Spike-and-Slab Generalized Additive Models and Fast Algorithms for High-Dimensional Data

Boyi Guo and Nengjun Yi

Department of Biostatistics University of Alabama at Birmingham

August 8th, 2021

High Dimensional Generalized Additive Model

- Models that can handle grouped predictors
 - Penalized model with grouped penalty: Lasso, SCAD
 - Bayesian regularized models with grouped prior: spike-and-slab prior
- Overly shrinking due to sparse penalty
- Reduced interpretation due to the "all-in-all-out" functional selection
- Lack of uncertainty measure for penalized models
- Scaling problem for Bayesian regularized models

Bayesian Hierarchical Additive Model

- Re-parameterization of smoothing function design matrix
 - Eigen-decompose the smoothing matrix of a smoothing function
 - Deploy smoothing penalty on the smoothing function
 - ▶ Isolate the linear and polynomial spaces of a smoothing function
- Two-part spike-and-slab lasso prior
 - ▶ Independent SS-Lasso priors of linear and polynomial spaces for sparse solution
 - ► Two latent indicator variables for bi-level selection
 - Hyperpior of latent indicator variables for local adoptation

Optimization Algorithms

- EM algorithms
- Combine with coordinate descent algorithm for fast computating and sparse solution
- Combine with iterative weighted least square for uncertainty measures
 - Accomodate other pirors: Bayesian ridge, lasso priors, spike-and-slab priors

Software Support

- ► R package: BHAM
 - Ancillary functions for setting up high-dimensional spline formulation
 - Model summary and variable selection
 - Curve plotting
 - Covariate adjustment without penalty
 - Website via boyiguo1.github.io/BHAM