In []:	# Library import numpy as np import matplotlib.pyplot as plt 1. (Matrix Arithmetic)
	Let consider a matrix A and a vector b , $A = \begin{bmatrix} 1 & 1 & -2 \\ 3 & 3 & -5 \\ 3 & 2 & -10 \\ 1 & 1 & -7 \\ -4 & -4 & 11 \end{bmatrix}, b = \begin{bmatrix} 2 & 7 & 2 & -3 & -4 \end{bmatrix}$
	$\begin{bmatrix} 1 & 1 & -7 \\ -4 & -4 & 11 \end{bmatrix}$ (1) Generate arrays for A matrix and b vector using NumPy library
In []:	<pre>A = np.array([[1, 1, -2],[3, 3, -5],[3, 2, -10], [1,1,-7], [-4,-4,11]]) b = np.array([2, 7, 2, -3, -4]) print('\n','1. A is') print(A)</pre> <pre>print('\n','2. b is')</pre>
	print(b) 1. A is [[1
	[-4 -4 11]] 2. b is [2 7 2 -3 -4] (2) Transpose A and apply matrix multiplication with the original matrix(A^TA)
In []:	<pre>transA = A.T print('\n','1. Transpose A is') print(transA)</pre>
	ATA = np.dot(transA,A) print('\n','2. Trans(A) * A is') print(ATA) 1. Transpose A is [[1
	[-2 -5 -10 -7 11]] 2. Trans(A) * A is [[36 33 -98] [33 31 -88] [-98 -88 299]]
Tn [].	(3) Calculate x as the solution of $A^TAx = A^Tb$ $x = (A^TA)^{-1}A^Tb$
TII [].	<pre>ATAinv = np.linalg.inv(ATA) print('\n','1. inverse(trans(A)*A) is') print(ATAinv) B = np.dot(transA,b) print('\n','2. trans(A)*b is') print(B)</pre>
	<pre>x = np.dot(ATAinv,B) print('\n','3. the solution x is') print(x) 1. inverse(trans(A)*A) is [[2.03604806 -1.65954606 0.17890521]</pre>
	[-1.65954606 1.54873164 -0.08811749] [0.17890521 -0.08811749 0.03604806]] 2. trans(A)*b is [42 40 -82] 3. the solution x is
	[4.46194927 -0.52603471 1.03337784] (4) Calculate the norm of Ax $-$ b with line-by-line coding and using NumPy library. Let $X = Ax - b$,
In []:	$L_p = (\Sigma_i^n X(i) ^p)^{1/p}$ print('\n 1. Line-by-Line coding') diff_mat = np.dot(A, x) - b print(' (1) Ax - b is')
	<pre>print(diff_mat) # L1 norm norm1 = sum(abs(diff_mat)) print('\n (2)-1. 1-norm :', norm1) # L2 norm</pre>
	<pre>normsq = np.dot(diff_mat, diff_mat) print(' (2)-2. (Ax - b)*(Ax - b) = ', normsq) norm2 = np.sqrt(normsq) print('</pre>
	<pre>print(' (2)-3. infinity-norm :', norminf) # Using Numpy Library print('\n 2. Using numpy norm') norm1_ = np.linalg.norm(diff_mat,1) norm2_ = np.linalg.norm(diff_mat,2)</pre>
	<pre>norminf_ = np.linalg.norm(diff_mat,np.inf) print(' (1) 1-norm is',norm1_) print(' (2) 2-norm is',norm2_) print(' (3) infinity-norm is',norminf) 1. Line-by-Line coding (1) Ax - b is</pre>
	[-1.30841121e-01 -3.59145527e-01 2.84217094e-14 -2.97730307e-01 -3.76502003e-01] (2)-1. 1-norm : 1.164218958611504 (2)-2. (Ax - b)*(Ax - b) = 0.3765020026702274 2-norm : 0.6135975901763527
	(2)-3. infinity-norm : 2.842170943040401e-14 2. Using numpy norm (1) 1-norm is 1.164218958611504 (2) 2-norm is 0.6135975901763527 (3) infinity-norm is 2.842170943040401e-14
	2. (Drawing Graps) A two-dimensional Ackley function, $f(x,y)$, has many local minima and one global minimum in the domain, $(x,y)\in [-4,4]\times [-4,4].$
	$f(x,y)=-a\exp{(-b\sqrt{0.5(x^2+y^2)})}-\exp{(0.5(cos(cx)+cos(cy)))}+a+\exp{(1)}$ where $a=20,b=0.2,$ and $c=2\pi.$
In []:	(1) Plot a 2D contour of the Ackley function on $(x,y) \in [-4,4] \times [-4,4]$. # Setting the function def Ackley(x, y): a = 20 b = 0.2
	<pre>c = 2*np.pi f1 = -a * np.exp(-b * np.sqrt(0.5 * (x**2 + y**2))) f2 = np.exp(0.5 * np.cos(c*x) + np.cos(c*y)) f = f1 - f2 + a + np.exp(1) return f</pre>
In []:	<pre>lb = -4 ub = 4 N = 100 x = np.linspace(lb, ub, N) y = np.linspace(lb, ub, N)</pre>
In []:	<pre>X, Y = np.meshgrid(x, y) Z = Ackley(X, Y) # Set plot params plt.rcParams['figure.figsize'] = [10,10] plt.rcParams['font.size'] = 15 plt.rcParams['font.family'] = 'Times New Roman'</pre>
	<pre>plt.rcParams['axes.linewidth'] = 2 plt.rcParams['lines.linewidth'] = 2 plt.rcParams['xtick.direction'] = 'out' plt.rcParams['ytick.direction'] = 'out' plt.rcParams['xtick.minor.visible'] = True plt.rcParams['ytick.minor.visible'] = True</pre>
	<pre>plt.rcParams['xtick.major.size'] = 7 plt.rcParams['ytick.major.size'] = 7 plt.rcParams['xtick.minor.size'] = 3.5 plt.rcParams['ytick.minor.size'] = 3.5 plt.rcParams['xtick.major.width'] = 1.5 plt.rcParams['ytick.major.width'] = 1.5 plt.rcParams['xtick.minor.width'] = 1.5</pre>
In []:	<pre>plt.rcParams['ytick.minor.width'] = 1.5 plt.rcParams['xtick.top'] = True plt.rcParams['ytick.right'] = True from mpl_toolkits.axes_grid1 import make_axes_locatable fig = plt.figure()</pre>
	cont = plt.contourf(X,Y,Z, cmap='magma') plt.xlabel('X') plt.ylabel('Y') cs=plt.contour(X,Y,Z,colors='k') # 등고선 표현 plt.clabel(cs)
Out[]:	plt.title('2D contour of the Ackley function') fig.colorbar(cont, shrink=1, aspect=15) <matplotlib.colorbar.colorbar 0x7fde089d0b10="" at=""> 2D contour of the Ackley function 4 14</matplotlib.colorbar.colorbar>
	3 2 3 6 4 6 4 10 10 10 10 10 10 10 10 10 10 10 10 10
	2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
	1 8
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	2 -3 -3 -3 -3 -3 -3 -3 -3 -3 -3
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
In []:	(2) Plot a 3D graph of the Ackley function on $(x,y)\in [-4,4] imes [-4,4]$. from mpl_toolkits.mplot3d import Axes3D
	<pre>fig= plt.figure() ax=fig.add_subplot(111, projection='3d') surf=ax.plot_surface(X,Y,Z, cmap='magma') plt.xlabel('X') plt.ylabel('Y') plt.title('3D graph of the Ackley function')</pre>
Out[]:	fig.colorbar(surf, shrink=0.5, aspect=10)
	12 10 0
	8 6 4 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
In []:	(3) Find the global minimum and its position. global_min = np.min(Z) # numpy.unravel_index(indices[], shape()) : indices를 shape에 매핑시킨 index 반환 min_index = np.unravel_index(np.argmin(Z), Z.shape) print(' 1 Clobal minimum = ' global min)
	print(' 1. Global minimum = ', global_min) # Cartesian 과 Matrix는 반대로 indexing 됨 # 따라서, x와 y의 indexing 반대임 print(' 2. The position (x,y) =', (x[min_index[1]], y[min_index[0]])) 1. Global minimum = -1.3920738434531574 2. The position (x,y) = (-0.040404040404022, -0.040404040404022)
In []:	(4) Plot a graph for $f(y x=-2)$, $f(y x=0)$, and $f(y x=2)$ in one plot with legends. $\begin{array}{cccccccccccccccccccccccccccccccccccc$
	<pre>fig, ax = plt.subplots() for x_value, color, shapes in zip(x_values, colors, shapes): ax.plot(y, Ackley(x_value, y), shapes, color=color, label=f'f(y x = {x_value})') plt.xlabel('y') plt.ylabel('Z')</pre>
	ax.legend() plt.grid()
	f(y x = -2) $f(y x = 0)$ $f(y x = 2)$
	(5) Plot the x-direction averaged one-dimensional graph and the y-direction averaged one-dimensional graph on the same canyas.
In []:	# numpy.mean(a, axis) # axis = 0> x축, axis = 1> y축 x_average = np.mean(Z, axis=0) y_average = np.mean(Z, axis=1)
	<pre>fig, ax = plt.subplots() ax.plot(x, x_average,'', label='x-direction average') ax.plot(y, y_average,'', label='y-direction average') plt.grid() plt.xlabel('interval') plt.ylabel('direction average') ax.legend()</pre>
Out[]:	ax.legend()
	direction average
	gilled The state of the state o
	5 x-direction average y-direction average
	-4 -3 -2 -1 0 1 2 3 4 interval

HW1. NumPy and Matplotlib

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