

Lecture :- Hashmap Implementation

Agenda

└ Hashmap implementation challenges

Qn Given arr[n] and Q queries. In each query, an element is given. Check whether that element exists in an array or not.

2	4	11	15	6	8	14	9
---	---	----	----	---	---	----	---

Queries	
k = 4	t
k = 10	f
k = 17	f
k = 14	t

Brute force approach

Tc: $O(n * Q)$

Sc: $O(1)$

Observation

A =

2	4	11	15	6	8	14	9
---	---	----	----	---	---	----	---

DAT = Direct access table

dat[] =

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
f	f	f	f	f	f	f	f	f	f	f	f	f	f	f	f

```
for(i=0; i<n; i++) {  
    dat[A[i]] = true;  
}
```

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
f	f	t	f	t	f	t	f	t	t	f	t	f	f	t	t

TC: $O(1) + O(n)$
SC: $O(\max)$

Advantages of DAT

1. T.C of insertion = $O(1)$
2. T.C of deletion = Point of discussion.
3. T.C of searching = $O(1)$

Issue with such representation

1. > Wastage of space.

23	60	37	91
----	----	----	----

→ DAT array size \Rightarrow 92

2. > Inability to create big arrays.

1	10^{10}	10^9	8
---	-----------	--------	---

 DAT[$10^{10}+1$]

3. > Storing values other than +ve integer.

1	2	-100	26
---	---	------	----

 DAT[27]

Overcoming issues while retaining advantage

Assumption: DAT array \longrightarrow Restrict size = 10

21	42	37	45	99	30
----	----	----	----	----	----

How to map all values with indices?

Hash

Mapping funcⁿ: $idx = A[i] \% 10$

array elements	mapped index $A[i] \% 10$
21	1
42	2
37	7
45	5
99	9
30	0

$dat[] \Rightarrow$

0	1	2	3	4	5	6	7	8	9
↑	↑				↑		↑		↑
30	21				45		37		99

Issues with hashing

A \Rightarrow

21	42	37	45	77	99	31
----	----	----	----	----	----	----

Mapped idx of 21 and 31 = 1

" " " 37 and 77 = 7

$21 \longrightarrow \text{idx} = 21 \% 10 = 1$
 $31 \longrightarrow \text{idx} = 31 \% 10 = 1$ } collision

Can we completely avoid collision? No

Reason: Pigeon hole principle

Pigeon = 11

Hole = 8

At least 1 hole ≥ 2 pigeons.

Collision resolution technique

Open hashing

✓ chaining
(interviews)

closed hashing

Linear
probing

quadratic

Double
hashing

↓
Do it yourself.

chaining

$\{ \text{Hash Mapped func} = A[i] \% 10 \}$

$A \Rightarrow$

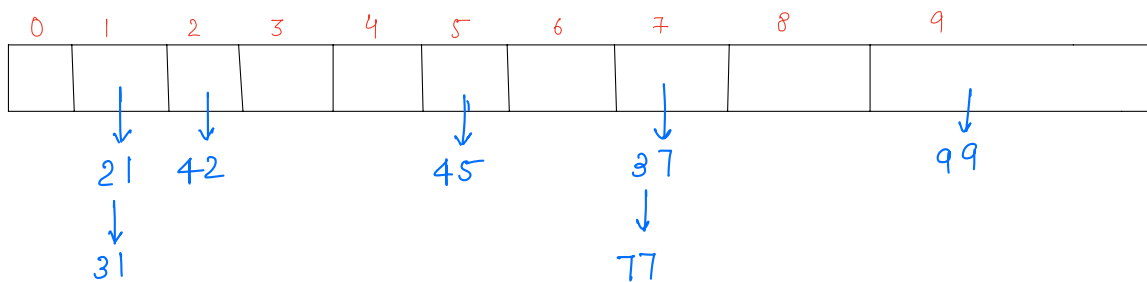
21	42	37	45	77	99	31
----	----	----	----	----	----	----

Mapped idx of 21 and 31 = 1

" " " 37 and 77 = 7

How can we resolve collision here?

Somehow store 21 & 31
37 & 77 at same idx.



chaining is a technique used in data structures, particularly hash tables, to resolve collisions. When multiple items hash to same index, chaining stores them in a linked list or another data structures at that index.

Time complexity of insertion

el \longrightarrow hash func \longrightarrow idx \longrightarrow Go to that idx

insert at tail \Rightarrow $\frac{11}{O(n)}$

ArrayList
 $O(1)$

insert at head \Rightarrow $O(1)$

$O(n)$

Time complexity of deletion and searching

Average

Worst

Lambda (λ)

$\lambda \Rightarrow \frac{\text{total el inserted}}{\text{size of array.}}$

Random example:

DAT array

Hash table

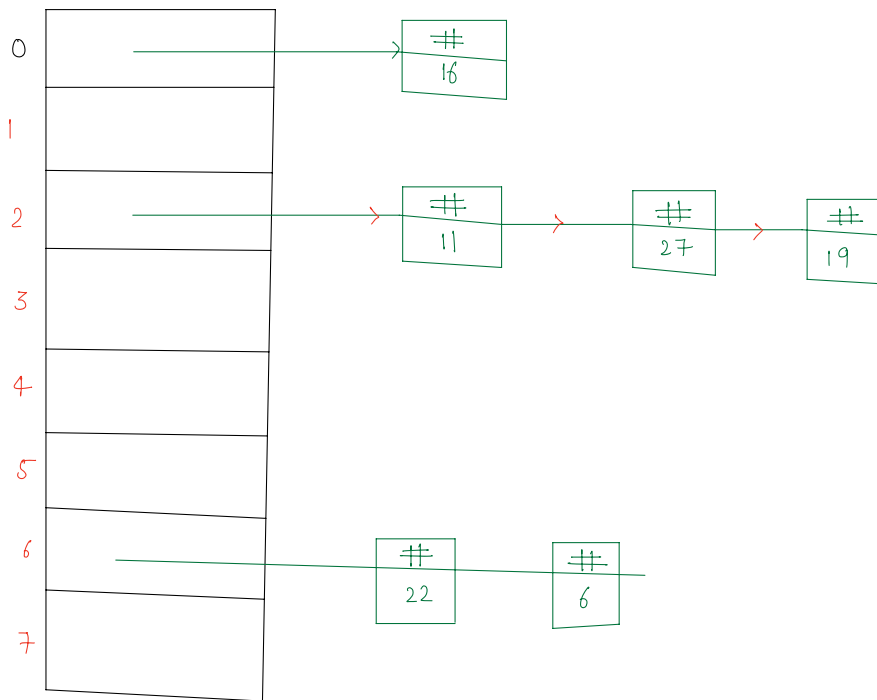


Table size $\Rightarrow 8$

Inserted elements $\Rightarrow 6$

$\lambda \Rightarrow \frac{6}{8} = 0.75 \text{ \{load factor\}}$

Predefined threshold $\Rightarrow 0.7$

Rehashing

Hash table

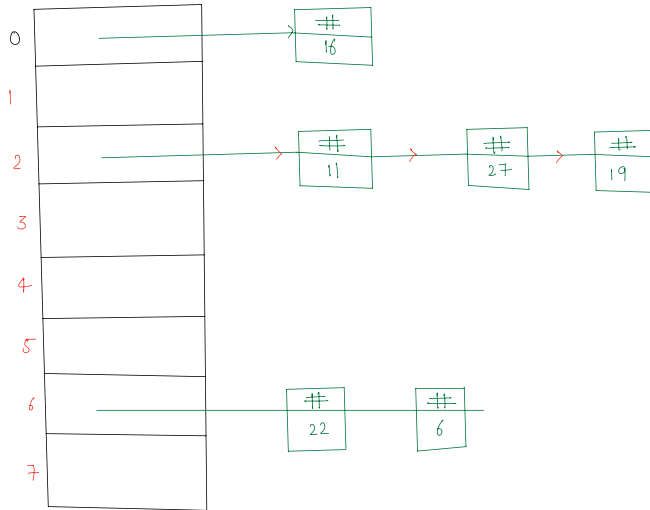


Table size $\Rightarrow 8$

Inserted elements $\Rightarrow 6$

$$\lambda \Rightarrow \frac{6}{8} = 0.75 \text{ [load factor]}$$

Insert a new value: probability $\rightarrow x$

Steps

Double size of DAT array.

Rehashing all again

Table size $\Rightarrow 16$

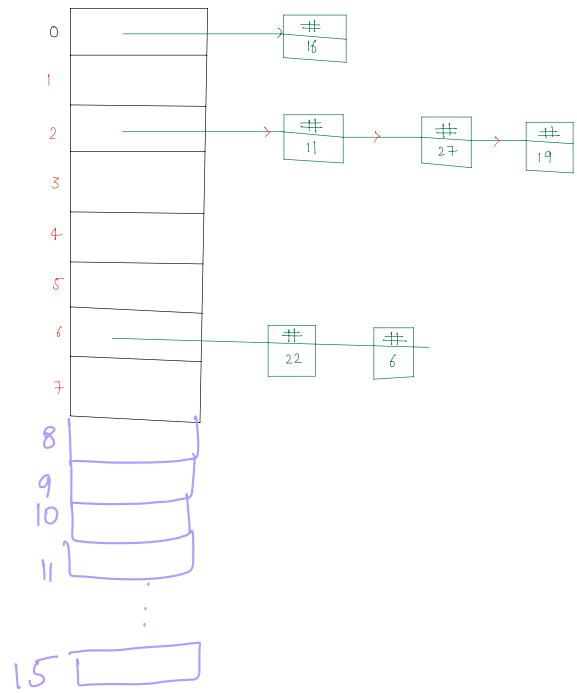
Inserted elements $\Rightarrow 6$

$$\lambda \Rightarrow \frac{6}{16} = 0.375$$

Insert a new value: probability $= y$

$$\underline{\underline{y \lll x}}$$

Hash table



Break: 8:03 - 8:15

Code implementation

Structure

```
class AyuehHashMap<K, V> {
```

```
    class HMNode {
```

```
        K key;
```

```
        V value;
```

```
        Constructor
```

```
    };
```

```
    ArrayList<HMNode>[] buckets
```

```
    int size;
```

```
int getIndexWithinBucket (K key, int bi) {
```

```
    di = 0;
```

```
    for (HMNode node: buckets[bi]) {
```

```
        if (node.key == key) {
```

```
            return di; // key found
```

```
        }
```

```
        di++;
```

```
    }
```

```
    return -1; // key not found
```

```
}
```

Put method

```
public void put (K key, V value) {
```

$b_i = \text{hash}(\text{key});$

✓ $id_i = \text{getIndexWithinBucket}(\text{key}, bi)$ — ~~$O(n)$~~

if $\langle di \rangle = -12$ {

key found, update the value.

```

    buckets[bi].get(di).value = value;
} else {

```

```
HMnode node = new HMnode( key, value);
```

```
buckets[bi].add(node);
```

```
size++;
```

Check for rehashing

$$\text{lamda} = \frac{\text{size} * 1.0}{\text{buckets length}}$$

if ($\lambda > 0.7$) {

rehash(); ~~o(n)~~

 \sim

3

Hash Method

```
int hash(K key) {  
    hc = key.hashCode(); // anything  
    bi = Math.abs(hc) % buckets.length;  
    return bi;  
}
```

Rehash method

void rehash() {

ArrayList<HMNode>[] oldBuckets = buckets;

buckets = new ArrayList<HMNode>[oldBuckets.length
*
2];

for (ArrayList<HMNode> bucket: oldBuckets) {

for (HMNode node: bucket) {

put (node.key, node.value);

}

}

}

Get method

```
V get (K key) {  
    bi = hash(key);  
    di = getIndexWithinBucket (key, bi);  
    if (di == -1) {  
        Key not found.  
        return null;  
    }  
    return buckets[bi].get (di).value;  
}
```


Contains Key method

```
boolean containsKey(K key) {  
    bi = hash(key);  
    di = getIndexWithinBucket(key, bi);  
    if (di == -1) {  
        return false;  
    }  
    return true;  
}
```

Remove method

```
V remove(K key) {  
    bi = hash(key);  
    di = getIndexWithinBucket(key, bi);  
    if (di == -1) {  
        return null;  
    }  
    size--;  
    return buckets[bi].remove(di).value;  
}
```

Size method

```
public int size() {  
    return size;  
}
```

TC
Avg time complexity
 └ O(1)

LIS

$A[]$ — length of longest sub sequence
such that el in subsequence
are consecutive integers.

1 9 3 10 4 20 2 [1 3 4 2]

Ans = 4

36 41 56 35 44 33 34 42 43 32 42

Ans = 5

Approach set / map

→ Insert all el in set

36 41 56 35 44 33 34 42 43 32 42

↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↓

① ④ ① ① ① ① ① ① ⑤

```
if (A[i] - 1 present in set) {  
    sequence cont start  
    from here  
} else {  
  
}
```