#### - MODULE VoucherCancel

This specification describes the cancellation of Voucher between an Issuer and a Holder. It is implemented over the Two-Phase Commit protocol, in which a Voucher Transaction Provider (VTP) coordinates the Voucher Issuers (Is) to cancel vouchers (Vs) to Voucher Holders (Hs) as described in the VoucherLifeCycle specification module. In this specification, Hs and Is spontaneously issue Prepared messages. We ignore the Prepare messages that the VTP can send to the Hs and Is.

For simplicity, we also eliminate Abort messages sent by an Hs / Is when it decides to abort. Such a message would cause the VTP to abort the transaction, an event represented here by the VTP spontaneously deciding to abort.

Note: This operation is an addendum to the operations described in RFC 3506. This operation is not described in the RFC.

#### CONSTANT

 $egin{array}{ll} V\,, & {
m The \ set \ of \ Voucher} \ H\,, & {
m The \ set \ of \ Voucher \ Holders} \ I & {
m The \ set \ of \ Voucher \ Issuers} \ \end{array}$ 

#### VARIABLES

vState, vState[v] is the state of voucher v. vlcState, vlcState[v] is the state of the voucher life cycle machine. hState, hState[h] is the state of voucher holder h. iState, iState[i] is the state of voucher issuer i. vtpState, vtp

msgs

In the protocol, processes communicate with one another by sending messages. For simplicity, we represent message passing with the variable msgs whose value is the set of all messages that have been sent. A message is sent by adding it to the set msgs. An action that, in an implementation, would be enabled by the receipt of a certain message is here enabled by the presence of that message in msgs. For simplicity, messages are never removed from msgs. This allows a single message to be received by multiple receivers. Receipt of the same message twice is therefore allowed; but in this particular protocol, that's not a problem.

"Prepared for Voucher Cancel" messages.

 $Messages \triangleq$ 

The set of all possible messages. Messages of type "Prepared" are sent from the H indicated by the message's vh field to the VTP. Similar "Prepared" is also sent from I indicated by message's vh field to the VTP. Messages of type "Cancel" and "Abort" are broadcast by the VTPs, to be received by all Hs and Is. The set msgs contains just a single copy of such a message.

```
 \begin{split} [type: \{ \text{``Prepared''} \}, \ vh: H] \cup \\ [type: \{ \text{``Prepared''} \}, \ vi: I] \ \cup \\ [type: \{ \text{``Cancel''}, \text{``Abort''} \}] \end{split}
```

## $VTPTypeOK \triangleq$

The type-correctness invariant

## $VTPInit \triangleq$

The initial predicate.

We now define the actions that may be performed by the processes, first the VTP's actions, the Hs' actions, then the Is' actions.

```
VTPRcvPrepared(h, i) \triangleq
```

The VTP receives a "Prepared" message from Voucher Holder h and the Voucher Issuer i. We could add the additional enabling condition  $h, i \notin vtpCP$  repared, which disables the action if the VTP has already received this message. But there is no need, because in that case the action has no effect; it leaves the state unchanged.

# $VTPCancel(v) \triangleq$

The VTP Cancels the voucher; enabled iff the VTP is in its initial state and every H and I has sent a "Prepared" message.

```
\land vState[v] = "valid"
   \land vlcState[v] = "working"
   \land vtpState = "init"
   \land vtpCPrepared = H \cup I
   \wedge vtpState' = "done"
   \land vState' = [vState \ \texttt{EXCEPT} \ ![v] = "cancelled"]
  \land vlcState' = [vlcState \ EXCEPT \ ![v] = "done"]
   \land \mathit{msgs'} = \mathit{msgs} \cup \{[\mathit{type} \mapsto \text{``Cancel''}]\}
   \land UNCHANGED \langle hState, iState, vtpCPrepared \rangle
VTPAbort(v) \stackrel{\triangle}{=}
  The VTP spontaneously aborts the transaction.
   \land \mathit{vState}[\mathit{v}] = \mathit{``valid''}
  \land vlcState[v] = "working"
  \land vtpState = "init"
   \land vtpState' = "done"
   \land msgs' = msgs \cup \{[type \mapsto \text{``Abort''}]\}
   \land UNCHANGED \langle vState, vlcState, hState, iState, vtpCPrepared <math>\rangle
HPrepare(h) \triangleq
  Voucher holder h prepares.
  \land vState = [v \in V \mapsto "valid"]
  \land vlcState = [v \in V \mapsto "working"]
   \wedge hState[h] = "holding"
   \land hState' = [hState \ \texttt{EXCEPT} \ ![h] = "prepared"]
   \land msgs' = msgs \cup \{[type \mapsto "Prepared", vh \mapsto h]\}
   \land UNCHANGED \langle vState, vlcState, vtpState, iState, vtpCPrepared <math>\rangle
HChooseToAbort(h) \triangleq
  Voucher holder h spontaneously decides to abort. As noted above, h does not send any message
  in our simplified spec.
  \land vState = [v \in V \mapsto "valid"]
   \land vlcState = [v \in V \mapsto "working"]
  \wedge hState[h] = "holding"
   \land hState' = [hState \ EXCEPT \ ![h] = "aborted"]
   \land UNCHANGED \langle vState, vlcState, vtpState, iState, vtpCPrepared, msgs <math>\rangle
HRcvCancelMsg(h) \triangleq
  Voucher holder h is told by the VTP to Cancel
  \land vState \in [V \rightarrow \{\text{"valid"}, \text{"cancelled"}\}]
   \land vlcState \in [V \rightarrow \{\text{"working"}, \text{"done"}\}]
  \wedge hState[h] = \text{"holding"}
   \land [type \mapsto "Cancel"] \in msgs
   \wedge hState' = [hState \ EXCEPT \ ![h] = "cancelled"]
   \land UNCHANGED \langle vtpState, vState, vlcState, iState, vtpCPrepared, msgs <math>\rangle
```

```
HRcvAbortMsg(h) \triangleq
```

```
Voucher holder h is told by the VTP to abort.
   \land vState = [v \in V \mapsto "valid"]
   \land vlcState = [v \in V \mapsto "working"]
   \land hState[h] = "holding"
   \land [type \mapsto \text{``Abort''}] \in msgs
   \land \ hState' = [hState \ \texttt{EXCEPT} \ ![h] = \texttt{"aborted"}]
   \land UNCHANGED \langle vState, vlcState, vtpState, iState, vtpCPrepared, msgs <math>\rangle
IPrepare(i) \triangleq
  Voucher issuer i prepares.
   \land vState = [v \in V \mapsto \text{``valid''}]
   \land vlcState = [v \in V \mapsto "working"]
   \land \mathit{iState}[\mathit{i}] = \mathit{``waiting''}
   \land iState' = [iState \ EXCEPT \ ![i] = "prepared"]
   \land msgs' = msgs \cup \{[type \mapsto "Prepared", vi \mapsto i]\}
   \land UNCHANGED \langle vState, vlcState, vtpState, hState, vtpCPrepared <math>\rangle
IChooseToAbort(i) \stackrel{\Delta}{=}
  Voucher issuer i spontaneously decides to abort. As noted above, i does not send any message
  in our simplified spec.
   \land vState = [v \in V \mapsto "valid"]
   \land vlcState = [v \in V \mapsto "working"]
   \land \mathit{iState}[\mathit{i}] = \mathit{``waiting''}
   \wedge iState' = [iState \ EXCEPT \ ![i] = "aborted"]
   \land UNCHANGED \langle vState, vlcState, vtpState, hState, vtpCPrepared, msgs <math>\rangle
IRcvCancelMsg(i) \triangleq
  Voucher issuer i is told by the VTP to Cancel.
   \land vState \in [V \rightarrow \{\text{"valid"}, \text{"cancelled"}\}]
   \land vlcState \in [V \rightarrow \{\text{"working"}, \text{"done"}\}]
   \wedge iState[i] = "waiting"
   \land [type \mapsto \text{``Cancel''}] \in msqs
   \land iState' = [iState \ EXCEPT \ ![i] = "cancelled"]
   \land UNCHANGED \langle vtpState, vState, vlcState, hState, vtpCPrepared, msgs <math>\rangle
IRcvAbortMsg(i) \triangleq
  Voucher issuer i is told by the VTP to abort.
   \land vState = [v \in V \mapsto \text{``valid''}]
   \land vlcState = [v \in V \mapsto "working"]
   \wedge iState[i] = "waiting"
   \land [\mathit{type} \mapsto \text{``Abort"}] \in \mathit{msgs}
```

 $\land \ \, \mathsf{UNCHANGED} \ \left\langle vState, \ vlcState, \ vtpState, \ hState, \ vtpCPrepared, \ msgs \right\rangle$ 

 $\land iState' = [iState \ EXCEPT \ ![i] = "aborted"]$ 

```
VTPNext \triangleq \\ \lor \exists v \in V : \\ VTPCancel(v) \lor VTPAbort(v) \\ \lor \exists h, i \in H \cup I : \\ VTPRcvPrepared(h, i) \\ \lor \exists h \in H : \\ HPrepare(h) \lor HChooseToAbort(h) \\ \lor HRcvAbortMsg(h) \lor HRcvCancelMsg(h) \\ \lor \exists i \in I : \\ IPrepare(i) \lor IChooseToAbort(i) \\ \lor IRcvAbortMsg(i) \lor IRcvCancelMsg(i) \\ \end{aligned}
```

### $VTPConsistent \triangleq$

A state predicate asserting that a H and an I have not reached conflicting decisions. It is an invariant of the specification.

 $VTPVars \triangleq \langle hState, iState, vState, vlcState, vtpState, vtpCPrepared, msgs \rangle$ 

 $VTPSpec \triangleq VTPInit \land \Box [VTPNext]_{VTPVars}$ 

The complete spec of the a Voucher Cancel using Two-Phase Commit protocol.

### THEOREM $VTPSpec \Rightarrow \Box(VTPTypeOK \land VTPConsistent)$

This theorem asserts the truth of the temporal formula whose meaning is that the state predicate  $VTPTypeOK \wedge VTPConsistent$  is an invariant of the specification VTPSpec. Invariance of this conjunction is equivalent to invariance of both of the formulas VTPTypeOK and VTPConsistent.

We now assert that the Voucher Cancel specification implements the Voucher Life Cycle specification of a voucher mentioned in module VoucherLifeCycle. The following statement imports all the definitions from module VoucherLifeCycle into the current module.

INSTANCE VoucherLifeCycle

### THEOREM $VTPSpec \Rightarrow VSpec$

This theorem asserts that the specification VTPSpec of the Two-Phase Commit protocol implements the specification VSpec of the Voucher life cycle specification.

- **\\*** Modification History
- \\* Last modified Tue Jun 12 13:03:21 IST 2018 by Fox
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