

Full Insurance in the Presence of Aggregate Uncertainty

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Full Insurance in the Presence of Aggregate Uncertainty

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This paper tests implications of full consumption insurance. The object is to determine how much mileage can be obtained from a model with complete markets, with such features as private information or liquidity constraints omitted. The implication exploited is that individual consumption responds to aggregate risk but not to idiosyncratic risk. The test involves regressing the change in household consumption onto the change in aggregate consumption and other right-hand-side variables such as the change in household income and change in employment status. All variables other than the change in aggregate consumption are predicted to be insignificant in explaining the change in household consumption. With observations on consumption and income for 10,695 households from the Consumer Expenditure Survey, the results are mixed. The results for one specification (exponential utility) are mostly consistent with full consumption insurance; the results for the other specification (power utility) are not.

I. Introduction

In this paper, I analyze and test the implications of full consumption insurance in the presence of aggregate uncertainty. The object is to

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determine how much mileage can be obtained from a model with complete markets, with such features as private information or liquidity constraints omitted. The goal of this research is not to provide evidence that all markets are perfect, but rather to determine whether market imperfections or lack of completeness is an essential feature in explaining consumption allocations. Hence a complete-markets model provides a useful benchmark without requiring researchers to literally accept market perfection.

An insurance scheme may be approximated in the actual economy by various risk-sharing opportunities and markets. For example, some possible sources of insurance include stocks and securities markets, borrowing and lending in a credit market, unemployment insurance, contracts between employer and employee, crop insurance for farmers, and insurance among family members or close communities.

The principal implication of risk sharing is that individual consumption responds to aggregate risk but not to idiosyncratic risk. In the current setting, aggregate risk is represented by changes in aggregate consumption, and idiosyncratic risk includes changes in individual income and employment status. The implications of risk sharing are emphasized in the early work by Wilson (1968) and in more recent work by Constantinides (1982), Scheinkman (1984), Eichenbaum, Hansen, and Richard (1987), and Townsend (1987). Empirical work related to the current approach includes Leme (1984), Mace (1988), Townsend (1989), and Cochrane (this issue). The current paper emphasizes the empirical implication that changes in individual consumption are determined by changes in aggregate consumption rather than by changes in individual income or employment status.

The current research is closely related to the literature on the permanent income hypothesis (PIH). In contrast to the PIH, all changes in idiosyncratic income, both permanent and transitory, are insured in the current risk-sharing model. Hence the current model can be viewed as an extreme version of the PIH. Understanding the benchmark case of full insurance may help us to sort out the large volume of mixed evidence on various forms of the PIH.

The paper is organized as follows. A model of risk sharing is analyzed in Section II. For homothetic preferences, the principal implication of risk sharing is that individual consumption varies positively with aggregate consumption. While an individual's share of aggregate consumption is determined by the individual's wealth relative to aggregate wealth, changes in individual consumption are determined by changes in aggregate consumption.

The testable implications of risk sharing are developed in Section III: in particular, once the change in aggregate consumption is ac-

counted for, the change in individual income does not help to explain the change in individual consumption. The data source is described in Section IV. I use observations on consumption and income for 10,695 households from the Consumer Expenditure Survey for 1980–83. In Section V, the results are reported and various econometric issues are addressed. The test involves regressing the change in household consumption onto the change in aggregate consumption and other right-hand-side variables such as the change in household income and the change in employment status. All variables other than the change in aggregate consumption are predicted to be insignificant in explaining the change in household consumption. The summary and conclusions are provided in the final section (Sec. VI). Overall, the results are mixed. The results for one specification are mostly consistent with full consumption insurance; the results for the other specification are not.

II. Theory of Risk Sharing

The major implication of risk sharing is that individual consumption varies positively with aggregate consumption rather than with idiosyncratic variables such as individual income. The positive relationship between individual and aggregate consumption is not a new result in the literature on risk sharing and complete markets. The model analyzed in this section draws heavily from this literature. Of the early risk-sharing literature, studies by Wilson (1968) and Kihlstrom and Pauly (1971) emphasize particular preference specifications and the associated sharing rules. In contrast to the current study, the subject of Wilson's paper is really the sharing of income from a risky project. The implications of risk sharing are also emphasized in more recent work by Constantinides (1982), Scheinkman (1984), Eichenbaum et al. (1987), and Townsend (1987).

The current approach to risk sharing is also closely related to the literature pertaining to aggregation properties of preferences. The characterization of risk-sharing outcomes for a class of homothetic preferences stems from the early work on preferences by Gorman (1953). This includes the study of syndicate behavior by Wilson (1968) and of Rubinstein's (1974) composite individual. The aggregation property of preferences in the presence of uncertainty is examined in a static risk-sharing model by Brennan and Kraus (1978) and in a dynamic risk-sharing model by Eichenbaum et al. (1987).

The risk-sharing problem is cast in the setting of a social planner.¹

¹ The risk-sharing implications developed in this paper also apply to a decentralized economy (e.g., Mace 1988).

The planner maximizes the weighted sum of the expected utilities of individuals subject to an aggregate resource constraint. Optimal resource allocation entails a distribution of the aggregate endowment that equalizes weighted marginal utilities across individuals. The solutions are specialized for two specifications of homothetic preferences: exponential and power utility. For exponential utility, the first differences of consumption, net of preference shocks, are equalized across individuals. The growth rates of consumption are equalized across individuals in the case of power utility.

A. Optimal Resource Allocation

Described below are the general characteristics of the economy, including the information structure, preferences, and endowments. The analysis is limited to the case of a single nondurable good. The risk-sharing implications continue to hold for more general homothetic preferences and for various assumptions on the number, separability, and durability of goods. These results are summarized in the Appendix.

1. Information

Individuals' common information at time t is represented by events $s_{\tau t}$, $\tau = 1, 2, \ldots, S$, where each event is a collection of states of the world. The number of events S is finite, but the number of states may be infinite because of the accumulation of information over time. The term $\pi(s_{\tau t}) \in [0, 1]$ denotes the probability that event τ occurs at time t with $\sum_{\tau=1}^{S} \pi(s_{\tau t}) = 1$, for all t.

2. Preferences

There are J infinitely lived consumers. Consumer j has preferences for the consumption good; thus expected lifetime utility is expressed as

$$\sum_{t=0}^{\infty} \beta^{t} \sum_{\tau=1}^{S} \pi(s_{\tau t}) U[C_{t}^{j}(s_{\tau t}), b_{t}^{j}(s_{\tau t})], \tag{1}$$

where $C_l^j(s_{\tau l})$ denotes consumption for individual j in event τ at time t, $b_l^j(s_{\tau l})$ a preference shock, and $0 < \beta < 1$ the discount factor.

3. Endowments

Each individual j receives an exogenous endowment of the consump-

tion good

$$y_t^j(s_{\tau t}) = \overline{y}_t^j + \eta_t^j(s_{\tau t}) + \epsilon_t^j(s_{\tau t}), \tag{2}$$

where \bar{y}_l^j denotes a deterministic component of output, $\eta_l^i(s_{\tau l})$ represents the aggregate shock to individual j's endowment, and $\epsilon_l^i(s_{\tau l})$ denotes the idiosyncratic shock. Although $\eta_l^i(s_{\tau l})$ is labeled an aggregate shock, its magnitude may differ across individuals. For example, some endowments are more cyclical than others.

When equation (2) is aggregated over J individuals, the aggregate endowment is given by

$$y_t^a(s_{\tau t}) = \bar{y}_t^a + \eta_t^a(s_{\tau t}). \tag{3}$$

The aggregate variables are simply averages of the individuals and tend to the economy averages as the number of individuals J becomes large. Aggregate uncertainty is represented by $\eta_t^a(s_{\tau t}) \neq 0$ for at least one event, for all t. The idiosyncratic shock is defined such that $\epsilon_t^a(s_{\tau t}) = 0$ for all events and for all t. This property is also an approximation: $\epsilon_t^a(s_{\tau t})$ approaches zero as J tends to infinity.

This particular form of endowments is employed in order to stress the feature of aggregate uncertainty. It is not crucial for the principal implications of risk sharing: more general technologies render the same implications.

The social planner maximizes the weighted sum of the expected utilities of the J individuals, given by the objective function (4), by choosing an allocation of consumption across individuals subject to the aggregate resource constraint in equation (5) for each date and event:

$$\sum_{t=1}^{J} \omega^{j} \sum_{t=0}^{\infty} \beta^{t} \sum_{\tau=1}^{S} \pi(s_{\tau t}) U[C_{t}^{j}(s_{\tau t}), b_{t}^{j}(s_{\tau t})], \tag{4}$$

$$\sum_{j=1}^{J} C_{t}^{j}(s_{\tau t}) = \sum_{j=1}^{J} y_{t}^{j}(s_{\tau t}), \tag{5}$$

with the planner's weights ω^j satisfying $0 < \omega^j < 1$ and $\sum_{j=1}^J \omega^j = 1$ (see Negishi 1960). The aggregate endowment is distributed across individuals such that weighted marginal utilities are equated across individuals; more precisely, individual consumption varies positively with the aggregate endowment (e.g., Townsend 1987).

 $^{^2}$ A shock in this economy is any output movement away from the deterministic component \bar{y}_l . The idiosyncratic shock, $\epsilon_l^i(s_{\tau l})$, does not have to be unanticipated. It should not be interpreted as transitory income. The only restriction is that $\epsilon_l^a(s_{\tau l}) = 0$. Depending on the generating processes, there may be components of both $\eta_l^i(s_{\tau l})$ and $\epsilon_l^i(s_{\tau l})$ that are fully anticipated.

B. Preference Specifications

Preferences are specialized to a class of homothetic functions. The first specification is exponential utility:

$$U[C_{t}^{j}, b_{t}^{j}] = -\frac{1}{\sigma} \exp[-\sigma (C_{t}^{j} - b_{t}^{j})], \quad \sigma > 0.$$
 (6)

The preferences are both time and state separable. The state notation is suppressed for expositional convenience. Individuals have the same coefficient of constant absolute risk aversion σ .

The first-order conditions for individual j include

$$\hat{\mathbf{\mu}}_t = \mathbf{\omega}^j \exp[-\mathbf{\sigma}(C_t^j - b_t^j)],\tag{7}$$

where $\hat{\mu}_t = \mu_t/\beta^t \pi_t$ and μ_t is the Lagrange multiplier associated with the resource constraint (5) at time t. When we take the logarithm of equation (7) and aggregate over J individuals, it follows that consumption for individual j is

$$C_t^j = C_t^a + \frac{1}{\sigma} (\log \omega^j - \omega^a) + (b_t^j - b_t^a),$$
 (8)

where

$$\omega^a = \frac{1}{J} \sum_{j=1}^J \log \omega^j, \quad C_t^a = \frac{1}{J} \sum_{j=1}^J C_t^j, \quad b_t^a = \frac{1}{J} \sum_{j=1}^J b_t^j.$$

The major implication of risk sharing is reflected in equation (8): individual consumption varies positively with aggregate consumption, which varies by state and over time.

Consumption for individual j is above (below) the economywide average of consumption if the sign of $\log \omega^j - \omega^a$ is positive (negative). This term is positive for individuals with above-average wealth. Hence there is a positive relationship between the share of aggregate consumption allocated to individual j and the magnitude of individual j's wealth relative to aggregate wealth. Also note that the planner's weight (ω^j) does not depend on time. Therefore, an individual's share of aggregate consumption does not vary over time. However, the level of individual consumption fluctuates over time and across states because of fluctuations in aggregate consumption.

The risk-sharing implication is expressed in terms of changes by taking the first difference of equation (8):

$$C_{t+1}^{j} - C_{t}^{j} = C_{t+1}^{a} - C_{t}^{a} + [(b_{t+1}^{j} - b_{t}^{j}) - (b_{t+1}^{a} - b_{t}^{a})].$$
 (9)

Consequently, the changes in consumption, net of preference shocks, are equalized across individuals. The individual fixed effect in equation (8), $\log \omega^{j} - \omega^{a}$, is removed with the first difference.

The risk-sharing implication that individual consumption varies positively with aggregate consumption also holds for an additional preference specification: power utility with multiplicative preference shocks. Again, this is illustrated for the case of a single nondurable good:

$$U[C_i^j, b_i^j] = \exp(\sigma b_i^j) \frac{1}{\sigma} (C_i^j)^{\sigma}. \tag{10}$$

Strict concavity requires $\sigma < 1$. Individuals have the same coefficient of constant relative risk aversion $(1 - \sigma)$.³

The logarithm of consumption for individual j is

$$\log C_t^j = \log C_t^a + \frac{1}{1 - \sigma} (\log \omega^j - \omega^a) + \frac{\sigma}{1 - \sigma} (b_t^j - b_t^a), \quad (11)$$

where

$$\omega^a = \frac{1}{J} \sum_{j=1}^{J} \log \omega^j, \quad C_t^a = \exp\left(\frac{1}{J} \sum_{j=1}^{J} \log C_t^j\right), \quad b_t^a = \frac{1}{J} \sum_{j=1}^{J} b_t^j.$$

Taking the first difference of equation (11) yields

$$\log C_{t+1}^{j} - \log C_{t}^{j} = \log C_{t+1}^{a} - \log C_{t}^{a} + \frac{\sigma}{1 - \sigma} [(b_{t+1}^{j} - b_{t}^{j}) - (b_{t+1}^{a} - b_{t}^{a})],$$
(12)

where

$$\log C_{t+1}^a - \log C_t^a = \frac{1}{J} \sum_{i=1}^J (\log C_{t+1}^j - \log C_t^j).$$

Hence for power utility there is a positive and linear relationship between the growth rates of individual consumption and the growth rate of aggregate consumption.

In summary, a major implication of risk sharing is that individual consumption varies positively with aggregate consumption. This relationship is further specialized for two classes of homothetic preferences. For exponential preferences, the changes in consumption, net of preference shocks, are equalized across individuals. For a class of power utility functions with multiplicative preference shocks, the growth rates of consumption, net of preference shocks, are equalized across individuals.

³ Some special cases of power utility include logarithmic and Cobb-Douglas preferences. See the Appendix for more details.

III. Empirical Implications

The risk-sharing implications are recast for empirical implementation. The major implication is that changes in individual consumption are determined by changes in aggregate consumption rather than by changes in idiosyncratic variables. Empirical specifications for individual observations are developed for both exponential and power utility.

For exponential preferences, there is a direct relationship between the change in individual j's consumption and the change in aggregate consumption (refer to eq. [9]):

$$\Delta C_t^j = \Delta C_t^a + (\Delta b_t^j - \Delta b_t^a), \tag{13}$$

where

$$\Delta C_{t}^{j} = C_{t}^{j} - C_{t-1}^{j}, \quad \Delta C_{t}^{a} = \frac{1}{J} \sum_{j=1}^{J} \Delta C_{t}^{j}, \quad \Delta b_{t}^{a} = \frac{1}{J} \sum_{j=1}^{J} \Delta b_{t}^{j}.$$

Equation (13) presents a nontrivial approach for testing the full insurance implications: regress the changes in individual consumption onto the change in aggregate consumption and other right-hand-side variables such as changes in individual income and changes in employment status. All variables other than the aggregate consumption variable are predicted to enter insignificantly. This reflects the key feature of risk sharing: individual consumption responds to aggregate risk but not to idiosyncratic risk. Formally, the empirical specification is

$$\Delta C_t^j = \beta_1 \Delta C_t^a + \beta_2 \Delta \gamma_t^j + u_t^j, \tag{14}$$

where Δy_l^j is the change in individual j's income. The disturbance term u_l^j includes the time-varying component of both individual and aggregate preference shocks and might also include measurement errors from the consumption and income data. The predictions of the risk-sharing model are $\beta_1 = 1$ and $\beta_2 = 0$. The model also predicts a zero coefficient for other right-hand-side variables such as change in employment status.

There are many possible types of risk and sources of insurance. The current test is not complete in that the income measure does not include all types of risk. To match up the test exactly with the model requires data on a measure of income that has not been insured. Here the theoretical endowments are proxied by data on reported income. Reported income includes after-tax wages and salaries, pension income, interest income, and various lump-sum receipts. Hence some of the risk sharing has already taken place and is included in

the reported income measure. This may include wage and salary insurance between employer and employees and interest income from assets. However, at least some of the risk sharing takes place between receipt of reported income and actual consumption. These other forms of insurance may include borrowing and lending on a credit market, unrealized gains in securities, and other formal and informal insurance arrangements.

For econometric reasons, the implication for differenced consumption of equation (9) is exploited in the empirical work rather than the implication for level consumption from equation (8). Remember that equation (9) is the first difference of equation (8). Individual j's additive fixed effect, $\log \omega^j - \omega^a$ in equation (8), is removed by first-differencing. Using the first-difference specification avoids problems from an omitted-variables bias when the fixed effect is not observed by the econometrician.

In the previous section, risk-sharing implications are also derived for a class of power utility functions. For these preferences, there is a direct relationship between the growth rates of individual consumption and the growth rate of aggregate consumption (refer to eq. [12]):

$$\Delta \log C_t^j = \Delta \log C_t^a + \frac{\sigma}{1 - \sigma} (\Delta b_t^j - \Delta b_t^a), \tag{15}$$

where

$$\begin{split} \Delta \log C_t^j &= \log C_t^j - \log C_{t-1}^j, \\ \Delta \log C_t^a &= \frac{1}{J} \sum_{j=1}^J \Delta \log C_t^j, \\ \Delta b_t^a &= \frac{1}{J} \sum_{j=1}^J \Delta b_t^j. \end{split}$$

The empirical specification for power utility is

$$\Delta \log C_t^j = \beta_1 \Delta \log C_t^a + \beta_2 \Delta \log \gamma_t^j + v_t^j, \tag{16}$$

where $\Delta \log y_l^{\gamma}$ is the growth rate of individual j's income. As before, the disturbance term v_l^{γ} includes the time-varying components of individual and aggregate preference shocks and might also include measurement errors from the data. The risk-sharing model predicts that $\beta_1 = 1$ and $\beta_2 = 0$. The consumption growth rate implication of equation (12) is implemented rather than the implication for logarithmic consumption from equation (11). As with the previous specification for exponential preferences, the individual fixed effects are removed when the observations are first-differenced.

In summary, the implications of risk sharing are recast for empirical implementation. Fluctuations in individual consumption are determined by fluctuations in aggregate consumption rather than by fluctuations in own income. However, another model delivers some of these same implications. The positive relationship between individual and aggregate consumption exists in risk-sharing models, both with and without aggregate shocks to endowments. This positive relationship also exists in models with no risk sharing if there are aggregate shocks. To take an extreme example, suppose that there is autarky, aggregate shocks, and no storage. Because there are common shocks to endowments and each individual consumes his or her own endowment, individual consumption is positively related to aggregate consumption. So is it possible to distinguish empirically between risk sharing and autarky in the case of aggregate shocks since both models exhibit this positive relationship between individual and aggregate consumption? The answer is yes, as long as endowments differ somewhat across individuals. If they differ across individuals under autarky, an individual's consumption is more closely related to his own income than to aggregate consumption. This permits an empirical distinction between the two benchmarks of risk sharing and autarky.

IV. Data

Equations (14) and (16) are the specifications tested in Section V: one involves growth rates of consumption and income; the other involves first differences of the levels. The data requirements for these tests are observations on consumption and income at the individual or household level. Also required is a minimum of two observations for each individual or household for computing first differences and growth rates. Hence cross-sectional data are not suitable.

The implications are tested using data from the Consumer Expenditure Survey (CES) for 1980–83. The CES data satisfy the two criteria of consumption and income observations at the household level, and there are at least two data points for each household. The surveys are sponsored by the U.S. Bureau of Labor Statistics and administered by the U.S. Bureau of the Census. The survey provides unusually rich consumption data, as well as data on income, assets and liabilities, employment, and numerous demographic characteristics.

The CES data contain a panel aspect. The data are actually a collection of overlapping panels of 1-year duration with a quarterly sampling frequency. Aside from attrition, data are available for each household from four consecutive quarterly interviews. The 1-year panels overlap because of the rotating nature of the sample: 20 percent of the sample is replaced by new households each quarter. The

annual sample size varies between 4,800 and 5,000 households for 1980–83.

The panel aspect of the CES data is suitable for testing the implications in differenced form in equations (14) and (16). Pooling the differenced household observations exploits both the cross-sectional and time-series aspects of these specifications. Note that the aggregate consumption variable on the right-hand side does not vary across individuals at each point in time. However, there is individual variation in the other right-hand-side variable, individual income.

Household expenditures are reported on a monthly basis in all interviews. Approximately 500 expenditure categories are available on each quarterly questionnaire. An enormous amount of aggregation is required to reduce expenditure categories to a manageable number. For each household, I group expenditures into three broad categories of services, nondurables, and durables and into 13 more narrowly defined categories.

Income is reported for the year ending at the time of the interview. Disposable income is the income measure used in the empirical analysis. Disposable income is defined as before-tax income minus income taxes, deductions for social security and other pension plans, and occupational expenses such as union dues. Household income before taxes is the sum of regular income and other income such as lump-sum receipts. Regular income includes such items as wages, salaries, pension income, and interest income.⁴

A. Full Sample

The full sample consists of 227,949 monthly observations for the 1980:1–1984:1 period. This represents approximately 20,000 households, with each household contributing a maximum of 12 monthly observations. Summary statistics for income and the broad expenditure groups of total consumption, services, nondurables, and durables are displayed in table 1. Because of the rotating nature of the sample, the statistics are computed on a monthly basis for each quarter.

Although mean before-tax income exceeds mean consumption in all quarters, mean consumption exceeds mean disposable income. This is not a surprising outcome because of the different survey collection procedures used for expenditures and income. At each interview, expenditures are reported for the three previous months, while income is reported for the 12 previous months. With positive growth

⁴ See app. C of Mace (1988) for details on the surveys, exact definitions of the expenditure groups and income, sample exclusions, and sample size.

of consumption and income over time, this result could follow. Also, the income data include losses from farm and nonfarm businesses. In addition, disposable income is net of not only income taxes but also retirement deductions and occupational expenses.

B. Household Sample

The household sample includes 10,695 households, for which there is one differenced observation per household. The two observations used for differencing are taken from the first and last interviews. There are 9 months between these two interviews. Expenditures are taken from the last month reported in both interviews.

The choice of the first and last interviews is based on the survey's collection procedures for income. Data on expenditures are collected in all interviews, whereas the primary income data are collected in only the first and last interviews. Changes in employment status are collected in all interviews, and this information is used by the Bureau of Labor Statistics to adjust the income data for the second and third interviews. Income changes are reflected in the data for the middle interviews only if there is a change in employment status.

The aggregate consumption variable for the first-difference specification (eq. [14]) is constructed from the entire sample of 10,695 households. Expressed as a range over 12 months, the numbers of households used to compute monthly values of aggregate consumption are 214–492 households in 1980, 424–520 in 1981, 518–77 in 1982, and 262–579 in 1983. There are 282 households in both January and February of 1984.

The sample for the growth rate specification (eq. [16]) is a subset of the sample above. Because logarithms are employed, a household is included in the sample only if both the reported expenditure and income are positive for both interviews. Hence the numbers of observations differ by the measure of consumption. For example, the numbers of households used to compute the aggregate consumption variables in 1982 range from 120–65 for household furnishings to 440–510 for total nondurables.

V. Results and Econometric Issues

In this section, the empirical specifications are tested using data from the CES for 1980–83. Results are reported for various measures of consumption: the broad categories of total consumption, services, nondurables, and durables and the more narrowly defined categories of food, housing, utilities, household furnishings, clothing, medical care, transportation, and recreation.⁵ The consumption data are ex-

⁵ The percentages of total CES expenditures accounted for by services, nondurables, and durables are 44, 36, and 20, respectively. For the more narrow categories, food

TABLE 1

Means and Standard Deviations of Consumption and Income

	Quarter 1	Quarter 2	Quarter 3	Quarter 4
		19	80	
Total consumption	1,378.2	1,396.8	1,430.1	1,431.9
	(1,547.9)	(1,829.0)	(1,568.0)	(1,463.1)
Services	631.3	591.7	648.6	639.8
	(706.1)	(594.5)	(738.5)	(670.6)
Nondurables	522.6	523.1	529.4	542.9
	(383.4)	(372.5)	(409.5)	(399.3)
Durables	225.4	279.5	252.8	249.7
	(1,138.6)	(1,525.2)	(1,091.8)	(983.8)
Disposable income	1,271.2	1,274.2	1,240.8	1,227.6
	(1,119.0)	(1,096.0)	(1,097.4)	(1,067.9)
		19	81	
Total consumption	1,315.0	1,349.1	1,380.0	1,391.8
-	(1,361.8)	(1,414.5)	(1,424.3)	(1,473.9)
Services	616.3	593.7	628.1	633.4
	(589.5)	(596.1)	(666.2)	(703.8)
Nondurables	492.3	506.7	520.2	501.0
	(333.5)	(344.6)	(387.4)	(383.3)
Durables	206.6	246.6	230.7	257.0
	(1,042.1)	(1,054.4)	(979.2)	(1,039.5)
Disposable income	1,223.4	1,247.9	1,253.5	1,257.2
•	(1,059.6)	(1,064.3)	(1,073.5)	(1,090.6)
		19	82	
Total consumption	1,289.4	1,346.1	1,359.3	1,413.7
	(1,298.3)	(1,382.0)	(1,448.9)	(1,444.7)
Services	639.7	608.0	639.8	656.6
	(612.1)	(570.9)	(651.6)	(729.3)
Nondurables	454.1	489.1	495.3	509.9
	(321.2)	(353.7)	(378.2)	(390.4)
Durables	194.6	248.8	224.0	247.7
	(910.2)	(1,040.7)	(1,030.2)	(943.9)
Disposable income	1,284.7	1,313.5	1,292.5	1,284.5
	(1,140.5)	(1,176.3)	(1,201.3)	(1,221.3)
		19	83	
Total consumption	1,336.7	1,405.4	1,450.5	1,443.6
-	(1,399.5)	(1,585.4)	(1,728.4)	(1,614.6)
Services	662.0	642.7	697.5	654.6
	(651.2)	(624.7)	(939.6)	(763.8)
Nondurables	467.4	495.3	503.2	514.8
	(331.6)	(364.0)	(405.7)	(399.6)
Durables	208.2	268.2	250.1	272.7
	(1,013.1)	(1,230.8)	(1,139.6)	(1,101.5)
	(1,013.1)	(1,400.0)	(-,,	(-,,
Disposable income	1,315.7 (1,237.6)	1,354.2 (1,276.3)	1,333.7	1,325.8

TABLE 1 (Continued)

	Quarter 1	Quarter 2	Quarter 3	Quarter 4
		19	984	
Total consumption	1,407.6			
•	(1,767.4)			
Services	681.6			
	(697.5)			
Nondurables	463.0			
	(391.8)			
Durables	261.4			
	(1,431.2)			
Disposable income	1,317.3			
1	(1,260.7)			

Note.—Standard deviations are in parentheses. Means and standard deviations are expressed on a monthly basis in 1982 dollars. Each expenditure group is deflated by the relevant component of the nonseasonally adjusted monthly CPI. The original annual income data are deflated by annual averages of the monthly CPI for all items.

penditures rather than service flows. For the homothetic preferences analyzed here, the implications of risk sharing are applicable to all measures of consumption, with one exception: durable goods for the case of power utility with multiplicative preference shocks (see the Appendix).

A. Household Tests

Two specifications are tested at the household level: first differences for exponential preferences (eq. [14]) and growth rates for power utility (eq. [16]). The sample consists of two observations for each of 10,695 households. As previously discussed, the two observations represent the first and last interviews for each household. There are 9 months between these two interviews. For the first-difference specification, there is one differenced observation of consumption and income for each of the 10,695 households.

The sample for the growth rate specification is a subset of the sample above. Because logarithms are employed, a household is included in the sample only if both the reported expenditure and income are positive for both interviews. Hence the numbers of observations differ by the measure of consumption.

accounts for 22.3 percent of total expenditures, transportation for 20.5 percent, housing for 15.2 percent, and utilities for 8 percent. Recreation, clothing, and household furnishings each account for 5–6 percent, and medical care accounts for 4.7 percent. Results are not reported separately for domestic services, education, personal care, personal business, and contributions. Each accounts for less than 2.8 percent of total expenditures.

In addition to household income, employment status dummy variables are also used in the empirical tests. The survey collects data on the employment status of the reference person, spouse, and others in the household. There are eight possible categories for employment status: (1) reference person only; (2) reference person and spouse; (3) reference person, spouse, and others; (4) reference person and others; (5) spouse only; (6) spouse and others; (7) others only; and (8) no earners. There are 64 possible combinations of changes in employment status between the first and last interviews. Household income is replaced by the employment status dummy variables in half of the tests. The risk-sharing model predicts that the coefficients on these dummy variables are all zero.

Results are reported for 12 measures of consumption. The data are deflated by the relevant components of the consumer price index (CPI). The data are neither seasonally adjusted nor detrended prior to estimation. The coefficients are estimated using ordinary least squares. Various econometric issues concerning measurement error and possible estimation biases are addressed later in the section.

Results are reported in table 2 for the first-difference specification. Two regressions are reported for each measure of consumption. The dependent variable in all regressions is the first difference of household consumption. The first difference of aggregate consumption is included on the right-hand side in both regressions. The first regression includes the first difference of household income as a right-hand-side variable; the last regression includes employment status dummy variables (ΔE_i).

A summary of the two regressions is

$$\Delta C_t^j = \alpha + \beta_1 \Delta C_t^a + \beta_2 \Delta y_t^j, \tag{17}$$

$$\Delta C_t^j = \alpha + \beta_1 \Delta C_t^a + \sum_{k=1}^M \gamma_k \Delta E_{kt}^j, \qquad (18)$$

where ΔC_l^j is the first difference of household consumption, ΔC_l^a is the first difference of aggregate consumption, Δy_l^j is the first difference of household income, and ΔE_{kl}^j is a dummy variable for change in household employment status. The intercept term is included as a specification test.

B. Results

The results are reported in table 2 for 12 measures of consumption. The intercepts are reported in column 1. The coefficient on aggregate consumption (β_1) is in column 2, and the coefficient on house-

hold income (β_2) is in column 3. The standard errors of the estimated coefficients are in parentheses. In column 4, an *F*-ratio is reported for the joint test of $\beta_1 = 1$ and $\beta_2 = 0$. An *F*-ratio is also reported in column 5 for the regression with employment status, in which case the joint test is $\beta_1 = 1$ and all coefficients on the employment dummy variables ($\gamma_k = 0$) are jointly zero. The R^2 is in column 6.

For most of the measures of consumption, the results from the first regression in table 2 are consistent with the implications of risk sharing. In explaining the change in household consumption, the change in aggregate consumption enters with a coefficient of one; the change in household income has a zero coefficient. On the basis of the *F*-test in column 4, the risk-sharing implications cannot be rejected for 10 of the 12 goods (total consumption, services, durables, food, housing, utilities, household furnishings, medical care, transportation, and recreation). However, the results for food are marginal because $\beta_2 > 0$. For the remaining goods (nondurables and clothing), the risk-sharing implications are decisively rejected. These two rejections are the result of a significant coefficient on income.

Most of the results from the second regression in table 2 are also consistent with full insurance. This regression includes employment status dummy variables instead of household income. The risk-sharing implications cannot be rejected for eight of the 12 goods (total consumption, services, durables, housing, utilities, household furnishings, medical care, and recreation). The implications are rejected for nondurables, food, clothing, and transportation. The employment status variables are significantly different from zero for these four goods.

When the results for the two regressions are compared, the eight goods for which the implications cannot be rejected in both regressions are total consumption, services, durables, housing, utilities, household furnishings, medical care, and recreation. The significance of household income and employment status differs across two of the goods. Income is not significant, although employment status is for transportation. For recreation, employment status is not significant, although income is. Income and employment status are both significant for nondurables, food, and clothing.

Results are reported in table 3 for the growth rate specification.⁷ Two regressions are reported for each of the 12 goods. The specifi-

⁶ All statements regarding the statistical significance or rejection of the risk-sharing implications are based on a 5 percent level of significance.

⁷ As previously noted, the numbers of observations differ by the measure of consumption because of the requirement of positive values for logarithms. The numbers of observations are listed in the note to table 3.

TABLE 2
HOUSEHOLD CONSUMPTION REGRESSIONS: FIRST DIFFERENCES

					.013	.023		.032		.004		.010		.016		.025		800.		0.03
$\beta_1 = 1, \gamma_k = 0 \ \mathbf{V} \ k $ (5)		1.11	:	Š	92.	:		1.84*		:		1.01		::		1.69*				96.
$\beta_1 = 1, \beta_2 = 0$ (4)	1.27	;	1.14		:	7.71*		:		90.		:		2.52		•		1.10		
$\begin{array}{c} \Delta y_i^{\ell} \\ (3) \end{array}$.03	(.02)	.01	(.007)	•	.01	(.003)	:		.004	(.02)	:		.005	(.002)	:		.004	(.003)	:
$ \Delta C_t^a \\ (2)$	1.06	(.11)	(.11) 1.01	(.10)	1.01	96.	(90.)	86:	(90.)	1.03	(.15)	1.03	(.15)	1.01	(.08)	1.00	(80.)	.92	(.10)	.92
Intercept (1)	77.87	(19.32) - 69.07	(43.55) -30.47	(7.48)	-30.97	-13.97	(3.33)	-6.03	(7.57)	-32.44	(16.87)	-32.00	(38.36)	-7.46	(2.12)	-5.01	(4.76)	-13.80	(3.45)	-9.37
Consumption Measure	Total consumption		Services			Nondurables				Durables				Food				Housing	o	
	INTERCEPT ΔC_i^a $\Delta y_i'$ $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ V (1) (2) (3) (4)	Intercept ΔC_t^a Δy_i^a $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ V (1) (2) (3) (4) (4) (5) (5) (5) (7.87 1.063	INTERCEPT ΔC_t^a Δy_t^i $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ V (5) (1) (2) (3) (3) (4) (4) (5) (5) (5) (7) (7) (19.32) (11) (02) (10)	PITON INTERCEPT ΔC_i^a Δy_i^{j} $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ ∇y_i^{j}	CONSUMPTION INTERCEPT ΔC_l^a $\Delta \gamma_l^i$ $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ $\Delta \gamma_k = 0$ MEASURE (1) (2) (3) (4) (4) (5) (5) (5) (7) (101 (19.32) (111) (02) (111) (02) (112) (111 (19.32) (111) (CONSUMPTION INTERCEPT ΔC_l^a Δy_l^i $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ ΔV_l^i $\Delta V_$	nsumption Intercept ΔC_i^a Δy_i^b $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ Δy_i^b $\Delta y_i^$	CONSUMPTION INTERCEPT ΔC_l^a Δy_l^i $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ δ MEASURE (1) (2) (3) (3) (4) (5) (5) (5) (6) (9) (9) (1) (2) (1) (1) (1) (1) (1) (1) (1) (1) (1) (1	CONSUMPTION INTERCEPT ΔC_l^a Δy_l^i $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ δ MEASURE (1) (2) (3) (4) (4) (5) (5) (5) (7) (1) (02) (1.27 (1.11) (0.02) (0.03	Consumption Intercept ΔC_i^a $\Delta y_i'$ $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ V Measure (1) (2) (3) (4) (4) (5) Total consumption -77.87 1.06 .03 1.27 -69.07 1.06 .03 1.27 -69.07 1.06 1.11 (43.55) (11) .01 1.14 Services (7.48) (10) (.007) (7.48) 1.01 (16.47) (.10) (.007) (16.47) (.10) (16.47) (.10) (.007) (16.47) (.10) (.003) (2.33) (.06) (.003) 1.84*	Consumption Intercept ΔC_i^a $\Delta \gamma_i'$ $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ β_1 Measure (1) (2) (3) $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ β_1 Total consumption -77.87 1.06 0.3 1.27 \dots Total consumption -77.87 1.06 0.3 1.27 \dots Geometric consumption -77.87 1.06 0.3 1.11 0.1 0.11 Action consumption -77.87 0.10 0.07 0.07 0.07 0.07 0.07 Services -30.97 0.01 0.07	Consumption Intercept ΔC_i^a $\Delta \gamma_i'$ $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ β_1 Measure (1) (2) (3) (4) $\beta_1 = 1, \gamma_k = 0$ β_1 Total consumption -77.87 1.06 $.03$ 1.27 $$ Total consumption -77.87 (11) $(.02)$ $$ $$ Geometric consumption -77.87 $(.11)$ $(.02)$ $$ $$ Geometric consumption -77.87 $(.10)$ $(.007)$ $$ $$ Services -30.47 $(.10)$ $(.007)$ $$ $$ Services -30.97 $(.10)$ $(.007)$ $$ $$ Nondurables -13.97 $(.96)$ $(.003)$ $$ $$ Durables -32.44 $(.05)$ $(.06)$ $(.06)$ $(.06)$ $(.06)$ $(.06)$ $(.06)$ $(.06)$ $(.06)$ $(.06)$ $(.06)$ $(.06)$ $(.06)$ $(.06)$ $(.06)$	Consumption Intercept ΔC_t^a $\Delta y_t'$ $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_t = 0$ Measure (1) (2) $3y_t'$ $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_t = 0$ Total consumption -77.87 1.06 Total consumption -77.87 1.06 Geometric consumption -77.87 Hold consumption -77.87 Services -7.48 Services -30.97 Nondurables -13.97 Hourables -32.44 Hourables -32.44 Hourables Hourables -32.44	CONSUMPTION INTERCEPT ΔC_i^a Δy_i^i $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_i = 0$ (5) MEASURE (1) (2) (3) (4) (4) (5) (5) Total consumption -77.87 (1.06) (0.2)	Consumption Intercept ΔC_t^a Δy_t^i $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_t = 0$ Measure (1) (2) (3) (4) $\beta_1 = 1, \gamma_t = 0$ $\beta_1 = 1, \gamma_t = 0$ Total consumption -77.87 1.06 $.03$ 1.27 $$ Total consumption -77.87 $(.11)$ $(.02)$ $$ $$ Geometric consumption -77.87 $(.11)$ $(.02)$ $$ $$ Geometric consumption -77.87 $(.10)$ $$ $$ $$ Geometric consumption -77.87 $(.10)$ $$ $$ $$ Services -60.47 1.01 $$ $$ $$ $$ Services -30.47 1.01 $$ $$ $$ $$ Nondurables -13.97 $$ $$ $$ $$ $$ Nondurables -6.03 $$ $$ $$ $$ $$	CONSUMPTION INTERCEPT ΔC_l^a Δy_l^i $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ (5) MEASURE (1) (2) (3) $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ $\beta_1 = 1, \gamma_k = 0$ Total consumption -77.87 1.06 0.03 1.27 \dots Total consumption -77.87 $(.11)$ $(.02)$ 1.27 \dots Georgia -69.07 $(.11)$ $(.007)$ \dots 1.11 Services -69.07 $(.10)$ $(.007)$ \dots 1.11 Services -30.47 $(.10)$ $(.007)$ \dots $$ Nondurables -30.47 $(.10)$ $(.007)$ $$ $$ $$ Nondurables -13.97 $$ $$ $$ $$ $$ Outables -13.97 $$ $$ $$ $$ $$ Durables -13.44 $$ $$ $$ $$ Food	CONSUMPTION INTERCEPT ΔC_i^a Δy_i^i $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_k = 0$ We have the solution of the solut	CONSUMPTION Intercept ΔC_t^a ΔV_t^i $\beta_1 = 1$, $\beta_2 = 0$ $\beta_1 = 1$, $\gamma_h = 0$ Measure Measure (1) (2) (3) (4) (4) (5) Total consumption -77.87 1.06 $.03$ 1.27 $$ Total consumption -77.87 (1.0) $$ $$ $$ Geometric consumption -77.87 1.06 $$ $$ $$ Geometric consumption -77.87 1.01 $$ $$ $$ $$ Services -30.97 1.01 0.07	CONSUMPTION Intercept ΔC_i^a $\Delta \gamma_i'$ $\beta_1 = 1, \beta_2 = 0$ $\beta_1 = 1, \gamma_i = 0$ MEASURE (1) (2) (3) λ_i' $\beta_1 = 1, \gamma_i = 0$ $\beta_1 = 1, \gamma_i = 0$ Total consumption - 77.87 1.06 - 69.07 (11) - 69.07 1.06 (43.55) (.11) Services - 50.47 1.01 Assistances - 30.47 1.01 Nondurables - 13.97 Nondurables - 13.97 Action Action Action Action	CONSUMPTION INTERCEPT ΔC_s^a ΔV_t^i

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090.	.065	.003	800°	.058	.072	.004	600.	005		.013	.005		900.	sion. The degrees
:	.93	:	06.	:	2.78*	:	.92	:		1.39*	:		.20	in parentheses For each measure of consumption, there are 10,692 degrees of freedom in the first regression and 10,633 in the second regression. The degrees level for the Fratios.
1.60	:	1.72	:	3.51*	:	.18	:	1.68			2.78		:	reedom in the first regression a
.002	(100.)	02		900.	(2021)	002	(.003)	.02	(.01)	:	.01	(900.)	:	ere are 10,692 degrees of frond regression.
1.00	1.00	.94	18) .94 .18)	1.00	1.00	.98 .98	(.16) .99	(.16)	(.14)	1.02	(.14) .93	(.13)	.94 (.13)	e of consumption, th on and 61 in the sec
.62	(10:1) 06:- 09:90)	-17.01	(10.69) - 9.83 (94.98)	-6.83	-6.05	$(4.92) \\ 1.92$	$(2.79) \\ 1.30$	(6.36) - 15.40	(12.11)	-21.22	(27.41) - 11.65	(5.70)	-13.58 (13.00)	entheses For each measure s are 2 in the first regression the Fratios.
Utilities		Household furnishings		Clothing		Medical care		Transportation		~	Recreation			Note.—Standard errors are in parentheses For each measure of consumption, there are 10,692 of freedom for the F-ratio numerators are 2 in the first regression and 61 in the second regression. * Significant at the 5 percent level for the F-ratios.

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1 ABLE 3
HOUSEHOLD CONSUMPTION REGRESSIONS: GROWTH RATES

Consumption Measure Total consumption Services Nondurables	INTERCEPT					
Total consumption Services Nondurables Durables	(1)	ΔC_t^a (2)	$\begin{array}{c} \Delta \mathbf{y}_{l}^{J} \\ (3) \end{array}$	$\beta_1 = 1, \beta_2 = 0$ (4)	$\beta_1 = 1, \gamma_k = 0 \forall k$ (5)	R^2 (6)
Services Nondurables Durables	04	1.06	.04	14.12*		.021
Services Nondurables Durables	(.01)	(.08)	(.007)			
Services Nondurables Durables	01	1.05	:	:	1.85*	.029
Services Nondurables Durables	(.01)	(.08)			(A)	
bles	02	.93	.04	12.44*	• • •	.011
Nondurables Durables	(.01)	(.10)	(10.)			
Nondurables Durables	.02	.94	:	:	1.34*	.017
bles	(.02)	(.11)			(B)	
	02	.97	.04	22.69*		.027
	(.01)	(.07)	(900.)			
	01	.95	:	:	1.76*	.033
	(.01)	(.07)			(C)	
	05	1.00	03	.39		046
	(.03)	(90.)	(.03)			
	14	1.01	:	:	1.20	.057
	(60.)	(90.)			(D)	
Food	02	.91	.04	18.67*		.020
	(.01)	(.07)	(900)			
	.01	.89	. :	•	1.81*	.027
	(.01)	(.07)			(E)	
- Housing	05	.79	.01	1.77		900.
	(.01)	(.12)	(.01)			
	03	.79	:		1.47*	.018
	(.03)	(.12)			(F)	

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Utilities	.02	86:	.002	.10	:	.050
	(.01)	(.05)	(.01)			
	01	86:	:		1.40*	.058
	(.02)	(.05)			(9)	
Household furnishings	02	1.00	004	.01		.017
	(.04)	(.14)	(.04)			
	.07	86.	` .		06:	.032
	(.11)	(.15)			(H)	
Clothing	01	1.01	.04	2.19	• •	.078
0	(.02)	(.04)	(.02)			
	.03	1.01	•		.92	.085
	(.05)	(.04)			(I)	
Medical care	90.	99.	.02	3.85*		.004
	(.02)	(.14)	(.02)			
	.12	.65	` :		1.13	.013
	(.04)	(.14)			(1)	
Transportation	04	.83	900.	1.72	· :	.010
•	(.01)	(60.)	(.02)			
	70. –	.84	•		1.06	.017
	(.04)	(60.)			(K)	
Recreation	90	.97	90.	7.44*	. •	.042
	(.02)	(.05)	(.02)			
	03	.97	:	:	.91	.046
	(.04)	(.05)			(L)	

NOTE.—Standard errors are in parentheses. Degrees of freedom for the first regression are listed in order for the 12 measures of consumption: 9,230, 9,270, 9,295, 6,041, 9,281, 6,928, 9,009, 2,276, 6,794, 6,791, 8,386, and 8,786, and 8,746, and 8,746; (1) 57, 6,740; (1) 54, 6,015; (K) 58, 8,326; (L) 56, 8,076. * Significant at the 5 percent level for the F-ratios.

cations are identical to those in table 2, with the first differences of household consumption, aggregate consumption, and household income replaced by growth rates.

For the first regression with income, there are now fewer results consistent with full insurance. On the basis of the *F*-ratio in column 4, the test of the risk-sharing implications of $\beta_1 = 1$ and $\beta_2 = 0$ cannot be rejected for six goods (durables, housing, utilities, household furnishings, clothing, and transportation). The implications are rejected for the remaining six (total consumption, services, nondurables, food, medical care, and recreation). All the rejections in the first regression are the result of $\beta_2 > 0$, with the exception of medical care, for which $\beta_1 < 1$.

The results for the second regression with employment status are consistent with risk sharing for six goods (durables, household furnishings, clothing, medical care, transportation, and recreation). The implications are rejected for total consumption, services, nondurables, food, housing, and utilities.

The common results for income and employment status in table 3 are that the implications cannot be rejected for durables, household furnishings, clothing, and transportation and are rejected for total consumption, services, nondurables, and food. The results for income and employment status differ for four goods. For housing and utilities, income is not significant, although employment status is. For clothing and recreation, employment status is not significant, although income is.

The growth rate implications for power utility, with multiplicative preference shocks, are not applicable in the case of durable goods. If the risk-sharing model is an accurate description of observed allocations and if power utility is the correct specification of preferences, then one expects to find the risk-sharing implications rejected only for the more durable goods. The results in table 3 fail to support this scenario. Of the goods for which the risk-sharing implications cannot be rejected, three are possibly the most durable of the 12: durables, household furnishings, and transportation. The implications are rejected for the least durable goods: services, nondurables, and food.

When the results in tables 2 and 3 are compared, the first-difference specification fares reasonably well whereas the growth rate specification does not. The results common to both specifications are rejections for nondurables in the first regression and for both nondurables and food in the second regression. The coefficients on income and employment status are significant for these goods. For both specifications, the implications cannot be rejected in the first regression for five goods (durables, housing, utilities, household furnishings, and transportation) and in the second regression for four goods (durables, household furnishings, medical care, and recreation).

One possible explanation for the divergence in results between the first-difference and growth rate specifications is that lower-income households are effectively given a larger weight than other households in the growth rate specification. For example, the first difference of income, $\Delta y_l^j = y_l^l - y_{l-1}^j$, is weighted by $1/y_{l-1}^l$ to compute the growth rate of income. This weight is larger the lower the household's income. If some households are not fully insured, they would tend to be households in the lower-income groups. Hence, in the growth rate specification, the group that would be more likely to cause rejections of the risk-sharing model are weighted most heavily.

One way to evaluate this argument is to test the model separately on high- and low-income households. According to the argument above, there would tend to be more rejections of full insurance for the low-income households. However, that is not the outcome for the current sample (not reported here). This might be due to the heavy concentration of the oldest age cohort in the low-income group. Households with a reference person 60 years of age and older account for 31 percent of the entire sample. Of this cohort, 74 percent have income below the sample mean. The oldest age cohort accounts for 42 percent of the low-income households. This concentration occurs because households are classified by reported income and not by wealth or accumulated assets. Other empirical studies tend to exclude retired individuals from the sample.

C. Econometric Issues

Unbiased estimation of the coefficients requires a zero correlation between the disturbance term and the right-hand-side variables of aggregate consumption and household income. The disturbance term may include both preference shocks and measurement errors from the data. For example, correlations between preference shocks to consumption and income might arise, such as an illness resulting in no employment and reduced consumption. Correlations between the disturbance and right-hand-side variables might also arise because of measurement errors in the data. The following discussion is limited to the first-difference specification.

The current results do not correct for possible correlations between household income and the disturbance. However, a bias of the coefficient on aggregate consumption can be avoided by testing a modified version of the first-difference specification:

$$\Delta C_t^j - \Delta C_t^a = \beta_2 \Delta y_t^j + u_t^j. \tag{19}$$

The change in aggregate consumption is simply subtracted from the

⁸ This was pointed out to me by Marjorie Flavin.

change in household consumption so that a unit coefficient on aggregate consumption is imposed. The only right-hand-side variable is the change in household income or employment status. As before, the risk-sharing model predicts zero coefficients for these variables. The results (not reported here) are identical to those in table 2.

A related but more specific issue is whether the seasonal preference shocks to consumption and income are correlated. The CES consumption data are monthly observations and reveal large seasonal fluctuations. In contrast, the income data are reported as annual figures. In addition to household income, the risk-sharing model is also tested using quarterly changes in employment status. Hence seasonal preference shocks to consumption and employment status might be correlated.

To account for the common seasonal component of preference shocks, a simple procedure is to include seasonal dummy variables in the specifications in equations (17) and (18). For the two interview months used for each household, there are 12 possible combinations of months. For example, the first interview takes place in January and the last interview in October, the first interview takes place in February and the last interview in November, and so forth. Hence 11 seasonal dummy variables and an intercept are incorporated.

The seasonal results (not reported here) are almost identical to the nonseasonal results in tables 2 and 3. The seasonal dummies are jointly insignificant in all cases. There are no changes in the significance of income and employment status when the seasonals are added. Overall, the results are not sensitive to the inclusion of seasonal dummies. However, these findings are not interpreted as an indication of no seasonals in preference shocks.

Finally, a small-sample issue arises because individual consumption, the dependent variable, is included in aggregate consumption. It appears that the monthly samples from which aggregate consumption is constructed are sufficiently small for the individual to influence the aggregate. A solution is to create a different aggregate consumption variable for each individual by excluding that individual's consumption from the average. The aggregate consumption variable for individual j is denoted

$$C_t^{aj} = \frac{1}{J-1} \sum_{k \neq j}^J C_t^k.$$

An implication of risk sharing is that an individual's consumption moves together with the consumption of all other individuals.

The results (not reported here) using the modified aggregate consumption as a right-hand-side variable show dramatic changes in β_1

but no changes in β_2 . The coefficient on the modified aggregate consumption (β_1) is smaller for all goods. Hence, the monthly samples are "small enough" for the individual to influence the aggregate.

This small-sample correction can also be combined with the modified test in equation (19). The modified aggregate consumption variable is simply subtracted from the change in household consumption:

$$\Delta C_t^j - \Delta C_t^{aj} = \beta_2 \Delta \gamma_t^j + u_t^j. \tag{20}$$

As before, this imposes a unit coefficient on aggregate consumption. The results (not reported here) reveal no change in the coefficient on income.

In summary, a biased coefficient on aggregate consumption is avoided through various modifications of the empirical specification. However, the current tests do not correct for possible biases of the coefficient on income. The current results are fairly consistent across income and employment status. This is encouraging if, as one would expect, there is less measurement error in employment status responses than in reported income.

VI. Summary

The principal implication of risk sharing is that individual consumption varies positively with aggregate consumption. The solutions are specialized for two specifications of homothetic preferences: exponential and power utility. For exponential utility, the first differences of consumption, net of preference shocks, are equalized across individuals. The growth rates of consumption are equalized in the case of power utility.

Although the overall results are somewhat indecisive, the first-difference specification registers considerable success for the benchmark case of full insurance. Once the change in aggregate consumption is accounted for, the change in household income does not help to explain the change in household consumption. In contrast, many of the results for the growth rate specification reject full insurance.

The most striking results are the insignificant coefficients for the changes in household income and employment status. This is especially noteworthy considering the tremendous spectrum of households included in the sample. Those included are not limited to employed heads of households. Also included are single individuals as young as 18 years of age, the unemployed, the retired, and others not in the labor force such as welfare recipients.

Using a fresh data source adds further interest to the findings. The thoroughness of the CES consumption data is unmatched by any other source of household data for the United States. Previous empir-

ical work is primarily based on aggregate data or on food expenditures from the Panel Study of Income Dynamics.

The current evidence suggests that market imperfections or incomplete markets are not "the" essential features in explaining allocations. Although this might not hold perfectly for an entire life cycle, there appear to be ample sources of insurance in the economy. In addition to the traditional sources of credit and securities markets, these include private and family sources of insurance and various institutional sources such as unemployment compensation, contracts between employers and employees, and crop insurance for farmers.

The current research does not identify the sources of the proposed insurance, but it does suggest its presence. Additional research in the area of risk sharing is justified. The evidence in this paper strongly suggests that it is too soon to close the door on complete markets.

Appendix

The principal risk-sharing implications continue to hold for more general homothetic preferences. This includes the case of multiple goods—for both separable and nonseparable within-period preferences—and durable goods.

Multiple Nondurable Goods

I begin with a class of homothetic power utility functions (see Eichenbaum and Hansen 1990). These preferences are both time and state separable but are nonseparable across goods if $\sigma \neq \alpha$:

$$U[C_{i}^{j}, b_{i}^{j}] = \frac{1}{\alpha} \left\{ \sum_{i=1}^{m} \theta_{i} V[C_{il}^{j}, b_{il}^{j}] \right\}^{\alpha/\sigma} - \frac{1}{\alpha}, \tag{A1}$$

where *i* denotes good *i*, *m* is the number of goods, and $\sum_{i=1}^{m} \theta_i = 1$. For the case of a single good, m = 1, $\sigma = \alpha$, and $\theta_i = 1$. For power utility,

$$V[C_{tt}^{j}, b_{tt}^{j}] = \exp(\sigma b_{tt}^{j})(C_{tt}^{j})^{\sigma}. \tag{A2}$$

Strict concavity requires $\sigma < 1$. Individuals have the same coefficient of constant relative risk aversion $(1 - \sigma)$.

Some special cases of the utility function are noted. First, within-period preferences are separable across goods if $\sigma = \alpha$:

$$U[C_{i}^{j}, b_{i}^{j}] = \frac{1}{\sigma} \left[\sum_{i=1}^{m} \theta_{i} \exp(\sigma b_{il}^{j}) (C_{il}^{j})^{\sigma} \right] - \frac{1}{\sigma}.$$
 (A3)

More specifically, preferences are logarithmically separable if $\sigma = \alpha = 0$:

$$U[C_{i}^{j}, b_{i}^{j}] = \sum_{i=1}^{m} \theta_{i} \exp(b_{u}^{j}) \log C_{u}^{j}.$$
 (A4)

With multiplicative rather than additive preference shocks, the utility function in equation (A3) must be modified in order to obtain multiplicative preference shocks for the special case of logarithmic preferences. The cur-

rent specification of $\exp(\sigma b)C^{\sigma} - 1$ in equation (A3) must be replaced by $\exp(b)(C^{\sigma} - 1)$ so that preference shocks are included in the marginal utility of consumption.

The social planner's problem is now solved subject to m aggregate constraints, corresponding to the m goods. There are m marginal conditions for each individual j, as in equation (7). The marginal condition for each good is independent of the consumption and preference shocks of all other goods. Hence with separable preferences across goods, the risk-sharing implication of equation (11) holds in the case of multiple nondurable goods. With consumption indexed by good i,

$$\log C_{u}^{j} = \log C_{u}^{a} + \frac{1}{1 - \sigma} (\log \omega^{j} - \omega^{a}) + \frac{\sigma}{1 - \sigma} (b_{u}^{j} - b_{u}^{a}), \quad i = 1, \dots, m.$$
(A5)

The next extension involves preferences that are nonseparable across goods ($\sigma \neq \alpha$ in eq. [A1]). A special case is Cobb-Douglas preferences. If $\alpha = 1$ and $\sigma = 0$,

$$U[C_{i}^{j}, b_{i}^{j}] = \prod_{i=1}^{m} \exp(\theta_{i} b_{il}^{j}) (C_{il}^{j})^{\theta_{i}}.$$
 (A6)

To illustrate, suppose that preferences are Cobb-Douglas, there are two goods, and $\theta_1 + \theta_2 \neq 1$. Consumption of good 1 for individual j is

$$\log C_{1t}^{j} = \log C_{1t}^{a} + \frac{1}{\Phi} (\log \omega^{j} - \omega^{a}) + \frac{\theta_{1}}{\Phi} (b_{1t}^{j} - b_{1t}^{a}) + \frac{\theta_{2}}{\Phi} (b_{2t}^{j} - b_{2t}^{a}), \quad (A7)$$

where $\phi = 1 - \theta_1 - \theta_2$. For Cobb-Douglas preferences, an individual's consumption of good 1 is positively related to the aggregate consumption of good 1. However, in contrast to the separable case, consumption of good 1 depends on the preference shocks of both goods.

The next example of nonseparable preferences involves the more general power utility in equation (A2). While one is unable to obtain a direct analytical solution, conditions implied by the solutions for separable preferences are satisfied by the first-order conditions in the nonseparable case. For example, in the two-good case, the relationship between individual and aggregate consumption of the two goods is

$$\log C_{1t}^{j} - \log C_{2t}^{j} - \frac{\sigma}{1 - \sigma} (b_{1t}^{j} - b_{2t}^{j})$$

$$= \log C_{1t}^{a} - \log C_{2t}^{a} - \frac{\sigma}{1 - \sigma} (b_{1t}^{a} - b_{2t}^{a}).$$
(A8)

This condition is satisfied by the following expressions for consumption:

$$\log C_{1t}^{j} = \log C_{1t}^{a} + \frac{1}{1 - \sigma} (\log \omega^{j} - \omega^{a}) + \gamma_{1} (b_{1t}^{j} - b_{1t}^{a}) + \gamma_{2} (b_{2t}^{i} - b_{2t}^{a})$$
 (A9)

and

$$\log C^{j}_{2t} = \log C^{a}_{2t} + \frac{1}{1 - \sigma} (\log \omega^{j} - \omega^{a}) + \gamma_{3} (b^{j}_{1t} - b^{a}_{1t}) + \gamma_{4} (b^{j}_{2t} - b^{a}_{2t}).$$
(A10)

If $\gamma_1 = \gamma_4 = \sigma/(1 - \sigma)$ and $\gamma_2 = \gamma_3 = 0$, consumption in the nonseparable case is identical to that in the separable case (see eq. [11]). The Cobb-Douglas case is represented by $\gamma_1 = \gamma_3 = \theta_1/\varphi$ and $\gamma_2 = \gamma_4 = \theta_2/\varphi$.

Next, the risk-sharing implications continue to hold for various modifications of exponential preferences. For good i,

$$V[C_{tt}^{j}, b_{tt}^{j}] = -\exp[-\sigma(C_{tt}^{j} - b_{tt}^{j})]. \tag{A11}$$

For multiple goods and separable preferences ($\sigma = \alpha$), consumption of good i for individual j is

$$C_{u}^{j} = C_{u}^{a} + \frac{1}{\sigma}(\log \omega^{j} - \omega^{a}) + (b_{u}^{j} - b_{u}^{a}).$$
 (A12)

This is identical to the case of a single good.

For exponential preferences that are nonseparable ($\sigma \neq \alpha$), a direct analytical solution is not obtained. However, as with the previous example for two goods, it is possible to derive the relationship between individual and aggregate consumption of the two goods:

$$C_{1t}^{j} - C_{2t}^{j} - (b_{1t}^{j} - b_{2t}^{j}) = C_{1t}^{a} - C_{2t}^{a} - (b_{1t}^{a} - b_{2t}^{a}).$$
 (A13)

This condition is satisfied by the expression for consumption under separable preferences.

Durable Goods

The previous risk-sharing implications analyzed for nondurable goods also apply to the acquisition of durable goods in the case of exponential preferences. This does not hold for the class of power utility functions with multiplicative preference shocks.

A durable good is defined as a risk-free claim to services in current and future time periods. Preferences are defined over current services, where services refer to the previous nondurable goods. The number of services is equal to the number of durable goods.

The current treatment of durable goods concentrates on the measurement of durables for empirical implementation. Data are available on acquisitions of durable goods but not on the services derived from these goods. Although preferences are time separable for services, they are not time separable for the durable good. The current analysis does not take into account this departure from time separability: allocations are made in terms of services, which are simply proportional to the stocks of durable goods.

An additional assumption is that, in the initial trading period, the distribution of endowments of durable goods across individuals is identical to the distribution of the social planner's weights. This restriction on initial conditions, together with the former assumptions, is sufficient for the previous risk-sharing implications to carry over to the acquisition of durable goods.

Consider the case of a single durable good. For individual j, let D_i^j denote the time t acquisition of the durable good and let K_i^j denote the stock of the durable good. The stock depreciates at the rate 1 - a (0 < a < 1). Consequently, aK_{i-1}^j units of the stock from time t-1 remain at time t. The current stock is equal to the remaining stock from time t-1 plus the current acquisition of the durable good:

$$K_{t}^{j} = aK_{t-1}^{j} + D_{t}^{j}. (A14)$$

Services are proportional to the stock of the durable good, with w representing the factor of proportionality:

$$C_t^j = wK_t^j. (A15)$$

The expression for service consumption is identical to that previously derived in equation (8). Substituting (A15) into equation (8) yields

$$K_t^j = K_t^a + \frac{1}{w\sigma} (\log \omega^j - \omega^a) + \frac{1}{w} (b_t^j - b_t^a),$$
 (A16)

where

$$K_t^a = \frac{1}{J} \sum_{j=1}^J K_t^j.$$

Equation (A14) is then substituted into equation (A16) to yield

$$D_t^j = D_t^a + a(K_{t-1}^a - K_{t-1}^j) + \frac{1}{w\sigma}(\log \omega^j - \omega^a) + \frac{1}{w}(b_t^j - b_t^a), \quad (A17)$$

where

$$D_t^a = \frac{1}{J} \sum_{j=1}^J D_t^j.$$

Equation (A17) is further reduced by substituting in the time t-1 expression for equation (A16):

$$D_t^j = D_t^a + (1-a)\frac{1}{w\sigma}(\log \omega^j - \omega^a) + \frac{1}{w}[(b_t^j - ab_{t-1}^j) - (b_t^a - ab_{t-1}^a)].$$
 (A18)

Taking the first difference of equation (A18) yields

$$\Delta D_t^j = \Delta D_t^a + \frac{1}{w} [(\Delta b_t^j - a \Delta b_{t-1}^j) - (\Delta b_t^a - a \Delta b_{t-1}^a)], \tag{A19}$$

where

$$\Delta D_{t}^{j} = D_{t}^{j} - D_{t-1}^{j}, \quad \Delta D_{t}^{a} = \frac{1}{J} \sum_{j=1}^{J} \Delta D_{t}^{j}.$$

The risk-sharing implication for services carries over to the acquisition of durable goods. An individual's acquisition of durables varies positively with the aggregate acquisition of durables. As previously stated, this is important for empirical implementation since data are available on acquisitions of durable goods but not on the services derived from these goods.

The result above is sensitive to assumptions regarding initial conditions. If the initial distribution of endowments of durable goods differs from the distribution of planner weights, then the risk-sharing implication for durables must be interpreted as an asymptotic one. Even then, the relationship between individual and aggregate acquisitions of durables is a useful approximation.

References

- Brennan, Michael J., and Kraus, Alan. "Necessary Conditions for Aggregation in Securities Markets." *J. Financial and Quantitative Analysis* 13 (September 1978): 407–18.
- Cochrane, John H. "A Simple Test of Consumption Insurance." J.P.E., this issue.
- Constantinides, George M. "Intertemporal Asset Pricing with Heterogeneous Consumers and without Demand Aggregation." J. Bus. 55 (April 1982): 253–67.
- Eichenbaum, Martin S., and Hansen, Lars Peter. "Estimating Models with Intertemporal Substitution Using Aggregate Time Series Data." J. Bus. and Econ. Statis. 8 (January 1990): 53–69.
- Eichenbaum, Martin S.; Hansen, Lars Peter; and Richard, Scott. "Aggregation, Durable Goods, and Nonseparable Preferences in an Equilibrium Asset Pricing Model." Working Paper no. 87-9. Chicago: Nat. Opinion Res. Center, August 1987.
- Gorman, William M. "Community Preference Fields." *Econometrica* 21 (January 1953): 63–80.
- Kihlstrom, Richard, and Pauly, Mark. "The Role of Insurance in the Allocation of Risk." A.E.R. Papers and Proc. 61 (May 1971): 371–79.
- Leme, Paulo. "Integration of International Capital Markets." Manuscript. Chicago: Univ. Chicago, February 1984.
- Mace, Barbara. "Consumption Volatility: Full Insurance in the Presence of Aggregate Uncertainty." Ph.D. dissertation, Univ. Chicago, 1988.
- Negishi, Takashi. "Welfare Economics and Existence of an Equilibrium for a Competitive Economy." *Metroeconomica* 12 (August/December 1960): 92–97.
- Rubinstein, Mark. "An Aggregation Theorem for Securities Markets." J. Financial Econ. 1 (September 1974): 225–44.
- Scheinkman, José A. "General Equilibrium Models of Economic Fluctuations: A Survey of Theory." Manuscript. Chicago: Univ. Chicago, 1984.
- Townsend, Robert M. "Arrow-Debreu Programs as Microfoundations of Macroeconomics." In *Advances in Economic Theory: Fifth World Congress*, vol. 2, edited by Truman Bewley. New York: Cambridge Univ. Press, 1987.
- ——. "Risk and Insurance in Village India." Manuscript. Chicago: Univ. Chicago, 1989.
- Wilson, Robert B. "The Theory of Syndicates." *Econometrica* 36 (January 1968): 119–32.