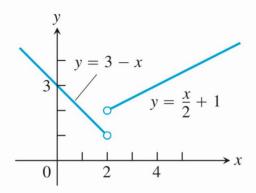


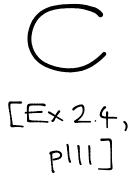
3. Let
$$f(x) = \begin{cases} 3 - x, & x < 2 \\ \frac{x}{2} + 1, & x > 2. \end{cases}$$



- **a.** Find $\lim_{x\to 2^+} f(x)$ and $\lim_{x\to 2^-} f(x)$.
- **b.** Does $\lim_{x\to 2} f(x)$ exist? If so, what is it? If not, why not?
- **c.** Find $\lim_{x\to 4^-} f(x)$ and $\lim_{x\to 4^+} f(x)$.
- **d.** Does $\lim_{x\to 4} f(x)$ exist? If so, what is it? If not, why not?

$$f(x) = \begin{cases} x^2 - 1, & -1 \le x < 0 \\ 2x, & 0 < x < 1 \\ 1, & x = 1 \\ -2x + 4, & 1 < x < 2 \\ 0, & 2 < x < 3 \end{cases}$$

- **5. a.** Does f(-1) exist?
 - **b.** Does $\lim_{x\to -1^+} f(x)$ exist?
 - **c.** Does $\lim_{x\to -1^+} f(x) = f(-1)$?
 - **d.** Is f continuous at x = -1?
- **6. a.** Does f(1) exist?
 - **b.** Does $\lim_{x\to 1} f(x)$ exist?
 - **c.** Does $\lim_{x\to 1} f(x) = f(1)$?
 - **d.** Is f continuous at x = 1?
- 7. a. Is f defined at x = 2? (Look at the definition of f.)
 - **b.** Is f continuous at x = 2?
- **8.** At what values of x is f continuous?



37.
$$f(x) = \frac{2}{x} - 3$$

39.
$$g(x) = \frac{1}{2 + (1/x)}$$

$$43. h(x) = \frac{\sin 2x}{x}$$



35. Define g(3) in a way that extends $g(x) = (x^2 - 9)/(x - 3)$ to be continuous at x = 3.

37. Define f(1) in a way that extends $f(s) = (s^3 - 1)/(s^2 - 1)$ to be continuous at s = 1.



In Exercises 11–18, find the slope of the function's graph at the given point. Then find an equation for the line tangent to the graph there.

11.
$$f(x) = x^2 + 1$$
, (2, 5)

11.
$$f(x) = x^2 + 1$$
, (2,5) **12.** $f(x) = x - 2x^2$, (1,-1)

In Exercises 13–16, find y' (a) by applying the Product Rule and (b) by multiplying the factors to produce a sum of simpler terms to differentiate.

13.
$$y = (3 - x^2)(x^3 - x + 1)$$
 14. $y = (x - 1)(x^2 + x + 1)$