

1.1 Basic questions

1.1.1 find missing number

Find missing number problem can have many different formulas.

First, let's look at find one missing number.

Problem 1.1 *Given an array containing n distinct numbers taken from $0, 1, 2, \dots, n$, find the one that is missing from the array.*

For example, Given $\text{nums} = [0, 1, 3]$ return 2.

In this problem we need to use XOR(\oplus) to prevent the overflow. XOR have some properties:

1. For bit:

(a) $0 \oplus 0 = 0$

(b) $0 \oplus 1 = 1$

(c) $1 \oplus 0 = 1$

(d) $1 \oplus 1 = 0$

2. For numbers

(a) $x \oplus x = 0$

(b) $x \oplus 0 = x$ actually this is the special case for $x \oplus y = z$, then $x \oplus z = y$

(c) $x \oplus y \oplus z = x \oplus z \oplus y = y \oplus x \oplus z$

Thus we only need to do is xor all the numbers in the array with the array of the index. Thus we can find the missing number.