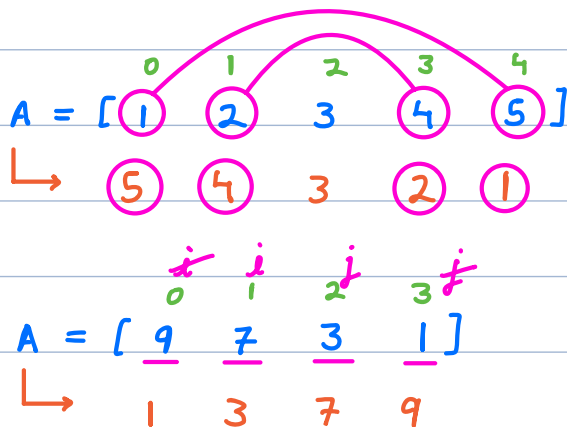


Q → Reverse the given integer array.



$i = 0$      $j = N - 1$

while ( $i < j$ ) {

<p>    swap (<math>A, i, j</math>) → <math>t = A[i]</math></p> <p>    <math>i++</math>                      <math>A[i] = A[j]</math></p> <p>    <math>j--</math>                      <math>A[j] = t</math></p> <p>}</p>	<p>    </p>
--	-------------

swap ( $x, y$ )

$x = 7$

$y = 4$

$x = x + y$     ( $7 + 4$ )

$y = x - y$     ( $7$ )

$x = x - y$

$TC = O(N)$      $SC = O(1)$

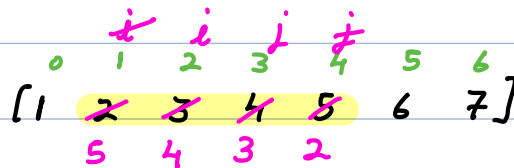
Q → Reverse a subarray from index  $L$  to  $R$ .

continuous part of array

$i = L$      $j = R$

while ( $i < j$ ) {

<p>    swap (<math>A, i, j</math>)</p> <p>    <math>i++</math></p> <p>    <math>j--</math></p> <p>}</p>	<p>    </p>
---	-------------



$L = 1$

$R = 4$

$TC = O(N)$      $SC = O(1)$

Q → Given an integer array & multiple queries, for each query find sum of elements from L to R.

Perform a task multiple times.

A = [-3, 6, 2, 4, 5, 2, 8]

Queries

(L, R)

2 5 → 13

0 1 → 3

4 6 → 15

// B[N][2] → B[i][0] } i<sup>th</sup> query  
B[i][1]

Bruteforce →

```
for i → 0 to (Q-1) {
    L = B[i][0]    R = B[i][1]
    sum = 0
    for j → L to R {
        sum += A[j]
    }
    print(sum)
}
```

TC =  $O(Q \times N)$

SC =  $O(1)$

Q, N ≤  $10^5$

⇒ TLE

Cricket (Harsh)

Over → 1 2 3 4 5 6 7 8 9 10  
Score → 0 2 8 14 29 31 49 65 79 88 97  
after every over

Runs scored in 7<sup>th</sup> over =  $65 - 49 = 16$

Runs scored from 6<sup>th</sup> to 10<sup>th</sup> over =  $97 - 31 = 66$

Runs scored in 10<sup>th</sup> over =  $97 - 88 = 9$

Runs scored from 3<sup>rd</sup> to 6<sup>th</sup> over =  $49 - 8 = 41$

Runs scored from 4<sup>th</sup> to 9<sup>th</sup> over =  $88 - 14 = \underline{74}$

### Prefix sum

$$P[i] = A[0] + A[1] + A[2] + \dots + A[i]$$

$$P[0] = A[0]$$

$$P[i] = P[i-1] + A[i]$$

$$\begin{array}{cccccc} & 0 & 1 & 2 & 3 & 4 & 5 \\ A = & [10 & 32 & 6 & 12 & 20 & 1] \\ P = & [10 & 42 & 48 & 60 & 80 & 81] \end{array}$$

$$P[0] = A[0]$$

```
for i → 1 to (N-1) {  
    |   P[i] = P[i-1] + A[i]  
}
```

$$TC = \underline{O(N)}$$

### Queries

$$\begin{array}{cccccc} & 0 & 1 & 2 & 3 & 4 & 5 \\ A = & [10 & 32 & 6 & 12 & 20 & 1] \\ P = & [10 & 42 & 48 & 60 & 80 & 81] \end{array}$$

$$1 \quad 5 \quad \rightarrow \quad 81 - 10 = 71$$

$$L \quad R \quad \rightarrow \quad P[R] - P[L-1]$$

$$0 \quad 2 \quad \rightarrow \quad P[2] = 48$$

```
for i → 0 to (Q-1) {
```

$$L = B[i][0] \quad R = B[i][1]$$

```
    |   if (L > 0) print (P[R] - P[L-1])
```

```
    |   else print (P[R])
```

$$TC = \underline{O(Q)}$$

```
}
```

$$\text{Total } TC = \underline{O(N + Q)}$$

$$SC = \underline{O(N)} \rightarrow P[]$$

$O(1)$  (update  $A[i]$  to prefix sum)

$$\underline{A[0] = A[0]}$$

for  $i \rightarrow 1$  to  $(N-1)$  {  
 $A[i] = A[i-1] + A[i]$   
 }

$$A = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 \\ 10 & 32 & 6 & 12 & 20 & 1 \end{matrix}$$

$$42 \quad 48 \quad 60 \quad 80 \quad 81$$

$a \rightarrow$  Given an integer array, find the **count** of equilibrium index i.e an index 'i' s.t  
 sum of elements on **left** of  $i$  =  
 sum of elements on **right** of  $i$ .

$$A = \begin{matrix} 0 & 1 & 2 & 3 \\ -3 & 2 & 4 & -1 \end{matrix}$$

$$\text{Ans} = \underline{1}$$

$i$	Left	Right	
0	0	5	x
1	-3	3	x
2	-1	-1	✓
3	3	0	x

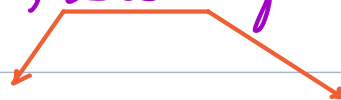
$$A = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ -7 & 1 & 5 & 2 & -4 & 3 & 0 \end{matrix}$$

$$\text{Ans} = \underline{2}$$

$i$	Left	Right	
3	-1	-1	✓
6	0	0	✓

Bruteforce  $\rightarrow \forall i$ , check if its eq. index.

$$TC = \underline{O(N^2)}$$



$$\frac{\text{Sum}(0 \text{ --- } (i-1))}{P[i-1]}$$

$$\frac{\text{Sum}((i+1) \text{ --- } (N-1))}{P[N-1] - P[i]}$$

Prefix Sum  $\rightarrow$

$$T.C = O(N + N) = \underline{O(N)}$$

$$S.C = \underline{O(N)} / O(1)$$


---

Q → How many subarray of length  $K$  are present in array.

$A = [1 \ 2 \ 3 \ 4 \ 5]$

$K = 2$        $Ans = 4$

$K = 5$        $Ans = 1$

$N = 7$

$K = 4$

0 1 2 3 4 5 6

First subarray →  $start = 0$        $[L \ R] \rightarrow \underline{R - L + 1}$   
 $end = K - 1$

Last subarray →  $start = N - K$        $[x \ (N-1)] \rightarrow (N-1) - x + 1 = K$   
 $end = N - 1$        $\Rightarrow \underline{N - K = x}$

# subarrays →  $[0 \ N - K] \rightarrow N - K - 0 + 1 = \underline{N - K + 1}$   
 of len  $K$        $[K - 1 \ N - 1] \rightarrow N - 1 - (K - 1) + 1 = \underline{N - K + 1}$  ✓

---

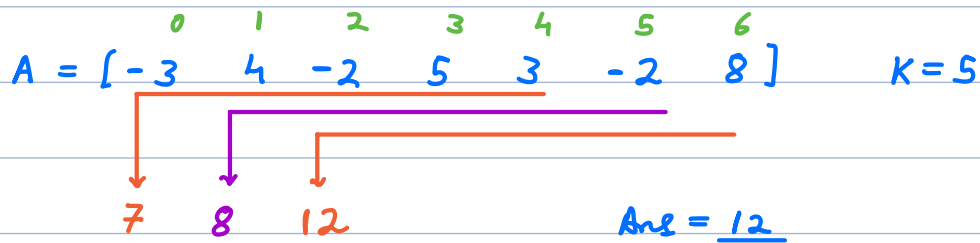
Q → Print start & end index of every subarray.

```
for s → 0 to (N-K) {
    |   e = s + K - 1
    |   print(s, e)
}
```

```
for e → (K-1) to (N-1) {
    |   s = e - K + 1
    |   print(s, e)
}
```

---

Q → Given an integer array, find max subarray sum of len K subarray.



Brute force →  $\forall$  subarray of len K, travel & calculate sum.

$$TC = O((N - K + 1) * K)$$

$$K=1 \rightarrow (N - 1 + 1) * 1 = N$$

$$K=N \rightarrow (N - N + 1) * N = N$$

$$K = \frac{N}{2} \rightarrow (N - \frac{N}{2} + 1) * \frac{N}{2} \approx \frac{N^2}{4} \rightarrow \underline{O(N^2)}$$

Sol →  $\forall$  subarray of len K, calculate sum.

ans = INT\_MIN

for  $e \rightarrow (K-1)$  to  $(N-1)$  {

$s = e - K + 1$

    // Prefix sum

    if ( $s > 0$ )    sum =  $P[e] - P[s-1]$

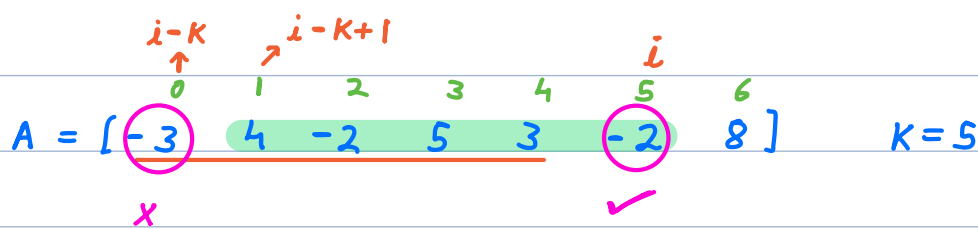
    else    sum =  $P[e]$

    ans = max(ans, sum)

}

$$TC = \underline{O(N)} \quad SC = \underline{O(N)}$$

Without updating A[] →  $O(1)$ ? ✓



### Sliding Window

$sum = 0$

```
for i → 0 to (K-1) { // K
    sum += A[i]
}
```

$ans = sum$

```
for i → K to (N-1) { // N-K
    sum += A[i] - A[i-K]
    ans = max(ans, sum)
}
```

$TC = \underline{O(N)}$

$SC = \underline{O(1)}$

Q → Given an integer array,  
find sum of all possible subarray sum.

$A = [2, 5, 3]$

2	→	2
2 5	→	7
2 5 3	→	10
5	→	5
5 3	→	8
3	→	<u>3</u>

35 (Ans)

$ans = 0$

```
for s → 0 to (N-1) {
    for e → s to (N-1) { // s — e
        sum = 0
```

```

    for i → s to e {
        sum += A[i]
    }
    ans += sum
}
return ans

```

→  $P[e] - P[s-1]$

Prefix Sum

TC =  $O(N^3)$  →  $(N^2)$   
 SC =  $O(1)$  →  $O(N)$

### Carry Forward

```

ans = 0
for s → 0 to (N-1) {
    sum = 0
    for e → s to (N-1) { // s — e
        sum += A[e]
        ans += sum
    }
}
return ans

```

$$A = \begin{bmatrix} 2 & 5 & 3 \end{bmatrix}$$
 $\begin{matrix} s & s & s \\ 0 & 1 & 2 \\ e \end{matrix}$

TC =  $O(N^2)$

SC =  $O(1)$

sum = 0 3

ans =  $0 + 2 + 7 + 10$

+  $5 + 8 + 3 = \underline{35}$

Contribution Technique → 1) One element is used multiple

times in answer calculation ✓

2)  $Ans = \sum_{i} (\text{contribution of } A[i])$



$$A = [2 \ 5 \ 3]$$

$$2 \rightarrow 2$$

$$2 \ 5 \rightarrow 7$$

$$2 \ 5 \ 3 \rightarrow 10$$

$$5 \rightarrow 5$$

$$5 \ 3 \rightarrow 8$$

$$3 \rightarrow \underline{3}$$

$$\underline{35 \text{ (Ans)}}$$

$$\text{Ans} = \sum_{i} (\text{contribution of } A[i])$$

$V_i$

$$A[i] * (\# \text{subarrays } A[i]$$

is a part of)

$$A = [ \overset{0}{3} \ \overset{1}{-2} \ \overset{2}{4} \ \overset{3}{-1} \ \overset{4}{2} \ \overset{5}{6} ]$$

$$\text{start} \rightarrow [0 \ 1] \rightarrow 2$$

$$\text{end} \rightarrow [1 \ 5] \rightarrow 5$$

$$2 * 5 = \underline{10}$$

$$A = [ \overset{0}{3} \ \overset{1}{-2} \ \overset{2}{4} \ \overset{3}{-1} \ \overset{4}{2} \ \overset{5}{6} ]$$

$$\text{start} \rightarrow [0 \ 2] \rightarrow 3$$

$$\text{end} \rightarrow [2 \ 5] \rightarrow 4$$

$$> 12$$

# subarrays where  $A[i]$  is present =

$$\text{start} \rightarrow [0 \ i] \rightarrow i+1$$

$$\text{end} \rightarrow [i \ (N-1)] \rightarrow N-1-i+1 = N-i$$

$$> (i+1) * (N-i)$$

$$\text{Ans} = \sum_{i} A[i] * (i+1) * (N-i)$$

$$TC = \underline{O(N)}$$

$$SC = \underline{O(1)}$$

for ( $i = N/2$  ;  $i \leq N$  ;  $i++$ )  $\rightarrow N/2$

for ( $j = 2$  ;  $j \leq N$  ;  $j = j * 2$ )  $\rightarrow \log(N)$



$2 \rightarrow 4 \rightarrow \dots \rightarrow 2^K = N$

$K = \log(N)$

$TC = O(N \log(N))$

---