Deep Learning with TensorFlow

Machine learning frameworks like TensorFlow, PaddlePaddle, Torch, Caffe, Keras, and many others can speed up our machine learning development significantly. Programing frameworks can not only shorten our coding time, but sometimes also perform optimizations that speed up the code.

In this notebook, we will build a standard L-layer deep neural network from scratch using TensorFlow.

The network consists of L layers (including the input layer). The last layer uses softmax activation, while the others use ReLU activation.

The training dataset is split into **mini batches**, which seeks to find a balance between stochastic gradient descent and batch gradient descent.

Xavier initialization method is used.

Two **regularization** techniques are implemented: inverted dropout and L2 regularization.

Two **optimization** algorithms are applied: gradient descent and Adam.

The constructed model is then applied to "Sign Language" project as an illustration.

```
In [1]: %load_ext autoreload
%autoreload 2
%matplotlib inline

import warnings
warnings.filterwarnings("ignore")
import math
import numpy as np
import tensorflow as tf
import matplotlib.pyplot as plt
from tensorflow.python.framework import ops
import h5py

plt.rcParams['figure.figsize'] = (6.0, 8.0)
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray' # set colormap
```

Part I: Build Deep Neural Network

1. Introduction

We are going to build a tensorflow model using a softmax output.

The model is LINEAR -> RELU -> LINEAR -> RELU ...-> LINEAR -> SOFTMAX. A SOFTMAX layer generalizes SIGMOID to when there are more than two classes.

Note:

- Tensorflow is a programming framework used in deep learning
- The two main object classes in tensorflow are **Tensors and Operators**.
- When we code in tensorflow we have to take the following steps:
 - Create a graph containing Tensors (Variables, Placeholders ...) and Operations (tf.matmul, tf.add, ...)
 - Create a session
 - Initialize the session
 - Run the session to execute the graph
- We can execute the graph multiple times
- The backpropagation and optimization is automatically done when running the session on the "optimizer" object.

2. Create Placeholders for Data

Create placeholders for X and Y. This will allow us to later pass our training data in when we run our session.

A placeholder is an object whose value we can specify only later.

To specify values for a placeholder, we can pass in values by using a "feed dictionary" (feed_dict variable). This allows us to pass in a number later when we run the session. We say that we feed data to these placeholders when running the session.

Here's what's happening: When we specify the operations needed for a computation, we are telling TensorFlow how to construct a computation graph. The computation graph can have some placeholders whose values we will specify only later. Finally, when we run the session, we are telling TensorFlow to execute the computation graph.

```
In [2]: def create_data_placeholders(n_x, n_y):
    """
    Create placeholders for the data

Arguments:
    n_x: scalar, number of the input features
    n_y: scalar, number of the output classes

Returns:
    X: placeholder for the input data, with the shape [n_x, None] and dtype 'float'
    Y: placeholder for the input labels, with the shape [n_y, None] and dtype 'float'

Note that we use None in the shape because it lets us be flexible on the number of examples.

X = tf.placeholder(tf.float32, shape = [n_x, None])
    Y = tf.placeholder(tf.float32, shape = [n_y, None])
    return X, Y
```

3. Split Data into Mini Batches

```
In [3]: # create mini batches randomly, each with the size of mini_batch_size.
        def random mini batches(X, Y, mini batch size, seed = 0):
            Argument:
            X: input features, with dimension of (number of features, number of training examples)
            Y: true labels, the actual y values, with the dimension of (1, number of training examples)
            mini batch size: size of each mini batch.
            seed: random seed
            Returns:
            mini batches: list of (mini batch X, mini batch Y)
            np.random.seed(seed)
            m = X.shape[1] # total number of examples
            mini batches = []
            # for batch gradient descent, no need to shuffle
            if mini batch size == X.shape[1]:
                mini batch = (X, Y)
                mini batches.append(mini batch)
                return mini_batches
            # Step 1: shuffle
            permutation indices = list(np.random.permutation(m))
            shuffled X = X[:, permutation indices]
            shuffled Y = Y[:, permutation indices]
            # Step 2: partition
            num batch except last = math.floor(m / mini batch size)
            for i in range(num_batch_except_last):
                mini batch X = shuffled X[:, i * mini batch size:(i + 1) * mini batch size - 1]
                mini batch Y = shuffled Y[:, i * mini batch size:(i + 1) * mini batch size - 1]
                mini batches.append((mini batch X, mini batch Y))
            # Last mini batch
            if m % mini batch size != 0:
                mini_batch_X = shuffled_X[:, num_batch_except_last * mini_batch_size:]
                mini_batch_Y = shuffled_Y[:, num_batch_except_last * mini_batch_size:]
                mini batches.append((mini batch X, mini batch Y))
            return mini batches
```

4. Initialize the Parameters

Initialize the parameters, i.e., the weight matrices W and bias vectors b.

We use Xavier Initialization for weights and Zero Initialization for biases.

```
In [4]: # initialize parameters: weight matrices and bias vectors for each layer
        def init params(layer dims, initialization, seed = 0):
             Arguments:
             layer dims: python array, layer dims[l] is the number of units in the lth layer.
                         l = 0 is the input layer, the last l is the output layer.
             initialization: choose which initialization to use:
                         "xavier": Xavier initialization
             seed: random seed
             Returns:
             params: a dictionary of tensors containing weight matrices wl and bias vectors bl for the lth layer,
                    params['W1'], params['W2'], ..., params['WL'], ..., and params['b1'], params['b2'], ..., params['bl'], ...
                    WL has the dimension of (layer dims[l], layer dims[l - 1])
                     bl has the dimension of (layer dims[l], 1)
             Use random initialization for the weight matrices, and use zero initialization for the biases.
             params = \{\}
             L = len(layer dims) # total number of layers, including the input layer.
             # set the graph-level seed.
             tf.set random seed(seed)
             for 1 in range(1, L):
                 if initialization == "xavier":
                    params['W' + str(l)] = tf.get variable('W' + str(l), shape = (layer dims[l], layer dims[l-1]),
                                                            initializer = tf.contrib.layers.xavier initializer(seed = seed))
                     params['b' + str(l)] = tf.get_variable('b' + str(l), shape = (layer_dims[l], 1),
                                                            initializer = tf.zeros initializer())
             return params
```

5. Forward Propagation

5.1 Without Dropout

We now implement the forward propagation module in tensorflow. The function takes in a dictionary of parameters and completes the forward pass.

It is important to note that the forward propagation stops at z[L]. The reason is that in tensorflow the last linear layer output is given as input to the function computing the loss. Therefore, we don't need a[L]!

```
In [5]: # whole forward propagation of L-layer deep neural network, without dropout
        # The output is z[L] rather than a[L]
        def L layer forward(X, params):
            Arguments:
            X: input features placeholder, with dimension of (number of features, number of examples)
            params: a dictionary of tensors containing weight matrices wl and bias vectors bl for the lth layer,
                    params['W1'], params['W2'], ..., params['Wl'], ..., and params['b1'], params['b2'], ..., params['bl'], ...
                    WL has the dimension of (layer_dims[l], layer_dims[l - 1])
                    bl has the dimension of (layer_dims[l], 1)
            Returns:
            Zout: the linear output of the last layer, with the shape (number of classes, number of examples)
            L = len(params) // 2 + 1 # total number of layers including the input layer
            A prev = X
            # relu activation for the layers except the last one
            for 1 in range(1, L - 1):
                W = params['W' + str(1)]
                b = params['b' + str(1)]
                Z = tf.add(tf.matmul(W, A_prev), b)
                A = tf.nn.relu(Z)
                A prev = A
            # linear output for the last layer
            W = params['W' + str(L - 1)]
            b = params['b' + str(L - 1)]
            Zout = tf.add(tf.matmul(W, A_prev), b)
            return Zout
```

5.2 With Inverted Dropout

```
In [6]: # whole forward propagation of L-layer deep neural network, with inverted dropout
        # The output is z[L] rather than a[L]
        def L layer forward inverted dropout(X, params, drop rate):
            Arguments:
            X: input features placeholder, with dimension of (number of features, number of examples)
            params: a dictionary of tensors containing weight matrices wl and bias vectors bl for the lth layer,
                    params['W1'], params['W2'], ..., params['Wl'], ..., and params['b1'], params['b2'], ..., params['bl'], ...
                    WL has the dimension of (layer_dims[l], layer_dims[l - 1])
                    bl has the dimension of (layer dims[l], 1)
            drop_rate: A scalar Tensor. The probability that each element is discarded.
            Returns:
            Zout: the linear output of the last layer, with the shape (number of classes, number of examples)
            L = len(params) // 2 + 1 # total number of layers including the input layer
            A prev = X
            # relu activation for the layers except the last one
            for 1 in range(1, L - 1):
                W = params['W' + str(1)]
                b = params['b' + str(1)]
                Z = tf.add(tf.matmul(W, A_prev), b)
                A = tf.nn.relu(Z)
                # add dropout
                A = tf.nn.dropout(A, rate = drop rate)
                A prev = A
            # linear output for the last layer
            W = params['W' + str(L - 1)]
            b = params['b' + str(L - 1)]
            Zout = tf.add(tf.matmul(W, A prev), b)
            return Zout
```

6. Calculate Cost

6.1 Cross Entropy Cost

Compute the cross entropy cost.

Note:

- It is important to know that the "logits" and "labels" inputs of tf.nn.softmax_cross_entropy_with_logits_v2 are expected to be of shape (number of examples, number of classes). Thus We have to transpose Zout and Y.
- The returned shape of tf.nn.softmax_cross_entropy_with_logits_v2 is the same as labels except that it does not have the last dimension of labels. tf.reduce_mean basically does the mean over the examples.

6.2 L2 Regularization

```
In [8]: # calculate the cost function with L2 regularization
        def cost func L2 regul(Zout, Y, lambd, params, m):
            Arguments:
            Zout: the linear output of the last layer, with the shape (number of classes, number of examples)
            Y: true labels placeholder, the actual y values, with the dimension of (number of classes, number of examples)
            params: a dictionary of tensors containing weight matrices wl and bias vectors bl for the lth layer,
                    params['W1'], params['W2'], ..., params['Wl'], ..., and params['b1'], params['b2'], ..., params['bl'], ...
            lambd: the lambda parameter for L2 regularization
            m: number of examples
            Returns:
            cost: the cross-entropy cost tensor, with L2 regularization term
            L = len(params) // 2 + 1
            cross_entropy_cost = cost_func(Zout, Y)
            regularizer = 0
            for 1 in range(1, L):
                regularizer += tf.nn.12_loss(params['W' + str(1)])
            regularizer *= lambd / m
            cost = cross_entropy_cost + regularizer
            return cost
```

7. Backward Propagation

This is where we become grateful to programming frameworks. All the backpropagation and the parameters update is taken care of in 1 line of code. It is very easy to incorporate this line in the model.

After we compute the cost function, we create an "optimizer "object. We have to call this object along with the cost when running the tf.session. When called, it will perform an optimization on the given cost with the chosen method and learning rate.

For instance, for gradient descent the optimizer would be:

```
optimizer = tf.train.GradientDescentOptimizer(learning_rate = learning_rate).minimize(cost)
```

To make the optimization we would do:

```
_ , c = sess.run([optimizer, cost], feed_dict={X: minibatch_X, Y: minibatch_Y})
```

This computes the backpropagation by passing through the tensorflow graph in the reverse order, from cost to inputs.

Note: when coding, we often use _ as a "throwaway" variable to store values that we won't need to use later. Here, _ takes on the evaluated value of optimizer, which we don't need (and c takes the value of the cost variable).

8. Complete Model

Writing and running programs in TensorFlow has the following steps:

- 1. Create Tensors (variables) that are not yet executed/evaluated.
- 2. Write operations between those Tensors.
- 3. Initialize our Tensors.
- 4. Create a Session.
- 5. Run the Session. This will run the operations we have written above.

When we create a variable for the cost, we simply define the cost as a function of other quantities, but have not evaluated its value. To evaluate it, we have to run init=tf.global_variables_initializer(), which initializes the cost variable.

remember to initialize our variables, create a session and run the operations inside the session.

Note that there are two typical ways to create and use sessions in tensorflow:

Method 1:

```
sess = tf.Session()
# Run the variables initialization (if needed), run the operations
result = sess.run(..., feed_dict = {...})
sess.close() # Close the session
```

Method 2:

```
with tf.Session() as sess:
    # run the variables initialization (if needed), run the operations
    result = sess.run(..., feed_dict = {...})
# This takes care of closing the session
```

```
In [9]: # Build the L-layer deep neural network model
        def L layer model(train X, train Y, test X, test Y, layer dims, params seed = 0, mini batch size = None,
                          optimizer = "adam", learning rate = 0.0001, beta1 = 0.9, beta2 = 0.999, epsilon = 1e-8,
                          epochs = 1500, print cost freq = 0, save cost freq = 100, initialization = "xavier",
                          regularization = "none", lambd = 0, drop rate = 0):
            Arguments:
            train X: training set features, with the dimension of (number of features, number of training examples)
            train Y: training set labels, with the dimension of (number of classes, number of training examples)
            test X: training set features, with the dimension of (number of features, number of test examples)
            test Y: training set labels, with the dimension of (number of classes, number of test examples)
            layer dims: python array, layer dims[l] is the number of units in the lth layer.
                        l = 0 is the input layer, the last l is the output layer (i.e., number of classes)
            params seed: random seed for parameter initialization.
            mini batch size: size of each mini batch. By default it is the total number of examples, i.e., batch gradient descent
            optimizer: choose the optimization method:
                       "qd": qradient descent
                       "adam": Adam optimization
            learning_rate: learning rate for gradient descent
            beta1, beta2: hyperparameters for Adam optimization
            epsilon: hyperparameter preventing division by zero in Adam updates
            epochs: number of epochs
            print cost freq: if > 0, print the cost value every print cost freq epochs.
            save cost freq: save the cost value every save cost freq epochs into costs, for ploting the learning curve.
            initialization: choose which initialization to use:
                         "xavier": Xavier initialization
            regularization: choose the regularization method:
                        "none": no regularization
                        "L2": L2 regularization
            lambd: the lambda parameter for L2 regularization
            drop rate: parameter for inverted dropout, the probability of dropping a neuron. If it's 0, dropout is not used.
            Returns:
            params: python dictionary containing weight matrix wl and bias vector bl for the lth layer,
                    params['W1'], params['W2'], ..., params['Wl'], ..., and params['b1'], params['b2'], ..., params['bl'], ...
                    WL has the dimension of (layer dims[l], layer dims[l - 1]).
                    bl has the dimension of (layer dims[l], 1)
            assert(drop rate <= 1 and drop rate >= 0)
            ops.reset default graph() # to be able to rerun the model without overwriting tf variables
```

```
costs = []
tf.set random seed(1)
minibatch seed = 3 # random seed for creating mini batches
m = train_X.shape[1] # number of training examples
if mini_batch_size is None:
    mini batch size = m
num_mini_batches = math.ceil(m / mini_batch_size) # number of mini batches
# create placeholders for data
n x = train X.shape[0]
n y = train Y.shape[0]
X, Y = create_data_placeholders(n_x, n_y)
# initialization
params = init params(layer dims, initialization, params seed)
# forward propagation:
if drop rate > 0:
    drop_rate_placeholder = tf.placeholder("float")
    Zout = L_layer_forward_inverted_dropout(X, params, drop_rate_placeholder)
else:
    Zout = L layer forward(X, params)
# calculate the cost
if regularization == "L2":
    cost = cost_func_L2_regul(Zout, Y, lambd, params, mini_batch_size)
else:
    cost = cost func(Zout, Y)
# backward propagation: define the tensorflow optimizer
if optimizer == "gd":
    opt = tf.train.GradientDescentOptimizer(learning rate = learning rate).minimize(cost)
if optimizer == "adam":
    opt = tf.train.AdamOptimizer(learning rate = learning rate, beta1 = beta1, beta2 = beta2,
                                 epsilon = epsilon).minimize(cost)
# initialize all variables
init = tf.global variables initializer()
# start a session to compute the tensorflow graph
with tf.Session() as sess:
    # run initializer
    sess.run(init)
```

```
for i in range(1, epochs + 1):
    # define a cost related to an epoch, as the average cost over all mini batches within a single epoch
    epoch cost = 0
   # create mini batches
    minibatch seed += 1
   mini batches = random_mini_batches(train_X, train_Y, mini_batch_size, minibatch_seed)
   for mini batch in mini batches:
        (mini_batch_X, mini_batch_Y) = mini_batch
       # run the graph on a mini batch
       # run the session to excute the optimizer and the cost.
       if drop rate > 0:
            _, mini_batch_cost = sess.run([opt, cost], feed_dict = {X : mini_batch_X, Y : mini_batch_Y,
                                                                    drop_rate_placeholder : drop_rate})
       else:
            _, mini_batch_cost = sess.run([opt, cost], feed_dict = {X : mini_batch_X, Y : mini batch Y})
        epoch cost += mini batch cost / num mini batches
    # print and save the costs
   if print cost freq > 0 and (i == 1 or i % print cost freq == 0):
        print("current epoch: " + str(i) + ", cost: " + str(epoch cost))
    if save cost freq > 0 and (i == 1 or i % save cost freq == 0):
        costs.append(epoch cost)
# plot the cost
plt.plot(costs)
plt.ylabel('cost')
plt.xlabel('epochs * ' + str(save cost freq))
plt.title('learning rate = ' + str(learning rate))
plt.show()
# save the parameters
params = sess.run(params)
print('Parameters have been trained!')
# evaluate the model accuracy
# do not use dropout for testing
Zout = L layer forward(X, params)
# Get the correct predictions
# for each example (i.e., each column), the maximum Zout corresponds to the predicted class
correct pred = tf.equal(tf.argmax(Zout, axis = 0), tf.argmax(Y, axis = 0)) # shape is (number of examples,)
# calculate the accuracy
```

```
accuracy = tf.reduce_mean(tf.cast(correct_pred, "float"))

print("Training Set Accuracy: " + str(accuracy.eval({X : train_X, Y : train_Y})))
print("Test Set Accuracy: " + str(accuracy.eval({X : test_X, Y : test_Y})))

return params
```

```
In [10]: \# make predictions based on trained parameters and input X
         def predict(params, X):
             Arguments:
             X: input features, with the dimension of (number of features, number of examples)
             params: trained weight matrices and bias vectors of the neural network
             Returns:
             predicted labels for X, with the dimension of (1, number of examples)
             L = len(params) // 2 + 1 # number of layers including the input layer
             x = tf.placeholder("float")
             for 1 in range(1, L):
                 params['W' + str(1)] = tf.convert_to_tensor(params['W' + str(1)])
                 params['b' + str(1)] = tf.convert to tensor(params['b' + str(1)])
             Zout = L_layer_forward(x, params)
             Y pred = tf.argmax(Zout, axis = 0)
             with tf.Session() as sess:
                 Y_pred = sess.run(Y_pred, feed_dict = {x : X})
             Y pred = Y pred.reshape(1, X.shape[1])
             return Y pred
```

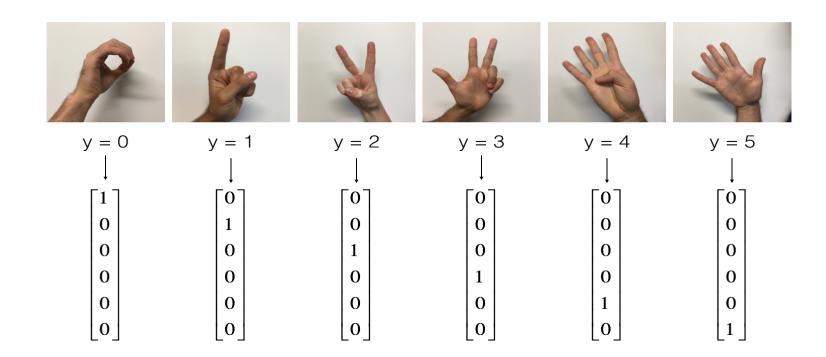
Part II: Example - Sign Language

1. Introduction

One afternoon, we decided to teach our computers to decipher sign language. We spent a few hours taking pictures in front of a white wall and came up with the following dataset:

- Training set: 1080 pictures (64 by 64 pixels) of signs representing numbers from 0 to 5 (180 pictures per number).
- Test set: 120 pictures (64 by 64 pixels) of signs representing numbers from 0 to 5 (20 pictures per number).

Here are examples for each number, and how we represent the labels. These are the original pictures, before we lowered the image resolutoion to 64 by 64 pixels.



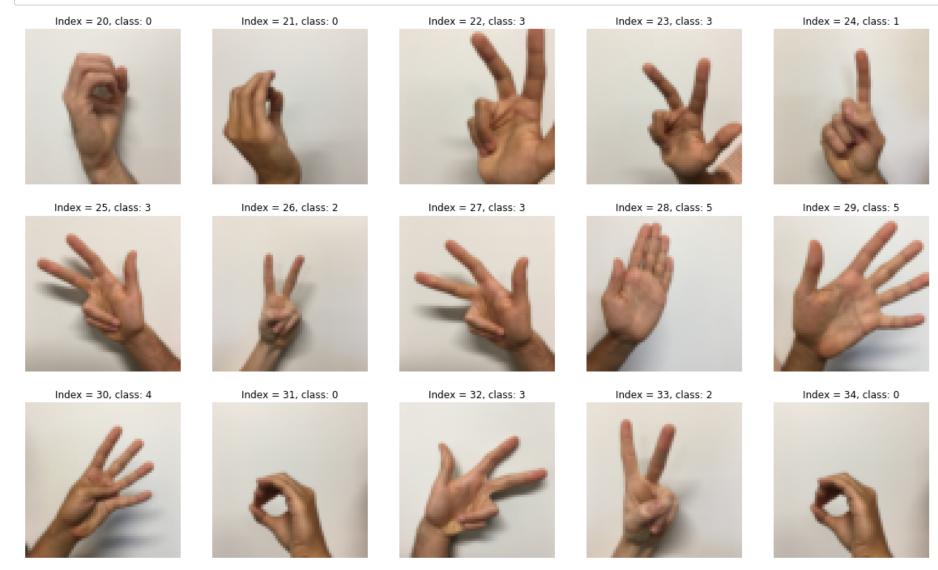
Our goal is to build an algorithm that would facilitate communications from a speech-impaired person to someone who doesn't understand sign language.

2. Load Data

```
In [11]: # Load training and test data, and list of classes
         def load data():
              11 11 11
             Returns:
             train x orig: numpy array, original training set features
             train y orig: numpy array, original training set labels
             test x orig: numpy array, original test set features
             test y orig: numpy array, original test set labels
             classes: numpy array, list of classes
             # training set
             train data = h5py.File('data/train signs.h5', 'r')
             train x orig = np.array(train data['train set x']) # training set features
             train y orig = np.array(train data['train set y']) # training set labels
             # test set
             test data = h5py.File('data/test signs.h5', 'r')
             test x orig = np.array(test data['test set x']) # test set features
             test y orig = np.array(test data['test set y']) # test set labels
             # list of classes
             classes = np.array(test data['list classes'])
             # reshape the labels, make sure the dimension is (1, number of examples)
             train y orig = train y orig.reshape((1, train y orig.shape[0]))
             test y orig = test y orig.reshape((1, test y orig.shape[0]))
             return train x orig, train y orig, test x orig, test y orig, classes
```

```
In [12]: # Load the data
         train x orig, train y orig, test x orig, test y orig, classes = load data()
         print("Total number of training examples: " + str(train x orig.shape[0]))
         print("Total number of test examples: " + str(test x orig.shape[0]))
         print("Size of each image: " + str(train x orig[0].shape))
         print("All classes: " + str(classes))
         print("train x orig shape: " + str(train x orig.shape))
         print("train y orig shape: " + str(train y orig.shape))
         print("test x orig shape: " + str(test x orig.shape))
         print("test y orig shape: " + str(test y orig.shape))
         Total number of training examples: 1080
         Total number of test examples: 120
         Size of each image: (64, 64, 3)
         All classes: [0 1 2 3 4 5]
         train x orig shape: (1080, 64, 64, 3)
         train y orig shape: (1, 1080)
         test x orig shape: (120, 64, 64, 3)
         test y orig shape: (1, 120)
In [13]: # show some examples of the images in the training set
         def example(indices, X, Y, classes):
             Arguments:
             indices: list of the indices of X to be shown
             X: image fearues, with the shape of (number of examples, num px, num px, 3)
             Y: image classes, with the shape of (1, number of examples)
             classes: numpy array, list of classes
             num = len(indices)
             columns = 5 # the number of columns to arrange the figures
             plt.figure(figsize = (20, 12))
             for i in range(num):
                  plt.subplot(math.ceil(num / columns), columns, i + 1)
                  plt.imshow(X[indices[i]])
                  plt.axis('off')
                 plt.title("Index = " + str(indices[i]) + ", class: " + str(classes[Y[0, indices[i]]]))
```

In [14]: indices = [i for i in range(20, 35, 1)]
 example(indices, train_x_orig, train_y_orig, classes)



3. Data Pre-Processing

We flatten the image dataset, then normalize it by dividing by 255. On top of that, we convert each label to a one-hot vector.

One Hot Encoding:

Many times in deep learning we will have a y vector with numbers ranging from 0 to C-1, where C is the number of classes. If C is for example 4, then we might have the following y vector which we will need to convert as follows:

$$y = \begin{bmatrix} 1 & 2 & 3 & 0 & 2 & 1 \end{bmatrix}$$
 is often converted to $\begin{bmatrix} 0 & 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 & 0 \end{bmatrix}$ class = 0 class = 1 class = 2 class = 3

This is called a "one hot" encoding, because in the converted representation exactly one element of each column is "hot" (meaning set to 1). In tensorflow, we can use one line of code:

• tf.one_hot(labels, depth, axis)

```
In [15]: # convert Y to one-hot vectors
          def convert to one hot(Y, C):
              Argument:
              Y: labels, with the dimension of (1, number of examples)
              C: number of classes
              Returns:
              Y converted: one-hot representation of Y, with the dimension of (C, number of examples)
              # numpy.eye() returns a 2-D array with ones on the diagonal and zeros elsewhere.
              # note that its ith column is exactly the one-hot representation of the ith class
              Y converted = np.eye(C)[:, Y.reshape(-1)]
              return Y converted
In [16]: # pre-processing the features
          # convert image features from (num px, num px, 3) to 1-D vector:
         train x = train x orig.reshape(train x orig.shape[0], -1).T
          test x = \text{test } x \text{ orig.reshape(test } x \text{ orig.shape[0], -1).T}
          # standardize, so the values are between 0 and 1.
          train x = train x / 255
          test x = test x / 255
          # convert labels to one-hot vectors
         train y = convert to one hot(train y orig, len(classes))
```

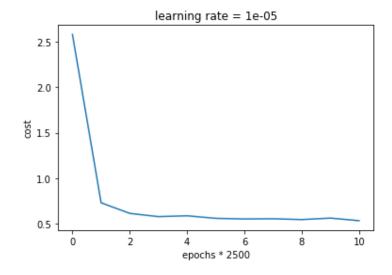
dimension of train_x: (12288, 1080)
dimension of test_x: (12288, 120)
dimension of train_y: (6, 1080)
dimension of test_y: (6, 120)

test y = convert to one hot(test y orig, len(classes))

print("dimension of train_x: " + str(train_x.shape))
print("dimension of test_x: " + str(test_x.shape))
print("dimension of train_y: " + str(train_y.shape))
print("dimension of test y: " + str(test y.shape))

4. Model Training and Evaluation

```
current epoch: 1, cost: 2.583696786095114
current epoch: 5000, cost: 0.6109305024147034
current epoch: 10000, cost: 0.5843909838620354
current epoch: 15000, cost: 0.5493054793161506
current epoch: 20000, cost: 0.542342079036376
current epoch: 25000, cost: 0.5303607758353738
```



Parameters have been trained! Training Set Accuracy: 1.0 Test Set Accuracy: 0.89166665

5. Result Analysis

```
In [19]: # show some mislabeled images
         def mislabeled example(X, Y, predicted Y, classes, max examples):
             Arguments:
             X: input features, numpy array of shape (number of features, number of examples)
             Y: true labels
             predicted Y: predicted labels
             max examples: maximum number of examples to be shown
             columns = 5 # number of columns to arrange the figures
             plt.figure(figsize = (20, 12))
             mislabeled indices = np.asarray(np.where(Y != predicted Y))
             num = min(len(mislabeled_indices[1, :]), max_examples) # determine the number of examples to be shown
             for i in range(num):
                 plt.subplot(math.ceil(num / columns), columns, i + 1)
                 plt.imshow(X[:, mislabeled_indices[1, i]].reshape(64, 64, 3))
                  plt.axis('off')
                 plt.title("predicted class: " + str(classes[int(predicted_Y[0, mislabeled indices[1, i]])]) +
                          "\n actual class: " + str(classes[int(Y[0, mislabeled indices[1, i]])]))
```

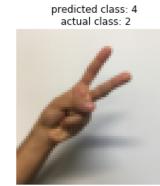
```
In [20]: predicted_Y = predict(params, train_x)
mislabeled_example(train_x, train_y_orig, predicted_Y, classes, 11)
```

<Figure size 1440x864 with 0 Axes>

In [21]: predicted_Y = predict(params, test_x) mislabeled_example(test_x, test_y_orig, predicted_Y, classes, 11)

predicted class: 0 actual class: 3

predicted class: 5 actual class: 4



predicted class: 4 actual class: 5



predicted class: 3 actual class: 5



predicted class: 5 actual class: 4



predicted class: 3 actual class: 1



predicted class: 3 actual class: 4



