Monthly Presentation of Drawdown project

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Overview

1. Maximum drawdown distribution and CED

2. Regime switching models

3. Time Series ARMA model

4. Time Series GARCH model

5. Current work: simulation

Maximum drawdown distribution

As we move to longer period, the maximum drawdown distribution tends to:

1. have larger mean and variance
2. be multi-mode
3. lack variability of values
4. be centered around several specific values

Take RMZ as an example. (RMZ: The MSCI US REIT Index, a free float-adjusted market capitalization index that is comprised of equity REITs.)
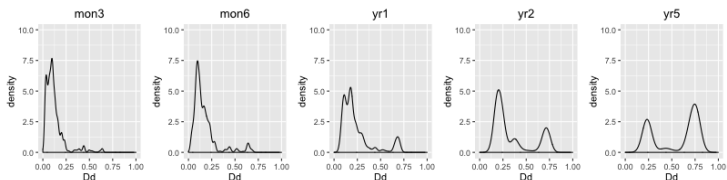

Figure: Maximum drawdown distribution of RMZ as rolling period increases

Later in our project, we mainly use 3 month period.

Maximum drawdown distribution

Maximum drawdown, expected shortfall (ES), value at risk (VaR) and volatility are highly correlated. For our 10 assets of interest, the correlation between the later three are all above 90%. The correlation between maximum drawdown and the later three are weaker with an average around 80%.

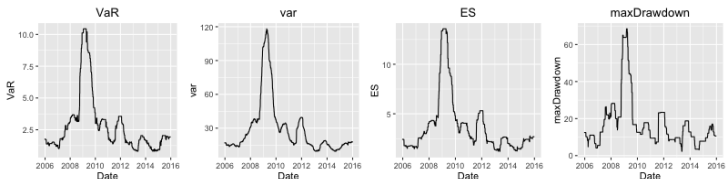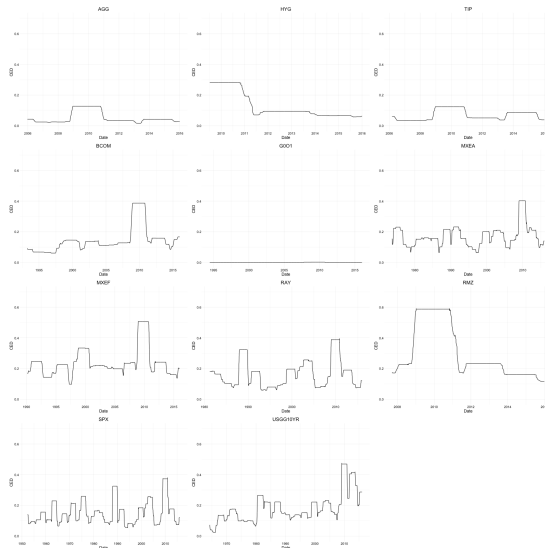The following figure shows the rolling risk measures of RMZ.

Figure: Comparison of different risk measures of RMZ

CED

The right column shows the rolling CED under 3-month-2-year Rolling Window (confidence level = 0.9). That means, the maximum drawdowns are calculated based on a 3-month rolling window and the tail means are calculated based on 2-year maximum drawdowns.

CED

Note that CED is also highly correlated with other risk measures. The following table is calculated based on 2 year and 3 month rolling windows.

Measures	Volatility	VaR	ES
AGG	0.94	0.89	0.95
HYG	0.98	0.97	0.97
TIP	0.77	0.85	0.85
BCOM	0.84	0.89	0.89
MXEA	0.84	0.83	0.86
MXEF	0.91	0.91	0.93
RAY	0.92	0.85	0.92
RMZ	0.96	0.96	0.97
SPX	0.84	0.81	0.84
USGG10YR	0.91	0.93	0.95

Table: Correlation between CED (confidence level = 0.9) and other risk measures

Regime switching models

Many economic time series data tend to behave differently in adjacent time period. We use the following two-regime switching model to fit the returns:

$$y_t - \mu_{s_t^*} = \phi_{s_t^*}(y_{t-1} - \mu_{s_{t-1}^*}) + \epsilon_t \tag{1}$$

where the number of autoregressive coefficient is set to 1. s_t^* is a two state Markov chain. $s_t^* = 1$ represent regime 1 and $s_t^* = 2$ represent regime 2. s_t^* depends on the past only through the most recent values:

$$P(s_t = j | s_{t-1}, s_{t-2}, \dots) = P(s_t = j | s_{t-1}) = p_{ij} \tag{2}$$

| Asset	Regime 1 High volatility	Regime 2 Low volatility
AGG	-0.134	-0.114
HYG	-0.010	0.025
TIP	0.039	-0.026
BCOM	-0.046	0.050
MXEA	0.095	0.109
MXEF	0.221	0.254
RAY	-0.039	0.052
RMZ	-0.244	0.007
SPX	-0.018	0.113
USGG10YR	-0.031	0.082

Regime switching models

Returns of high volatility regime has larger standard deviation, skewness and kurtosis than that of the low volatility regime. The return distribution of high volatility regimes are more like to be sknewed (both positive and negative). They also tend to have fatter tailed than the return distribution of low volatility regimes.

Asset	Volatility		Skewness		Kurtosis	
	Regime 1	Regime 2	Regime 1	Regime 2	Regime 1	Regime 2
AGG	0.141	0.036	-1.59	0.01	17.15	0.60
HYG	0.265	0.055	0.60	0.00	8.76	0.83
TIP	0.113	0.049	0.18	-0.06	2.50	0.16
BCOM	0.205	0.096	-0.25	-0.04	1.92	0.28
MXEA	0.253	0.101	-0.14	-0.02	4.26	0.25
MXEF	0.303	0.119	-0.08	-0.06	2.39	0.38
RAY	0.307	0.114	-0.39	-0.06	6.43	0.55
RMZ	0.661	0.159	0.29	-0.15	2.92	0.79
SPX	0.260	0.099	-0.43	-0.02	9.11	0.56
USGG10YR	0.314	0.098	0.09	-0.05	2.67	1.17

Table: Summary statistics of two regimes for various assets

Regime switching models–Example: RMZ

The right panel shows the regime plot
of RMZ returns and its smoothed
probabilities. The regime switching
model seperate the 2008 financial
crisis as high volatilty regimes. The
number of trading days of high and
low volatility regime is 699 and 1954
seperately.
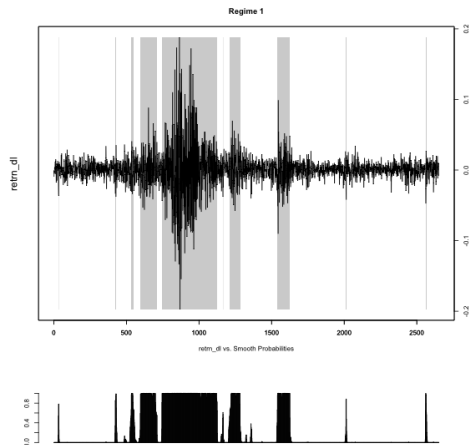
Regime switching models–Example: RMZ

In order to make a consistent comparison of risk diagnostics between two regimes, we ignore some short discontinuity and pick two longest single occurring episode for each regime. Both episode contain 530 trading days. The episode of regime 1 range from 10/30/2007 to 12/07/2009, and the episode of regime 2 range from 06/20/2013 to 07/29/2015. The right panel shows risk measures of two regimes.
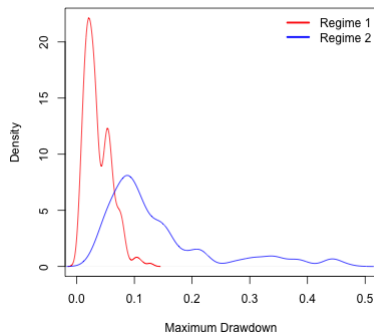
	Regime 1 High volatility	Regime 2 Low volatility
VaR (empirical, p $= 0.95$)	7.4%	1.5%
ES (empirical, p $= 0.95$)	9.9%	2.1%
CED (one-month, p $= 0.9$)	38.4%	8.4%
Serial correlation (order $= 1$)	-0.257	-0.026
Serial correlation (order $= 2$)	-0.023	0.008

Table: Risk diagnostics for RMZ of two equal-length episode of each regime
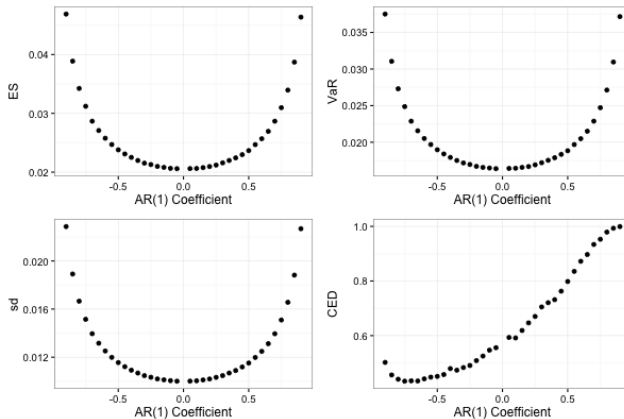
Regime switching models–Example: RMZ

The right panel shows the maximum drawdown distributions of two regimes. The regime with high volatility has larger mean, variance, skewness and kurtosis.

Density of maximum drawdown distribution of two regim

Simulation of AR(1) model

The End