"Challenges to Randomization:

Noncompliance and Missing Data"

Jake Bowers, Ben Hansen & Tom Leavitt
June 22, 2025

Today

- Agenda: One step away from easy to interpret experiments: non-random doses/compliance (Gerber and Green, 2012) Chapter 5, non-random missing data (Gerber and Green, 2012) Chapter 7 and the Threats module of The Theory and Practice of Field Experiments.
- Recap: We use statistics to infer about unobservable counterfactual quantities (functions of potential outcomes); we can estimate unobservable averages; we can test unobservable hypotheses; we can test unobservable hypotheses about averages.
- 3 Questions arising from the reading or assignments or life?

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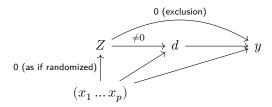
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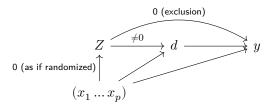
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- Causal effects when we do not control the dose
- 2 Hypothesis Tests about Complier causal effects
- 3 Learning about causal effects when data are missing

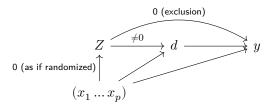
- Z_i is random assignment to a visit $(Z_i = 1)$ or not $(Z_i = 0)$.
- $d_{i,Z_i=1}=1$ means that person i would open the door to have a conversation when assigned a visit.
- $d_{i,Z_i=1}=0$ means that person i would not open the door to have a conversation when assigned a visit.
- Opening the door is an outcome of the treatment.



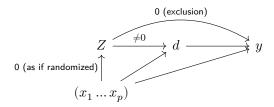
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- \bullet Y : outcome $(y_{i,Z} \mbox{ or } y_{i,Z_i=1} \mbox{ for potential outcome to treatment for person } i,$ fixed)
- X : covariate/baseline variable
- Z : treatment assignment ($Z_i=1$ if assigned to a visit, $Z_i=0$ if not assigned to a visit)
- D: treatment received $(D_i=1 \text{ if answered door, } D_i=0 \text{ if person } i \text{ did not answer the door)}$ (using D here because $D_i=d_{i,1}Z_i+d_{i,0}(1-Z_i)$)

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We have two causal effects of $Z\colon Z\to Y$ (known as δ , ITT, ITT $_Y$), and $Z\to D$ (known as ITT $_D,\,p_c$).

And different types of people can react differently to the attempt to move the dose with the instrument.

$$Z=1 \\ D=0 \qquad D=1$$

$$Z=0 \quad D=1 \quad \text{Never taker} \quad \text{Complier} \\ D=0 \quad D=1 \quad \text{Defier} \quad \text{Always taker}$$

The
$$ITT=ITT_Y=\delta=\bar{y}_{Z=1}-\bar{y}_{Z=0}.$$

But, in this design, $\bar{y}_{Z=1}=\bar{y}_1$ is split into pieces: the outcome of those who answered the door (Compliers and Always-takers and Defiers). Write p_C for the proportion of compliers in the study, p_A for proportion always-takers, etc... The proportions have to sum to 1. So, we have weighted averages:

$$\bar{y}_1 = (\bar{y}_1|C)p_C + (\bar{y}_1|A)p_A + (\bar{y}_1|N)p_N + (\bar{y}_1|D)p_D.$$

And \bar{y}_0 is also split into pieces:

$$\bar{y}_0 = (\bar{y}_0|C)p_C + (\bar{y}_1|A)p_A + (\bar{y}_0|N)p_N + (\bar{y}_0|D)p_D.$$

So, the ITT itself is a combination of the effects of ${\cal Z}$ on ${\cal Y}$ within these different groups.

People who are compliers tend to be different types of people than people who are always takers: comparisons across types would raise questions about how to interpret the results — interpretations that would focus more on differences in types than in differences caused by Z.

But, we can still estimate it because we have unbiased estimators of \bar{y}_1 and \bar{y}_0 within each type.

Learning about the ITT I

First, let's learn about the effect of the policy itself.

Let's assume we have no defiers ($p_D=0$). The we can write the ITT more simply.

$$\bar{y}_1 = (\bar{y}_1|C)p_C + (\bar{y}_1|A)p_A + (\bar{y}_1|N)p_N$$

$$\bar{y}_0 = (\bar{y}_0|C)p_C + (\bar{y}_0|A)p_A + (\bar{y}_0|N)p_N$$

Learning about the ITT II

First, let's learn about the effect of the policy itself. We assume no defiers ($p_D=0$), which allows us to write the ITT more simply.

$$\begin{split} ITT = & \bar{y}_1 - \bar{y}_0 \\ = & ((\bar{y}_1|C)p_C + (\bar{y}_1|A)p_A + (\bar{y}_1|N)p_N) - \\ & ((\bar{y}_0|C)p_C + (\bar{y}_0|A)p_A + (\bar{y}_0|N)p_N) \end{split}$$

collecting each type together — to have an ITT for each type

$$\begin{split} &= ((\bar{y}_1|C)p_C - (\bar{y}_0|C)p_C) + ((\bar{y}_1|A)p_A - (\bar{y}_0|A)p_A) + \\ &\quad ((\bar{y}_1|N)p_N - (\bar{y}_0|N)p_N) \\ &= \underbrace{((\bar{y}_1|C) - (\bar{y}_0|C))}_{\text{ITT among Compliers}} p_C + \\ &\underbrace{((\bar{y}_1|A) - (\bar{y}_0|A))}_{\text{ITT among Always-Takers}} p_A + \underbrace{((\bar{y}_1|N) - (\bar{y}_0|N))}_{\text{ITT among Never-Takers}} p_N \end{split}$$

Learning about the ITT III

$$\begin{split} ITT = & \bar{y}_1 - \bar{y}_0 \\ = & ((\bar{y}_1|C)p_C + (\bar{y}_1|A)p_A + (\bar{y}_1|N)p_N) - \\ & ((\bar{y}_0|C)p_C + (\bar{y}_0|A)p_A + (\bar{y}_0|N)p_N) - \\ = & ((\bar{y}_1|C)p_C - (\bar{y}_0|C)p_C) + ((\bar{y}_1|A)p_A - (\bar{y}_0|A)p_A) + \\ & ((\bar{y}_1|N)p_N - (\bar{y}_0|N)p_N) - \\ = & ((\bar{y}_1|C) - (\bar{y}_0|C))p_C + ((\bar{y}_1|A) - (\bar{y}_0|A))p_A + \\ & ((\bar{y}_1|N) - (\bar{y}_0|N))p_N - \\ = & (\text{ITT among compliers}) \text{(proportion of compliers)} + \\ & (\text{ITT among always takers}) \text{(proportion of always takers)} + \dots \end{split}$$

Learning about the ITT IV

And, if the effect of the dose can only occur for those who open the door, and you can only open the door when assigned to do so then:

$$((\bar{y}_1|A)-(\bar{y}_0|A))p_A=0$$
 and $((\bar{y}_1|N)-(\bar{y}_0|N))p_N=0$

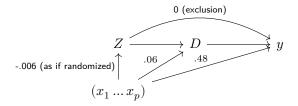
And so, under these assumptions, the ITT is a simple function of the ITT among compliers and the proportion of compliers.

$$ITT = ((\bar{y}_1|C) - (\bar{y}_0|C))p_C = (CACE)p_C.$$

The complier average causal effect I

If we want to can learn about the the causal effect of answering the door and having the conversation why not just compare people who answer the door to people who do not?

The problem with this "as-treated" or "per-protocol" comparison is that this comparison is confounded by x: a simple $\bar{Y}|D=1-\bar{Y}|D=0$ comparison tells us about differences in the outcome due to x in addition to the difference caused by D. (Numbers below from some simulated data)



The complier average causal effect II

In actual data:

```
with(dat, cor(Y, x)) ## can be any number
with(dat, cor(d, x)) ## can be any number
with(dat, cor(Z, x)) ## should be near 0
```

And we just saw that, in this design, and with these assumptions (including a SUTVA assumption) that $ITT=((\bar{y}_1|C)-(\bar{y}_0|C))p_C=(CACE)p_C$, so we can define $CACE=ITT/p_C$. That is, we can learn about the effect of answering the door without worrying about the bias from x (or any set of x's).

VERY COOL You can learn about the causal effect of a non-random intervention (deciding to open the door) without "controlling for" x_1,x_2,\ldots in this case.

How to calculate the ITT and CACE/LATE I

Some example data (where we know all potential outcomes):

	ID	u0	u	type	D_Z_0	D_Z_1	Y_D_0	Y_D_1	Y_D_0_Z_0	Y_D_1_Z_0	Y_D_0_Z_1	Y_D_1_
1	084	1.9981	1.9981	Complier	0	1	1.9981	2.3159	1.9981	1.9981	2.1570	2.1
2	088	0.2715	0.2715	Never-Taker	0	0	0.2715	0.5893	0.2715	0.2715	0.4304	0.4
3	058	0.5844	0.5844	Complier	0	1	0.5844	0.9022	0.5844	0.5844	0.7433	0.7
4	056	-0.2696	0.0000	Complier	0	1	0.0000	0.3178	0.0000	0.0000	0.1589	0.1
5	079	-0.5471	0.0000	Never-Taker	0	0	0.0000	0.3178	0.0000	0.0000	0.1589	0.1
6	037	-1.0258	0.0000	Never-Taker	0	0	0.0000	0.3178	0.0000	0.0000	0.1589	0.1
7	005	0.3836	0.3836	Always-Taker	1	1	0.3836	0.7014	0.3836	0.3836	0.5425	0.5
8	069	1.0501	1.0501	Never-Taker	0	0	1.0501	1.3679	1.0501	1.0501	1.2090	1.2
9	015	0.6378	0.6378	Never-Taker	0	0	0.6378	0.9556	0.6378	0.6378	0.7967	0.7
10	073	0.1597	0.1597	Never-Taker	0	0	0.1597	0.4775	0.1597	0.1597	0.3186	0.3
11	040	-0.4824	0.0000	Never-Taker	0	0	0.0000	0.3178	0.0000	0.0000	0.1589	0.1
12	081	-0.7989	0.0000	Always-Taker	1	1	0.0000	0.3178	0.0000	0.0000	0.1589	0.1
13	042	-1.1265	0.0000	Never-Taker	0	0	0.0000	0.3178	0.0000	0.0000	0.1589	0.1
14	098	-1.0627	0.0000	Complier	0	1	0.0000	0.3178	0.0000	0.0000	0.1589	0.1
15	052	-0.4323	0.0000	Never-Taker	0	0	0.0000	0.3178	0.0000	0.0000	0.1589	0.1
ı												

How to calculate the ITT and CACE/LATE II

The ITT and CACE (the parts)

How to calculate the ITT and CACE/LATE III

All together (the version dividing an unbiased estimator of ITT by an unbiased estimator of Proportion Compliers is often called Bloom's method from Bloom (1984)):¹

 $^{^1}$ works when Z o D is not weak see Imbens and Rosenbaum (2005) for a cautionary tale

Variance of IV estimator

- ullet Recall that there exist analytic expressions for $\mathrm{Var}\left[\widehat{\mathsf{ITT}}_Y
 ight]$ and $\mathrm{Var}\left[\widehat{\mathsf{ITT}}_D
 ight]$
- We can conservatively estimate $\operatorname{Var}\left[\widehat{\mathsf{ITT}}_Y\right]$ and $\operatorname{Var}\left[\widehat{\mathsf{ITT}}_D\right]$ via $\widehat{\operatorname{Var}}\left[\widehat{\mathsf{ITT}}_Y\right]$ and $\widehat{\operatorname{Var}}\left[\widehat{\mathsf{ITT}}_D\right]$
- However, in general, there is no closed-form analytic expression for the variance of a random ratio
- We do not have an estimator for $\operatorname{Var}\left[\frac{\widehat{\mathsf{ITT}}_Y}{\widehat{\mathsf{ITT}}_D}\right]$ that is known to be unbiased, consistent or conservative
- Bloom (1984) proposed treating $\widehat{\mathsf{ITT}}_D$ as fixed
- Others use Delta method (Taylor series approximation), e.g., in AER or estimatr package in R

How do our estimators perform?

```
First, setup estimands and estimators:
```

2 ITT_y 0.1731

```
estimands <- declare inquiry(
  CACE = mean(Y D 1[type == "Complier"] - Y D 0[type == "Complier"]),
  ITT v = mean(((Y D 1 Z 1 + Y D 0 Z 1) / 2) - ((Y D 1 Z 0 + Y D 0 Z 0) / 2)).
 ITT d = mean(D Z 1) - mean(D Z 0)
estimator_cace <- declare_estimator(Y ~ D | Z, .method = iv_robust, inquiry = c("CACE"), label =
estimator itt y <- declare estimator(Y ~ Z, inquiry = "ITT y", .method = lm robust, label = "diff
estimator pp <- declare estimator(Y ~ D. inquiry = "CACE", .method = lm robust, label = "per-prot
estimator_itt_d <- declare_estimator(D ~ Z, inquiry = "ITT_d", .method = lm_robust, label = "diff
full design <- base_design + estimands +
  estimator cace + estimator itt y + estimator itt d + estimator pp
draw estimands(full design)
  inquiry estimand
1 CACE 0.3462
```

3 ITT d 0.4300 estimator term estimate std.error outcome inquiry iv robust D 0.41648 0.24444 CACE 2 diff means ITT Z 0.16659 0.09036 Y ITT v 3 diff means ITT_D Z 0.40000 0.08122

4 per-protocol D 0.04589 0.09725

draw estimates(full design)[, c("estimator", "term", "estimate", "std.error", "outcome", "inquiry

D ITT d

Y CACE

How do our estimators perform?

Then repeat the design many times:

```
full_designs_by_size <-
  redesign(full_design, N = c(50, 100, 200, 1000), prop_comply = c(.2, .5, .8))
dat n20 <- draw data(full designs by size[["design 1"]])
my_diagnosands <-
  declare diagnosands(
    mean estimand = mean(estimand),
   mean_estimate = mean(estimate),
    bias = mean(estimate - estimand),
    rmse = sqrt(mean((estimate - estimand)^2)),
    ## power = mean(p.value <= alpha).
    coverage = mean(estimand <= conf.high & estimand >= conf.low).
    sd_estimate = sqrt(pop.var(estimate)),
   mean se = mean(std.error)
library(future)
library(future.apply)
plan(strategy = "multicore") ## won't work on Windows
which to sim <- rep(1, length = length(full design))
names(which_to_sim) <- names(full_design)</pre>
which_to_sim["the_assign"] <- 1000
set.seed(12345)
results <- diagnose_design(full_designs_by_size,
  bootstrap_sims = 0,
  sims = 1000, # which to sim,
 diagnosands = my diagnosands
                                                                                             20 / 40
```

Summary of Encouragement/Complier/Dose oriented designs:

- Analyze as you randomized: even when you don't control the dose you can learn something.
- The danger of per-protocol analysis: you give up the benefits of the research design (i.e. randomization)
- Variance calculations approximate (and can be untrustworthy in small samples, with weak instruments, and in other cases where we would worry about consistency (rare binary outcomes, very skewed outcomes, interdependence, ...)
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Hypothesis Tests about Complier causal effects

- We can test the sharp null hypothesis no effect among all units
- We know by random assignment that this test
 - 1) will have a type I error probability at least as small as α
 - 2 will have power greater than α for a class of alternative hypotheses
- Under what conditions /assumptions is a test of the sharp null of no effect among all units equivalent to a test of the sharp null of no effect among Compliers?
 - Exclusion restriction
 - No Defiers
 - 3 Non-zero proportion of Compliers
 - 4 Non-interference

Sharp null hypothesis testing example

The null hypothesis of no complier causal effect states that the individual causal effect of \mathbf{Z} on \mathbf{Y} is 0 among units who are Compliers.

Along with the exclusion restriction (i.e., that the individual causal effect is 0 for Always Takers and Never Takers) and the assumption of no Defiers, we can "fill in" missing potential outcomes according to the null hypothesis of no complier causal effect as follows:

$$\begin{split} Y_{c,0,i} &= \begin{cases} Y_i - D_i \tau_i & \text{if } D_i = 1 \\ Y_i + (1 - D_i) \, \tau_i & \text{if } D_i = 0 \end{cases} \\ Y_{t,0,i} &= \begin{cases} Y_i - D_i \tau_i & \text{if } D_i = 1 \\ Y_i + (1 - D_i) \, \tau_i & \text{if } D_i = 0, \end{cases} \end{split}$$

where $\tau_i = 0$ for all i.

Sharp null hypothesis testing example

Imagine that our observed data is as follows:

\mathbf{z}	\mathbf{y}	$\mathbf{y_c}$	$\mathbf{y_t}$	d	d_c	$\mathbf{d_t}$
1	14	?	14	0	?	0
0	22	22	?	0	0	?
1	21	?	21	1	?	1
1	36	?	36	1	?	1
0	23	23	?	0	0	?
0	12	12	?	1	1	?
0	25	25	?	1	1	?
1	27	?	27	0	?	0

Observed experimental data

The observed Difference-in-Means test statistic, $\hat{\tau}(\mathbf{Z}, \mathbf{Y})$, is 16.75. What is the distribution of that test statistic under the null hypothesis of no effects for any complier?

We can represent the sharp null hypothesis of no effect for all units without hypothesizing about non-random compliance (this is like the ITT_Y in that both can be assessed safely in a randomized experiment).

${f z}$	\mathbf{y}	$\mathbf{y_c}$	$\mathbf{y_t}$	d	$\mathbf{d_c}$	$\mathbf{d_t}$	Principal stratum
1	14	?	14	0	?	0	Never Taker or Defier
0	22	22	?	0	0	?	Complier or Never Taker
1	21	?	21	1	?	1	Complier or Always Taker
1	36	?	36	1	?	1	Complier or Always Taker
0	23	23	?	0	0	?	Complier or Never Taker
0	12	12	?	1	1	?	Always Taker or Defier
0	25	25	?	1	1	?	Always Taker or Defier
1	27	?	27	0	?	0	Never Taker or Defier

Sharp null of no effect for all units

We can represent the sharp null hypothesis of no effect for all units without hypothesizing about non-random compliance (this is like the ITT_Y in that both can be assessed safely in a randomized experiment).

${f z}$	\mathbf{y}	$\mathbf{y_c}$	$\mathbf{y_t}$	d	$\mathbf{d_c}$	$\mathbf{d_t}$	Principal stratum
1	14	14	14	0	?	0	Never Taker or Defier
0	22	22	22	0	0	?	Complier or Never Taker
1	21	21	21	1	?	1	Complier or Always Taker
1	36	36	36	1	?	1	Complier or Always Taker
0	23	23	23	0	0	?	Complier or Never Taker
0	12	12	12	1	1	?	Always Taker or Defier
0	25	25	25	1	1	?	Always Taker or Defier
1	27	27	27	0	?	0	Never Taker or Defier

Sharp null of no effect for all units

The null hypothesis of no effect among compliers under excludability (only a complier in the treatment group can have a causal effect), no defiers and nonzero proportion of compliers assumptions:

${f z}$	\mathbf{y}	$\mathbf{y_c}$	$\mathbf{y_t}$	d	$\mathbf{d_c}$	$\mathbf{d_t}$	Principal stratum
1	14	14	14	0	0	0	Never Taker or Defier
0	22	22	22	0	0	?	Complier or Never Taker
1	21	21	21	1	?	1	Complier or Always Taker
1	36	36	36	1	?	1	Complier or Always Taker
0	23	23	23	0	0	?	Complier or Never Taker
0	12	12	12	1	1	1	Always Taker or Defier
0	25	25	25	1	1	1	Always Taker or Defier
1	27	27	27	0	0	0	Never Taker or Defier

Sharp null of no effect among Compliers

We don't need to know which of units 2-5 are Compliers, only that at least one of these 4 units is a Complier.

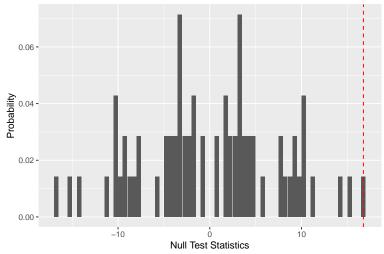
Excludability means that the effect must be 0 for all units who are not compliers (i.e. implying the sharp null).

The null hypothesis of no effect among compliers under excludability (meaning that only a complier in the treatment group can have a causal effect), no defiers and nonzero proportion of Compliers assumptions:

\mathbf{z}	\mathbf{y}	$\mathbf{y_c}$	$\mathbf{y_t}$	d	$\mathbf{d_c}$	$\mathbf{d_t}$	Principal stratum
1	14	14	14	0	0	0	Never Taker or Defier
0	22	22	22	0	0	?	Complier or Never Taker
1	21	21	21	1	?	1	Complier or Always Taker
1	36	36	36	1	?	1	Complier or Always Taker
0	23	23	23	0	0	?	Complier or Never Taker
0	12	12	12	1	1	1	Always Taker or Defier
0	25	25	25	1	1	1	Always Taker or Defier
1	27	27	27	0	0	0	Never Taker or Defier

Sharp null of no effect among Compliers

So: a regular test of the sharp null of no effects is also a test of the sharp null of no effects among compliers (under the assumptions of no defiers, non-zero compliers, exclusion, and no interference). The fact that $\tau_i=0$ for Never Takers and Always Takers is by assumption, not a hypothesis.



Distribution of the Difference-in-Means test statistic under the sharp null of no effect: under the assumptions of excludability (no effects on Always Takers and Never Takers), no defiers, at least one complier, and SUTVA, this is a test of the hypothesis of no effects on compliers.

Summary

- The sharp null of no effects is meaningful and can be tested in a randomized experiment using assignment to treatment and ignoring compliance.
- The assumptions of excludability, no defiers, and at least one complier mean that we can interpret the test of the sharp null of no effects as a test of the sharp null of no effects on compliers: those assumptions require no effects among always-takers and never-takers, and there are no defiers in the data (again, all of this by assumption).
- Notice: no need for approximations; weak instruments do not threaten the validity of the statistical inferences.

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- Causal effects when we do not control the dose.
- 2 Hypothesis Tests about Complier causal effects
- 3 Learning about causal effects when data are missing

Review of core assumptions from randomized experiments

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- Non-interference
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 - some records are lost.
- This is a problem when treatment affects missingness.
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 - For example, treatment may have caused units to migrate and cannot be reache
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Summary about Missing data and Experiments.

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