

WR# 14

E:

- 4: (b, h) ① ✓
- 4: (d, g) ② ✓
- 5: (a, c) ③ ✓
- 7: (b, g) ④ ✓
- 8: (a, h) ⑤ ✓
- 9: (b, c) ✗
- 10: (c, d) ✗
- 11: (g, h) ✗
- 12: (a, b) ✗
- 12: (d, e) ⑥ ✓
- 14: (c, e) ✗
- 18: (f, h) ⑦ ✓
- 19: (d, f) ✗

CC:

- {a}
- {b}
- {c}
- {d}
- {e}
- {f}
- {g}
- {h}

①

- {a}
- {b, h}
- {c}
- {d}
- {e}
- {f}
- {g}

②

- {a}
- {b, h}
- {c}
- {d, g}
- {e}
- {f}

③

- {a, c}
- {b, h}
- {d, g}
- {e}
- {f}

④

- {a, c}
- {b, h, d, g}
- {e}
- {f}

⑤

- {a, c, b, h, d, g}
- {e}
- {f}

⑥

- {a, c, b, h, d, g, e}
- {f}

⑦

- {a, c, b, h, d, g, e, f}

— A
— rank

Tree-Based Union-Find

After initialization.



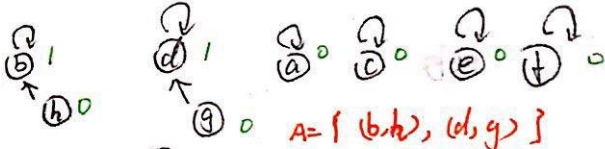
① (b, h)

b → rank = 0
h → rank = 0
we have



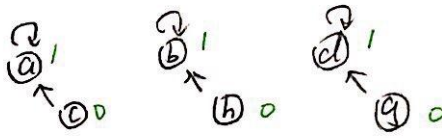
② (d, g)

d → rank = 0
g → rank = 0
we have



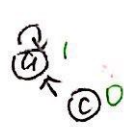
③ (a, c)

a → rank = 0
c → rank = 0



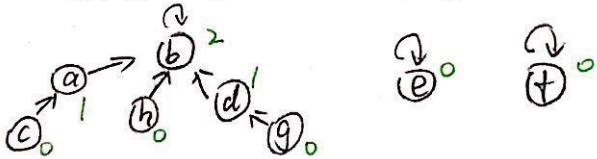
④ (b, g)

b → rank = 1 = d → rank = 1



⑤ (a, h)

a → rank = 1 < b → rank = 2



A = {b, h}, {d, g}, {a, c}, {b, g}, {a, h}

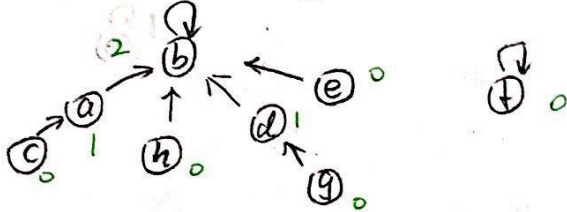
$$(b, c) \quad \text{find}(c(b)) = \text{find}(c(c)) \Rightarrow (b)$$

$$(c, d) \quad \text{find}(c(c)) = \text{find}(c(d)) \Rightarrow (b)$$

$$(g, h) \quad \text{find}(c(g)) = \text{find}(c(h)) \Rightarrow (b)$$

$$(a, b) \quad \text{find}(c(a)) = \text{find}(c(b)) \Rightarrow (b)$$

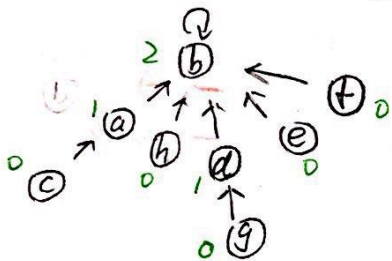
$$⑥ (d, e) \quad ⑥ \rightarrow \text{rank} = 2 > ⑤ \rightarrow \text{rank} = 0$$



$$A = \{(b, h), (d, g), (a, c), (b, g), (a, h), (d, e)\}$$

$$(c, e) \quad \text{find}(c(c)) = \text{find}(c(e)) \Rightarrow (b)$$

$$⑦ (f, h) \quad ⑦ \rightarrow \text{rank} = 0 < ⑥ \rightarrow \text{rank} = 2$$



$$A = \{(b, h), (d, g), (a, c), (b, g), (a, h), (d, e), (f, h)\}$$

$$\Rightarrow A = \{①, ②, ③, ④, ⑤, ⑥, ⑦\}$$

$$(d, f) \quad \text{find}(c(d)) = \text{find}(c(f)) \Rightarrow (b)$$

