Statistical Adjustment and Assessment of Adjustment in Observational Studies

ICPSR 2018 Session 2 August 02, 2018

Today

- Agenda: The problem of covariance adjustment to reduce "bias"/ confounding. How can we answer the question about whether we have adjusted enough. A simple approach: stratification on one categorical variable (and interaction effects). A more complex approach: find sets that are as similar as possible in terms of a continuous variable (bipartite matching). Balance assessment after stratification.
- 2 Reading for tomorrow and next week: DOS 8-9, 13 and Gelman and Hill, 2006, § 9.5, and Ho et al., 2007
- Questions arising from the reading or assignments or life?

- 1 Strategies for Causal Inference
- 2 But first, how to assess the randomization process in an experiment.
- 3 Did we control for enough?

Before fielding the study

- Plan the design for interpretability and power.
- Pre-register your analysis plan and experimental design.

After outcome data have been collected

- Make the case that randomization worked.
- Increase precision with design and test statistics (and even models of effects)
- Make sure that your estimator is estimating the right thing (i.e. is not biased or at least is consistent)
- Make sure that your test has a controlled false positive rate and is as powerful
 as possible (i.e. the coverage rate of a confidence interval is nominal, the Type
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- If you have randomized Z but not D, then IV. (Not really an observational study.)
- Find a discontinuity/A Natural Experiment (RDD: either natural experiment or continuous forcing function)
- Multiple controls (i.e. "Choice as an alternative to control" Rosenbaum, 1999)
- "Controlling For"
- Difference in Differences
- Matched Stratification (approximating a block-randomized experiment)
- Best matched subset selection (approximating a completely or simply randomized experiment)
- Weighting
- Direct theoretical modeling / Directed Acyclic Graphs (DAGS) to guide other data modeling choices.

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→ 5 / 39

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- 3 Did we control for enough?

This is what randomization ensures:

$$(Y_t, Y_c, X) \perp Z$$

I.e., each of X, Y_c and Y_t is balanced between treatment and control groups (in expectation; given variability from randomization).

- In controlled experiments, random assignment warrants this.
- In natural experiments, justified otherwise, this is an article of faith.
- In an experiment, the xes aren't necessary for inference (although they can be used, carefully, to increase precision in both the design and analysis phases of a project).
- However, the part with the xes has testable consequences.

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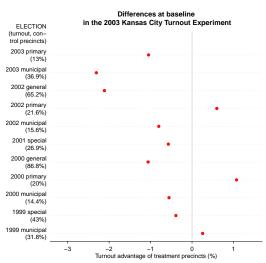
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Covariate balance in experiments

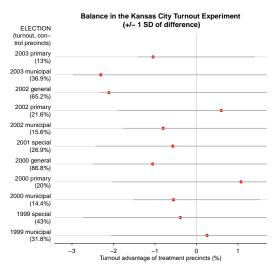
- Arceneaux, 2005
- Kansas City, November 2003
- Completely randomized design: 14 precincts → Tx; 14 → Control.
- Substantively large baseline differences
- Differences not large compared to other possible assignments from same design; compared to other possible experiments with the same design.
- $Pr(\chi^2 > x) = .91$ (Hansen and Bowers, 2008).



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Δ



How did we do this?

xh1\$results

v s1997

0.15490

0.15659 0.001684

```
, , strata = unstrat
stat
```

```
Control Treatment adi.diff adi.diff.null.sd std.diff
vars
 v p2003
          0.12996
                     0.11949 -0.010469
                                              0.013994 -0.28041 -0.74815 0.4544
 v m2003
          0.36868
                    0.34561 -0.023072
                                              0.029669 -0.29171 -0.77763 0.4368
 v_g2002
          0.65195
                    0.63083 -0.021119
                                              0.023207 -0.34283 -0.91003 0.3628
 v p2002
          0.21589
                    0.22187 0.005980
                                              0.018757 0.11848 0.31883 0.7499
 v m2002
          0.15567
                    0.14766 -0.008016
                                              0.017721 -0.16841 -0.45233 0.6510
 v s2001
          0.26898
                    0.26327 -0.005709
                                              0.024302 - 0.08722 - 0.23492 0.8143
 v g2000
          0.86812
                    0.85755 -0.010576
                                              0.024878 -0.15821 -0.42512 0.6707
                                              0.020187 0.19827 0.53177 0.5949
 v p2000
          0.20033
                     0.21106 0.010735
 v m2000
           0.14404
                     0.13849 -0.005552
                                              0.015249 -0.13536 -0.36405 0.7158
 v s1999
           0.42957
                     0.42569 -0.003887
                                              0.027343 -0.05275 -0.14216 0.8870
           0.31756
                                              0.020532 0.04624 0.12463 0.9008
 v m1999
                     0.32012 0.002559
 v g1998
           0.43718
                     0.44900 0.011824
                                              0.026134 0.16844 0.45243 0.6510
 v m1998
           0.18136
                     0.17315 - 0.008210
                                              0.021114 -0.14463 -0.38886 0.6974
 v s1998
          0.24104
                     0.24254 0.001496
                                              0.019385 0.02863 0.07719 0.9385
 v m1997
           0.13388
                     0.12856 -0.005326
                                              0.013300 -0.14898 -0.40047 0.6888
```

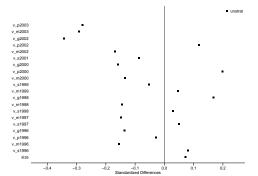
0.012635 0.04945 0.13327 0.8940

How did we do this?

xb1\$overall

chisquare df p.value unstrat 12.93 21 0.911

plot(xb1)



DeMystifying xBalance

```
d.stat<-function(zz, mm, ss){
    ## this is the d statistic (harmonic mean weighted diff of means statistic)
## from Hansen and Bowers 2008
h.fn<-function(n, m){(m*(n-m))/n}
myssn<-apply(mm, 2, function(x){sum((zz-unsplit(tapply(zz, ss, mean), ss))*x)})
hs<-tapply(zz, ss, function(z){h.fn(m=sum(z), n=length(z))})
mywtsum<-sum(hs)
myadjdiff<-myssn/mywtsum
return(myadjdiff)
}</pre>
```

Calculate the reference distribution of the d-stat and the

 d^2 stat Does d^2 follow a χ^2 distribution in this case?

For all vectors $z \in \Omega$ get adj.diffs. This is the distribution of the d statistic

```
acorncovs<-c("v_p2003","v_m2003","v_g2002","v_p2002","v_m2002","v_s2001","v_g2000","v_p2000","v_d.dist<-replicate(10000, d.stat(sample(acorn$z), acorn[,acorncovs], ss=rep(1,nrow(acorn))))
```

Get the randomization-based p-values:

```
xb1ds <- xb1$results[,"adj.diff",]
xb1ps <- xb1$results[,"p",]
obs.d<-d.stat(acorn$z, acorn[, acorncovs], rep(1,nrow(acorn)))
dps <- matrix(NA,nrow=length(obs.d),ncol=1)
for(i in 1:length(obs.d)){
    dps[i,] <- 2*min( mean(d.dist[i,] >= obs.d[i]),mean(d.dist[i,] <= obs.d[i]))
}
## You can compare this to the results from xBalance
round(cbind(randinfps=dps[,1],xbps=xb1ps,obsdstats=obs.d,xbdstats=xb1ds),3)</pre>
```

```
randinfps xbps obsdstats xbdstats
v_p2003
           0.454 0.454
                         -0.010
                                  -0.010
v m2003
           0.450 0.437
                        -0.023 -0.023
v_g2002
           0.384 0.363
                         -0.021 -0.021
v p2002
          0.775 0.750
                         0.006
                                 0.006
v m2002
           0.656 0.651
                         -0.008 -0.008
v s2001
           0.801 0.814
                         -0.006
                                  -0.006
v g2000
           0.726 0.671
                         -0.011
                                  -0.011
```

0 011

0 011

0 612 0 505 4

TT 70000

Calculate the reference distribution of the d-stat and the d^2 stat

The d^2 statistic is a linear function of the *d*-statistics that accounts for the covariance between those statistics (across the possible assignments under the null hypothesis of no effects).

```
d2.stat <- function(dstats,ddist=NULL,theinvcov=NULL){
  ## d is the vector of d statistics
  ## ddist is the matrix of the null reference distributions of the d statistics
  if(is.null(theinvcov) & !is.null(ddist)){
    as.numeric( t(dstats) %*% solve(cov(t(ddist))) %*% dstats)
} else {
    as.numeric( t(dstats) %*% theinvcov %*% dstats)
}
</pre>
```

Calculate the reference distribution of the d-stat and the

<u>d²</u> stat

The distribution of the d^2 statistic arises from the distribution of the d statistics — for each draw from the set of treatment assignments we can collapse the d-statistics into one d^2 . And so we can calculate the p-value for the d^2 .

xb1\$overall

chisquare df p.value unstrat 12.93 21 0.911

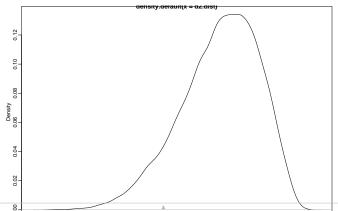
H 14 / 39

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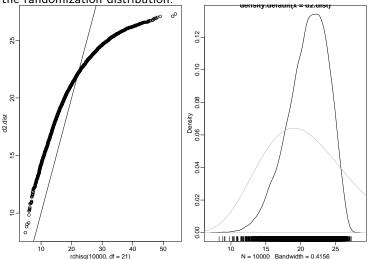
plot(density(d2.dist))
rug(d2.dist)



Why differences between xBalance and d2?

I suspect that ${\it N}=28$ is too small. xBalance uses an asymptotic approximation to

the randomization distribution.

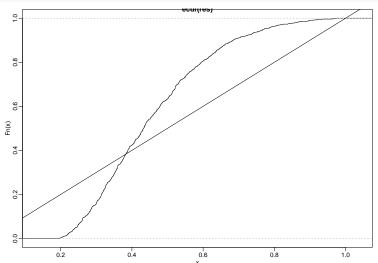


Does xBalance have a controlled false positive rate here?

```
xbfn <- function(){
    acorn$newz <- sample(acorn$z)</pre>
    xb1 <- xBalance(newz ~ v_p2003 + v_m2003 + v_g2002 + v_p2002 + v_m2002 + v_s2001 +
           v_g2000 + v_p2000 + v_m2000 + v_s1999 + v_m1999 + v_g1998 +
           v m1998 + v s1998 + v m1997 + v s1997 + v g1996 + v p1996 +
           v m1996 + v s1996 + size, data=acorn.
       report = 'chisquare.test')
    return(xb1$overall[["p.value"]])
res <- replicate(1000,xbfn())
summary(res)
  Min. 1st Qu. Median Mean 3rd Qu.
                                          Max.
  0.192 0.331 0.432
                         0.459 0.558
                                         0.976
mean(res <= .05)
[1] 0
mean(res \le .2)
[1] 0.003
```

Does xBalance have a controlled false positive rate here?

plot(ecdf(res))
abline(0,1)



Does the simulation based approach have a controlled false

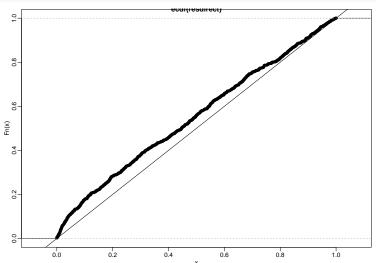
positive rate here?

```
d2pfn <- function(z,X){
    newz \leftarrow sample(z)
    d.dist<-replicate(1000, d.stat(sample(newz), X, ss=rep(1,nrow(X))))</pre>
    obs.d<-d.stat(newz, X, rep(1,nrow(X)))
    dps <- matrix(NA,nrow=length(obs.d),ncol=1)</pre>
    for(i in 1:length(obs.d)){
         dps[i,] \leftarrow 2*min(mean(d.dist[i,]) \rightarrow obs.d[i]), mean(d.dist[i,] \leftarrow obs.d[i]))
    invCovDDist <- solve(cov(t(d.dist)))</pre>
    obs.d2<- d2.stat(obs.d.d.dist.invCovDDist)
    d2.dist<-apply(d.dist, 2, function(thed){
                     d2.stat(thed,theinvcov=invCovDDist)
         1)
    d2p < -mean(d2.dist > = obs.d2)
    return(d2p)
```

Does the simulation based approach have a controlled false positive rate here?

Does xBalance have a controlled false positive rate here?

plot(ecdf(resdirect))
abline(0,1)



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Introducing the Medellin Data

```
load(url("http://jakebowers.org/Data/meddat.rda"))
```

The data Cerdá collected tell us about the roughly 45 neighborhoods in the study, 22 of which had access to the Metrocable line and 23 did not.

We don't have a formal codebook. Here are some guesses about the meanings of some of the variables. There are more variables in the data file than those listed here

```
## The Intervention
             Intervention neighborhood (0=no Metrocable station, 1=Metrocable station)
nhTrt.
## Some Covariates (there are others, see the paper itself)
nh03
             Neighborhood id
nhGroup
             Treatment (T) or Control (C)
nhTrt.
            Treatment (1) or Control (0)
nhHom
             Mean homicide rate per 100,000 population in 2003
nhDistCenter Distance to city center (km)
nhLogHom
             Log Homicide (i.e. log(nhHom))
## Outcomes (BEO3.CEO3.PVO3.QPO3.TPO3 are baseline versions)
BE
        Neighborhood amenities Score 2008
CE
        Collective Efficacy Score 2008
ΡV
        Perceived Violence Score 2008
QP
        Trust in local agencies Score 2008
TP
        Reliance on police Score 2008
        Homicide rate per 100,000 population Score 2008-2003 (in log odds)
hom
                                                                                            23 / 39
```

What is the effect of the Metrocable on Homicides? One approach: Estimate the average treatment effect of Metrocable on Homicides after the stations were built.

```
## code here
themeans<-group_by(meddat,nhTrt) %>% summarise(ybar=mean(HomRate08))
diff(themeans$ybar)

[1] -0.2899
lmOne <- lm(HomRate08-nhTrt,meddat)
coef(lmOne)["nhTrt"]
    nhTrt
-0.2899
library(estimatr)
difference_in_means(HomRate08-nhTrt,meddat)

Design: Standard</pre>
```

Estimate Std. Error t value Pr(>|t|) CI Lower CI Upper DF nhTrt -0.2899 0.1508 -1.922 0.06137 -0.5942 0.01445 41.87

In principle, how might we use the testing approach to take a first stab at this question?

code here

What are alternative explanations for this effect?

We claim that the policy intervention had some effect. What are alternative explanations?

Do we have any concerns about confounding?

Sometimes people ask about "bias from observed confounding" or "bias from selection on observables".

How would we interpret the following results? (Recall how we justified the use of xBalance in terms of randomization above.)

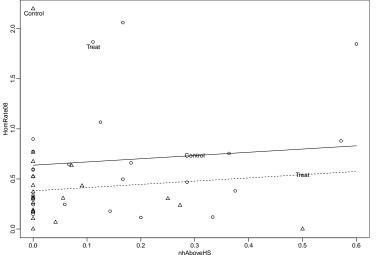
```
xbMed1 <- xBalance(nhTrt~nhAboveHS,data=meddat,report="all")
xbMed1$overall
       chisquare df p.value
           4.598 1 0.03201
unstrat
xbMed1$results
  , strata = unstrat
          stat
           Control Treatment adj.diff adj.diff.null.sd std.diff
                     0.05829 -0.1047 0.04883 -0.668 -2.144 0.03201
 nhAboveHS
             0.163
attr(, "originals")
[1] "nhAboveHS"
```

How would you adjust for Proportion Above HS Degree?

Part of the Metrocable effect is not about Metrocable per se, but rather about the education of people in the neighborhood. How should we remove nhAboveHS from our estimate or test? What strategies can you think of?

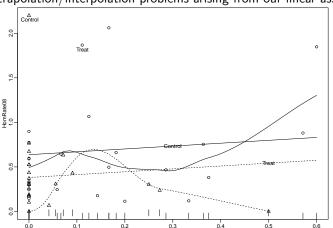
One approach to this problem: model-based adjustment

Let's try to just adjust for this covariate in a very common manner:



Did we adjust enough?

Maybe adding some more information to the plot can help us decide whether, and to what extend, we effectively "controlled for" the proportion of the neighborhood with more than High School education. Specifically, we might be interested in assessing extrapolation/interpolation problems arising from our linear assumptions.



How should we interpret this adjustment? How should we judge the improvement that we made? What concerns might we have?

nhAboveHS

Back to the randomized experiment to help make a case

for appropriate adjustment

It seems like arguments about plots may be difficult to resolve. How about going back to xBalance? The idea of a standard against which we can compare a given design. How might we do this in this case?

Attempt 1: Stratification ... but two estimates rather than one adjusted estimate

```
lm1a <- lm(HomRate08-nhTrt,data=meddat,subset=nhAboveHS>=.1)
lm1b <- lm(HomRate08-nhTrt,data=meddat,subset=nhAboveHS<=.1)</pre>
```

Attempt 2: Stratified adjustment

```
lm1c <- lm(HomRate08-nhTrt+I(nhAboveHS>=.1),data=meddat)
coef(lm1c)["nhTrt"]

nhTrt
-0.224
```

And balance assessment after stratification:

```
xbHS1 <- xBalance(nhTrt~nhAboveHS,strata=list(hs=~I(nhAboveHS>=.1)),data=meddat,report="all")
xbHS1$overall
```

```
chisquare df p.value
hs 0.3912 1 0.5317
```

The Curse of Dimensionality and linear adjustment for one more variable.

What about more than one variable? Have we controlled for both population density and educational attainment enough? How would we know?

```
lm2x <- lm(HomRate08 ~ nhTrt + nhPopD + nhAboveHS, data=meddat)
coef(lm2x)["nhTrt"]

nhTrt
-0.1224

Maybe another plot?

meddat$nhTrtF <- factor(meddat$nhTrt)
library(car)
scatter3d(HomRate08-nhAboveHS+nhPopD,
    groups=meddat$nhTrtF,
    data=meddat,surface=TRUE,
    fit=c("linear")) #additive"))</pre>
```

Can we improve stratified adjustment?

Rather than two strata, why not three?

```
lm1cut3 <- lm(HomRate08-nhTrt+cut(nhAboveHS,3),data=meddat)
coef(lm1cut3)["nhTrt"]</pre>
```

nhTrt -0.3161

But why those cuts? And why not 4? Why not ...?

One idea: collect observations into strata such that the sum of the differences in means of nhAboveHS within strata is smallest? This is the idea behind optmatch and other matching approaches.

The optmatch workflow: The distance matrix

tmp <- meddat\$nhAboveHS

[1] 0.1429

Introduction to optmatch workflow. To minimize differences requires a matrix of those differences (in general terms, a matrix of distances between the treated and control units)

Do the match

fm1 <- fullmatch(absdist,data=meddat)</pre>

summary(fm1, min.controls=0, max.controls=Inf)

```
Structure of matched sets:
7:1 2:1 1:1 1:2 1:4 1:5
1  2  7  2  1  1
Effective Sample Size: 17.4
(equivalent number of matched pairs).
```

table(meddat\$nhTrt,fm1)

Evaluate the design: Within set differences Look within sets:

```
meddat.fm1 <- fm1
rawmndiffs <- with(meddat, mean(nhAboveHS[nhTrt==1]) - mean(nhAboveHS[nhTrt==0]))
setdiffs <- meddat %>% group by(fm1) %>% summarize(mneddiffs =
                           mean(nhAboveHS[nhTrt==1]) -
                           mean(nhAboveHS[nhTrt==0]),
                       mnAboveHS = mean(nhAboveHS),
                       minAboveHS = min(nhAboveHS).
                       maxAboveHS = max(nhAboveHS))
setdiffs
```

```
# A tibble: 14 x 5
          mneddiffs mnAboveHS minAboveHS maxAboveHS
    fm1
    <fct>
              <dbl>
                        <dbl>
                                    <dbl>
                                               <db1>
  1 1.1
            0
                       0
  2 1.10
  3 1.15
         -0.0516
                       0.134
                                   0.0909
                                              0.167
  4 1.16
          -0.0102
                       0.0520
                                   0.0417
                                              0.0588
  5 1.17
  6 1.19
          -0.0667
                       0.326
                                   0.273
                                              0.375
  7 1.2
  8 1.20
            0.00476
                       0.0690
                                   0.0667
                                              0.0714
  9 1.3
 10 1.4
            0
                                   0
 11 1.5
 12 1.6
            0.0591
                       0.211
                                   0.182
                                              0.25
13 1.7
           -0.0857
                       0.557
                                   0.5
                                              0.6
```

Evaluate the design: Compare to a randomized experiment.

```
xbHS2 <- xBalance(nhTrt~nhAboveHS,
                strata=list(nostrat=NULL.
                           hsmatch=~fm1),
                data=meddat.report="all")
xbHS2$results
 . strata = nostrat
          stat
vars
          Control Treatment adj.diff adj.diff.null.sd std.diff z
 nhAboveHS 0.163 0.05829 -0.1047 0.04883 -0.668 -2.144 0.03201
, , strata = hsmatch
          stat
          Control Treatment adj.diff adj.diff.null.sd std.diff z
vars
 nhAboveHS 0.113 0.09937 -0.01366 0.008237 -0.08714 -1.658 0.09728
attr(, "originals")
[1] "nhAboveHS"
xbHS2$overall
```

chisquare df p.value 4.598 1 0.03201

hsmatch 2.750 1 0.09728

nostrat

→ 36 / 39

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- How to justify an adjustment strategy for an observational study? The linear model adjustment strategy is difficult to justify. A stratification based strategy is easier to justify, inspect, learn from. (We can compare our stratification to a block randomized experiment, to a known design, a known standard.)
- How to choose a stratification? We can do it by hand. Or we can delegate to a computer (i.e. optmatch) — we can think of it as an optimization problem and ask the computer to optimize.

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