

Trees - 1

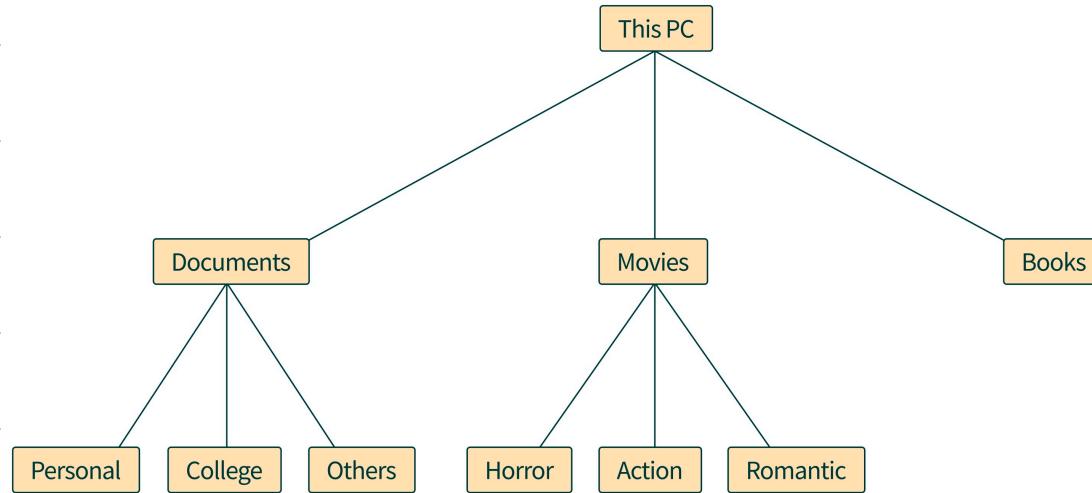
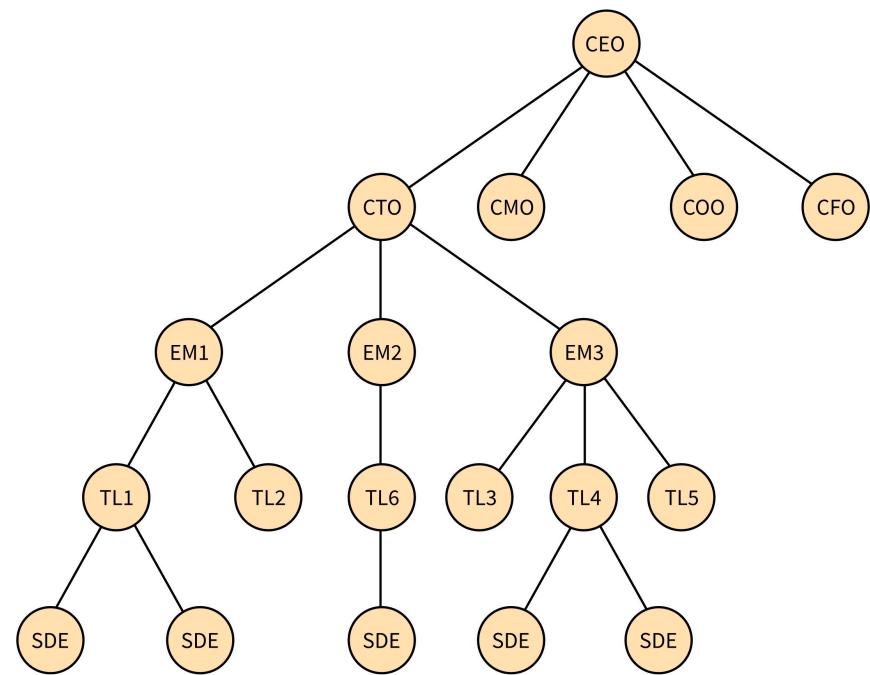
TABLE OF CONTENTS

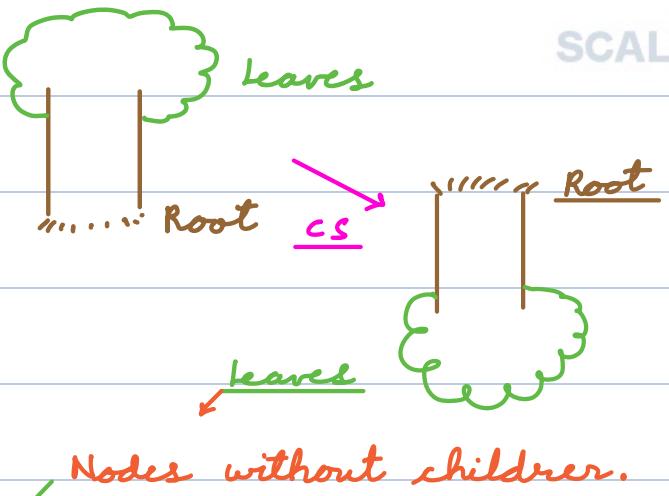
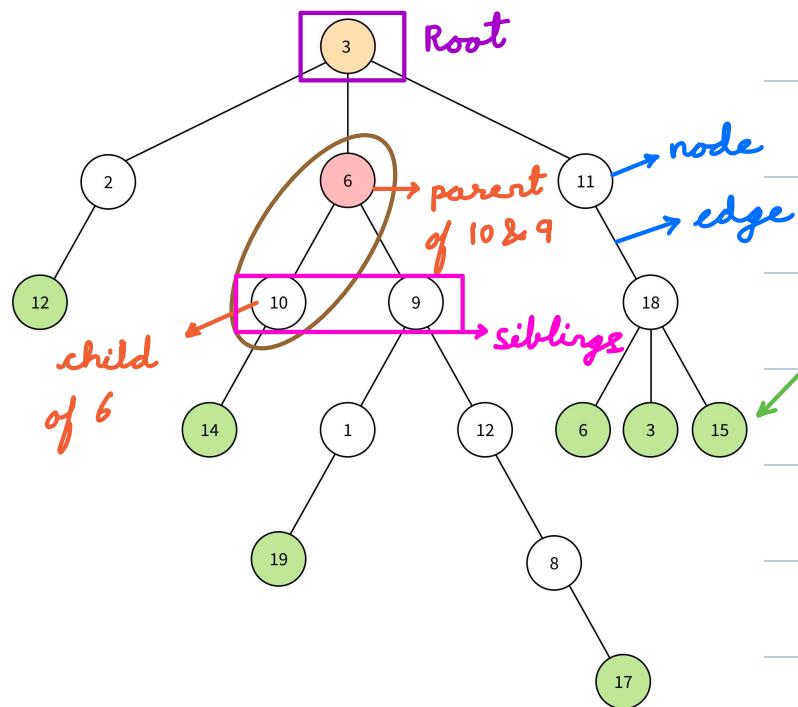
1. Introduction to Trees
2. Binary Tree
3. Traversal in Binary Tree
 - Pre-order
 - In-order
 - Post-order
4. Iterative In-order
5. Construct Tree from In-order and Post-order



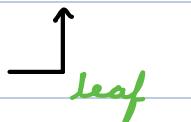
Trees

Hierarchical Data





Height of node \rightarrow count of edges (distance) to travel from current node to farthest leaf.



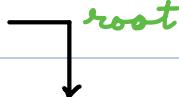
$$\text{height}(18) = 1$$

$$\text{height}(9) = 3$$

$$\text{height}(\text{leaf}) = 0$$

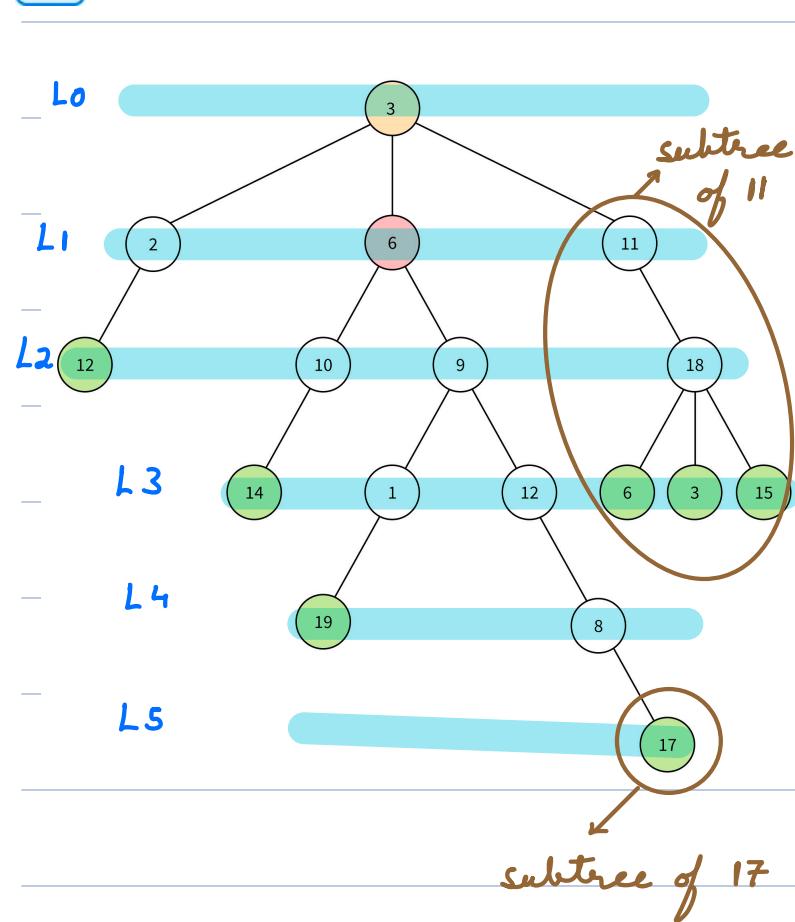
v.imp \rightarrow Height of tree = Height (root) = 5

Depth / Level of node \rightarrow count of edges (distance) to travel from root to reach the current node.



$$\text{depth}(9) = 2$$

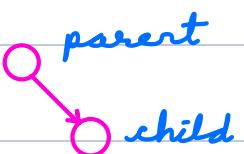
$$\text{depth}(14) = 3$$



Subtree of a node $x \rightarrow$

All the nodes we can

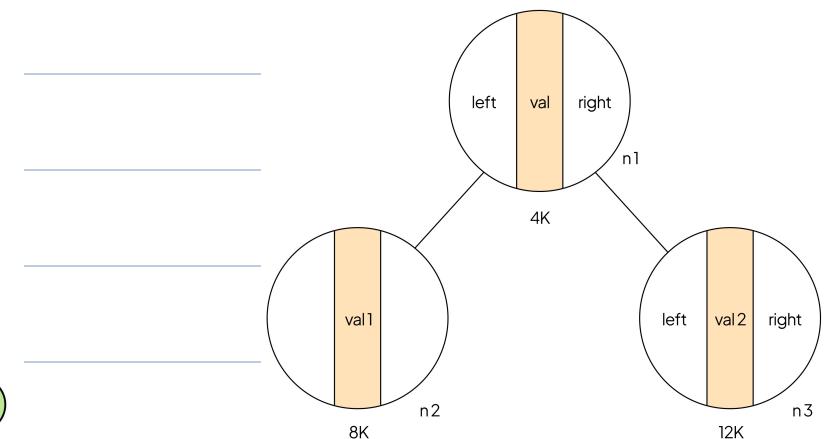
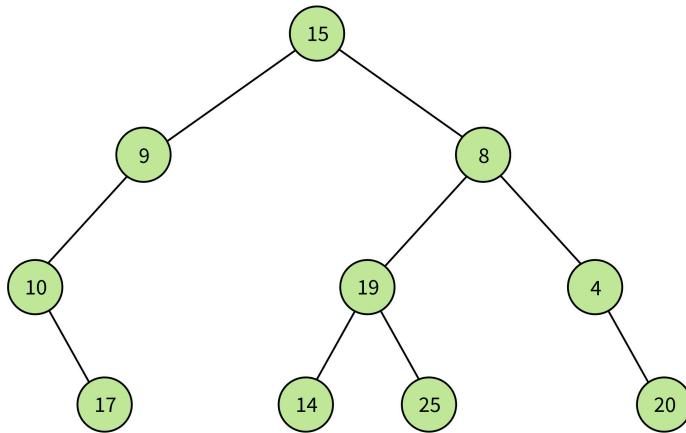
travel from node x are
part of subtree of x .



subtree (root) = complete tree

Binary Tree

✓ nodes, max # children = 2
 $\# \text{children} = \{0, 1, 2\}$



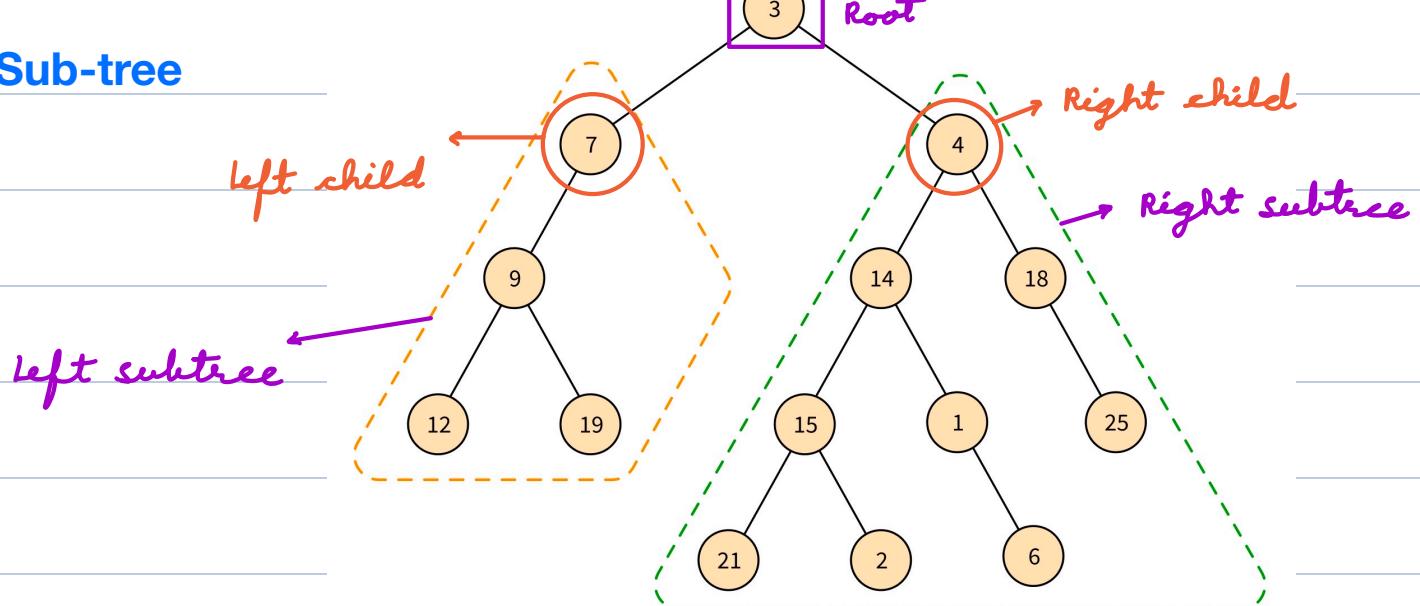
`class TreeNode {`

`int val;`

`TreeNode left, right;`

}

Sub-tree



Preorder

N L R

Levelorder → Next class

Inorder

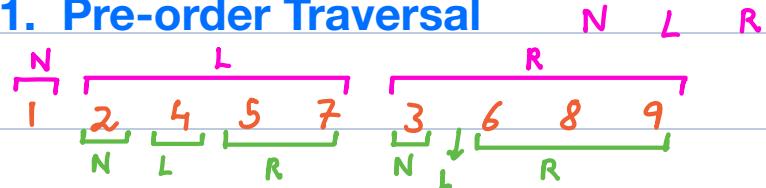
L N R

Postorder

L R N

Binary Tree Traversal

1. Pre-order Traversal



```
void preorder(root) {
```

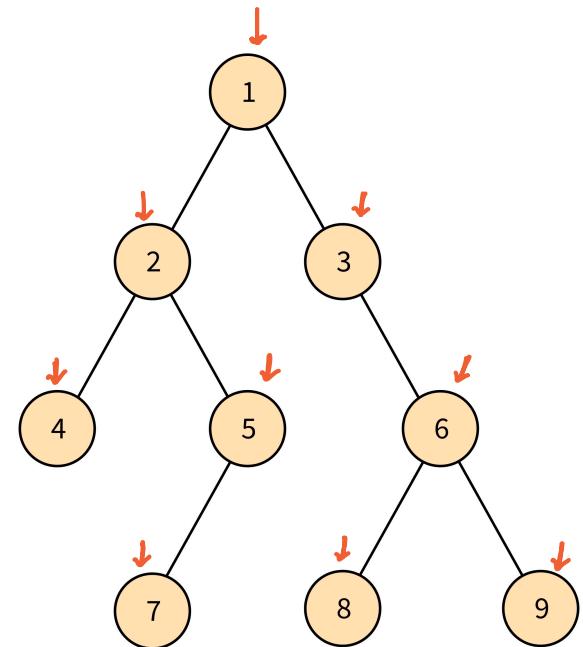
```
    if (root == null) return
```

```
    print (root.val) // Node
```

```
    preorder (root.left) // Left
```

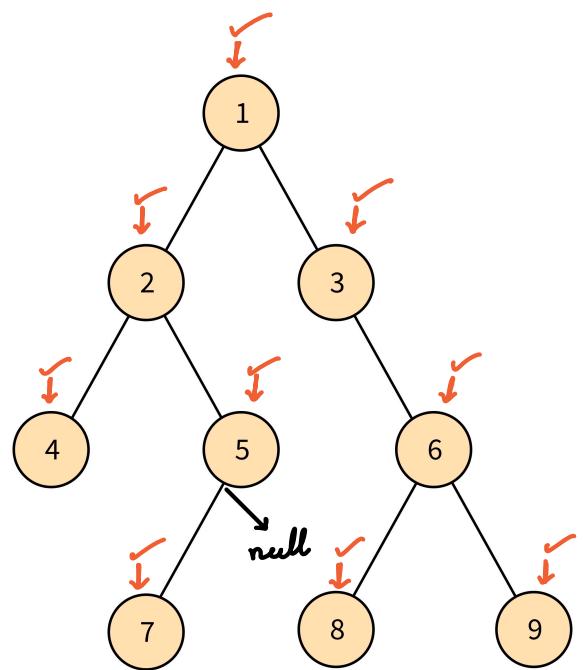
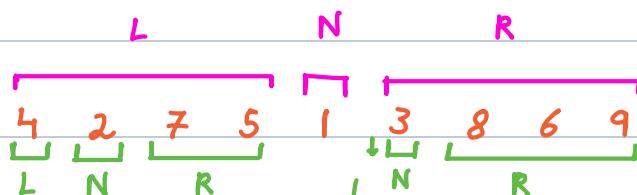
```
    preorder (root.right) // Right
```

$TC = O(N)$ $SC = O(H)$



2. In-order Traversal

L N R



```

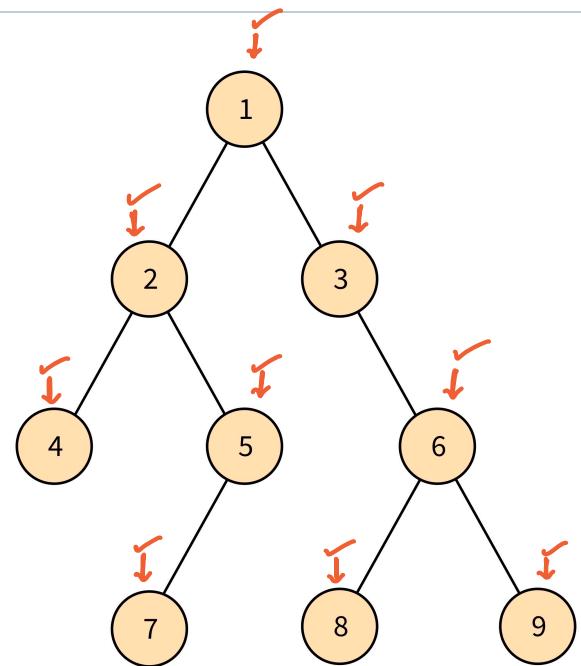
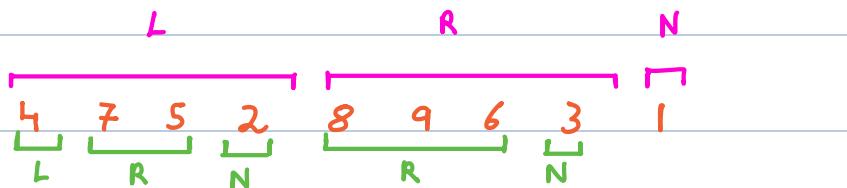
void inorder (root) {
    if (root == null) return
    inorder (root.left) // left
    print (root.val)      // Node
    inorder (root.right) // Right
}

```

$$TC = \underline{O(N)} \quad SC = \underline{O(H)}$$

2. Post-order Traversal

L R N



```

void postorder (root) {
    if (root == null) return
    postorder (root.left) // left
    postorder (root.right) // Right
    print (root.val)      // Node
}

```

$$TC = \underline{O(N)} \quad SC = \underline{O(H)}$$

Iterative In-order Traversal

L N R

DS to use → Stack

1) st.push(cur)

cur = cur.left

2) cur = st.pop()

print(cur.val)

cur = root

cur = cur.right

→ null

O/P → 4 2 7 5 1 3 10 8 6 9

→ null → 8 → null → null → 5 → null
 → 3 → null → 6 → 8 → 10 → null → 10 → null → 8
 → null → 6 → 9 → null → null

cur = root

while (cur != null || !st.isEmpty()) {

if (cur != null) { st.push(cur)

cur = cur.left }

else { cur = st.pop()

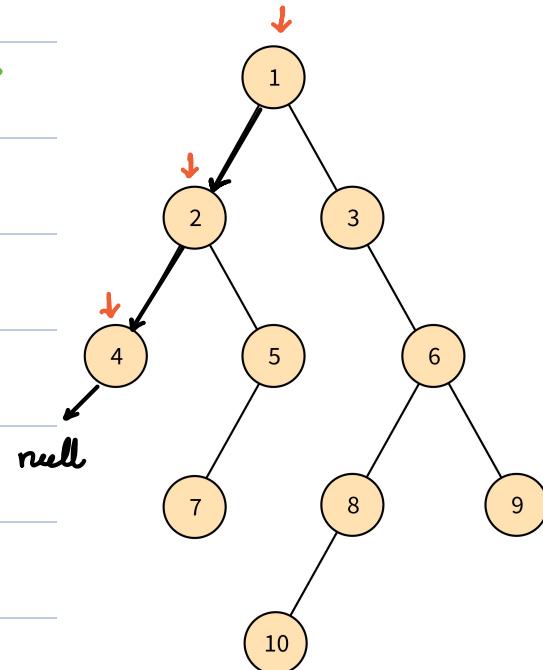
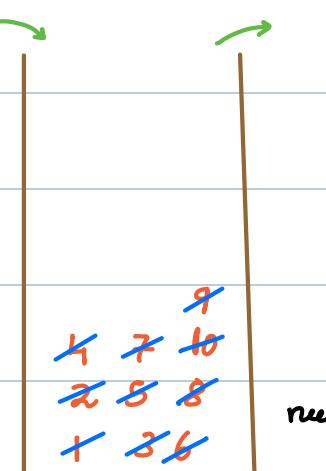
print(cur.val)

cur = cur.right }

}

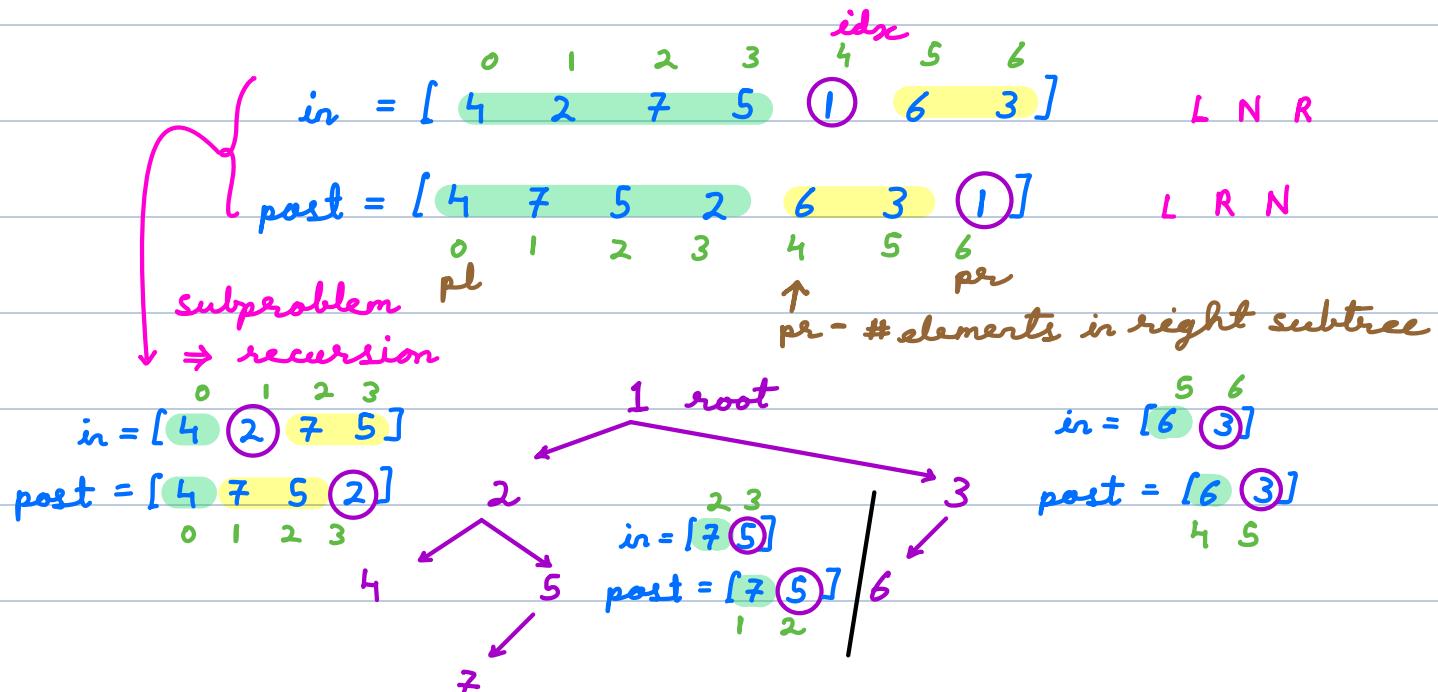
TC = O(N) SC = O(H)

H.W → Try iterative code for preorder & postorder. ✓



< Question > : Construct the binary tree from in-order and post-order.

Given two arrays in[], post[]. (unique elements)



TreeNode build (in[], il, ir, post[], pl, pr) {

if (ir < il) return null //empty array

root = new TreeNode (post[pr])

idx = index (in, root.val) // iterate
 $\langle A[i], i \rangle \rightarrow \text{hashmap} \checkmark$

// in \rightarrow left l = il r = idx - 1

// right l = idx + 1 r = ir

crt_r = ir - idx // R - L + 1 [L R]

// post \rightarrow left l = pl r = pr - crt_r - 1

right l = pr - crt_r r = pr - 1

root.left = build (in, il, idx - 1, post, pl, crt_r - 1)

root.right = build (in, idx + 1, ir, post, crt_r, pr - 1)



return root

}

$$TC = \underline{O(N)}$$

$$SC = \underline{O(N)}$$

