

Lecture 1

# Introduction to Scientific Computation with Python

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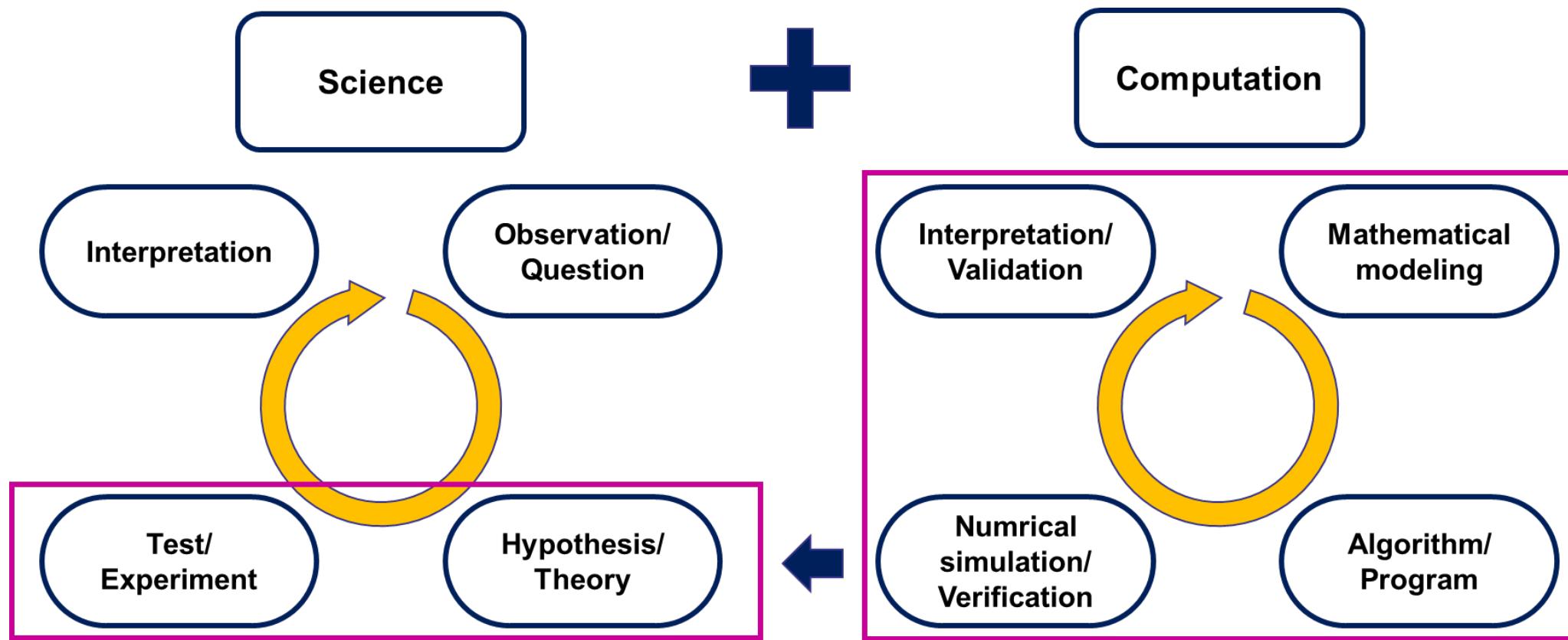


**YONSEI UNIVERSITY**

# Scientific Computation

## What is scientific computation?

- The process of using mathematical algorithms and computer technology to solve scientific problems



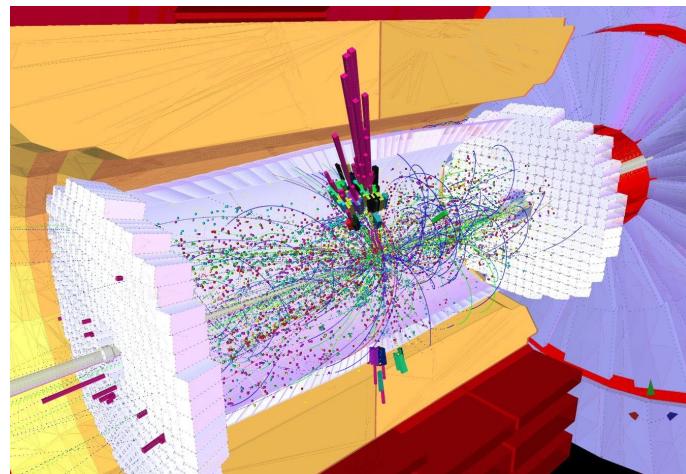
# Scientific Computation

## Why do we need to learn scientific computation?

- Through the **validated model and verified algorithm**, scientific computation allows

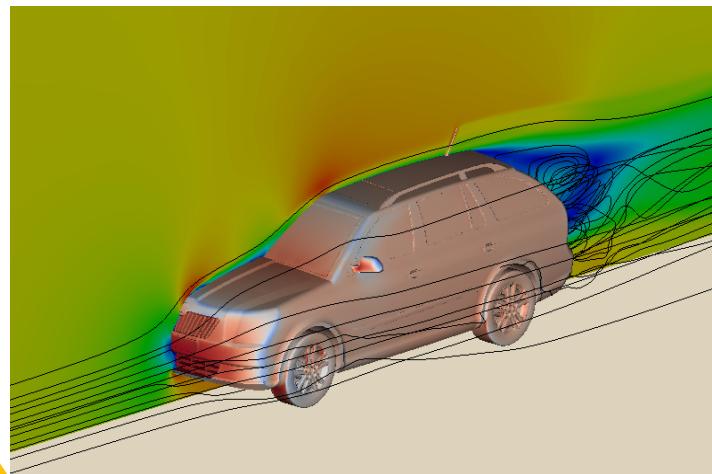
Science

scientists to simulate complex systems and processes that would be difficult or impossible to study through observation or experiment alone



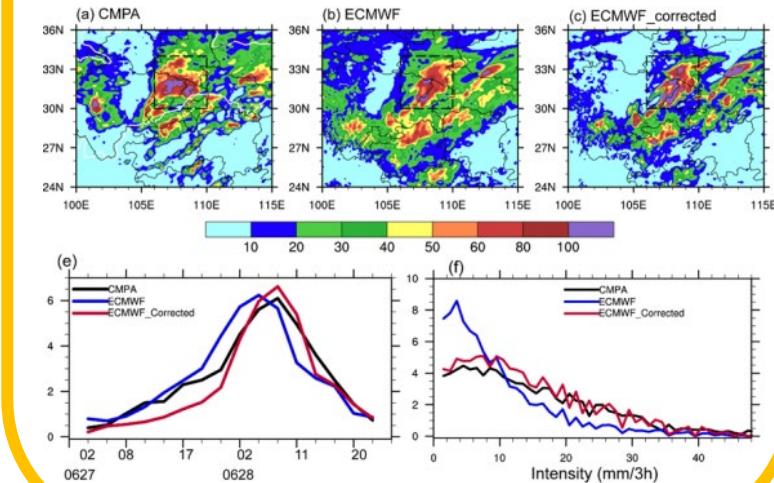
Engineering

engineers to simulate various conditions with various parameters so that they could find optimal conditions while reducing economical and environmental costs



Our lives

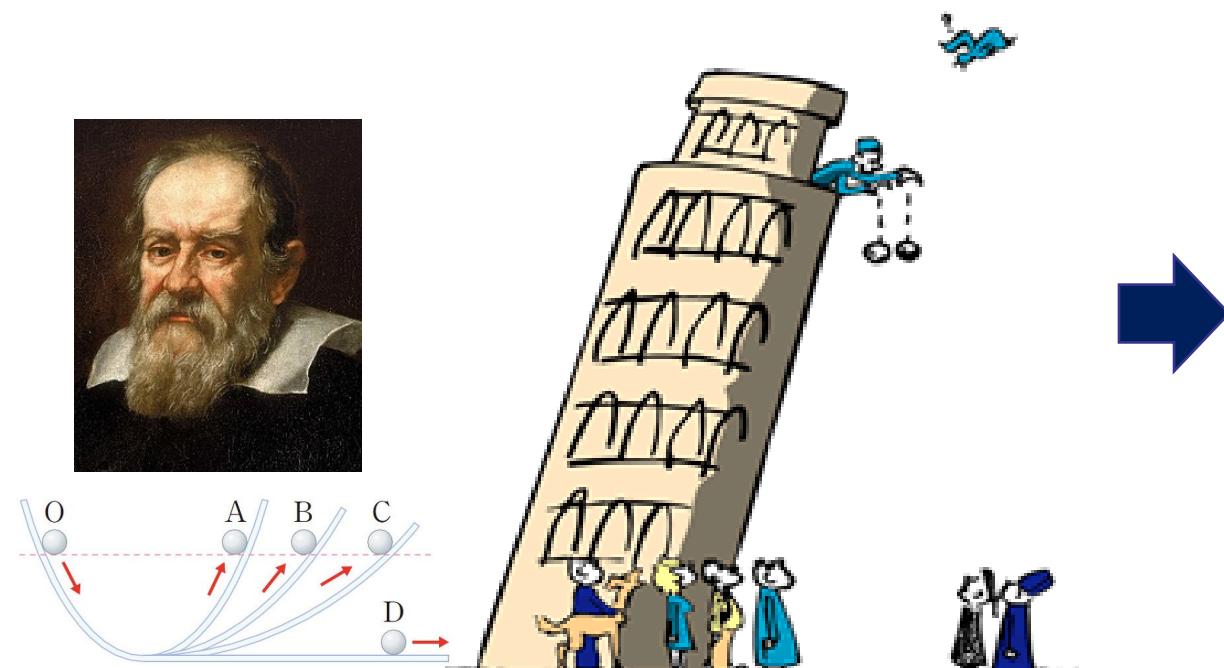
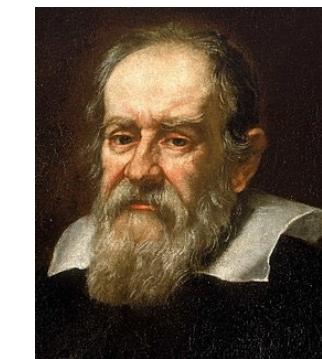
us to prepare in advance for issues that pose significant risks to our lives, such as natural disasters or explosions by simulating those kind of situations



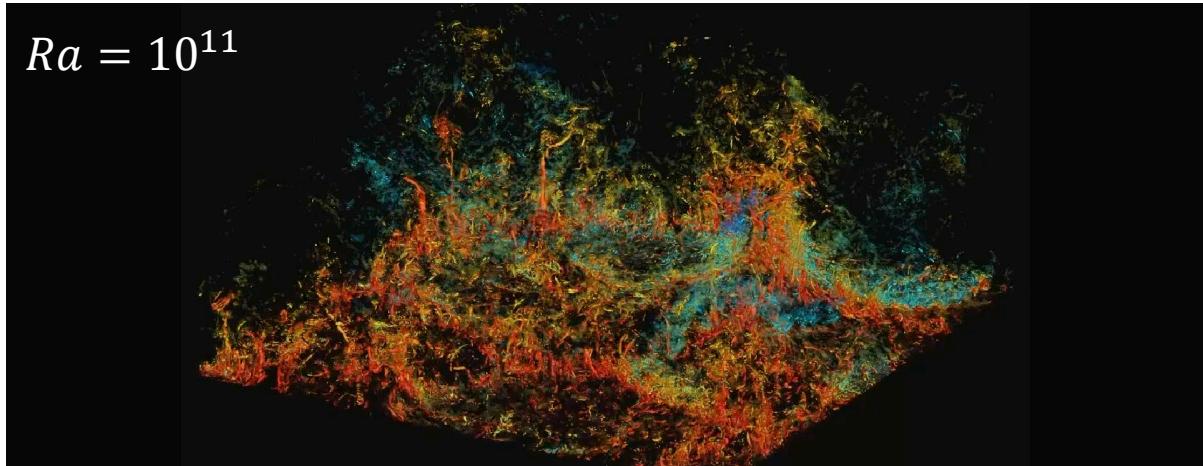
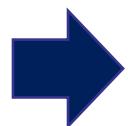
# Scientific Computation

## Why do we need scientific computation?

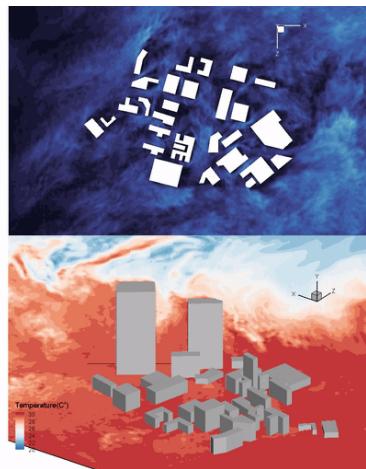
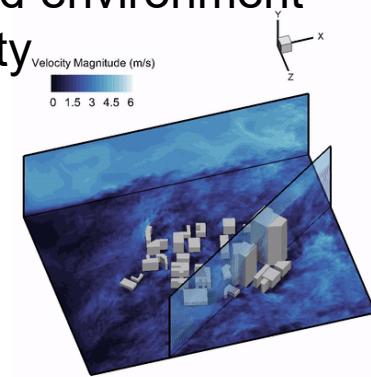
- Advancing science and theory : more macro/microscopic systems



Galileo Galilei's thought experiment



Simulation of the wind environment near Yonsei University

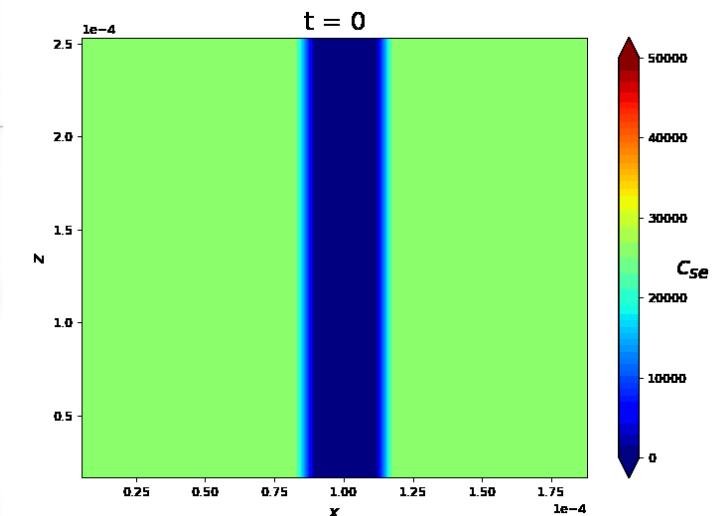
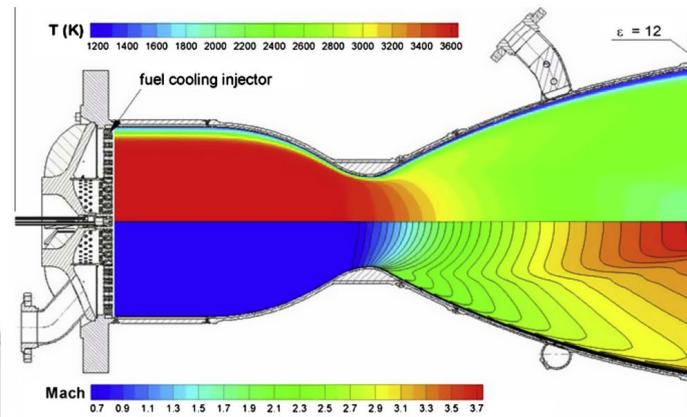
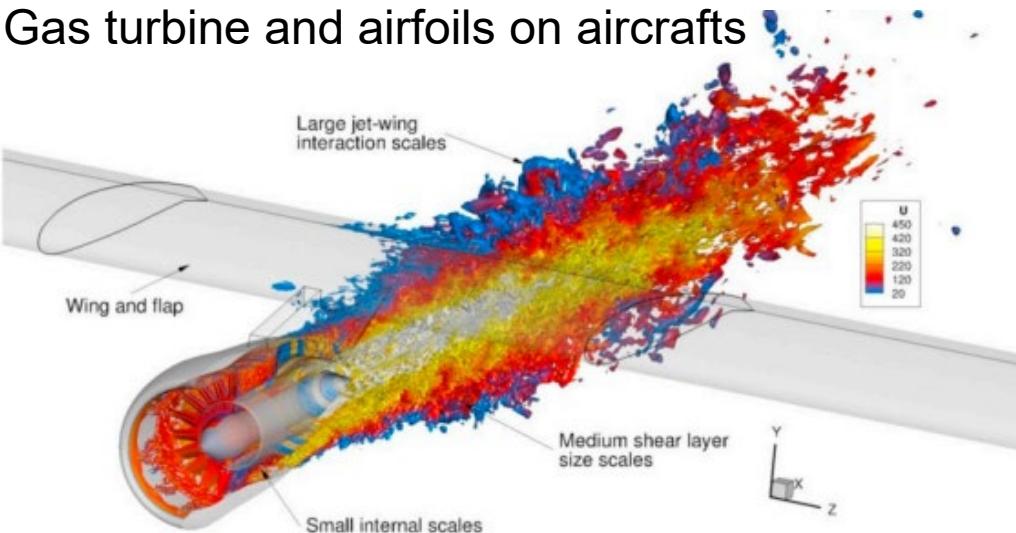


# Scientific Computation

## Why do we need scientific computation?

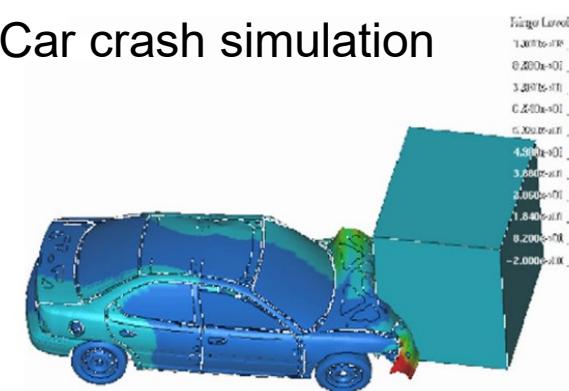
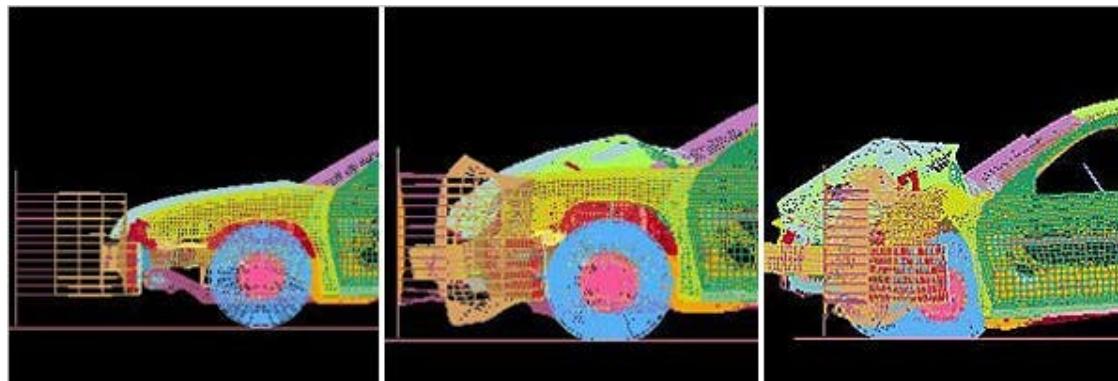
- Application to engineering

Gas turbine and airfoils on aircrafts



Rocket propulsion

Car crash simulation



Lithium-ion concentration in electrode

# Scientific Computation

## Why do we need scientific computation?

- Sustaining our lives and environment



### The 17 Goals

Adopted by all UN Member States in 2015.  
Part of the 2030 Agenda for Sustainable Development.

### Environmental fluid mechanics

Substantial role in SDGs no. 6, 7, 9, 11, 13, and 14.

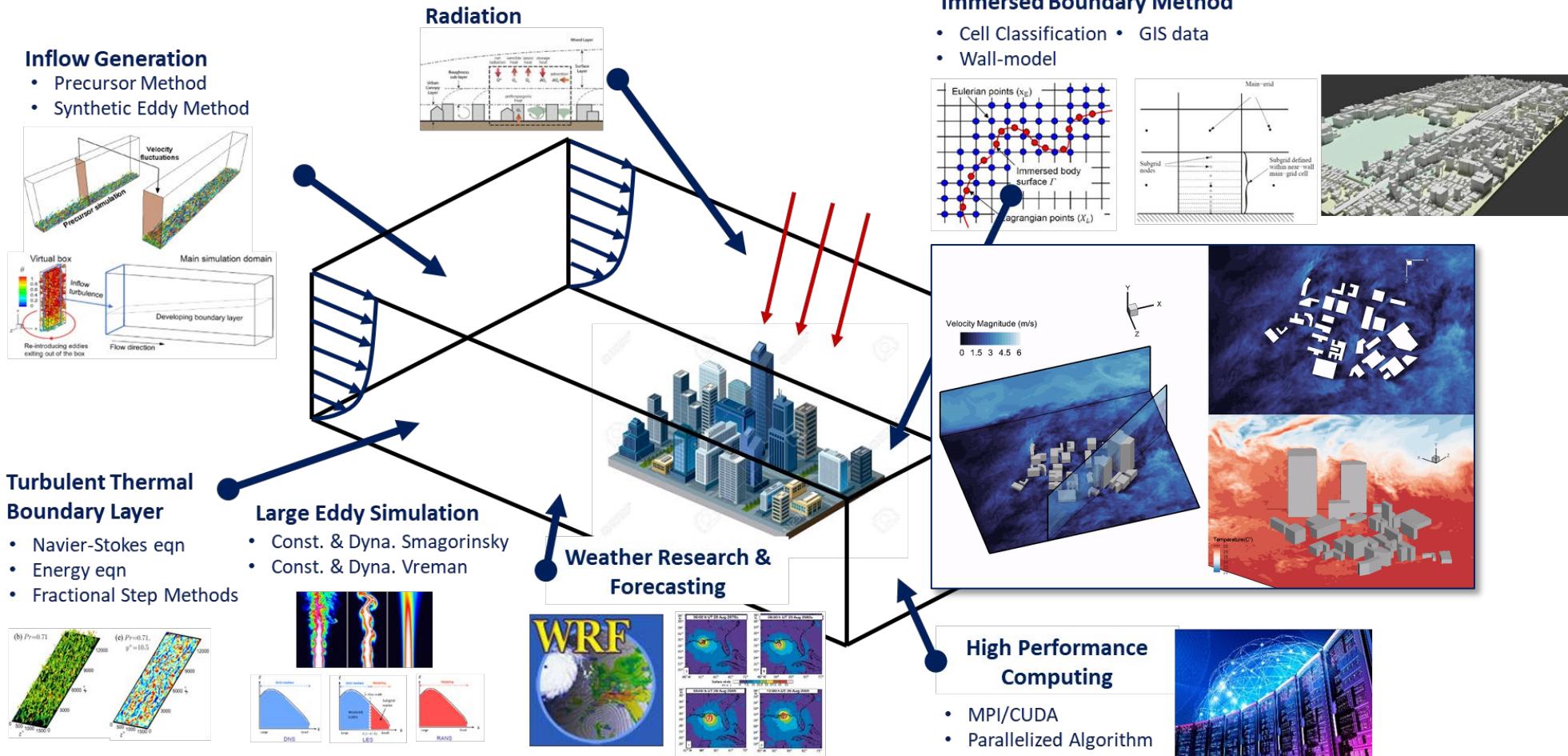
### Sustainable cities & communities

make cities and human settlements inclusive, safe, resilient and sustainable.

# Scientific Computation

## Why do we need scientific computation?

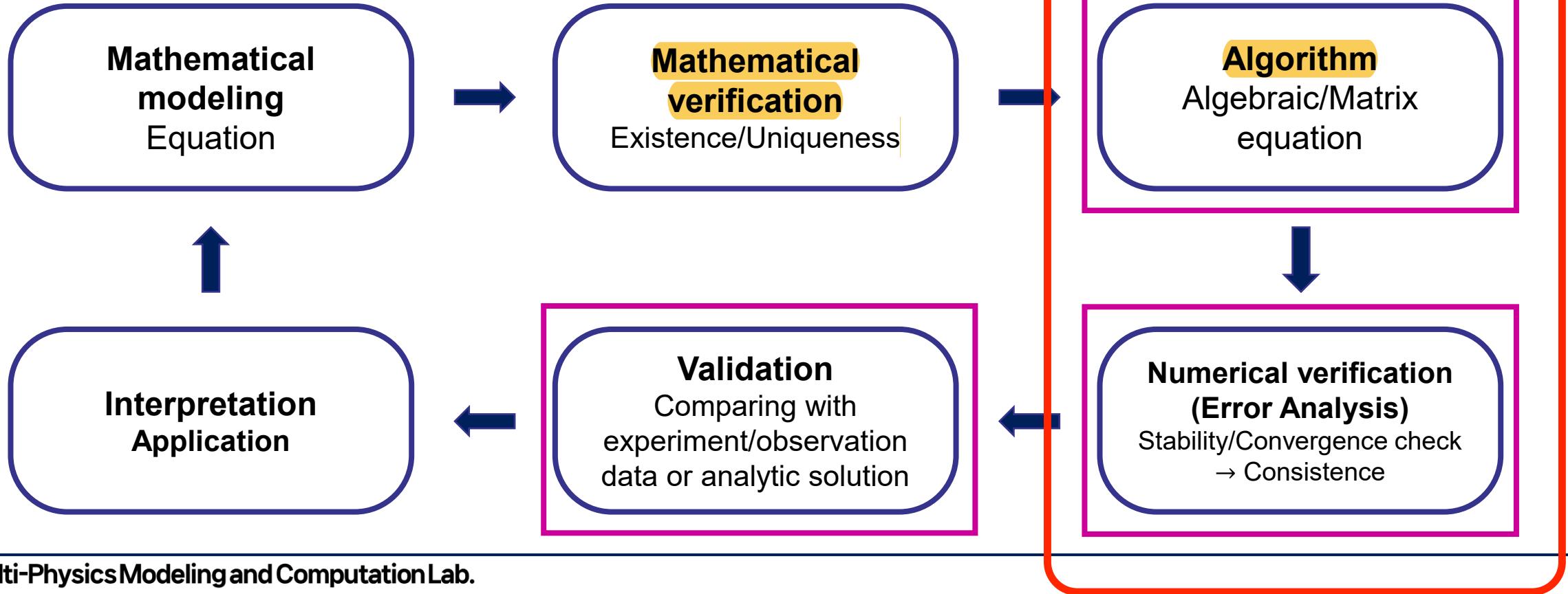
- Sustaining our lives and environment



# Scientific Computation

## Verification and validation(V&V) : Numerical simulation into science

- To bring numerical simulation into the realm of 'scientific' computation, two questions must be asked.
  - Did you solve it well?
  - Did you solve it properly?



# Scientific Computation

## Solving equation using computer Governing equations

Continuity Eqn.

$$\nabla \cdot \mathbf{u} = 0$$

Navier-Stokes Eqn.

$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} = -\nabla p + \frac{1}{Re} \nabla^2 \mathbf{u} + \mathbf{F}_b$$

Energy Eqn.

$$\frac{\partial T}{\partial t} + \mathbf{u} \cdot \nabla T = \frac{1}{RePr} \nabla^2 T$$

Novel methods

Approximate  
LU Decomposition  
Numerical Analysis  
schemes

Multigrid method

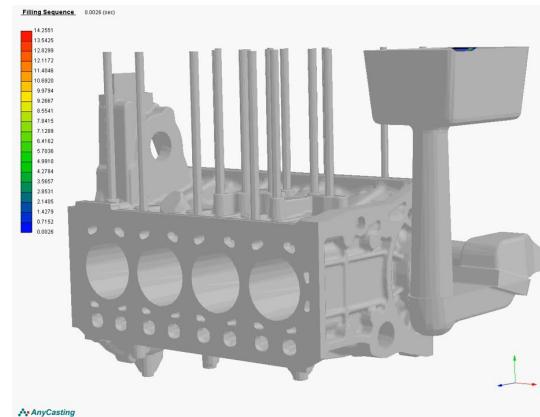
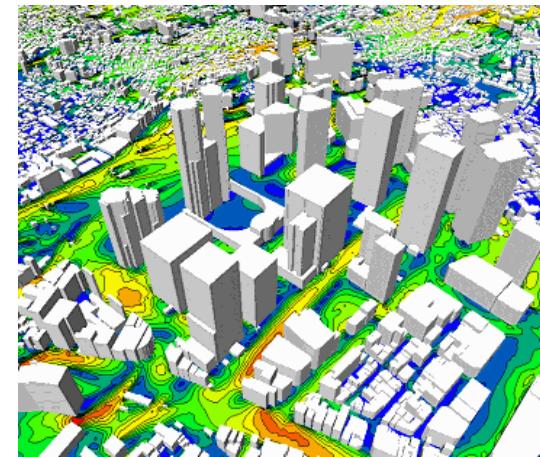
FFT

Novel TDMA solver  
Parallel computing  
skill(MPI, CUDA)...  
etc.

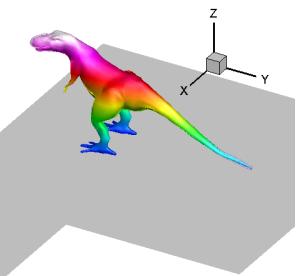
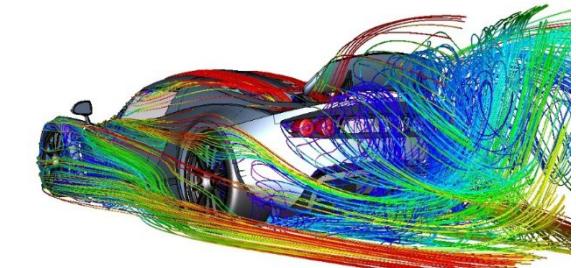
$$\begin{aligned} \frac{\mathbf{u}^{n+1} - \mathbf{u}^n}{\Delta t} + \frac{1}{2} (\mathbf{u}^{n+1} \cdot \mathcal{G} \mathbf{u}^{n+1} + \mathbf{u}^n \cdot \mathcal{G} \mathbf{u}^n) &= -\mathcal{G} p^{n+\frac{1}{2}} + \frac{1}{2} \sqrt{\frac{Pr}{Ra}} (\mathcal{L} \mathbf{u}^{n+1} + \mathcal{L} \mathbf{u}^n) + \mathbf{F} (\theta^{n+\frac{1}{2}}) + \mathbf{m} \mathbf{b} c_{cs}^{n+\frac{1}{2}} \\ \mathcal{D} \mathbf{u}^{n+1} &= c \mathbf{b} c_{cs}^{n+1}, \\ \frac{\theta^{n+\frac{1}{2}} - \theta^{n-\frac{1}{2}}}{\Delta t} + \frac{1}{2} \mathbf{u}^n \cdot (\mathcal{G} \theta^{n+\frac{1}{2}} + \mathcal{G} \theta^{n-\frac{1}{2}}) &= \frac{1}{2\sqrt{RaPr}} (\mathcal{L} \theta^{n+\frac{1}{2}} + \mathcal{L} \theta^{n-\frac{1}{2}}) + c \mathbf{b} c_{cs}^n, \\ \begin{pmatrix} \mathcal{A}_{\theta}^{n-\frac{1}{2}} & \mathcal{O} & \mathcal{O} \\ -\mathbf{F} & \mathbf{A}^n & \mathcal{G} \\ \mathcal{O} & \mathcal{D} & \mathcal{O} \end{pmatrix} \begin{pmatrix} \theta^{n+\frac{1}{2}} \\ \mathbf{u}^{n+1} \\ p^{n+\frac{1}{2}} \end{pmatrix} &= \begin{pmatrix} \mathcal{A}_{\theta}^{n-\frac{1}{2}} & \mathcal{O} & \mathcal{O} \\ -\mathbf{F} & \mathbf{A}^n & \mathcal{O} \\ \mathcal{O} & \mathcal{D} & -\Delta t \mathcal{D} \mathcal{G} \end{pmatrix} \begin{pmatrix} \mathcal{I} & \mathcal{O} & \mathcal{O} \\ \mathcal{O} & \mathbb{I} & \Delta t \mathcal{G} \\ \mathcal{O} & \mathcal{O} & \mathcal{I} \end{pmatrix} \begin{pmatrix} \theta^{n+\frac{1}{2}} \\ \mathbf{u}^{n+1} \\ p^{n+\frac{1}{2}} \end{pmatrix} \end{aligned}$$

$$\mathbf{A}^n \approx \frac{1}{\Delta t} \begin{pmatrix} \prod_{k=1}^3 (\mathcal{I} + \Delta t (\mathcal{M}_{11}^n)^k) & \mathcal{O} & \mathcal{O} \\ \Delta t \mathcal{M}_{21}^n & \prod_{k=1}^3 (\mathcal{I} + \Delta t (\mathcal{M}_{22}^n)^k) & \mathcal{O} \\ \Delta t \mathcal{M}_{31}^n & \Delta t \mathcal{M}_{32}^n & \prod_{k=1}^3 (\mathcal{I} + \Delta t (\mathcal{M}_{33}^n)^k) \end{pmatrix} \begin{pmatrix} \mathcal{I} & \Delta t \mathcal{M}_{12}^n & \Delta t \mathcal{M}_{13}^n \\ \mathcal{O} & \mathcal{I} & \Delta t \mathcal{M}_{23}^n \\ \mathcal{O} & \mathcal{O} & \mathcal{I} \end{pmatrix}$$

Efficient, reliable, large-scale, and  
fast computation for real problems



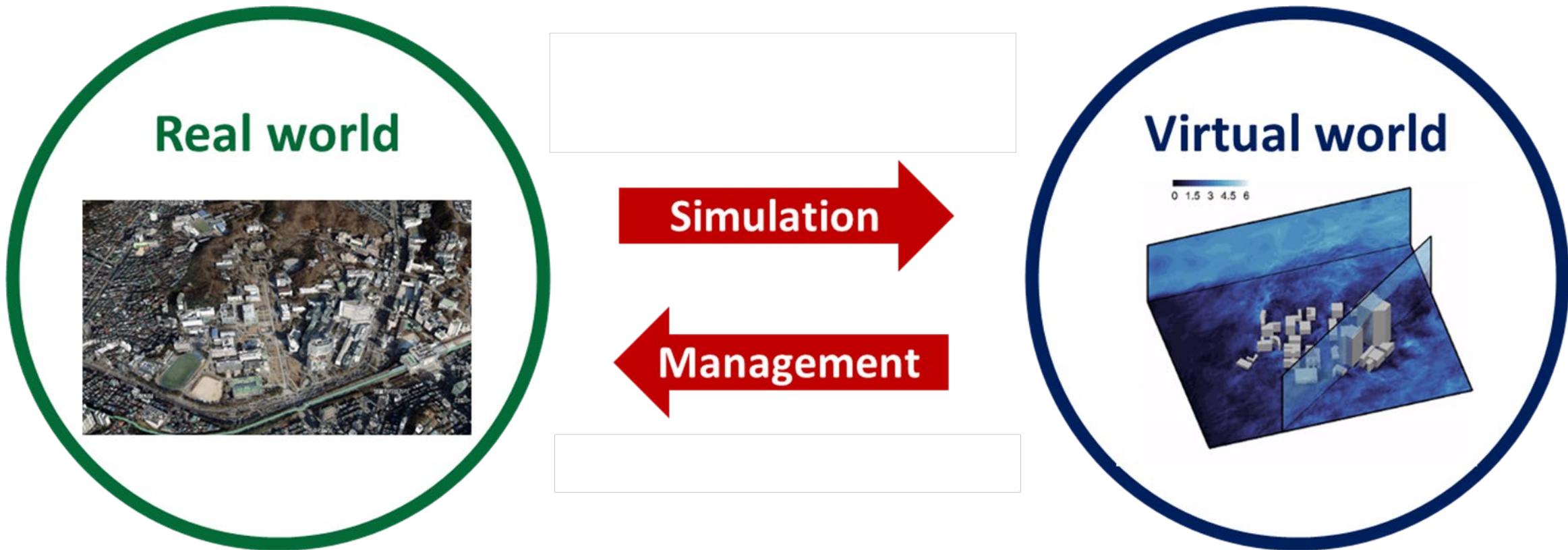
Applications



# Scientific Computation

## Why do we need a faster computer?

- For real-time application to the real world, high-speed calculation is required (Digital Twin)



# Scientific Computation

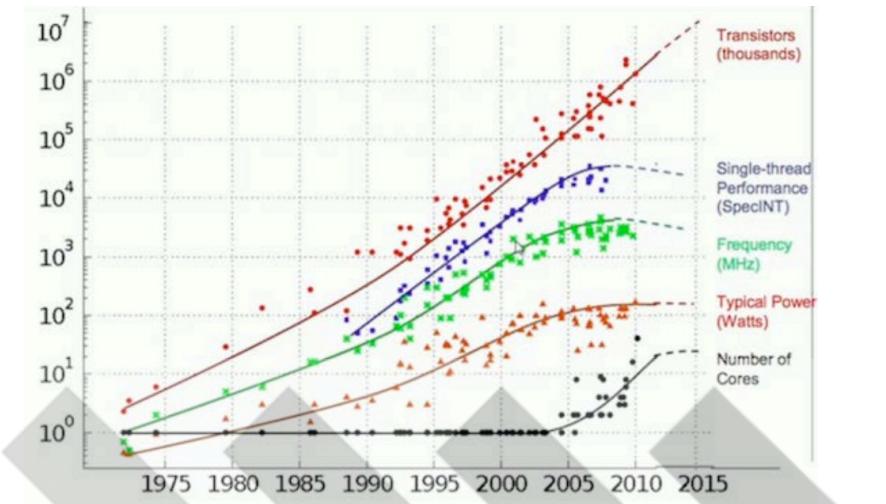
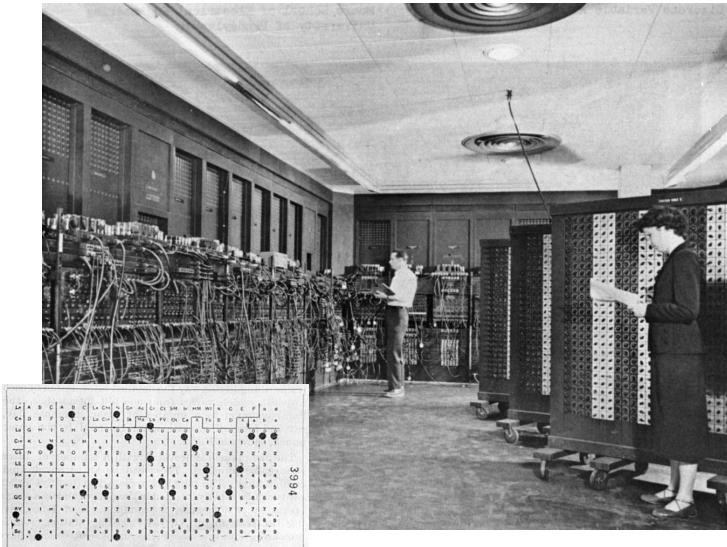
## Why do we need a faster computer?

| Challenges   | Enabling Technologies  |
|--|--|
| Data management, data privacy and security, data quality | Digital platforms, cryptography and blockchain technologies, big data technologies                                       |
| Real-time communication of data and latency              | Data compression, communication technologies like 5G and internet of things technologies                                 |
| <u>Physical realism and future projections</u>           | Sensor technologies, <u>high fidelity physics-based simulators, data-driven models</u>                                   |
| <u>Real time modeling</u>                                | <u>Hybrid analysis and modeling, reduced order modeling, multivariate data-driven models</u>                             |
| <u>Continuous model updates, modeling the unknown</u>    | Big data cybernetics, <u>hybrid analysis and modeling, data assimilation, compressed sensing and symbolic regression</u> |
| Transperancy and interpretability                        | <u>Hybrid analysis and modeling, explainable artificial intelligence</u>   |
| Large scale computation                                  | Computational infrastructure, edge, fog and cloud computing  |
| Interaction with physical asset                          | Human machine interface, natural language processing, visualization augmented reality and virtual reality                |

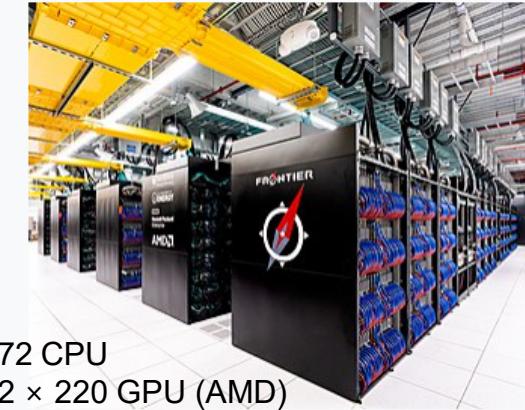
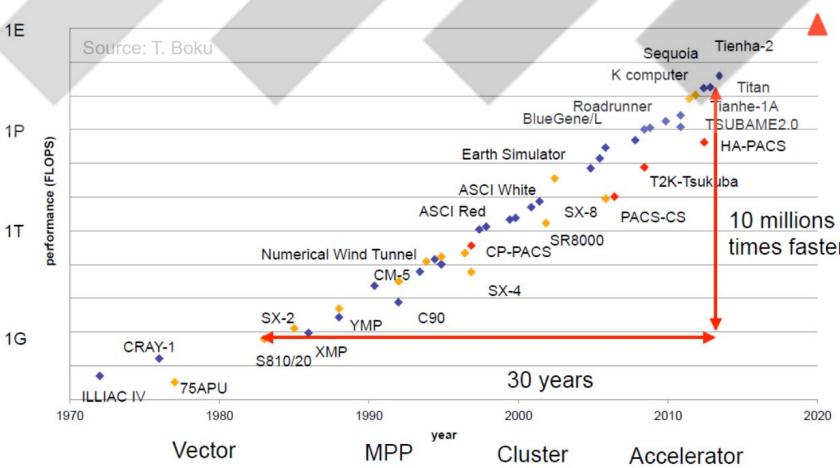
# Computer & Language

Frontier

## Evolution of computers



Original data collected and plotted by M. Horowitz, F. Labonte, O. Shacham, K. Olukotun, L. Hammond and C. Batten  
Dotted line extrapolations by C. Moore



591,872 CPU  
36,992 × 220 GPU (AMD)

|                         |  |
|-------------------------|--|
| <b>Active</b>           | Deployment: Sep. 2021<br>Completion: May 2022                                |
| <b>Operators</b>        | Oak Ridge National Laboratory and U.S. Department of Energy                  |
| <b>Location</b>         | Oak Ridge Leadership Computing Facility                                      |
| <b>Power</b>            | 21 MW  |
| <b>Operating system</b> | HPE Cray OS  |
| <b>Space</b>            | 680 m <sup>2</sup> (7,300 sq ft)   |
| <b>Speed</b>            | 1.102 exaFLOPS (Rmax) /<br>1.685 exaFLOPS (Rpeak) <sup>[1]</sup>             |
| <b>Cost</b>             | US\$600 million (estimated cost)   |
| <b>Purpose</b>          | Scientific research and development  |
| <b>Website</b>          | <a href="http://www.olcf.ornl.gov/frontier/">www.olcf.ornl.gov/frontier/</a> |

# Computer & Language

## Development of programming language

- Machine language
  - Language written in bits that the hardware can decode and execute directly
- Assembly language
  - More readable than machine language but still closely tied to the instruction set architecture of the specific computer
- High-level programming language
  - an easy(?) -to-understand programming language without relying on computer architecture

| High Level Language | Assembly Language | Maching Language |
|---------------------|-------------------|------------------|
| #include <stdio.h>  | MOV R0, 4 ;       | 11010101101001   |
|                     | MOV R1, 5 ;       | 01001010101100   |
| int main(){         | ADD R0, R0, 2 ;   | 10101010010100   |
| int a=4,b=5,c;      | ADD R1, R1, 3 ;   | 11010101000101   |
| a+=2; b+=3;         | SUB R2, R0, R1 ;  | 10101101010101   |
| c=a-b;              |                   | 11001010010101   |
|                     |                   | 11010101000101   |
| return 0;           |                   | 10101101010101   |
| }                   |                   |                  |

# Computer & Language

## Development of programming language

- Evolution of programming language
  - an easy(?) -to-understand programming language without relying on computer architecture
- ✓ FORTRAN(FORmular TRANslation, 1957) : The first successful advanced language, mainly for scientific and technological calculations
- ✓ ALGOL60(ALGOritmic Language 60, 1959): Languages that greatly influenced the development of later languages such as **pascal**, **C language**, etc
- ✓ COBOL(COMmon Business Oriented Language, 1960) : Language Created for Office Processing
- ✓ C (1972) : language that provides access to computer structures using **pointers**, used for programming computer systems
- ✓ C++ (1983) : Expanded C language with **object orientation**
- ✓ Python (1991) : **Interpreter-style, object-oriented, interactive language**

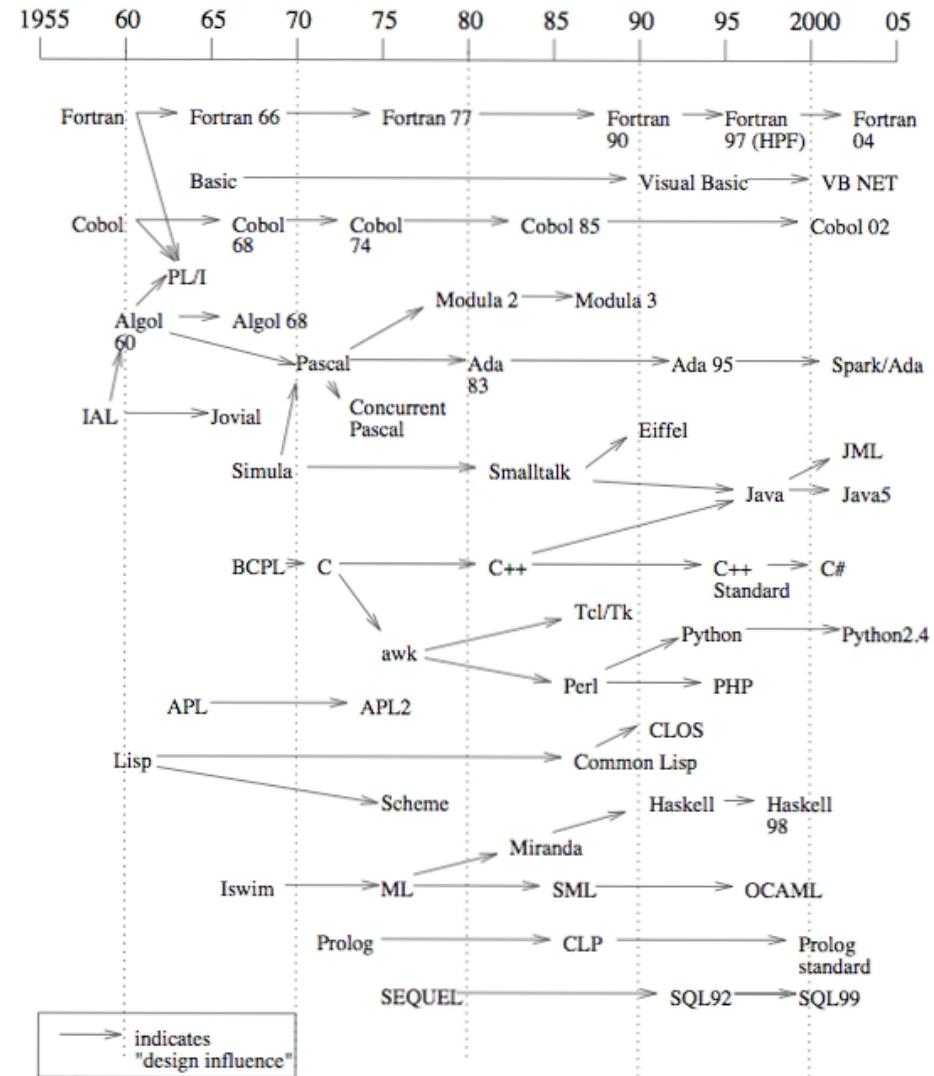


Figure 1.2: A Snapshot of Programming Language History

# Python

## A Brief History and Current Status

- Python was created in late 1980s by Guido van Rossum and first appeared 1991
- Python 2.0 was released in 2000 with major new features.
- Python 3.0 was released in 2008 with features backported to Python 2.6.x and 2.7.x.
- Python 2.7's end-of-life was postponed to 2020.
- Python 3.9.2 and 3.8.8 were expedited in 2021 due to security issues.
- Python 3.11.0 is the current stable releases with increased program execution speed and improved error reporting.
- The older series, including 3.9, 3.8 and 3.7, will only receive security fixes in the future.
- Four new releases were made in September 2022 due to a potential denial-of-service attack: 3.10.7, 3.9.14, 3.8.14, and 3.7.14.



Guido van Rossum  
Creator of Python programming language.



# Python

# Why do we use Python in this class?

- Simple and clear syntax
  - Huge and excellent library
  - Good support for interfacing C, C++, and Fortran (F2py)
  - Python is available for FREE!

## Comparison to languages

- Cubic spline code Python vs MATLAB vs Fortran

```
>>> import numpy as np  
>>> from scipy.interpolate import CubicSpline  
>>> import matplotlib.pyplot as plt  
>>> x = np.arange(10)  
>>> y = np.sin(x)  
>>> cs = CubicSpline(x, y)
```

# Interactive language

```
x = [0 1 2.5 3.6 5 7 8.1 10  
y = sin(x);  
xx = 0:.25:10;  
yy = spline(x,y,xx);
```

MATLAB

# Fortran

```
1 program cubic_spline
2
3 implicit none
4
5 integer :: i
6 real*8 :: x(10), y(10)
7 real*8 :: xx, yy
8
9 do i = 1,10
10 | x(i) = dble(i)
11 | y(i) = sin(x(i))
12 enddo
13
14 xx = 6.5
15 call spline(x, y, 10, 0.0d0, 0.0d0, xx, yy)
16
17 end program cubic_spline
18
```

```
19 subroutine spline(x_data, y_data, n, g_0, g_n, x, cs)
20
21 implicit none
22 integer, intent(in) :: n
23 integer :: i, j
24 real*8, intent(in) :: x, g_0, g_n
25 real*8, dimension(0:n), intent(in) :: x_data, y_data
26 real*8, dimension(0:n) :: RHS, LHS
27 real*8, dimension(0:n) :: delta
28 real*8, dimension(1:n-1, 1) :: TDM
29 real*8, intent(out) :: cs
30
31 delta(0)=x_data(1)-x_data(0)
32 do i=0, n-1
33 | delta(i)=x_data(i+1)-x_data(i)
34 end do
35 delta(n)=x_data(n)-x_data(n-1)
36
37 !Make TDM
38 do i=1, n-1
39 | TDM(i, i)=(delta(i+1)+delta(i))/2
40 end do
41 do i=1, n-2
42 | TDM(i, i+1)=delta(i)/(delta(i)+delta(i+1))
43 | TDM(i+1, i)=delta(i+1)/(delta(i)+delta(i+1))
44 end do
45
46 RHS(1)=(y_data(n)-y_data(0))/6
47 do i=1, n-1
48 | RHS(i)=(y_data(i+1)-y_data(i))/6
49 end do
50
51 RHS(0)=y_data(0)
52 RHS(1)=RHS(1)-delta(0)/6.*g_0
53 RHS(n-1)=RHS(n-1)-delta(n)/6.*g_n
54 RHS(n)=y_data(n)
55
56 LHS(0)=g_0
57 call TDMA(TDM, RHS(1:n-1), 1, n-1, LHS(1:n-1))
58
59 do i=0, n-1
60 | if ((x<=x_data(i)).and.(x>=x_data(i+1))) then
61 | | cs=(LHS(1)/6)*(x-x_data(i))**3/(delta(i)-delta(i)*x-x_data(i+1))+
62 | | +(LHS(i+1)/6)*(x-x_data(i+1))**3/(delta(i+1)-delta(i)*x-x_data(i+1))+
63 | | y_data(i)*(x-x_data(i+1))-y_data(i+1)*(x-x_data(i))/delta(i)
64 end if
65 end do
66
67 return
68 end subroutine spline
69
70 subroutine TDMA(TDM, RHS, bs, bf, LHS)
71
72 implicit none
73 integer, intent(in) :: bs, bf
74 real*8, dimension(bs:bf, bs:bf), intent(in) :: TDM
75 real*8, dimension(bs:bf), intent(in) :: RHS
76 real*8, dimension(bs:bf), intent(out) :: LHS
77 real*8, dimension(bs:bf) :: b, SOL
78 real*8, dimension(bs+1:bf) :: a
79 real*8, dimension(bs:bf-1) :: c
80 integer :: i
81
82 SOL=RHS
83 do i=bs, bf-1
84 | a(i+1)=TDM(i+1, i)
85 | b(i)=TDM(i, i)
86 | c(i)=TDM(i, i+1)
87 end do
88 b(bf)=TDM(bf,bf)
89 c(bs)=-(c(bs)/b(bs))
90 SOL(bs)=SOL(bs)/b(bs)
91 do i=bs+1, bf-1
92 | c(i)=c(i)-(b(i)-a(i)*c(i-1))
93 | SOL(i)=(SOL(i)-a(i)*SOL(i-1))/(b(i)-a(i)*c(i-1))
94 end do
95 SOL(bf)=(SOL(bf)-a(bf)*SOL(bf-1))/(b(bf)-a(bf)*c(bf-1))
96 do i=bf-1, bs, -1
97 | SOL(i)=SOL(i)-c(i)*SOL(i+1)
98 end do
99 LHS=SOL
100
101 return
102 end subroutine
```

# Python

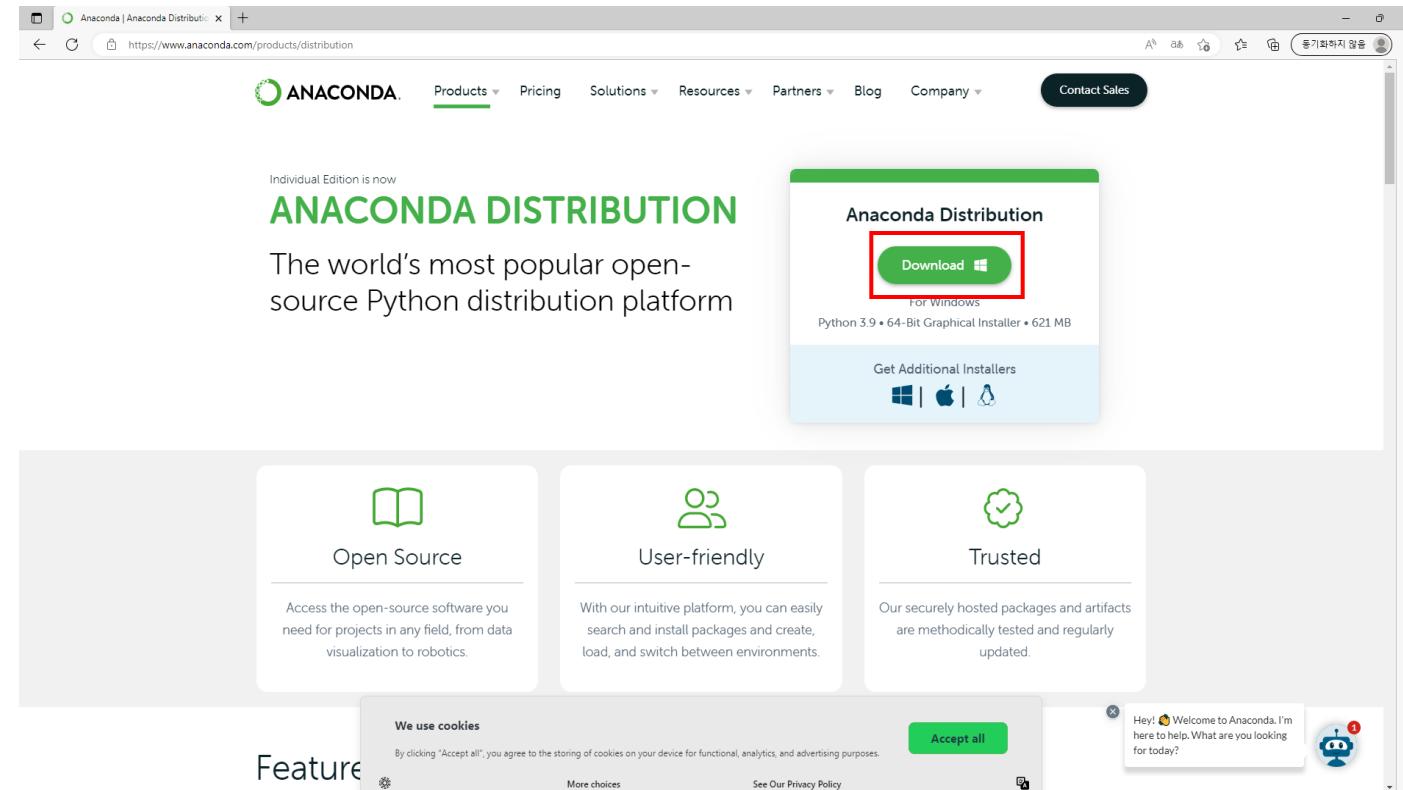
## How to build environment for python

- There are many IDE(Integrated Development Environment) to programming with Python  
→ ex) Jupyter, IDLE, Pycharm, VScode....
- You can use whatever you prefer for your purpose when it comes to IDEs.
- Here, explain how to use Jupyter notebook.

# Python

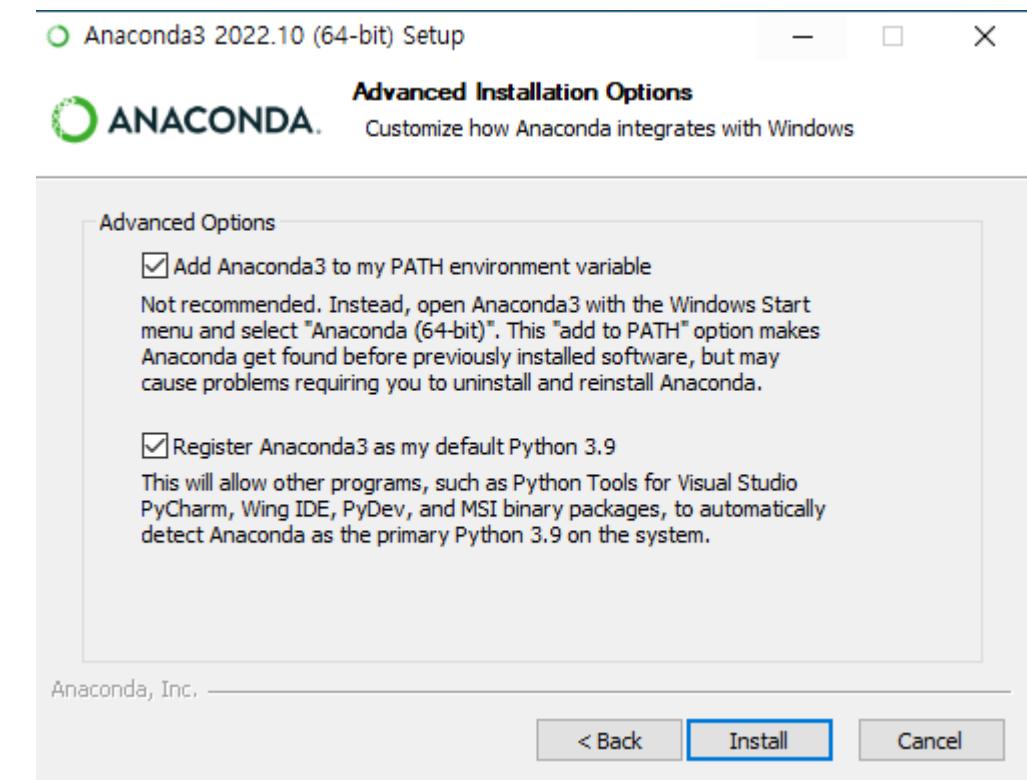
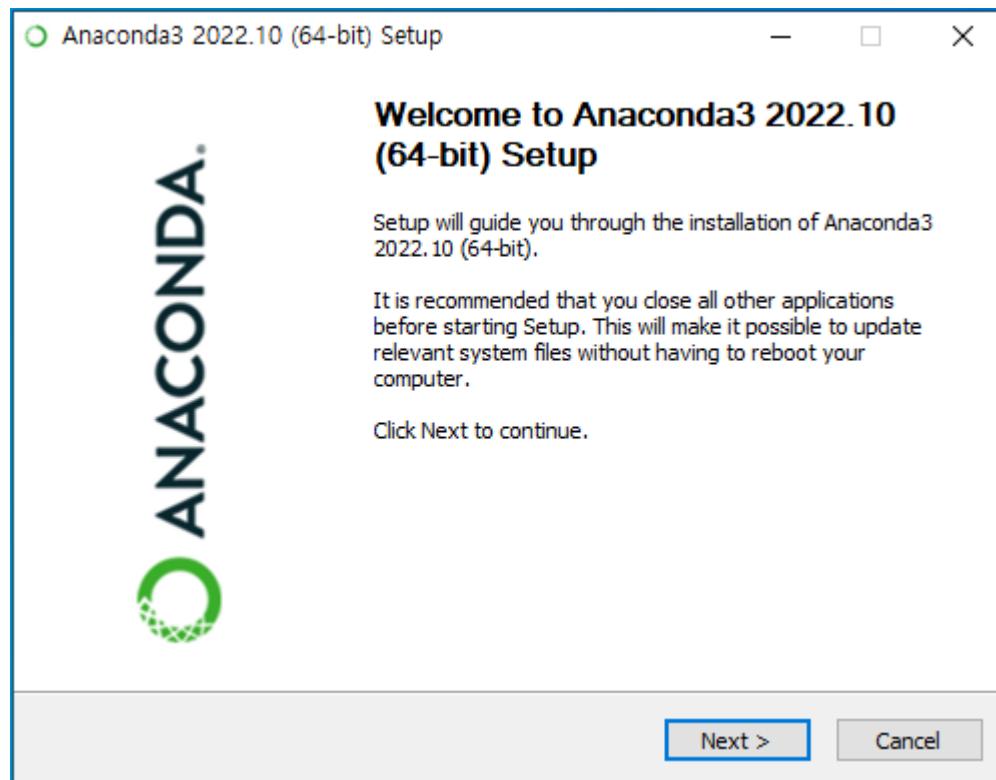
## 1. Download Anaconda3

- Anaconda3 is a distribution of the Python for scientific computing, that aims to simplify package management and deployment.
- <https://www.anaconda.com/products/distribution>



# Python

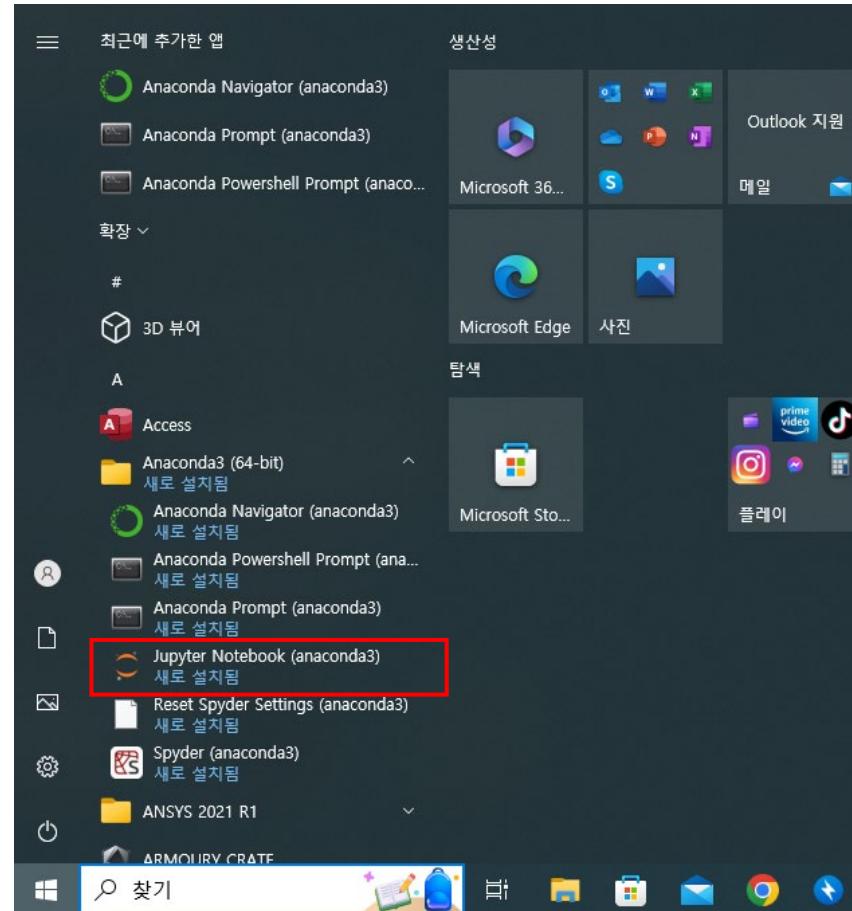
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# Python

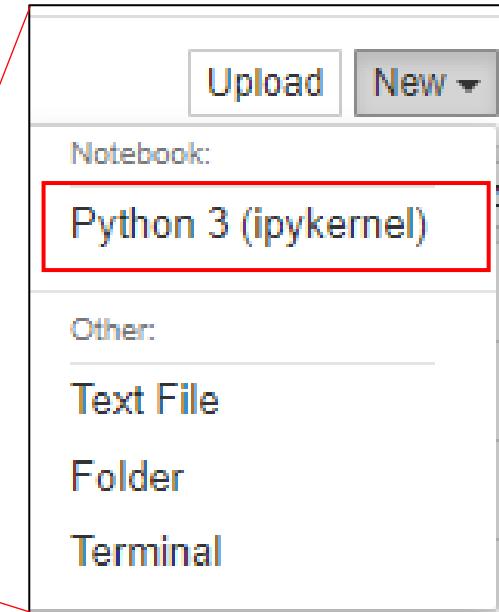
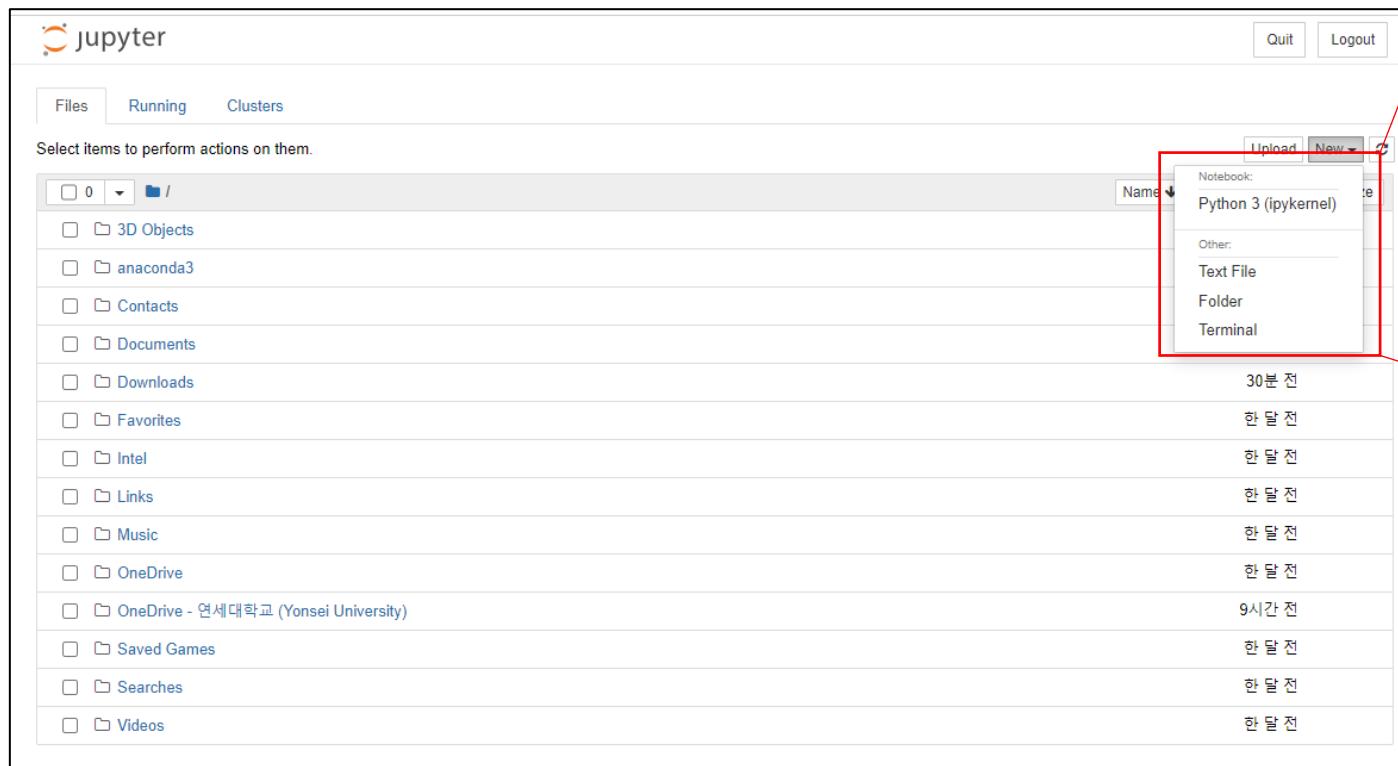
## 1. Download Anaconda3

- If you correctly downloaded Anaconda3, there is Jupyter Notebook in menu.



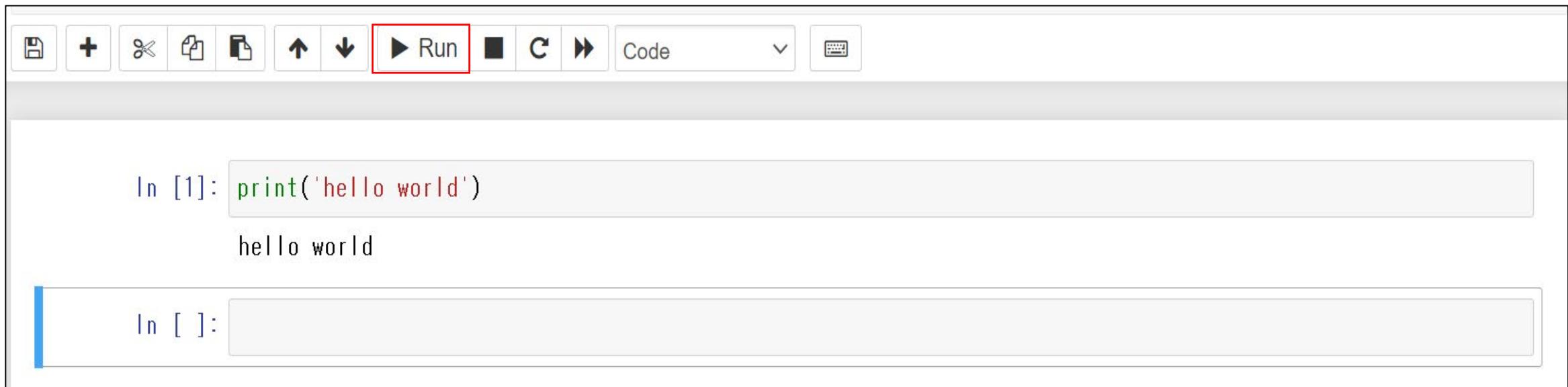
# Python

## 2. Run Jupyter Notebook and create file.



# Python

## 3. Print “hello world”



The screenshot shows a Jupyter Notebook interface. At the top, there is a toolbar with various icons: save, new, cut, copy, paste, up, down, run (which is highlighted with a red box), cell, code, and keyboard. Below the toolbar, the code cell In [1] contains the Python command `print('hello world')`. When the cell was run, the output was "hello world". A new code cell, In [ ], is currently selected and ready for input.

```
In [1]: print('hello world')
hello world
In [ ]:
```

**Q&A** *Thanks for listening*

