

CSCI-UA.0480-004

Algorithmic Problem Solving

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Lecture 3: Data Structures

Analyzing runtime

- Nested for loops runtime
 - How many `myOperation()` calls?

```
public static void main(String args[]) {  
    for (int i = 0; i < 300; i++) {  
        for (int j = 0; j < 600; j++) {  
            for (int k = 0; k < 200; k++) {  
                myOperation(i, j, k);  
            }  
        }  
    }  
}
```

Testing exercise

- You receive a time limit exceeded response for an your $O(N^3)$ solution. ($1 \leq N \leq 100$)
 - Abandon the problem
 - Improve the performance of your solution
 - Create tricky test cases and find the bug

Testing exercise

- You receive a time limit exceeded response for an your $O(N^3)$ solution. ($1 \leq N \leq \mathbf{1,000,000}$)
 - Abandon the problem
 - Improve the performance of your solution
 - Create tricky test cases and find the bug

Testing exercise

- You receive a runtime error response. Your code runs OK in your machine. What should you do?
 - Abandon the problem
 - Improve the performance of your solution
 - Create tricky test cases and find the bug



Handout exercises

- 5 minutes to read through exercises 1-3

Exercise 1

• Integer radix

```
public static void main(String[] args) throws Exception {  
    BufferedReader in = new BufferedReader(new InputStreamReader(System.in));  
    String line;  
  
    while ((line = in.readLine()) != null) {  
        StringTokenizer st = new StringTokenizer(line);  
  
        // Parse  
        int x = Integer.parseInt(st.nextToken());  
        int y = Integer.parseInt(st.nextToken());  
        String baseXIntStr = st.nextToken();  
  
        // Format  
        int theInt = Integer.parseInt(baseXIntStr, x);  
        String baseYIntStr = Integer.toString(theInt, y);  
        System.out.println(baseYIntStr);  
    }  
}
```

Exercise 2

- Pad with zeros

```
public static void main(String[] args) throws Exception {  
    BufferedReader in = new BufferedReader(new InputStreamReader(System.in));  
    String line;  
  
    while ((line = in.readLine()) != null) {  
        // Parse  
        int x = Integer.parseInt(line);  
  
        // Format  
        System.out.printf("%09d\n", x);  
  
        /* Also valid: */  
        // String outputString = String.format("%09d", x);  
        // System.out.println(outputString);  
    }  
}
```


Exercise 3

- Printing decimals (reference)

```
public static void main(String[] args) throws Exception {  
    BufferedReader in = new BufferedReader(new InputStreamReader(System.in));  
    String line;  
  
    while ((line = in.readLine()) != null) {  
        // Parse  
        double x = Double.parseDouble(line);  
  
        // Format  
        System.out.printf("%.3f\n", x);  
  
        /* Also valid: */  
        // String outputString = String.format("%.3f", x);  
        // System.out.println(outputString);  
    }  
}
```

Exercise 4

- Set intersection

```
public static void main(String[] args) throws Exception {  
    BufferedReader in = new BufferedReader(new InputStreamReader(System.in));  
    String line;  
  
    LinkedHashSet<Integer> A = new LinkedHashSet<Integer>();  
    LinkedHashSet<Integer> B = new LinkedHashSet<Integer>();  
  
    while ((line = in.readLine()) != null) {  
        StringTokenizer st = new StringTokenizer(line);  
  
        while (st.hasMoreTokens())  
            A.add(Integer.parseInt(st.nextToken()));  
  
        st = new StringTokenizer(in.readLine());  
  
        while (st.hasMoreTokens())  
            B.add(Integer.parseInt(st.nextToken()));  
  
        A.retainAll(B); // Set intersection  
        System.out.println(A.size());  
    }  
}
```



Exercise 5

- Greatest Euclidean distance, small
 - Brute force is fine!

Exercise 6

- Greatest Euclidean distance, large
 - Brute force is much too slow
 - Turns out convex hull works



Data Structures Lecture

Linear data structures

1) Static arrays

- `int myArray[] = new int[10];`
- Accessing and setting: $O(1)$ operations
- Don't forget to clear between test cases
 - `Arrays.fill(myArray, 0);`

Linear data structures

2) ArrayLists (convenient resizable arrays)

- `ArrayList myList = new ArrayList();`
- Constructor has one parameter, an integer
 - e.g., `new ArrayList(1000)` instantiates a new ArrayList with initial capacity of 1000 items
 - Default (no param): initial capacity is 10 items
- Unbounded growth (within memory limit of program)

Linear data structures

2) ArrayLists

- Appending to list: amortized $O(1)$ operation
 - When a resize occurs, all elements are copied to a new array, which is $O(n)$ operations
- Inserting to list: $O(n)$ operations
 - Elements are shifted over to accommodate
- If you reuse one between test cases, run `list.clear()` between runs!!
- Reference

Linear data structures

- Example pitfall:
 - Problem description:

Write a program that finds if an integer is in a list of integers.
 - Sample input:

1 2 4 7 5 9
5
 - Sample output:

yes

Linear data structures

```
BufferedReader in = new BufferedReader(new InputStreamReader(System.in));  
String line;
```

```
// Let's just use one ArrayList for this problem  
ArrayList<Integer> myList = new ArrayList<Integer>();
```

```
while ((line = in.readLine()) != null) {  
    StringTokenizer st = new StringTokenizer(line);  
  
    while (st.hasMoreTokens()) {  
        myList.add(Integer.parseInt(st.nextToken()));  
    }  
  
    line = in.readLine();  
  
    int x = Integer.parseInt(line);  
  
    if (myList.contains(x)) {  
        System.out.println("yes");  
    } else {  
        System.out.println("no");  
    }  
  
    myList.clear(); // Don't forget to clear!  
}
```

Linear data structures

- Common operations on arrays and ArrayLists
 - Sorting
 - `Arrays.sort(myArray)` – quicksort, $O(n \log n)$
 - `Collections.sort(myList)` – merge sort, $O(n \log n)$
 - Searching
 - Unsorted list: exhaustive search, $O(n)$
 - Sorted list: binary search, $O(\log n)$
 - `Arrays.binarySearch()` and `Collections.binarySearch()` – more later

Linear data structures

3) Bitmask

- Treat a primitive int or long as a set of booleans
- Further discussion next class

Linear data structures

4) LinkedList

- $O(n)$ time to access an indexed element
- $O(n)$ to search for an element
- $O(n)$ to insert (or $O(1)$ with a `ListIterator`)
- Just use an `ArrayList`

Linear data structures

5) Stack

- LIFO operations: Push, pop
- Useful when a stack could be useful

6) Queue

- FIFO operations: Push, pop
- In Java, implemented as an interface
 - Has a LinkedList data structure backend, not good to search through / insert
 - `Queue<X> myQueue = new LinkedList<X>();`
 - Will be used later in this class

Non-linear data structures

1) Binary search tree

- Java's TreeSet and TreeMap implement a Red-Black tree
 - Self-balancing binary tree
- Cost:
 - Insertion: `myTree.put(x)` - $O(\log n)$
 - Membership: `myTree.containsKey(x)` - $O(\log n)$
 - Remove: `myTree.remove(x)` - $O(\log n)$
 - Fetch (TreeMap): `myTree.get(x)` - $O(\log n)$
- Reference

Non-linear data structures

2) Hash table

- Java implements a standard hash table
 - Buckets (an array) of key-value objects called “Entries”
 - Keys with the same hash codes are stored in the same bucket using a linked list
 - Not LinkedList
 - Collision time/space trade-off regulated by the *load factor* (default 0.75)
 - How full the table can become before growing
 - Also can be given an initial capacity (default 16)

Non-linear data structures

2) Hash table

- Cost:
 - Insertion, fetch, removal, membership: expected $O(1)$
 - Depends on a good hash function
 - If you make a custom class, ensure you override the `hashCode()` so collisions are minimized
 - Eclipse is your friend: Source → Generate `hashCode()` and `equals()`
- HashMap and HashSet
- Reference

Non-linear data structures

3) Linked hash table

- Convenience class for efficiently traversing hash table keys
 - `for (Entry<K, V> e : myHashTable.getEntries())`
- Java: LinkedHashMap, LinkedHashSet
- Iteration order:
 - Order in which elements were added
- Cost of iterating:
 - Linear in size

Non-linear data structures

4)Heap

- Tree structure
- Each element:
 - Is larger than its parent
 - Is smaller than its children
- Java: PriorityQueue, a binary heap
- Operations:
 - Add: Put the element in the tree – $O(\log n)$
 - Poll: Remove and return top element from the heap tree, i.e., the smallest element – $O(\log n)$

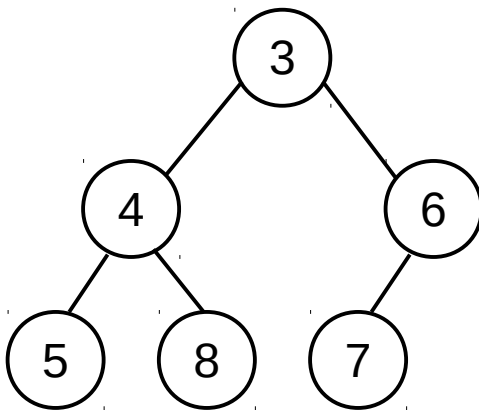
Testing exercise

- You receive a wrong answer response for a very easy problem. What should you do?
 - Abandon the problem
 - Improve the performance of your solution
 - Create tricky test cases and find the bug

Non-linear data structures

4) Heap

- Stored in contiguous memory for fast lookup



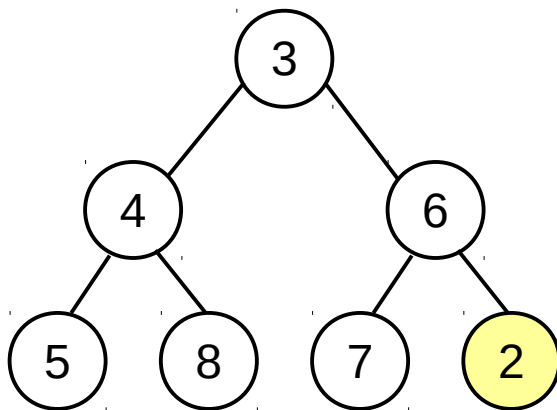
idx	0	1	2	3	4	5	6	7
val	3	4	6	5	8	7		

Parent: $(\text{idx} - 1) \ggg 1$

Non-linear data structures

4) Heap

- Add 2 – sift up



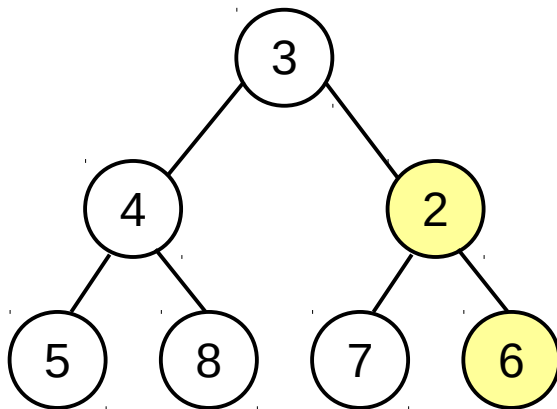
idx	0	1	2	3	4	5	6	7
val	3	4	6	5	8	7	2	

Parent: $(\text{idx} - 1) \ggg 1$

Non-linear data structures

4)Heap

- Add 2 – swap 2 and 6



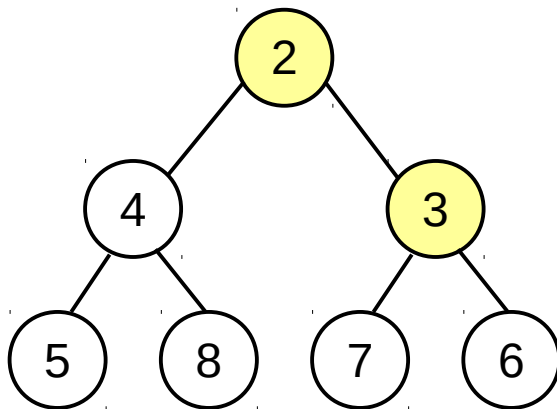
idx	0	1	2	3	4	5	6	7
val	3	4	2	5	8	7	6	

Parent: $(\text{idx} - 1) \ggg 1$

Non-linear data structures

4)Heap

- Add 2 – swap 2 and 3



idx	0	1	2	3	4	5	6	7
val	2	4	3	5	8	7	6	

Parent: $(\text{idx} - 1) \ggg 1$

Graphs

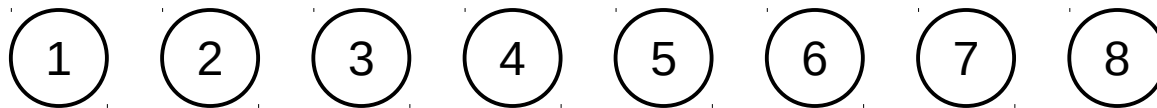
- A set of nodes connected by edges
 - Directed, undirected
 - Cyclic, acyclic
- Represented by:
 - 1)Adjacency Matrix
 - 2)Adjacency List
 - 3)Edge List
- Much more later

Union-find disjoint sets

- Motivation:
 - You want a data structure to quickly union two or more disjoint sets
 - You want to quickly find what set an element belongs to
- How to do this efficiently
 - Make a forest of trees for each element
 - The root of the tree is the set identifier

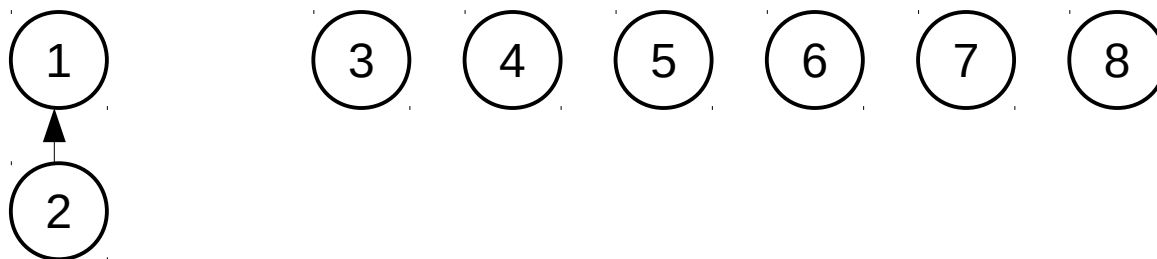
Union-find disjoint sets

- Starting with 8 disjoint sets / trees:



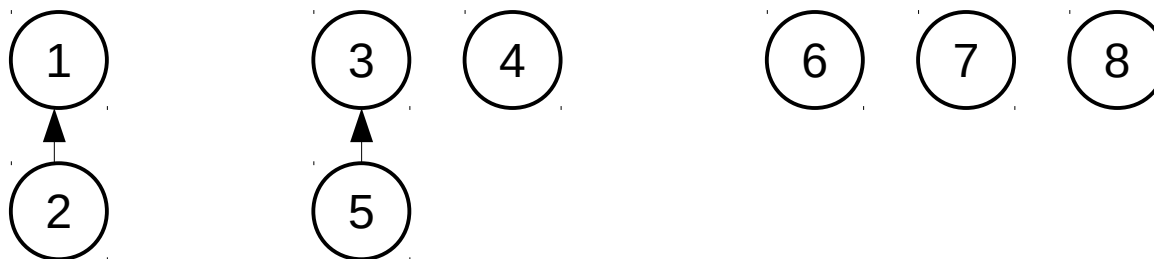
Union-find disjoint sets

- Union the sets containing 1 and 2



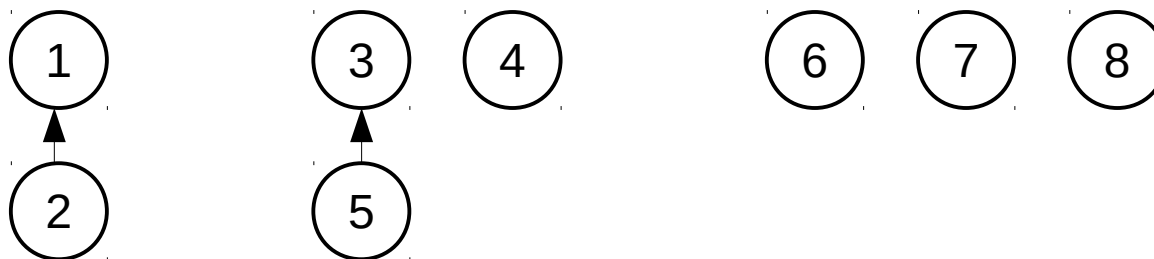
Union-find disjoint sets

- Union the sets containing 3 and 5



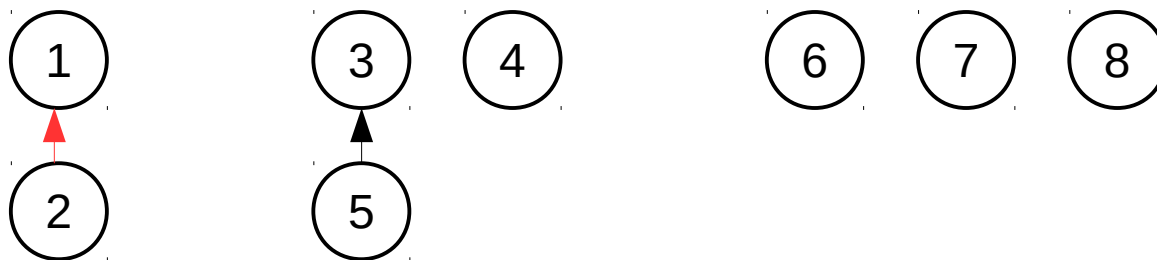
Union-find disjoint sets

- Are 2 and 6 in the same set?



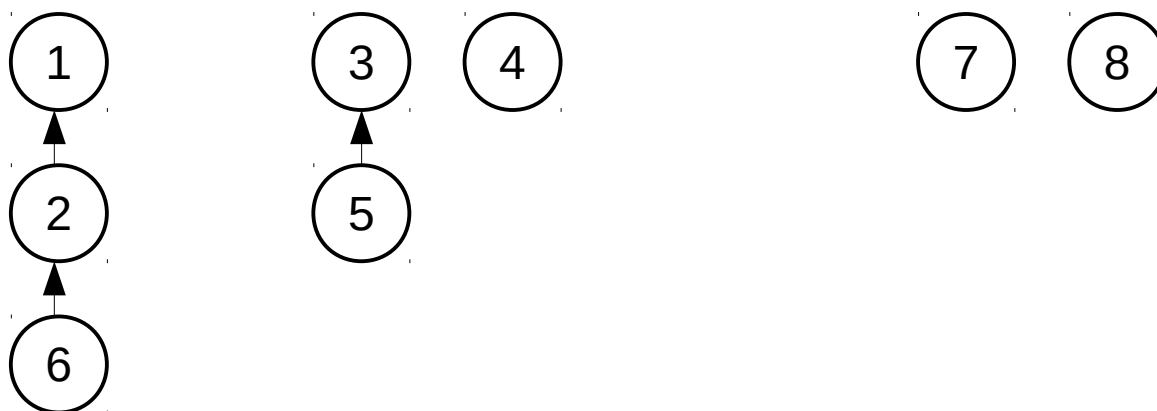
Union-find disjoint sets

- Are 2 and 6 in the same set? No.



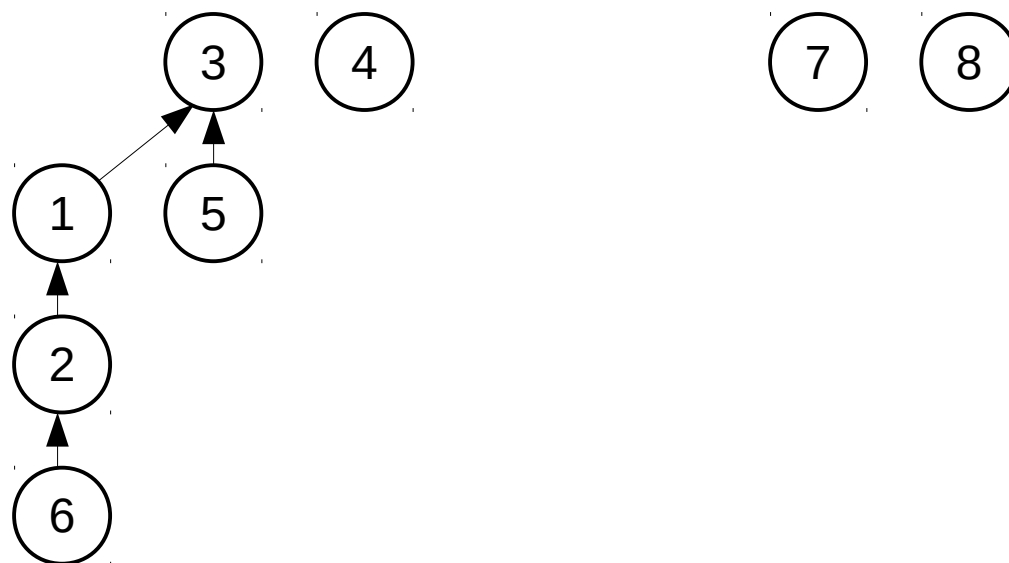
Union-find disjoint sets

- Union the sets containing 2 and 6



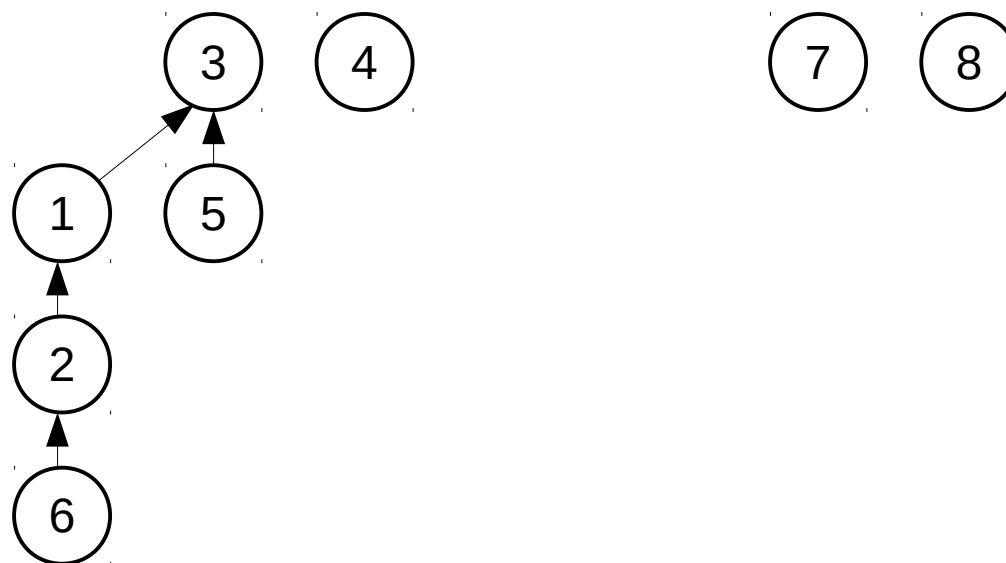
Union-find disjoint sets

- Union the sets containing 5 and 6



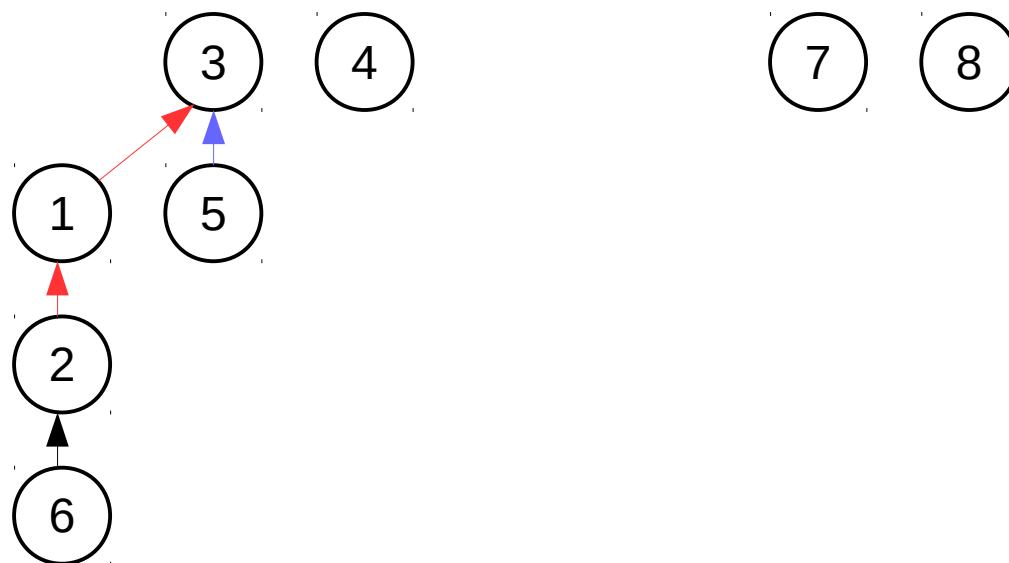
Union-find disjoint sets

- Are 2 and 5 in the same set?



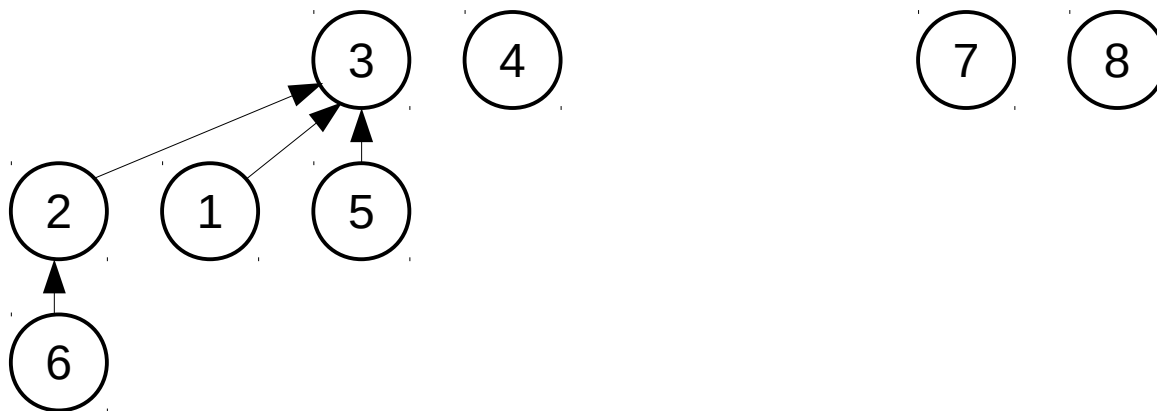
Union-find disjoint sets

- Are 2 and 5 in the same set? Yes.



Union-find disjoint sets

- Path compression after the find



Union-find disjoint sets

- Runtime:
 - Consider N union-find operations to take about $O(N)$ time

Union-find disjoint sets

- Union pseudo-code

```
function Union(x, y)
  xRoot := Find(x)
  yRoot := Find(y)
  xRoot.parent := yRoot
```

- Find pseudo-code

```
function Find(x)
  if x.parent != x
    x.parent := Find(x.parent)
  return x.parent
```

Data structure problems

- Read exercises 7-9

Data structure problems

- If we have time...
 - Hardwood Species
 - Minesweeper
 - List of Conquests



Readings

- Book reference:
 - Programming Challenges 2.1 to 2.4.2