

Homework 4 Hints

1. Ingenious Cubrency:

```
//Counts the ways of making amount using
//Cubes  $x^3$  with x in the range [1,last]
static long count(int amount, int last);
static long count(int amount) { return count(amount,21); }
```

2. Diving For Gold:

```
//ds: The depths of each treasure
//vs: The values of each treasure
//w: The constant from the problem (trip i costs 3*w*ds[i] air)
//Computes the maximum value you can achieve with treasures
//in the interval [pos,length(ds)-1] and t air left.
static int solve(int[] ds, int[] vs, int w, int pos, int t);
```

To reconstruct the choices made, we can use the solve function itself:

```
static int buildOut(int[] ds, int[] vs, int w, int pos,
                    int t, StringBuilder sb)
{
    if (pos == ds.length) return 0;
    int left = t-3*w*ds[pos];
    if (left >= 0 &&
        solve(ds,vs,w,pos+1,left)+vs[pos] == solve(ds,vs,w,pos,t))
    {
        sb.append(ds[pos]).append(' ')
          .append(vs[pos]).append('\n');
        return buildOut(ds,vs,w,pos+1,left,sb)+1;
    } else return buildOut(ds,vs,w,pos+1,t,sb);
}
```

Then you can just call:

```
System.out.println(solve(ds,vs,w,0,t));
StringBuilder sb = new StringBuilder();
System.out.println(buildOut(ds,vs,w,0,t,sb));
System.out.print(sb);
```

3. Garbage Heap: We can break this problem down into the following tasks. If the heap is stored in an `int` `[][][]` heap lets consider the first dimension to denote the height, and the remaining two to denote the length and width.

- (a) Construct a separate array **int** `sums`. At each fixed height, we must use sums to compute the sum over a rectangle at that height in $O(1)$ time.
- (b) Using 4 for loops, loop over all possible opposing corners of base rectangles.
- (c) Then use a 5th loop to implement Kadane's algorithm in the height direction on the rectangular pillar with base determined by your first 4 loops.

4. Chest of Drawers:

```
//Assume higher drawers are labeled with higher indices.
//L: 1 or 0 determining if region above drawer n is
    locked/safe or not.
//Counts the number of valid configurations using drawers [1,n]
//and requiring exactly s safe drawers with L as above.
static long solve(int L, int n, int s);
```