

# 114-1 電工實驗（通信專題）

## IQ Components & Frequency Conversion

Chia-Yi Yeh (葉佳宜)  
[ycyyeh@ntu.edu.tw](mailto:ycyyeh@ntu.edu.tw)

Department of Electrical Engineering  
National Taiwan University

# What is communications?

- Information transfer across space or time

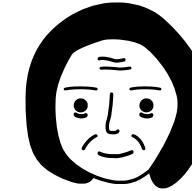
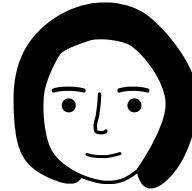
Transmitter



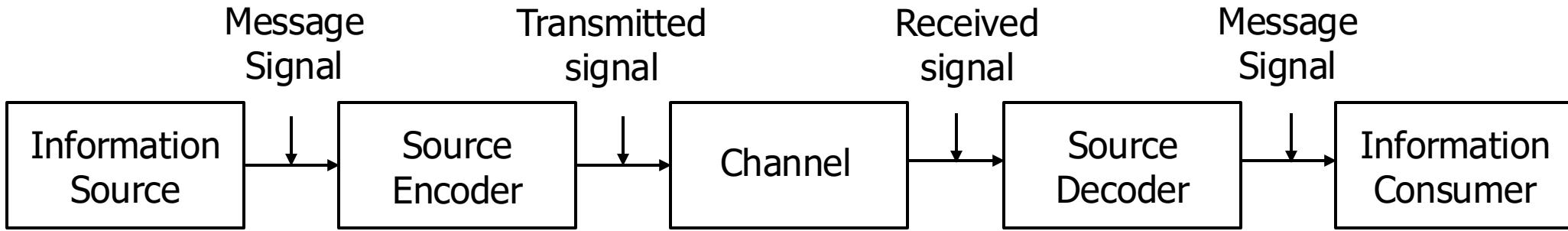
Channel

(air)

Receiver



# Analog vs Digital Communications - Analog

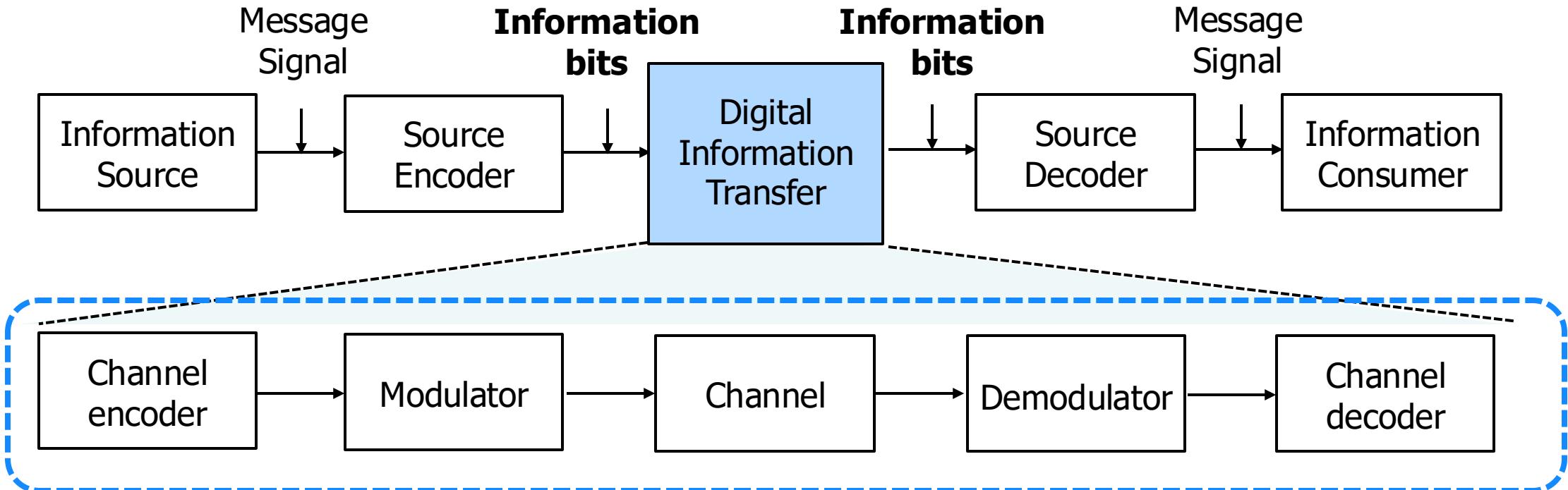


- AM (amplitude modulation) radio, vinyl records, ...

# Analog vs Digital Communications - Digital

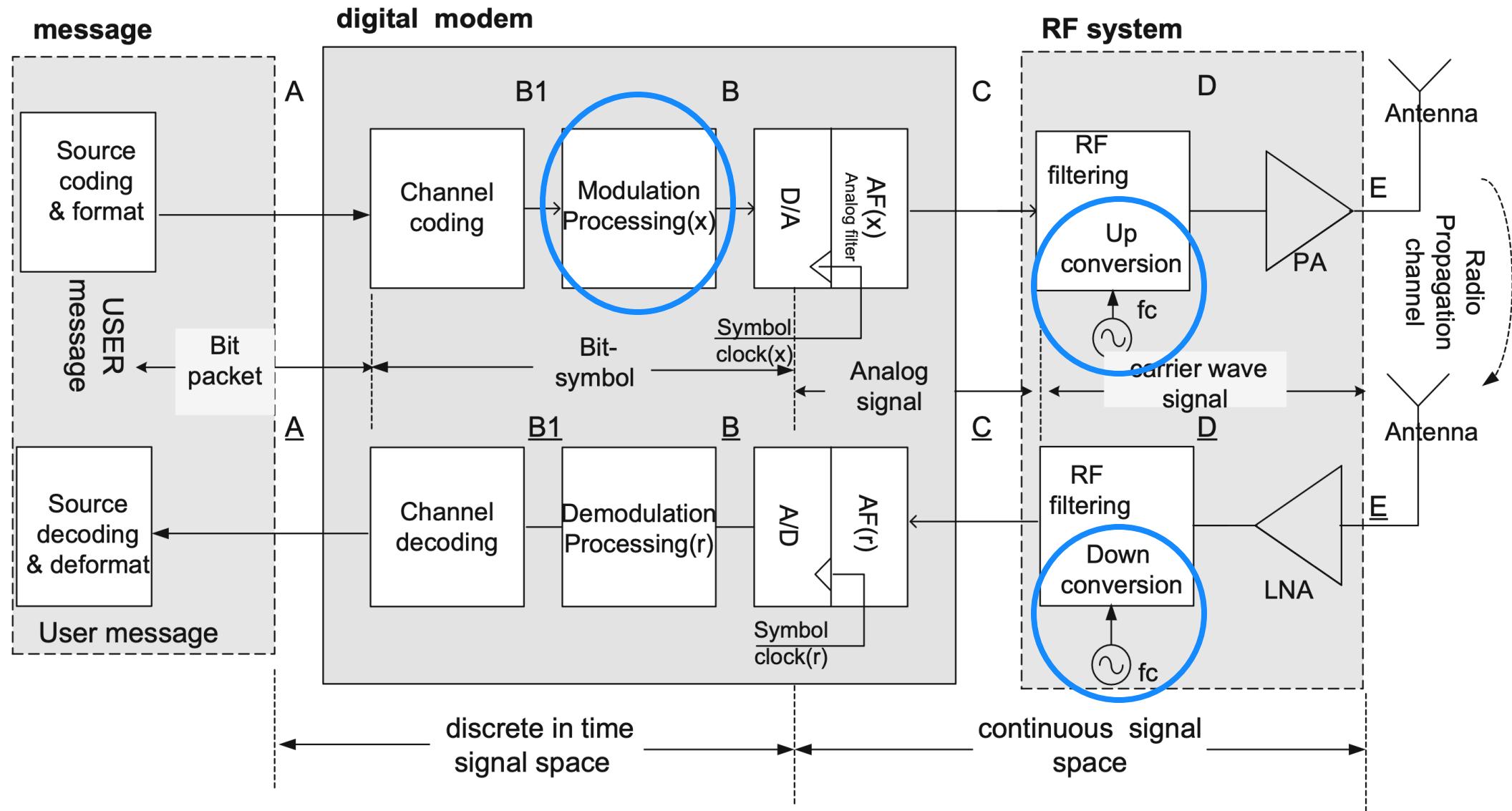
1. Source coding and compression
2. Digital information transfer

**Achieve reliable communications over unreliable channels**



**The focus of this class**

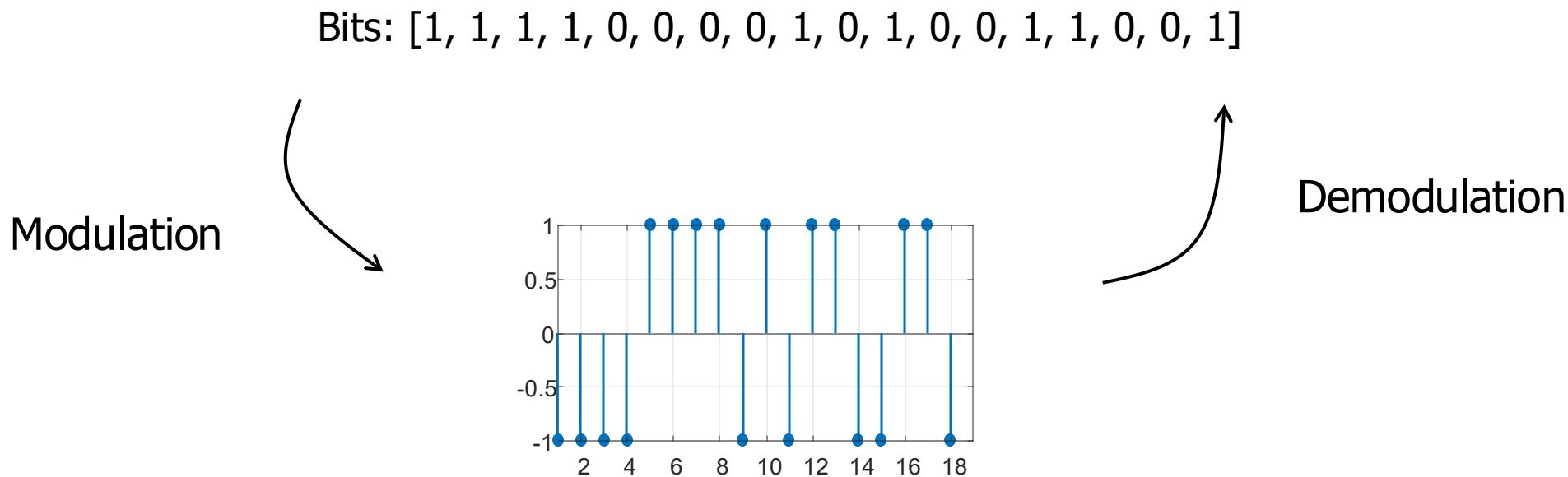
# Digital Radio Communication System Block Diagram



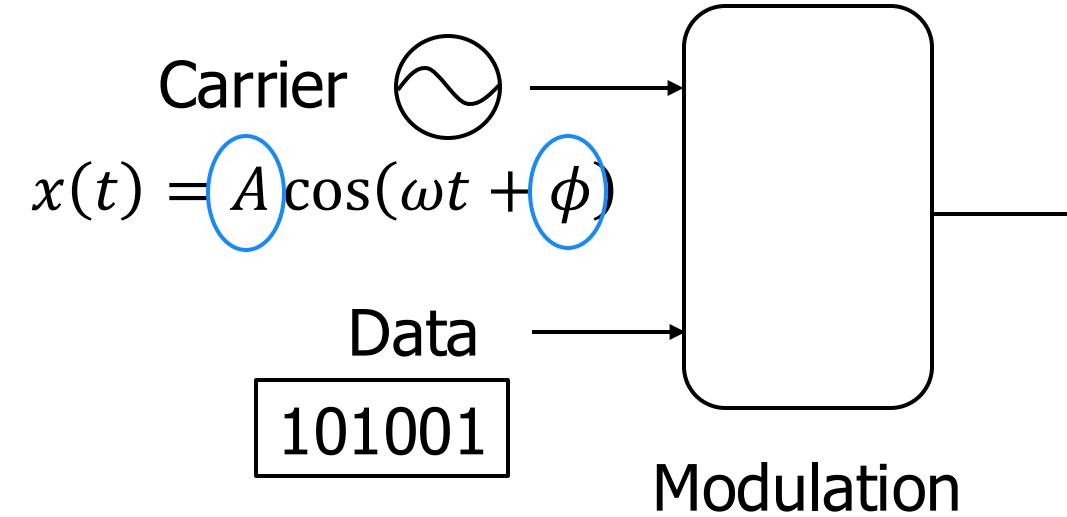
# Modulation with IQ Components

# Modulation & Demodulation

- Modulation: information to signal
- Demodulation: Signal to information



# Modulation in Radio Systems

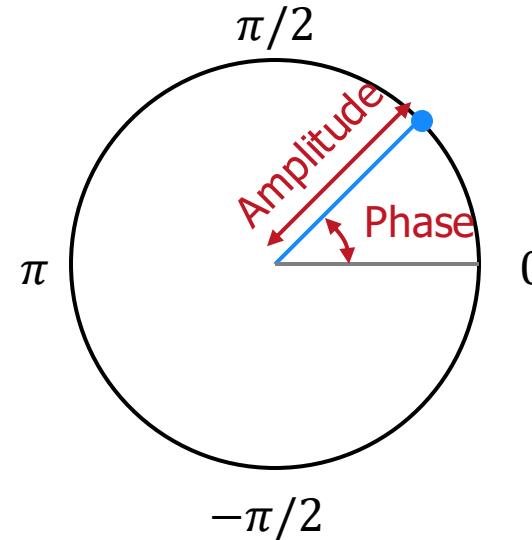


- Overlay data onto carrier signal (sinusoid)
- How? Sinusoids have two very accessible parameters
- Amplitude and Phase

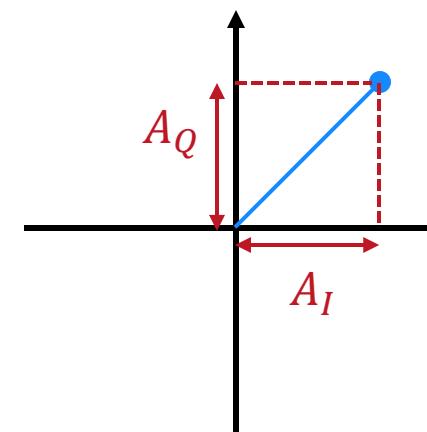
# Signal Representation: Phasor

Polar: Amplitude & Phase

Rectangular: In-phase (I) & Quadrature (Q)



$$x(t) = A \cos(\omega t + \phi)$$

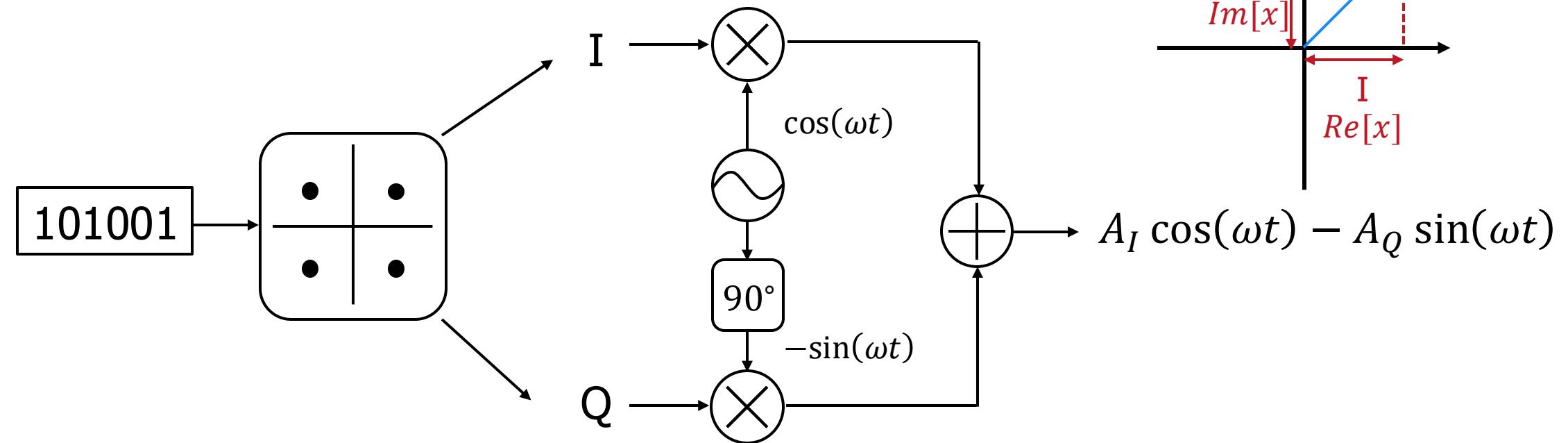


$$x(t) = A_I \cos(\omega t) - A_Q \sin(\omega t)$$

$$A_I = A \cos(\phi), A_Q = A \sin(\phi)$$

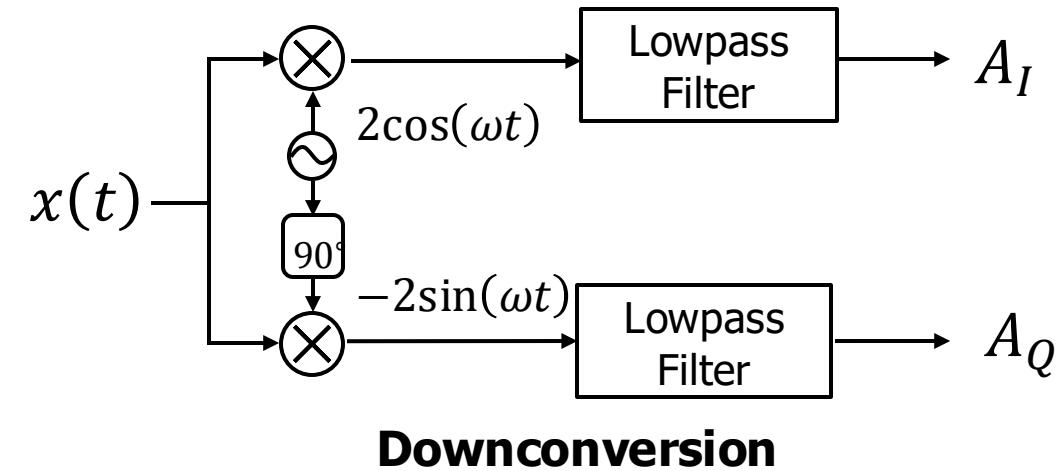
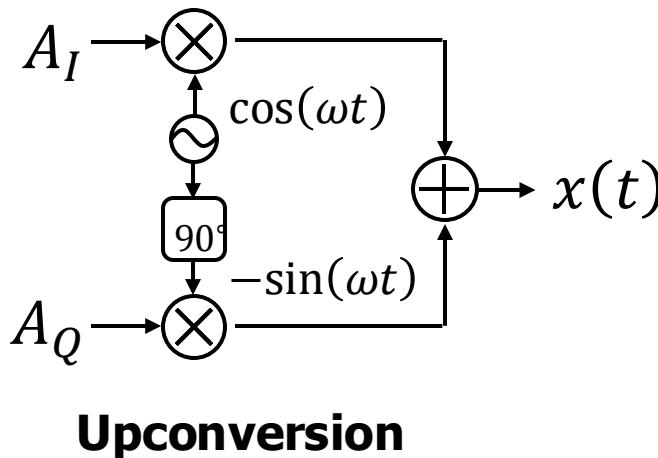
# Signal Representation

Rectangular (I,Q) form enables practical implementation



Modulation = mapping data bits to (I,Q) values

# Note: Get Back $A_I, A_Q$ with Downconversion



# Digital Modulation

## Symbols

Complex modulated values

## Constellation (or Alphabet)

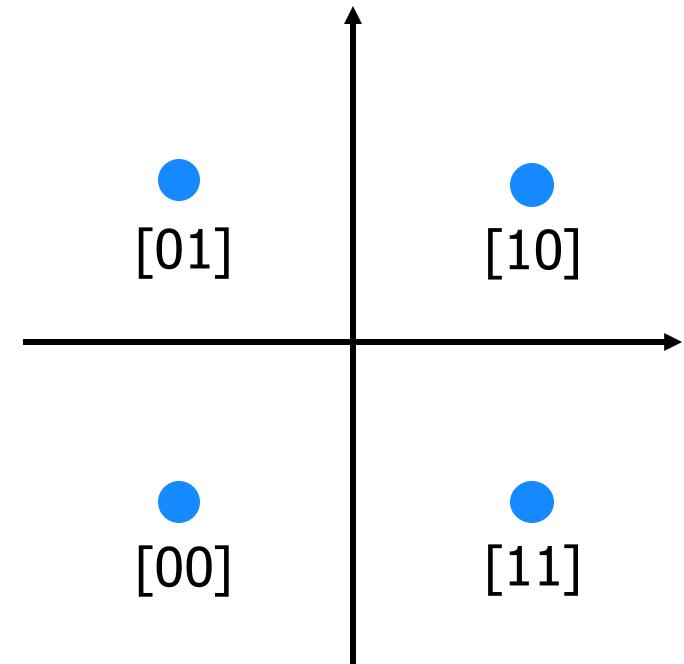
Set of symbols

## Modulation Order

Number of symbols in the constellation,  $M$

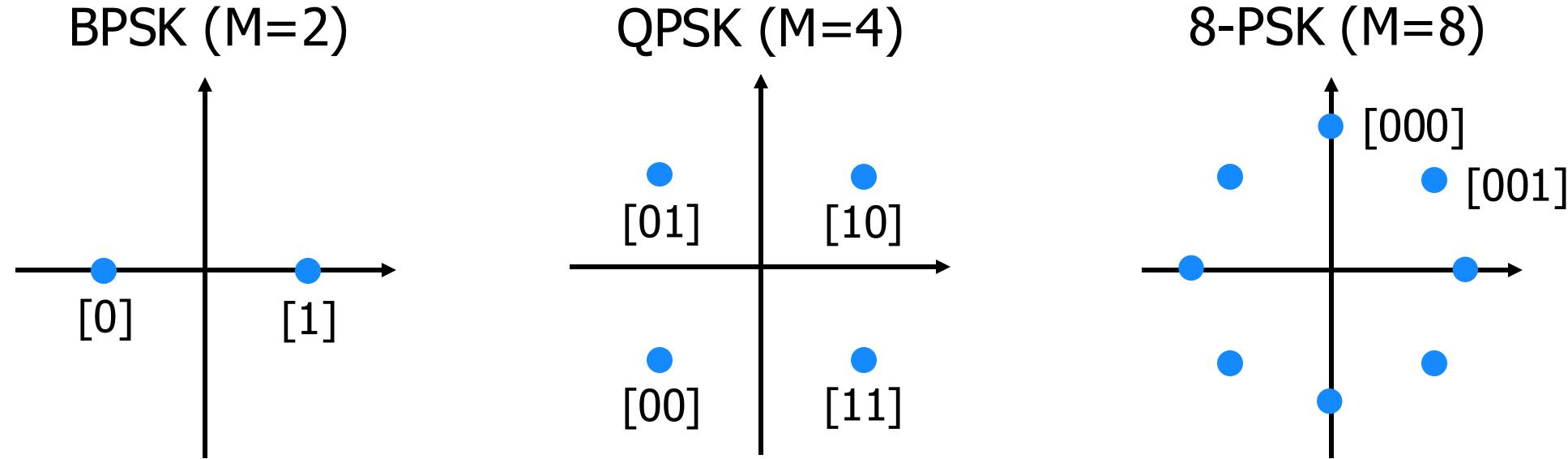
## Bits to Constellation

$M$ -order constellation can encode  $\log_2(M)$  bits per symbol



# Phase Shift Keying (PSK)

Encodes information only in phase



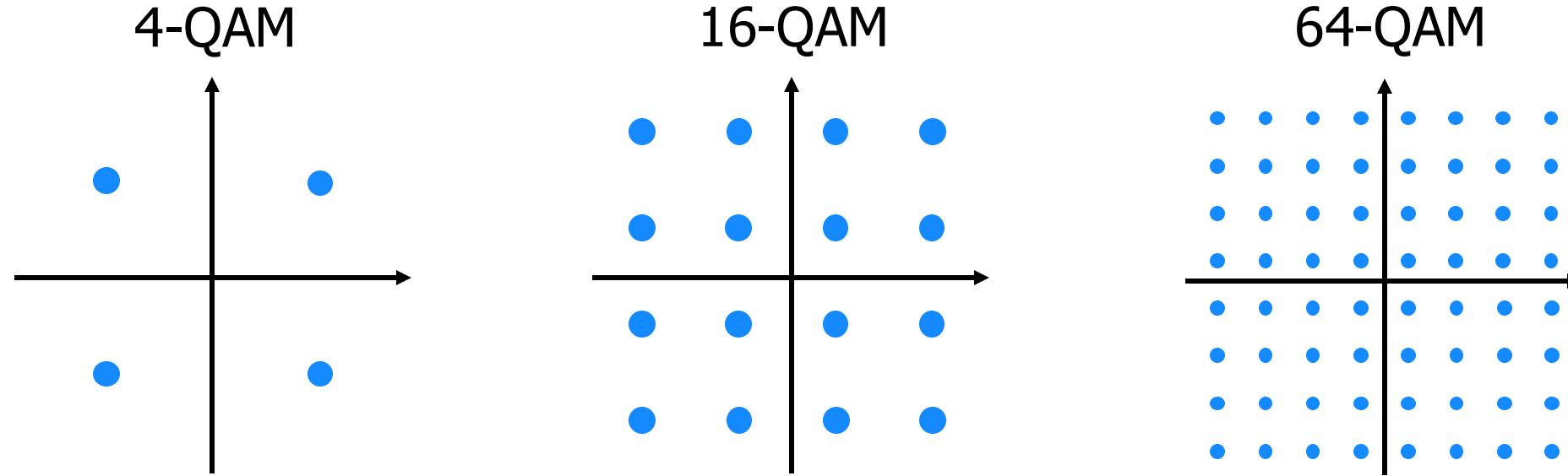
Constant Power envelope

Pros: no need to recover amplitude, no need for linear amplifier

Con: wastes amplitude dimension

# Quadrature Amplitude Modulation (QAM)

Encodes information in both amplitude and phase



Common in wideband systems

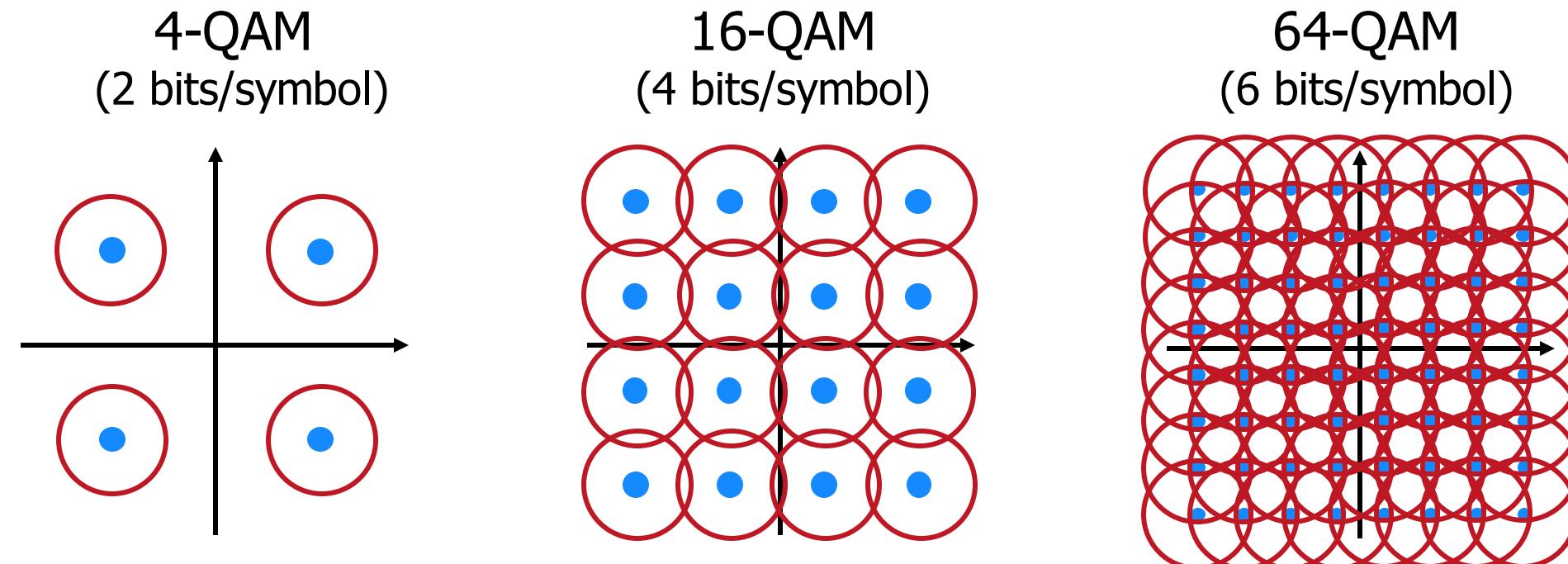
802.11b	802.11g/n	802.11ac
16-QAM	64-QAM	256-QAM

# Tradeoff: Rate vs. Error Probability

By increasing modulation order, M, we get:

More data in the same bandwidth

Lower noise tolerance (i.e., higher error probability)



SNR dictates feasible constellation size

# Signal-to-Noise Ratio (SNR)

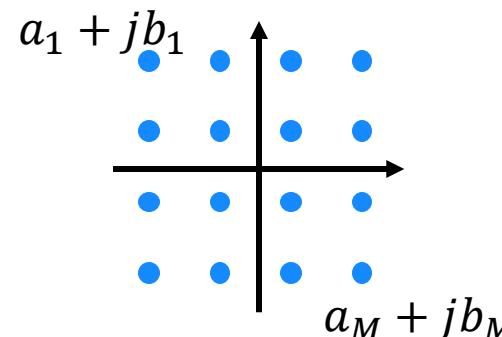
## Energy per symbol

For  $M$ -ary signaling with equal priors

$$E_s = \frac{1}{M} \sum_{m=1}^M \|a_m + jb_m\|^2$$

## Energy per bit

$$E_b = \frac{E_s}{\log_2 M}$$



## Signal-to-Noise Ratio (SNR)

$$SNR = \frac{E[S^2]}{E[N^2]} = \frac{P_{signal}}{P_{noise}}$$

Usually in dB

$$SNR_{dB} = 10 \log_{10} SNR$$

Eb/N0:

SNR normalized by bit (amount of information transferred)

$$\frac{E_b}{N_0} = \frac{SNR}{\log_2 M}$$

# Bit-to-Symbol Mapping

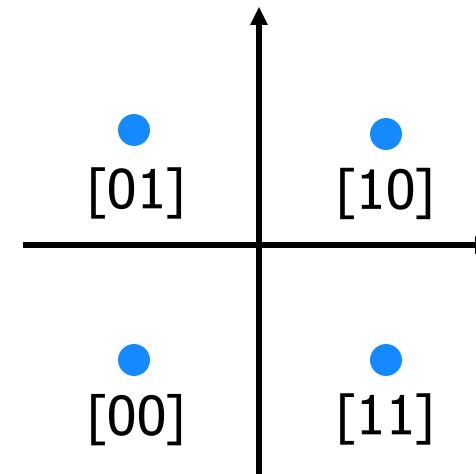
Confusing with neighbors is the most likely error

→ Best to minimize bit-difference between neighbors

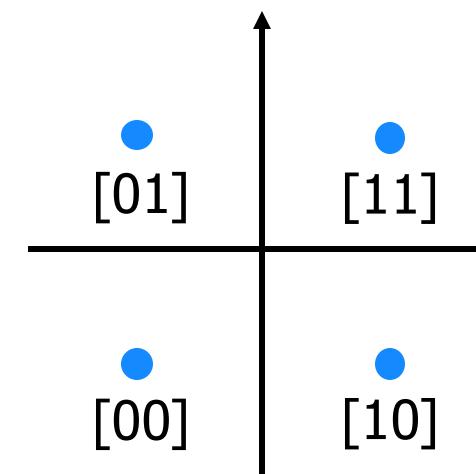
## Gray Coding

Neighboring symbols differ by only one bit

Extra performance at zero cost (this is rare!)



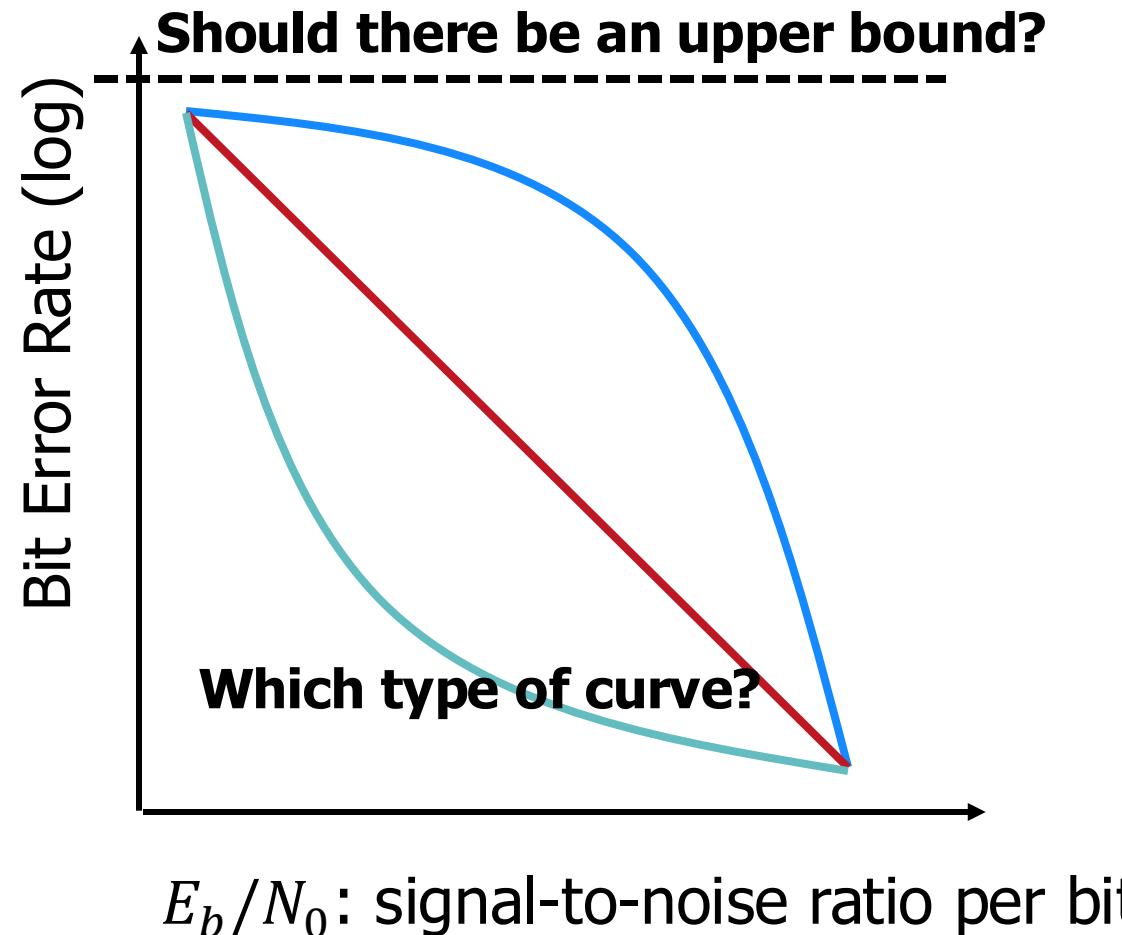
Natural-coded QPSK



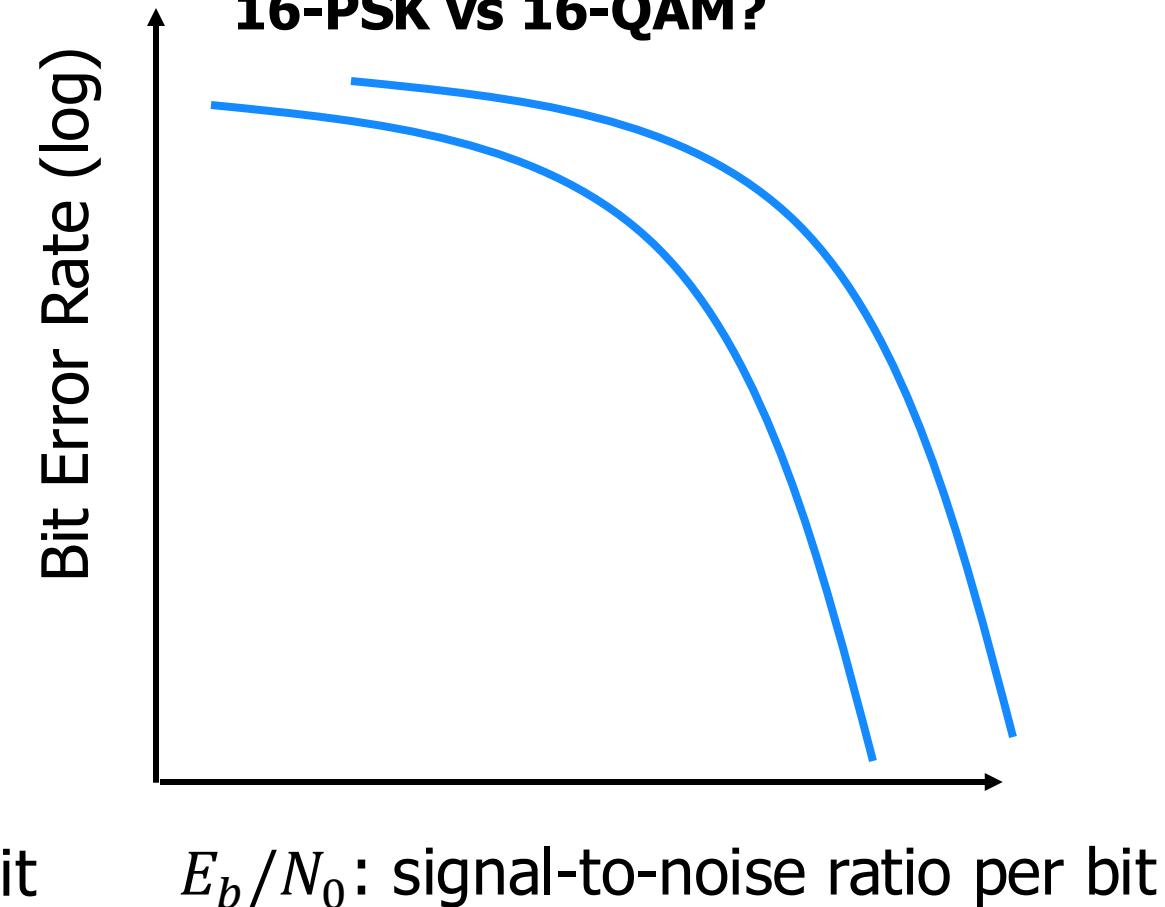
Gray-coded QPSK

# BER vs SNR

Let's have some thought experiments



**Natural code vs Gray code?**  
**4-PSK vs 8-PSK?**  
**16-PSK vs 16-QAM?**



# Acknowledgment

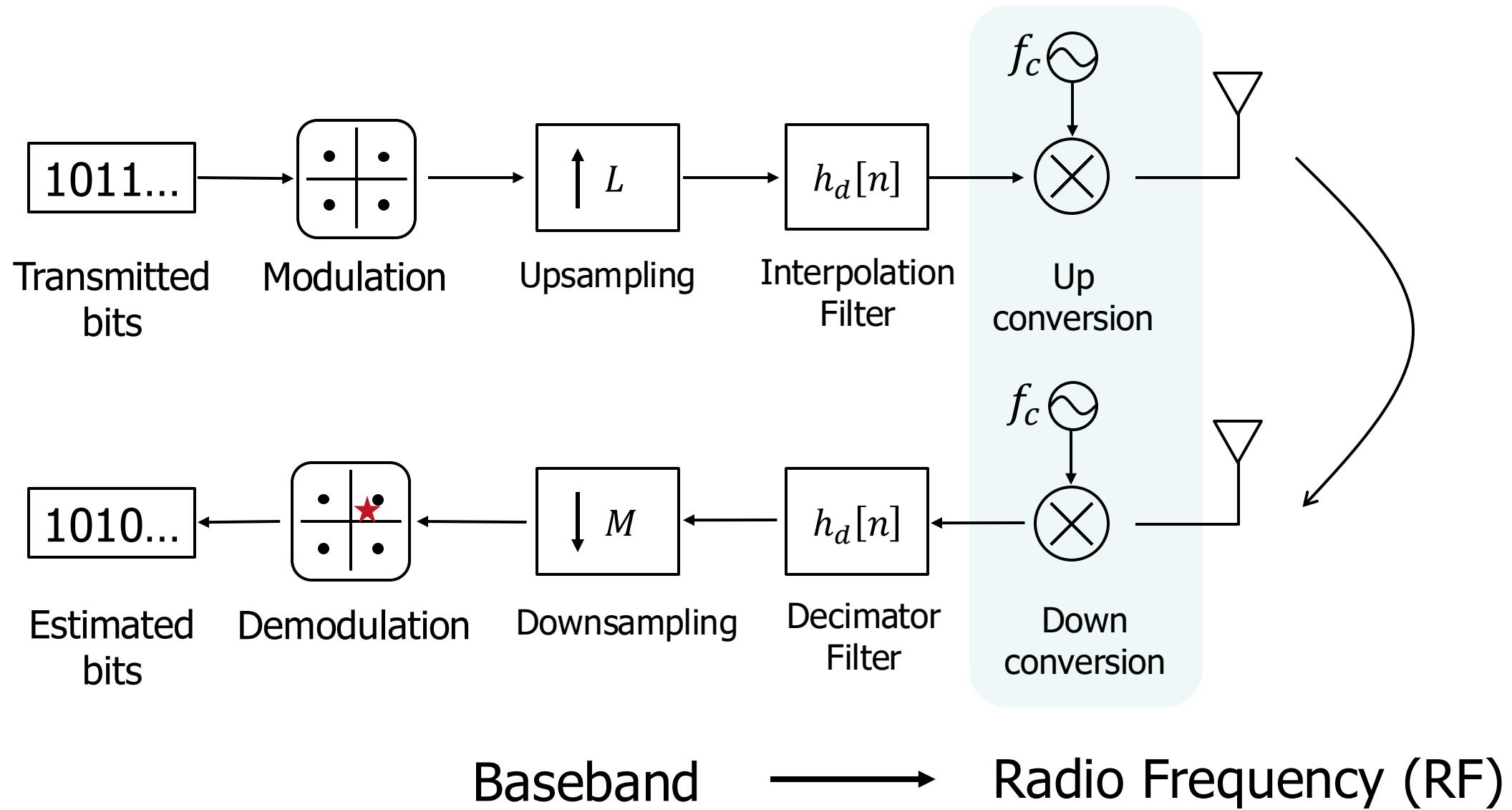
Dr. Clayton Shepard

Prof. Rahman Doost-Mohammady

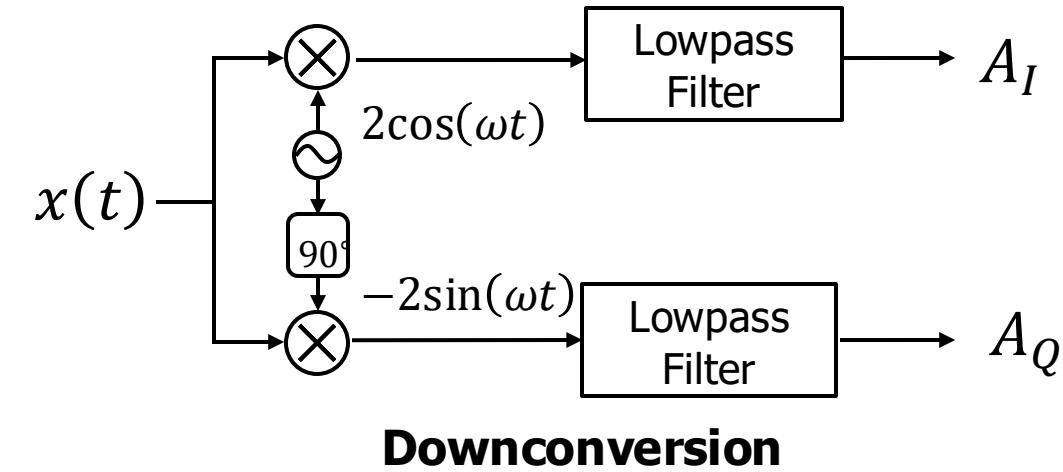
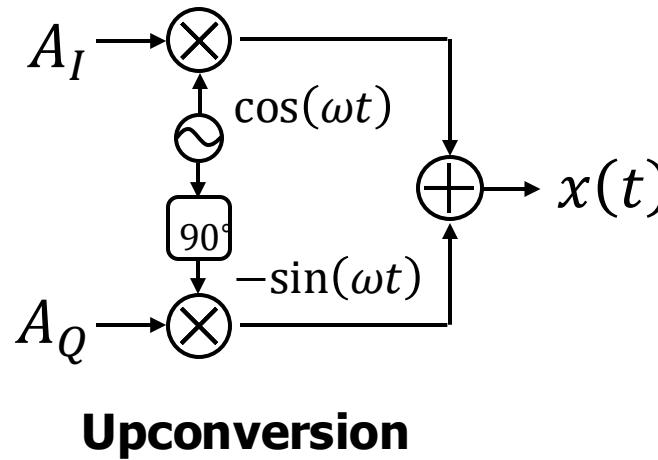


# Up/Down conversion

# Upconversion & Downconversion



# Upconversion & Downconversion



# Upconversion: Three Representations

$$x(t) = A \cos(2\pi f_c t + \theta) \quad (1)$$

**Polar** Cosine wave modulated by a baseband signal with amplitude ( $A$ ) and phase ( $\theta$ )

$$= A_I \cos(2\pi f_c t) - A_Q \sin(2\pi f_c t) \quad (2)$$

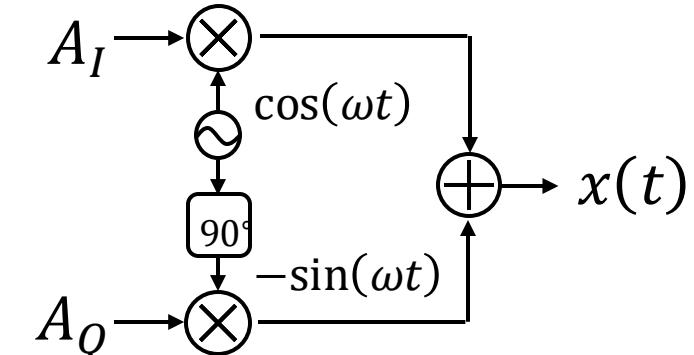
**Rectangular**  $A_I = A \cos(\phi), A_Q = A \sin(\phi)$

$$= \operatorname{Re}\{[A_I + jA_Q] e^{j2\pi f_c t}\} \quad (3)$$

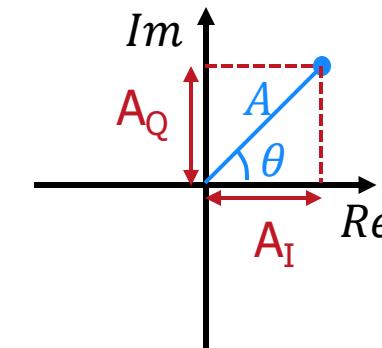
**Complex envelope**  $u = A_I + jA_Q$

## Question

- How to transmit complex signals/constellations over-the-air?
- Is the signal transmitted over-the-air real or complex?

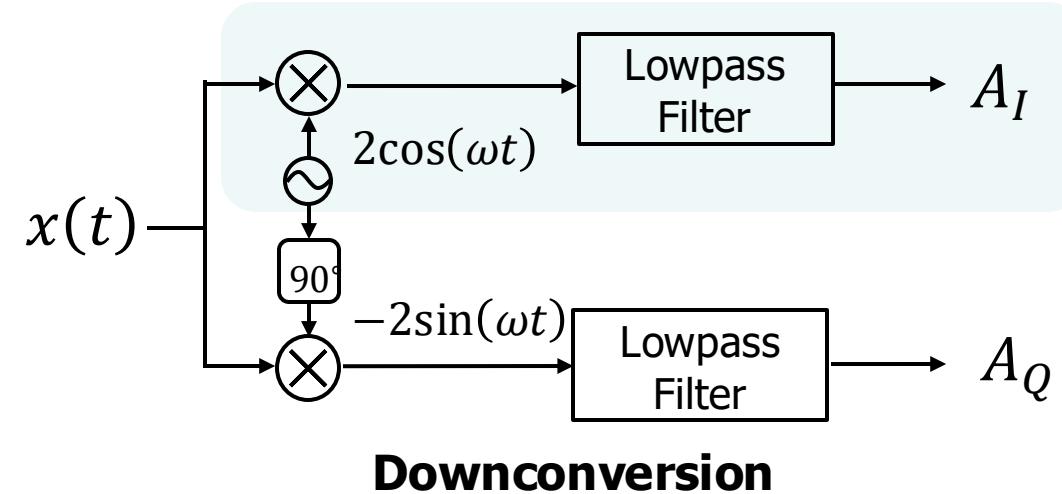
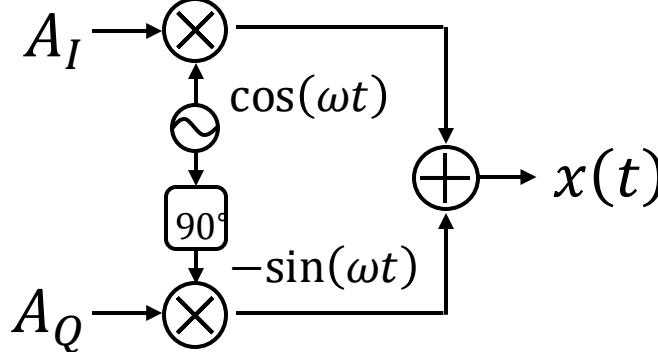


Hardware implementation



$A_I + jA_Q$ : Complex envelope

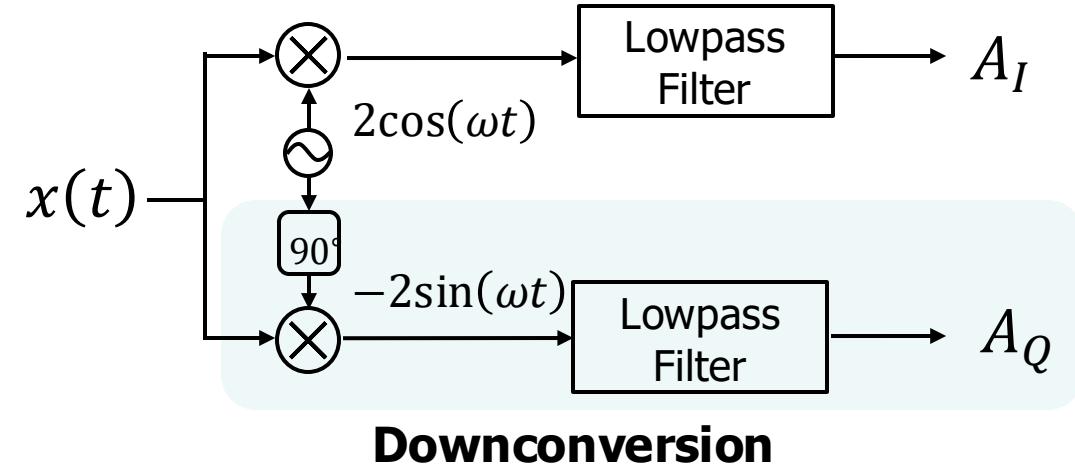
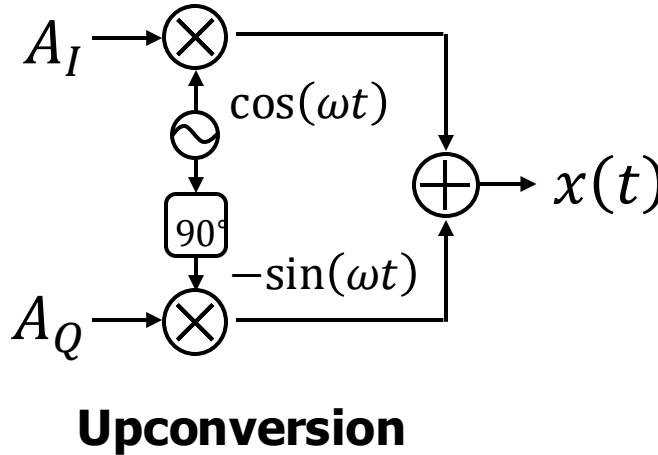
# Downconversion: Getting Back $A_I, A_Q$



$$\begin{aligned}
 x(t) \cdot 2 \cos(2\pi f_c t) \\
 &= 2A_I \cos^2(2\pi f_c t) - 2A_Q \sin(2\pi f_c t) \cos(2\pi f_c t) \\
 &= A_I + A_I \cos(4\pi f_c t) - A_Q \sin(4\pi f_c t)
 \end{aligned}$$

Get rid of them by lowpass filtering

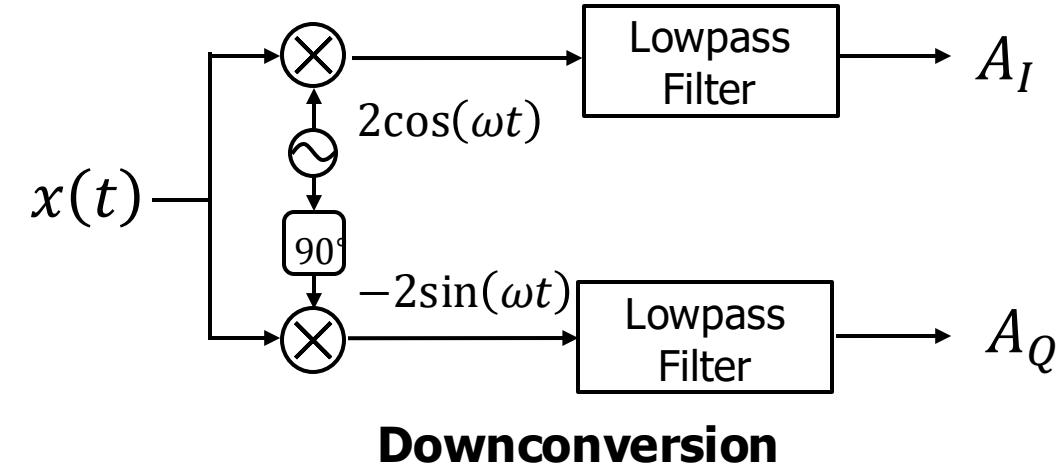
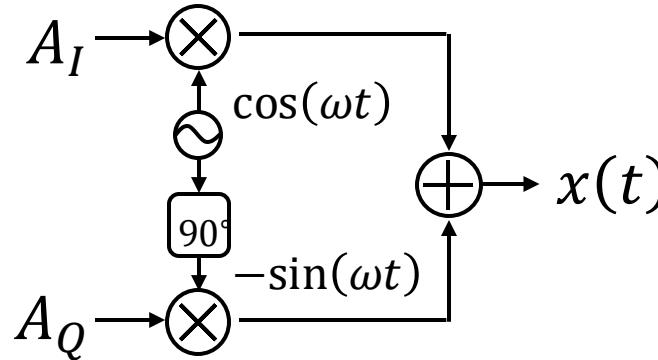
# Downconversion: Getting Back $A_I, A_Q$



$$\begin{aligned}
 & x(t) \cdot [-2 \sin(2\pi f_c t)] \\
 &= -2A_I \cos(2\pi f_c t) \sin(2\pi f_c t) + 2A_Q \sin^2(2\pi f_c t) \\
 &= A_Q - A_I \sin(4\pi f_c t) - A_Q \cos(4\pi f_c t)
 \end{aligned}$$

Get rid of them by lowpass filtering

# Downconversion: Back to Complex Envelope



$$x(t) \cdot 2e^{-j2\pi f_c t}$$

$$\begin{aligned} &= 2[A_I \cos(2\pi f_c t) - A_Q \sin(2\pi f_c t)][\cos(2\pi f_c t) - j \sin(2\pi f_c t)] \\ &= \boxed{A_I + jA_Q} + \boxed{C_1 \sin(4\pi f_c t) + C_2 \cos(4\pi f_c t)} \end{aligned}$$

Complex envelope

Get rid of them by lowpass filtering

# Upconversion: Frequency Domain

$$x(t) = \operatorname{Re}\{[A_I + jA_Q] e^{j2\pi f_c t}\}$$

Let  $u(t) = A_I + jA_Q$

$$= \operatorname{Re}\{u(t) e^{j2\pi f_c t}\}$$

Let  $c(t) = u(t) e^{j2\pi f_c t}$

$$= \operatorname{Re}\{c(t)\}$$

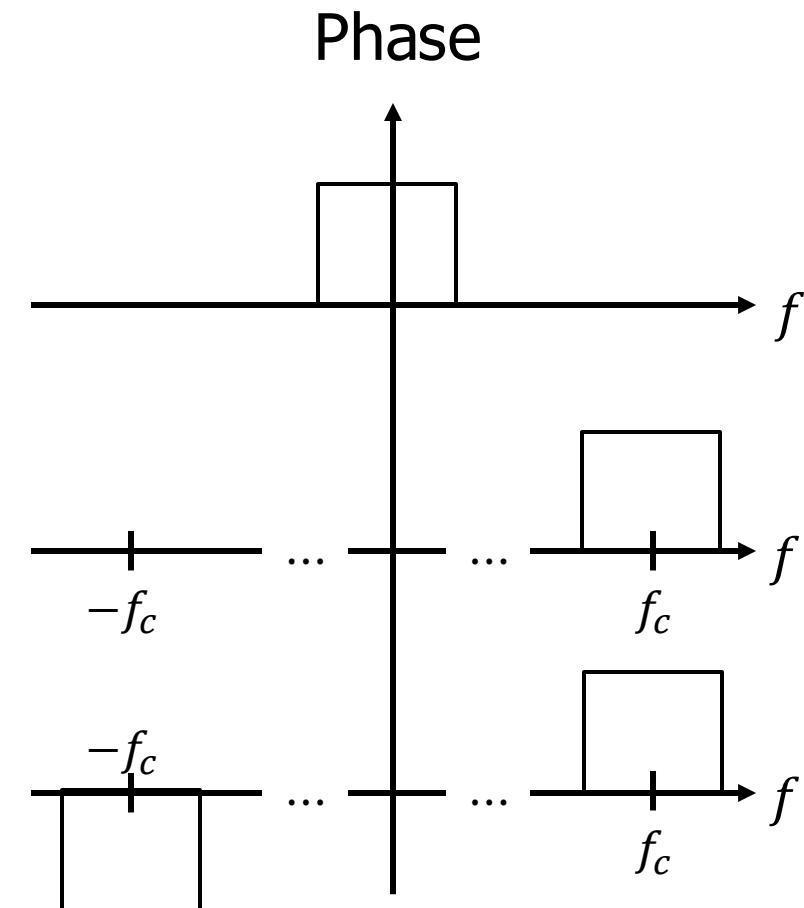
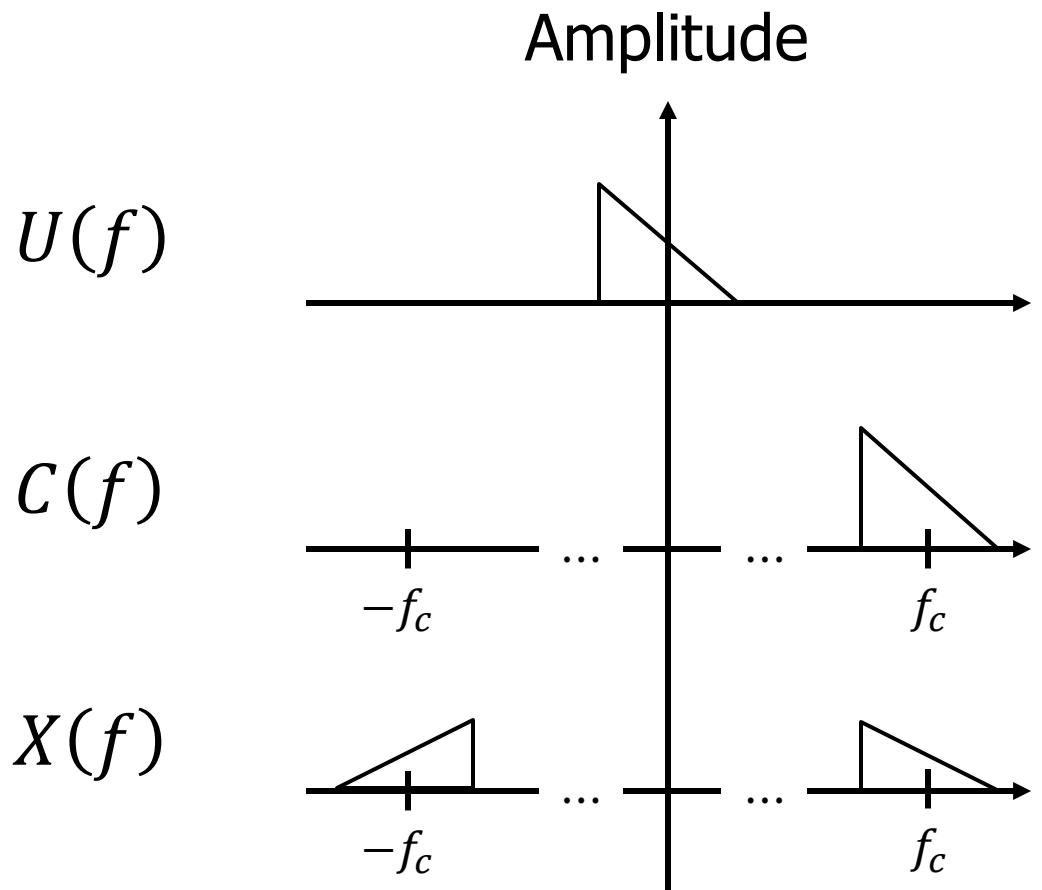


$$X(f) = \frac{1}{2} ( C(f) + C^*(-f) )$$

where  $C(f) = U(f - f_c)$

$$X(f) = \frac{1}{2} ( C(f) + C^*(-f) )$$

where  $C(f) = U(f - f_c)$



# Downconversion: Frequency Domain

$$y(t) = x(t) \cdot 2e^{-j2\pi f_c t}$$

Let  $d(t) = x(t) e^{-j2\pi f_c t}$

Lowpass filtering

$$u(t)$$

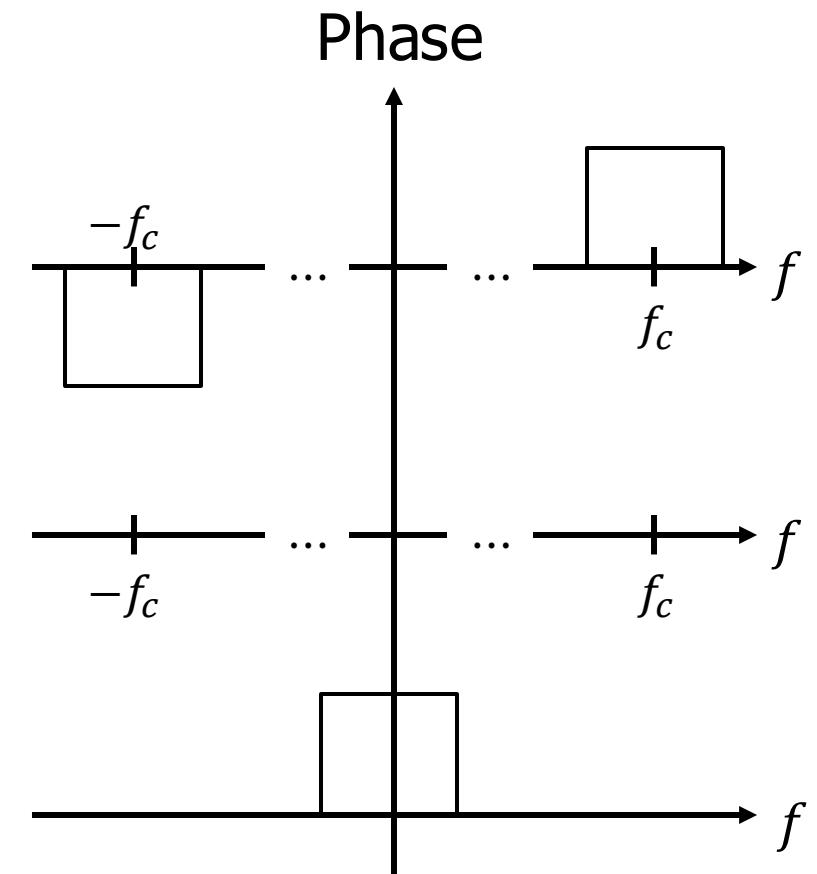
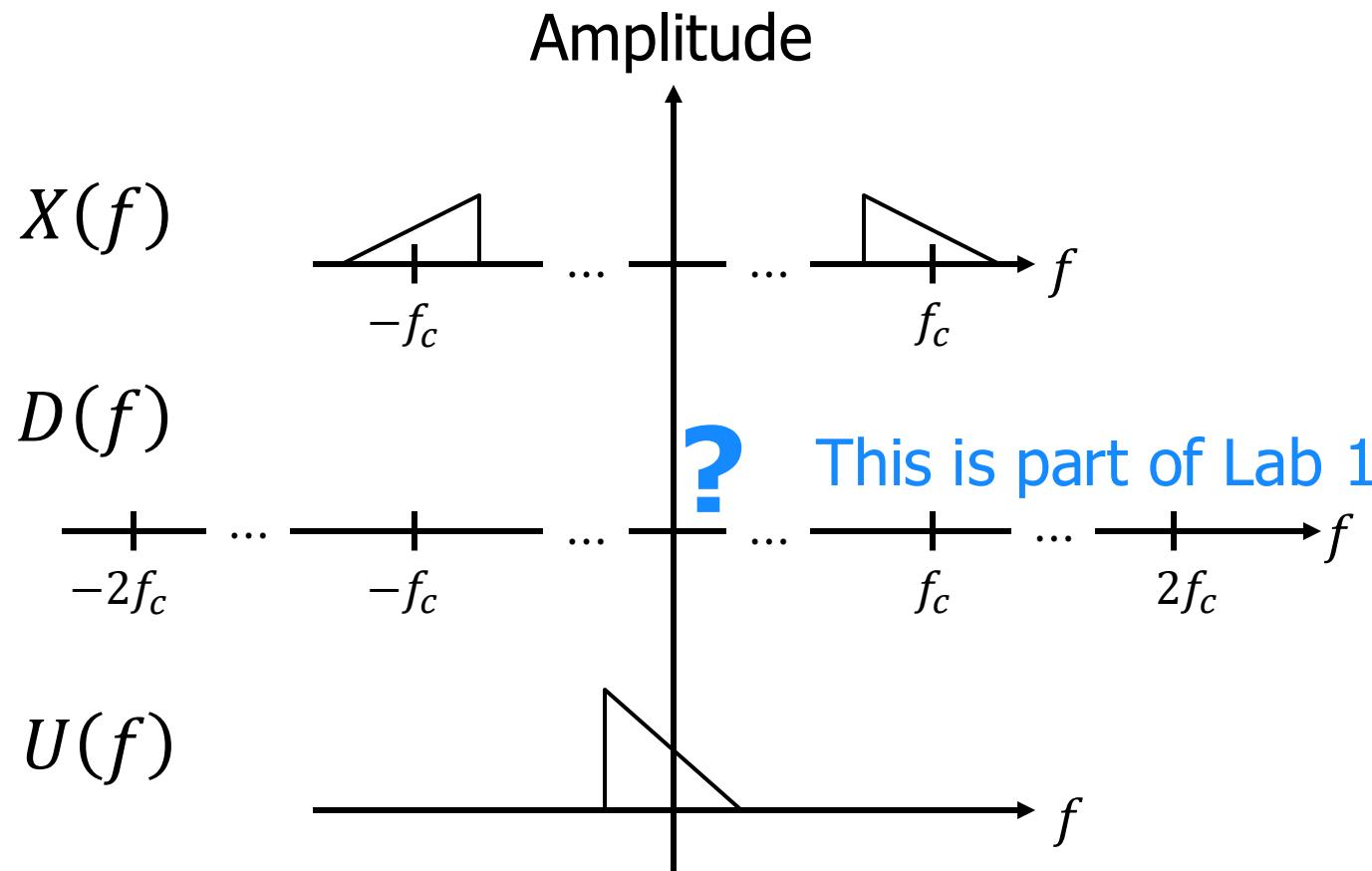


$$U(f) = \text{lowpass} \{ 2 \cdot D(f) \}$$

$$\text{where } D(f) = X(f + f_c)$$

$$U(f) = \text{lowpass} \{ 2 \cdot D(f) \}$$

$$\text{where } D(f) = X(f + f_c)$$



# References

- Modern Digital Radio Communication Signals and Systems by Sung-Moon Michael Yang [[NTU Library Link](#)]
  - Chap 1.2
- Introduction to Communication Systems 1st Edition by Upamanyu Madhow [[Unofficial version on UC Santa Barbara Website](#)]
  - Chap 2 & 3

Lab 1 is released.  
Due Sep. 16 (2 weeks from now)