Letter

To: the Puzzle Editor of the New York Times

Date: Monday, February 20, 2023

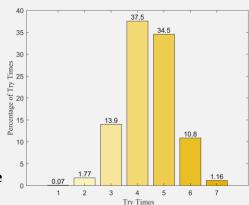
Subject: Wordle's Development Forecasts and Related Recommendations

Dear Mr. Editor:

With the help of the data provided by the MCM organizing committee, we analyze in detail the daily results of Wordle from January 7, 2022 to December 31, 2022. Wordle exploded thanks to its creative gameplay and the interesting puzzles provided by Puzzle Editor every day. While we marveled at the success of wordle, we also found some interesting phenomena through the data set and made some guesses about the future development of wordle, which I would like to share with you next.

First of all, we develop a prediction model for the number of daily reported results for wordle, mainly based on the **ARIMA** (1,1,1) model. It is predicted that 14,869 reports will be reported on March 1, 2023, probably due to the decline in wordle's popularity over time. We also found through analysis of the data that the attributes of the words do not affect the percentage of players who choose the hard mode that day, which is understandable because no one knows the difficulty of the words before they start the game, and thus does not affect their mode choice.

Secondly, we develop a model for predicting the distribution of daily attempts, based on coupled double **discrete normal distribution** to fit the overall distribution. Using this model, we predict the distribution of attempts for the word EERIE on March 1 as shown on the right. The model is subject to many uncertainties such as significant events, time lapse, word properties... and we can quantify our confidence in the model prediction in the form of confidence intervals.



Then, using multiple linear regression, we develop a difficulty classification model based on the various attributes of the words and determin a star classification model for difficulty through **boundary optimization**, concluding that **EERIE** is a 4-star difficulty word (the most difficult category of words).

Finally, we also found some interesting features of this dataset, such as

- 1) The change in difficulty coefficients from one day to the next is often the opposite of the change from the previous day
- 2) The percentage of One-try guesses is negatively correlated with the number of repeated letter in the word We hope that our prediction and classification models and the interesting features we summarized will help New York Times to better develop wordle as an excellent daily game.

Sincerely yours

MCM 2023 Team