

# 1 一元函数微分学的计算

## 1.1 基本求导公式

1.  $(x^a)' = ax^{a-1}$  ( $a$  为常数)
2.  $(a^x)' = a^x \ln a$  ( $a > 0, a \neq 1$ )
3.  $(e^x)' = e^x$
4.  $(\log_a x)' = \frac{1}{x \ln a}$  ( $a > 0, a \neq 1$ )
5.  $(\ln |x|)' = \frac{1}{x}$

### 6. 三角函数求导

- $(\sin x)' = \cos x$
  - $(\cos x)' = -\sin x$
  - $(\tan x)' = \sec^2 x$
  - $(\cot x)' = -\csc^2 x$
  - $(\sec x)' = \sec x \tan x$
  - $(\csc x)' = -\csc x \cot x$
  - $(\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$
  - $(\arccos x)' = -\frac{1}{\sqrt{1-x^2}}$
  - $(\arctan x)' = \frac{1}{1+x^2}$
  - $(x)' = -\frac{1}{1+x^2}$
7.  $[\ln(x + \sqrt{x^2 + 1})]' = \frac{1}{\sqrt{x^2 + 1}}$
  8.  $[\ln(x + \sqrt{x^2 - 1})]' = \frac{1}{\sqrt{x^2 - 1}}$

## 1.2 四则运算

1.  $(u \pm v)' = u' \pm v'$
2.  $(uv)' = u'v + uv'$
3.  $\left(\frac{u}{v}\right)' = \frac{u'v - uv'}{v^2} \quad (v \neq 0)$

- 1.3 基础概念
- 1.4 结论
- 1.5 定理
- 1.6 运算
- 1.7 公式
- 1.8 方法总结
- 1.9 条件转换思路
- 1.10 理解