

PRIM's MST algorithm

- Start with an arbitrary vertex r . Grow MST by repeatedly adding the smallest edge connecting a vertex in the tree with a vertex not in the tree
- To find the smallest edge we use a priority queue containing the *vertices* not in the tree yet:
 - The key/priority $d[v]$ of a vertex v is the weight of the smallest edge connecting v to the tree (implementation note: the priority of a vertex will be stored in an array $d[v]$ and also in the priority queue $(v, d[v])$; in order to be able to decrease the priority of a vertex we store a pointer to v 's location in the priority queue)
 - For each vertex v we store the edge that connects it to the tree; we call the other vertex of this edge by $pred(v)$

PRIM(G)

```
1 // initialize
2 Pick arbitrary vertex  $r$  and set  $d[r] = 0$ , PQ.INSERT( $r, 0$ ),  $pred(r) = NULL$ 
3 For each vertex  $u \in V (u \neq r)$ :  $d[u] = \infty$ , PQ.INSERT( $u, \infty$ )

4 while PQ not empty
5      $u =$  PQ.DELETE-MIN() //  $u$  is vertex closest to the tree
6     For each adjacent edge  $(u, v)$ 
7         IF  $v$  in PQ and  $w_{uv} < d[v]$ 
8             PQ.DECREASE-KEY( $v, w_{uv}$ )
9              $pred[v] = u$ 
10 Output the edges  $(u, pred(u))$  as the MST.
```

Analysis: $O(|E| \lg |V|)$

Kruskal's MST algorithm

KRUSKAL(G)

```
1 // initialize
2 For each vertex  $v \in V$ : MAKE-SET( $v$ )
3 Sort edges of  $E$  in increasing order by weight

4 for each edge  $e = (u, v)$  in order of weight
5     if FIND-SET( $u$ )  $\neq$  FIND-SET( $v$ )
6         output edge  $e$  as part of MST
7         UNION-SET( $u, v$ )
```

Analysis: $O(|E| \lg |V|)$