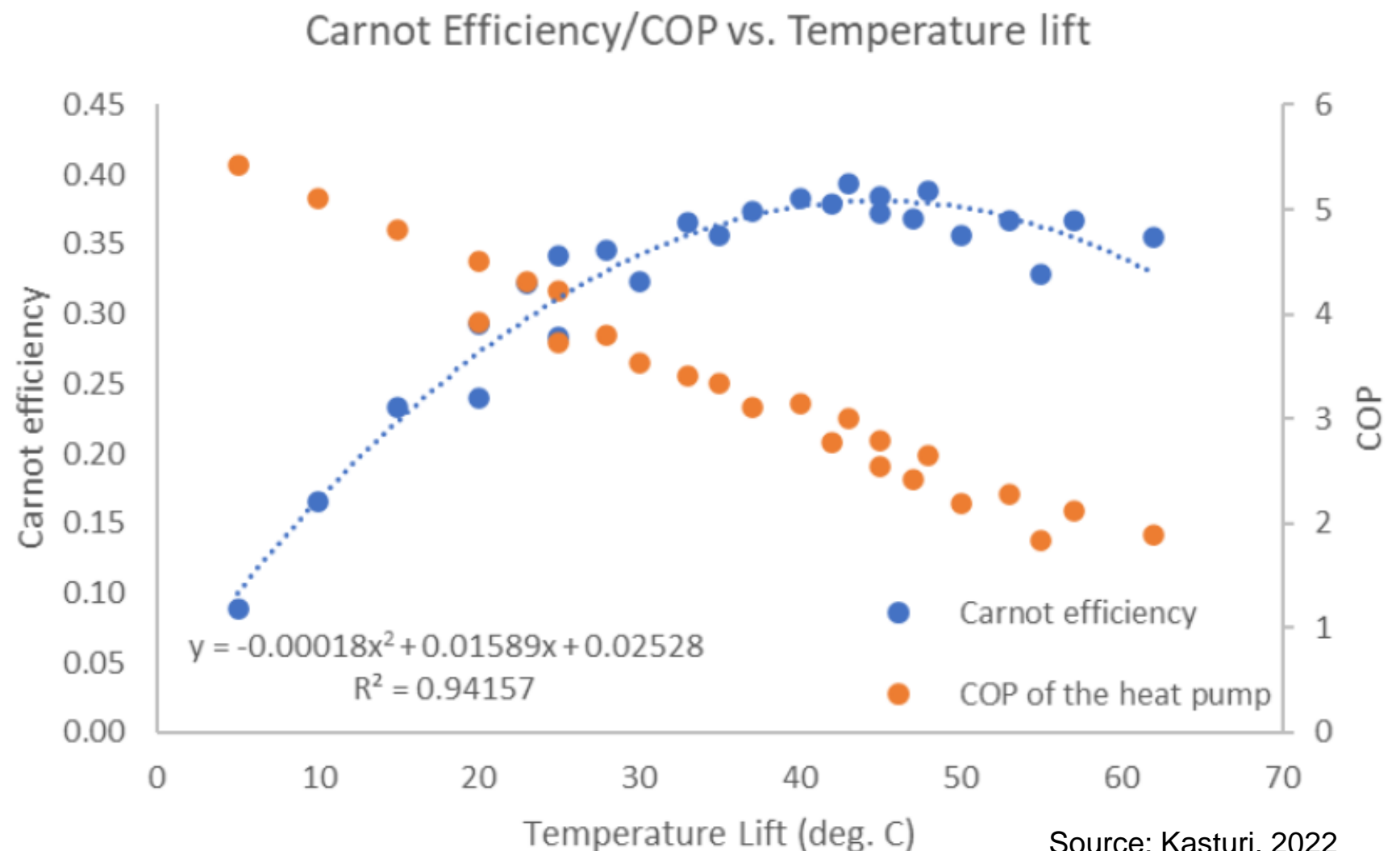
## The heat pump cycle

### Real (and ideal) COP

The real performance of a heat pump

$$\eta_{hp} = \frac{COP}{COP_{Carnot}}$$

- Carnot efficiencies are rather low
- Lower carnot efficiencies at lower temperature lifts,  $T_H - T_C$



# Agenda

- Heat pump overview
- Re-visiting thermodynamics
- Components and cycles

# Heat pump overview

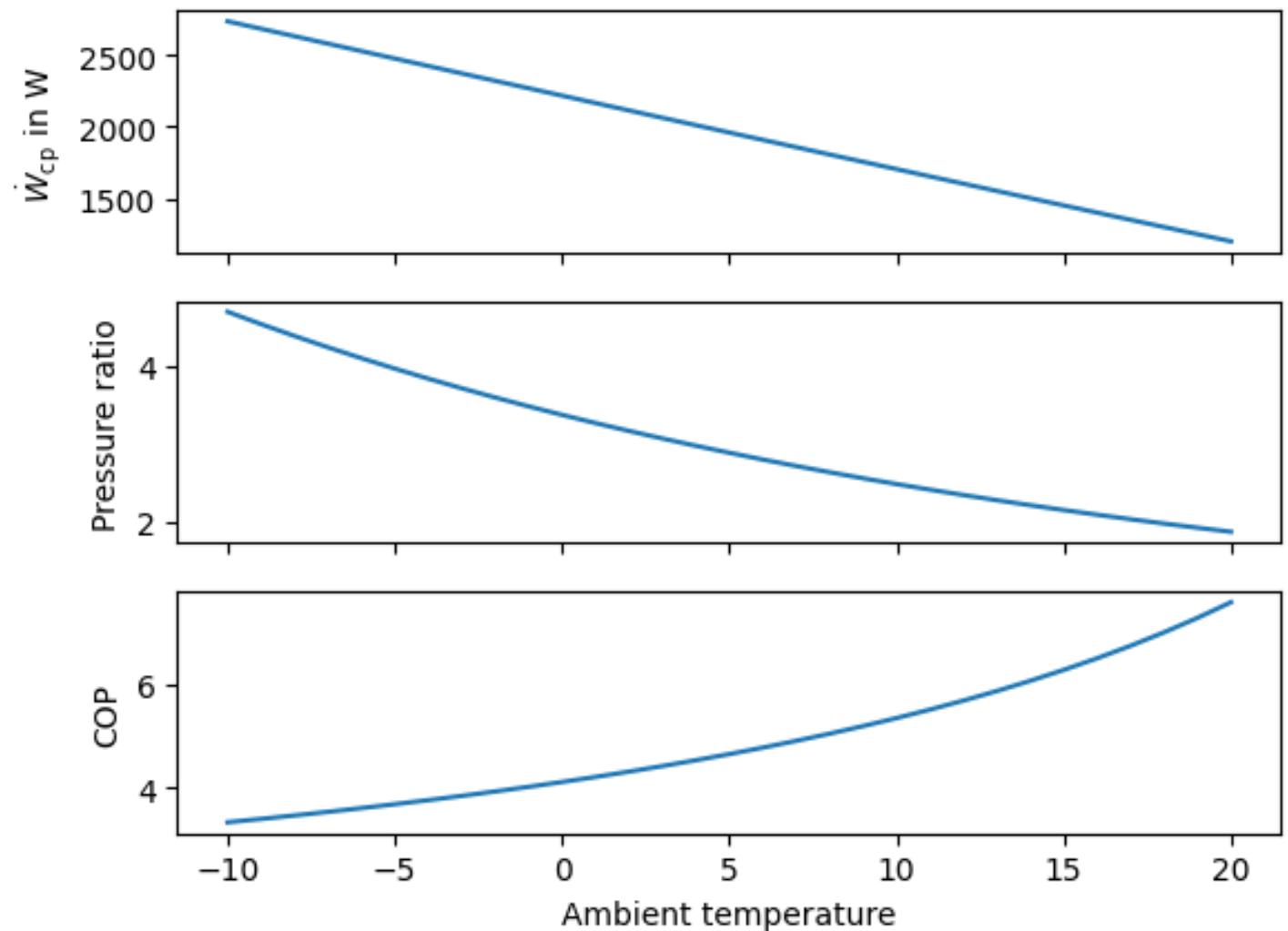
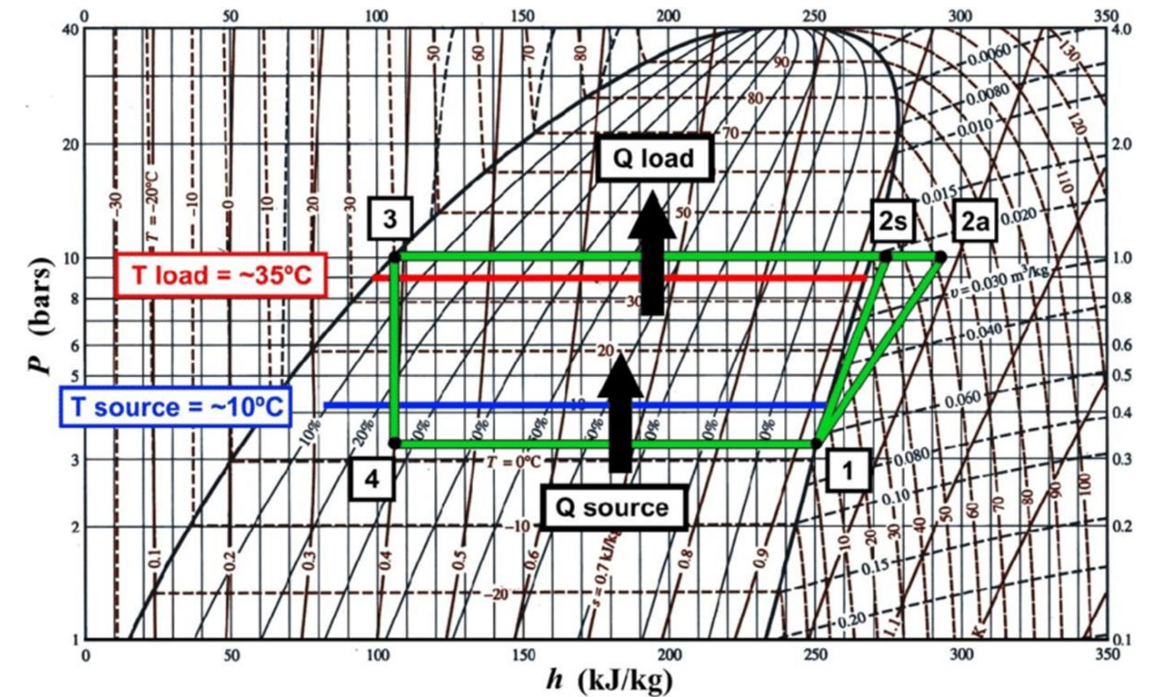
## The heat pump cycle

### Full load

Compressor efficiency can be considered as constant (calibration point)

Pressure ratio and electrical input decline with increasing source temperature

COP dependent on Temperatures



# Heat pump overview

## The heat pump cycle

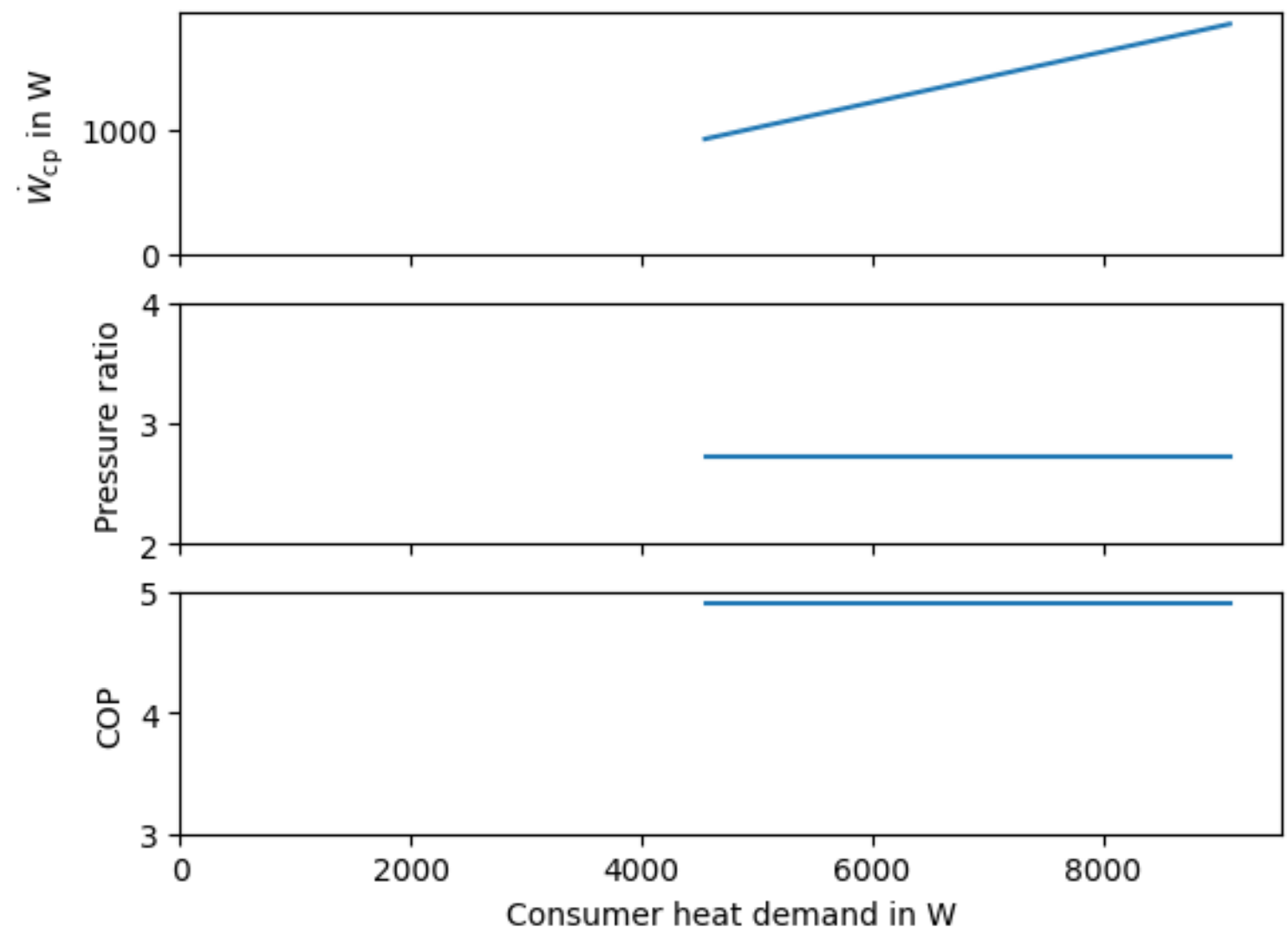
### Full load

Compressor efficiency can be considered as **constant** (calibration point)

Electrical input is a linear function of the heat supplied (constant compr. eff.)

Pressure ratio independent of load to be supplied

COP **I**ndependent on heat supplied ( $Q_{\text{cond}}$ )



# Heat pump overview

## The heat pump cycle

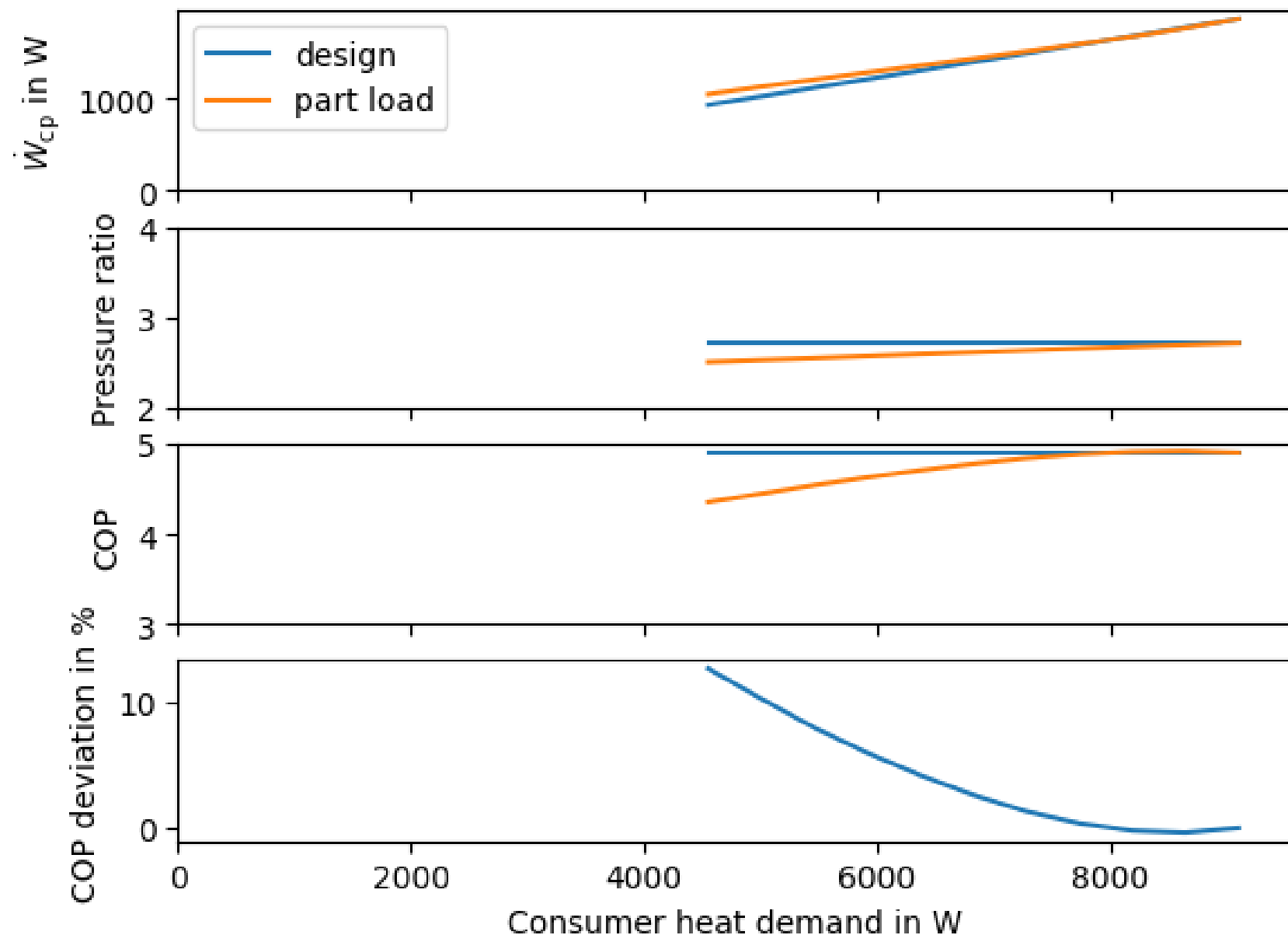
### Partial load

Compressor efficiency can be considered as **state-dependent** (non constant)

For loads lower than 75-50% of max.power higher deviations of the power ratio

Leading to higher differences in the COP

COP is dependent of the partial load behaviour





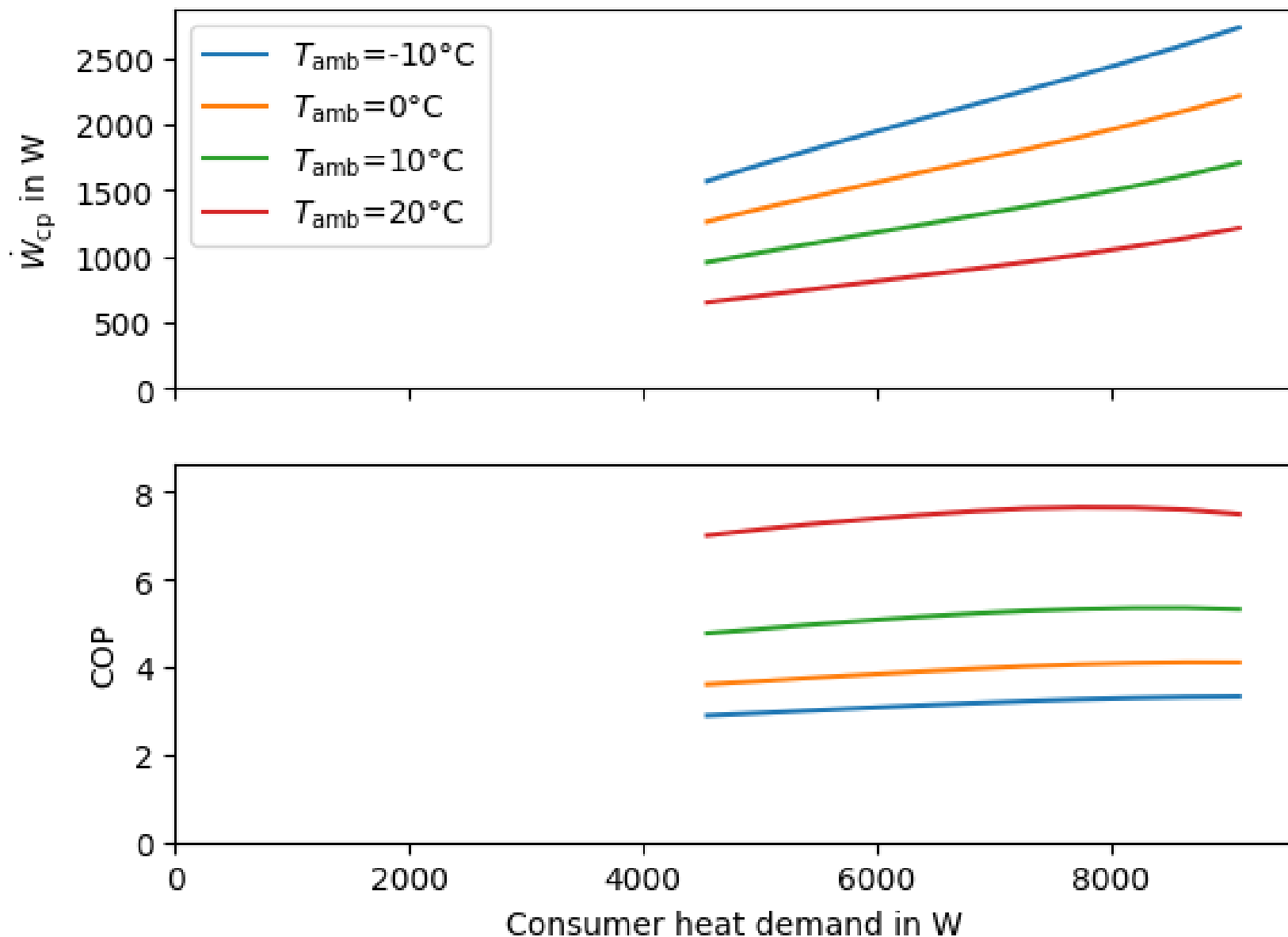
# Heat pump overview

## The heat pump cycle

### Partial load

Compressor efficiency can be considered as **state-dependent** (non constant)

- At part load COP decreases
- For loads lower than 75-50% of max.power compressor power is not a linear function of the load anymore
- COP is not fully constant for lower loads



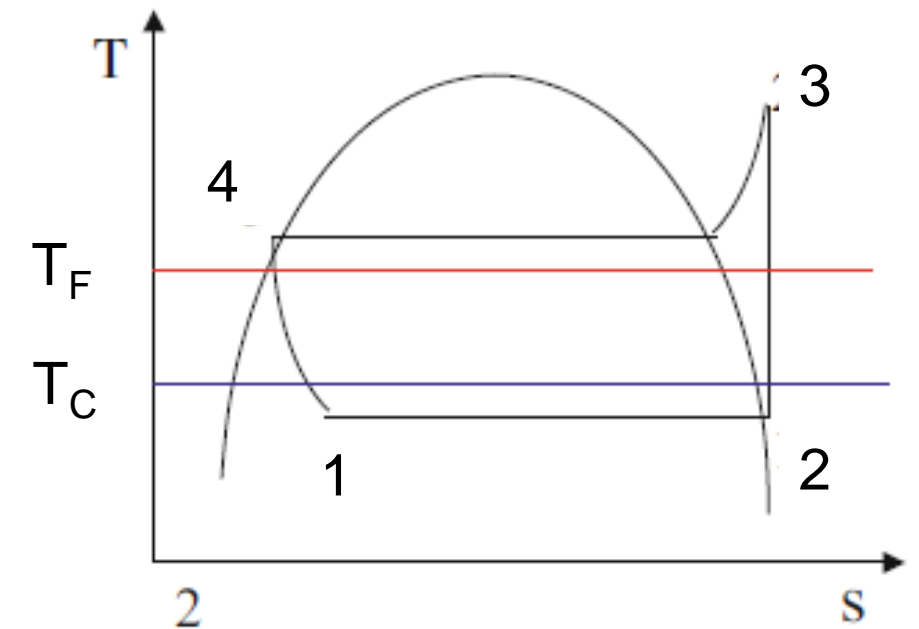
# Heat pump overview

## The heat pump cycle

### Operation - Real behaviour (simulated)

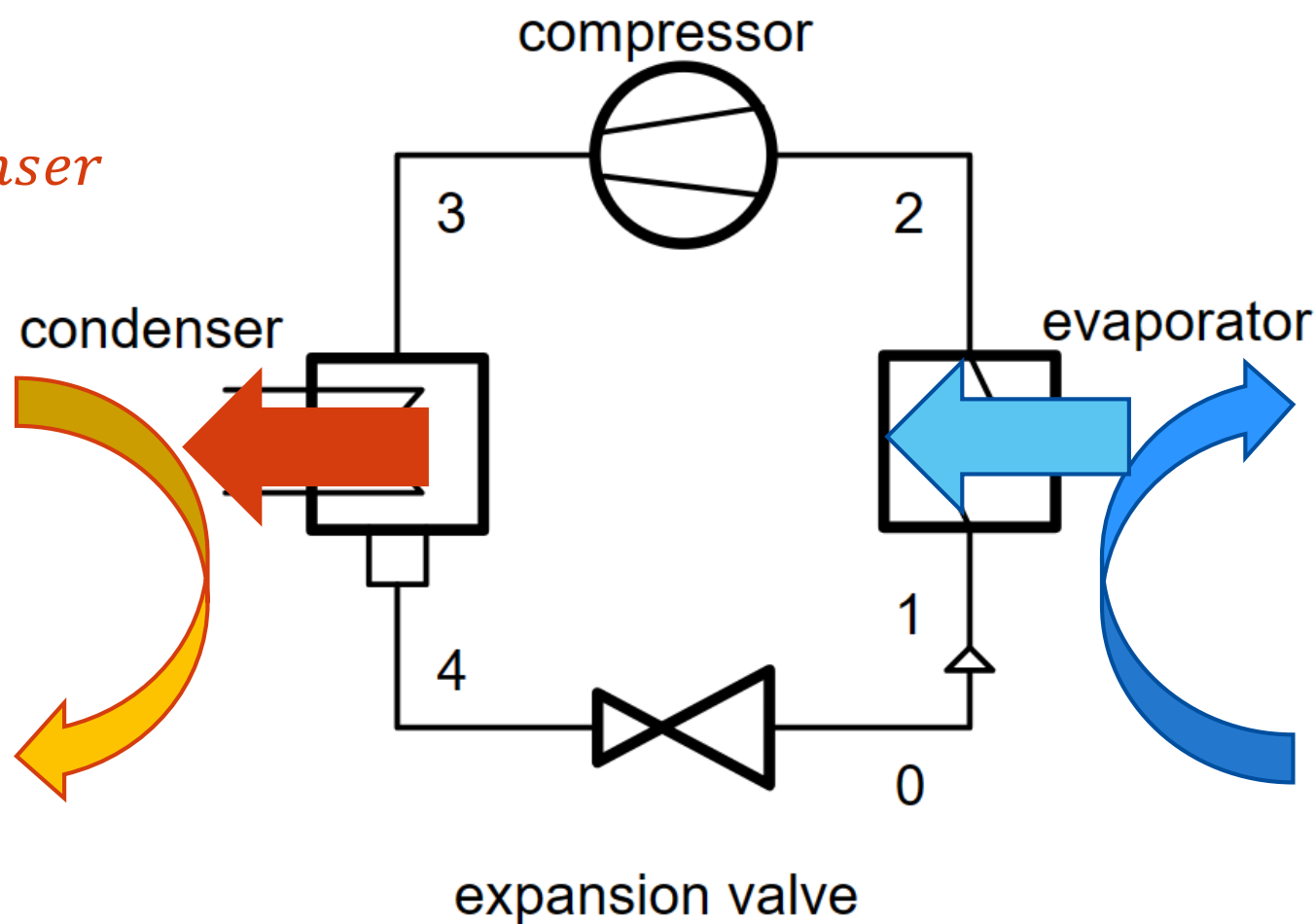
Constant mass flow vs. Constant temperature difference

(in the secondary sides of both evaporator and condenser)



$\dot{Q}_{condenser}$

Air  
Water



$\dot{Q}_{evaporator}$

Air  
Water

$$\dot{Q}_{evaporator} = \dot{m}c_p\Delta T$$

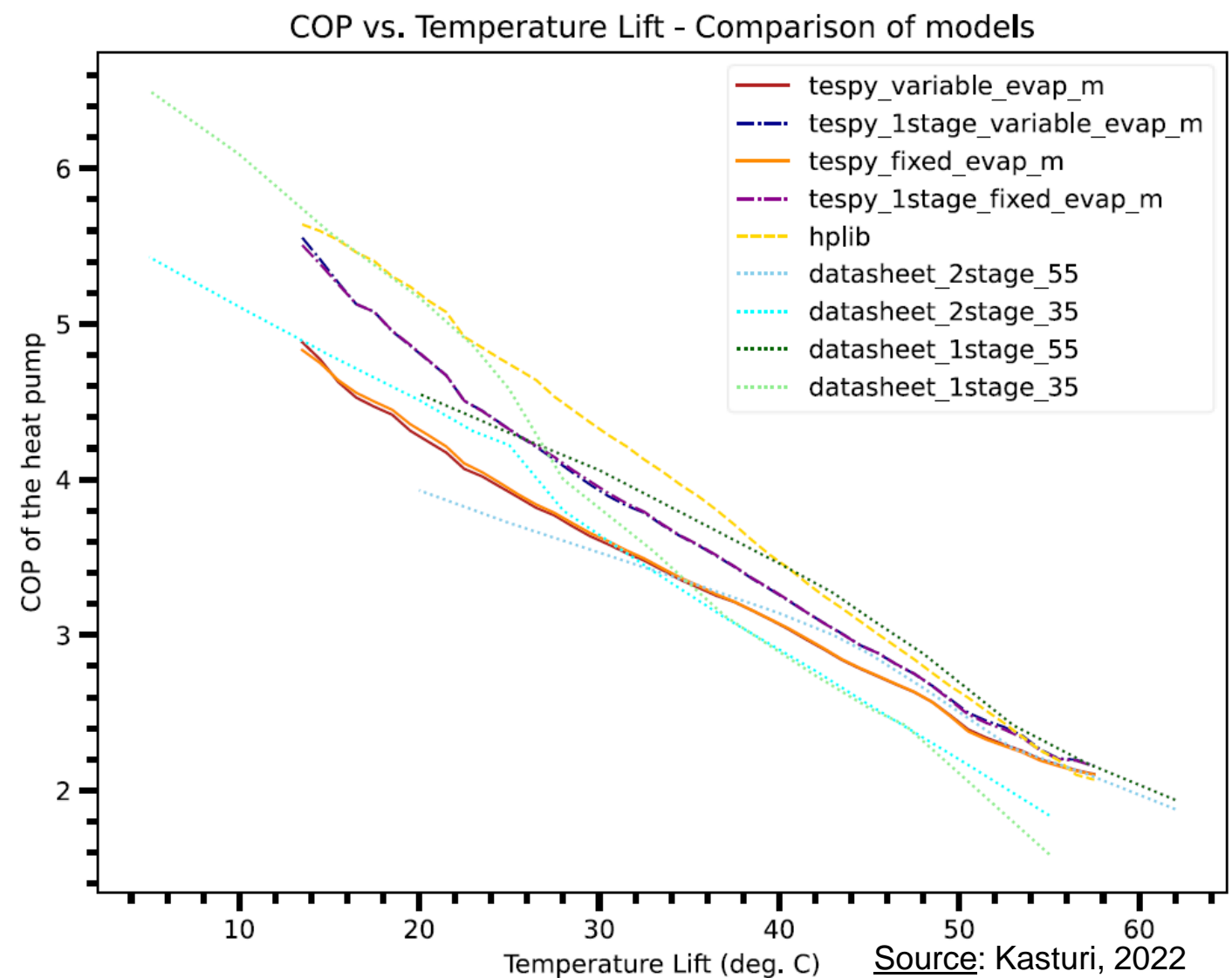
# Heat pump overview

## The heat pump cycle

### Operation

Constant mass flow vs. Constant temperature difference  
(in the secondary sides of both evaporator and condenser)

- Very similar COP - performance for both operation strategies



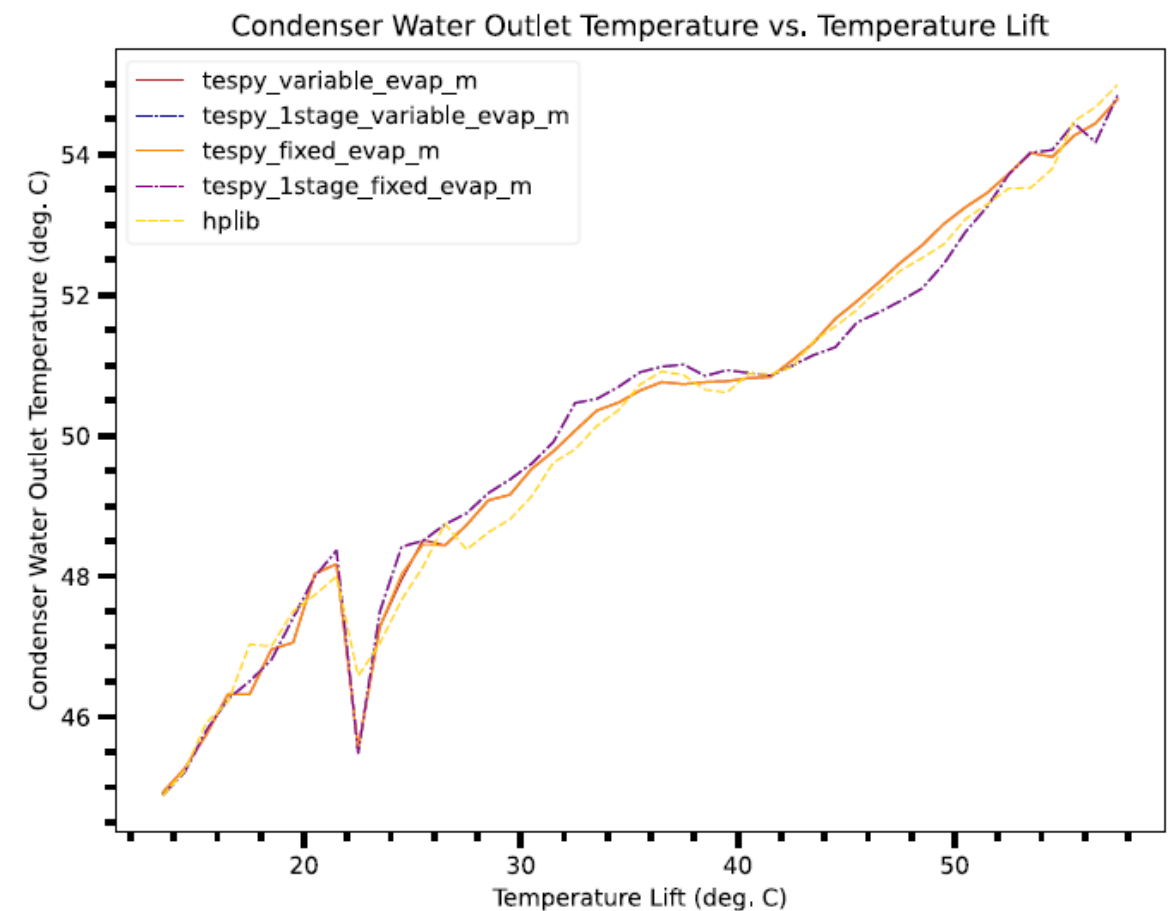
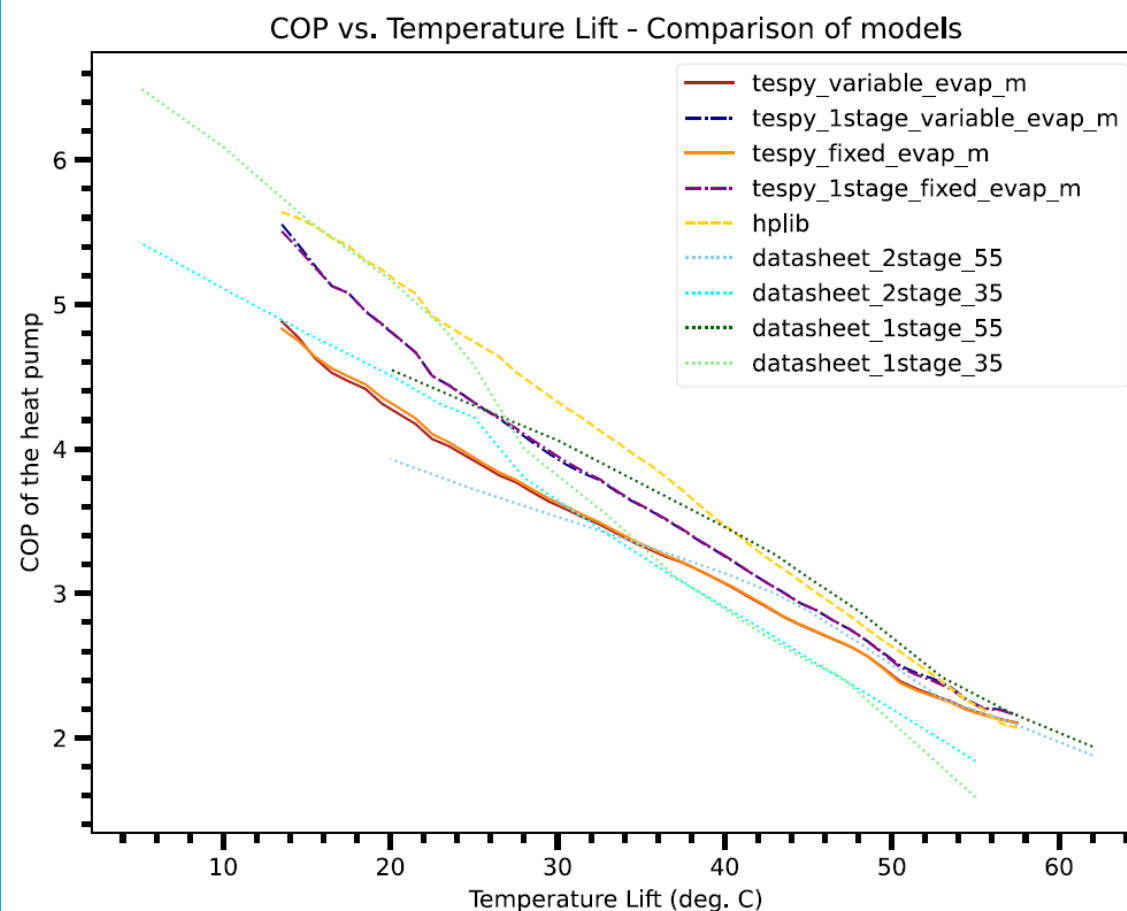
# Heat pump overview

## The heat pump cycle

### Operation

Constant mass flow vs. Constant temperature difference  
(in the secondary sides of both evaporator and condenser)

- Very similar COP performance for both operation strategies
- Very similar condenser outlet temperatures



## References

**Grassi 2018.** Heat pump fundamentals and applications. Green Energy and Technology, Springer Ed. Link: <https://link.springer.com/book/10.1007/978-3-319-62199-9>, Last accessed: Oct. 2023

**Kasturi 2023.** *Simulation of photovoltaic-thermal (PV-T) solar assisted heat pump (SAHP) systems for building thermal demands.* Master thesis at the UOL.

**Hervas Blanco. 2020.** Low temperature waste water heat recovery for Domestic Hot Water production based on heat pumps. PhD Thesis. Instituto Ingenieria Energetica. Universidad Politecnica de Valencia. Link: [Aprovechamiento del calor residual a baja temperatura mediante bombas de calor para la producción de agua caliente \(upv.es\)](https://upv.es/tesis/10424), Last accessed: 03.11.2023