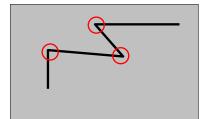
Notes on the Harris Detector

from Rick Szeliski's lecture notes, CSE576, Spring 05

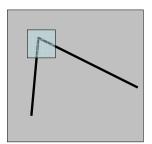
Harris corner detector

• C.Harris, M.Stephens. "A Combined Corner and Edge Detector". 1988

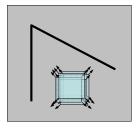


The Basic Idea

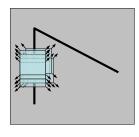
- We should easily recognize the point by looking through a small window
- Shifting a window in *any direction* should give *a large change* in intensity



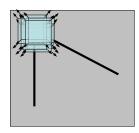
Harris Detector: Basic Idea



"flat" region: no change in all directions



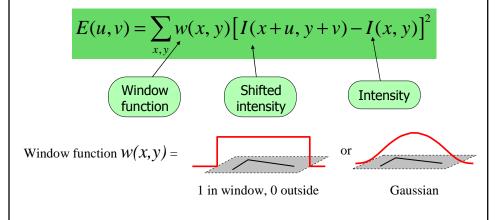
"edge": no change along the edge direction



"corner": significant change in all directions

Harris Detector: Mathematics

Change of intensity for the shift [u,v]:



Harris Detector: Mathematics

For small shifts [u,v] we have a *bilinear* approximation:

$$E(u,v) \cong \begin{bmatrix} u,v \end{bmatrix} M \begin{bmatrix} u \\ v \end{bmatrix}$$

where M is a 2×2 matrix computed from image derivatives:

$$M = \sum_{x,y} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

Harris Detector: Mathematics

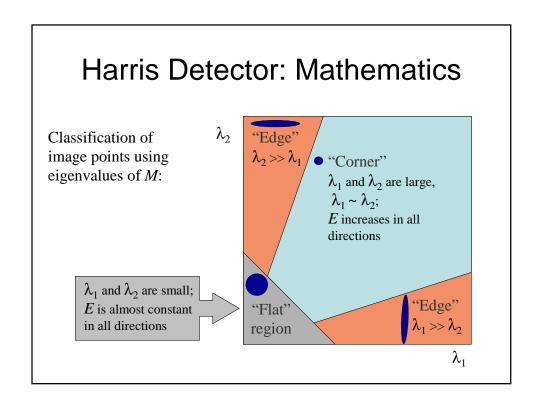
Intensity change in shifting window: eigenvalue analysis

$$E(u,v) \cong \begin{bmatrix} u \\ v \end{bmatrix} \quad M \quad \begin{bmatrix} u \\ v \end{bmatrix} \quad \lambda_1, \lambda_2 - \text{eigenvalues of } M$$

$$\text{direction of the fastest change}$$

$$\text{Ellipse } E(u,v) = \text{const}$$

$$\lambda_{\max}^{-1/2} \quad \lambda_{\min}^{-1/2}$$



Harris Detector: Mathematics

Measure of corner response:

$$R = \det M - k \left(\operatorname{trace} M \right)^2$$

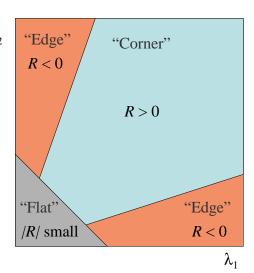
$$\det M = \lambda_1 \lambda_2$$

$$\operatorname{trace} M = \lambda_1 + \lambda_2$$

(k - empirical constant, k = 0.04-0.06)

Harris Detector: Mathematics

- *R* depends only on eigenvalues of M
- R is large for a corner
- *R* is negative with large magnitude for an edge
- |R| is small for a flat region

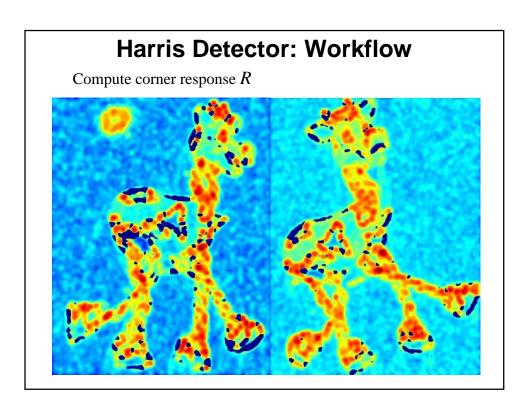


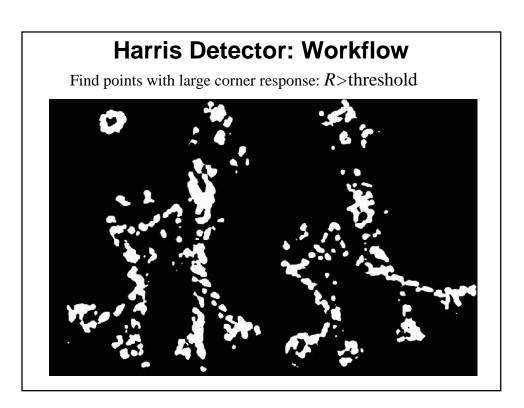
Harris Detector

- The Algorithm:
 - Find points with large corner response function R (R > threshold)
 - Take the points of local maxima of R

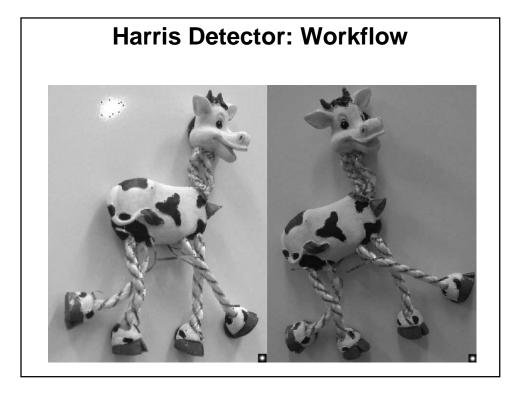
Harris Detector: Workflow







Harris Detector: Workflow Take only the points of local maxima of R



Harris Detector: Summary

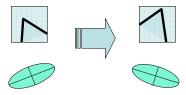
 Average intensity change in direction [u,v] can be expressed as a bilinear form:

 $E(u,v) \cong [u,v] \ M \begin{bmatrix} u \\ v \end{bmatrix}$

- Describe a point in terms of eigenvalues of M: measure of $c(R = \lambda_1 \lambda_2 k(\lambda_1 + \lambda_2)^2)$
- A good (corner) point should have a large intensity change in all directions, i.e. R should be large positive

Harris Detector: Some Properties

• Rotation invariance

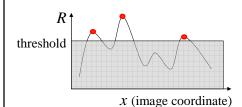


Ellipse rotates but its shape (i.e. eigenvalues) remains the same

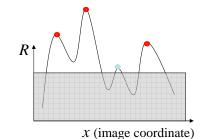
Corner response R is invariant to image rotation

Harris Detector: Some Properties

- Partial invariance to affine intensity change
 - $\ddot{\mathsf{u}}$ Only derivatives are used => invariance to intensity shift $I \to I + b$
 - $\ddot{\mathsf{u}}$ Intensity scale: $I \to a I$

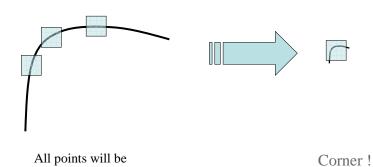


classified as edges



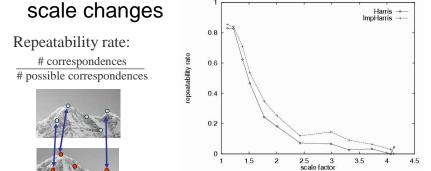
Harris Detector: Some Properties

• But: non-invariant to image scale!



Harris Detector: Some Properties

• Quality of Harris detector for different



C.Schmid et.al. "Evaluation of Interest Point Detectors". IJCV 2000

Models of Image Change

- Geometry
 - Rotation
 - Similarity (rotation + uniform scale)
 - Affine (scale dependent on direction)
 valid for: orthographic camera, locally
 planar object
- Photometry
 - Affine intensity change $(I \rightarrow a I + b)$

Rotation Invariant Detection

• Harris Corner Detector

