Dealing with CR

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Dealing with competing risks

GPC can be used to analyze time-to-event endpoints subject to competing risks. Only two competing risks can be handled for each endpoint so far: the event of interest and one competing event. The former should be denoted by 1 in the corresponding censoring variable while the latter should be denoted by 2. Note that no competing event should be present without an event of interest. As an example, let us analyze the time to an event of interest, say death due to cancer, with death due to other causes being a competing event, in the following dataset:

```
Treatment toxicity eventtime status
1:
           C
                     1 0.79755079
           С
2:
                     1 0.03044704
                                         0
3:
           C
                     1 0.63851884
                                         0
           C
4:
                     0 0.75133915
                                         1
5:
           C
                     0 0.05860070
                                         0
                                         2
6:
                     0 0.25592439
```

The censoring variable, called status in the dataset, contains the following levels:

```
levels(as.factor(dt.CR[,status]))
```

```
[1] "0" "1" "2"
```

with 0 indicating a censored observation, 1 an event of interest (time to death due to cancer is observed) and 2 a competing event (time to death due to other causes is observed). We perform the GPC analysis on this time-to-event endpoint with a threshold of 1 year setting scoring.rule to "Peron". In the presence of competing risks, the "Peron" method uses the estimate of the cumulative incidence functions to compute the pairs' score:

Generalized pairwise comparisons with 1 endpoint

0.1408

If we display the score of some pairs:

getPairScore(BT.CR)

\$eventtime_1

```
strata index.C index.T favorable unfavorable
                                                          neutral
                                                                         uninf
                                                      0 0.0000000 0.000000000
                            501 1.0000000
     1:
             1
                      1
     2:
             1
                      2
                            501 0.5808172
                                                      0 0.4092908 0.009892024
                                                      0 0.3583333 0.100000000
     3:
                      3
                            501 0.5416667
              1
                                                        0.0000000 0.000000000
     4:
             1
                      4
                            501 1.0000000
                            501 0.5947180
                                                      0 0.3940119 0.011270046
     5:
              1
                      5
                                                      0 1.0000000 0.000000000
249996:
             1
                    496
                           1000 0.0000000
249997:
              1
                    497
                           1000 1.0000000
                                                      0 0.0000000 0.000000000
249998:
                           1000 1.0000000
                                                      0 0.0000000 0.000000000
              1
                    498
249999:
                    499
                           1000 1.0000000
                                                      0 0.0000000 0.000000000
              1
                                                      0 0.2000000 0.300000000
250000:
              1
                    500
                           1000 0.5000000
        weight favorableC unfavorableC neutralC
                                                         uninfC
     1:
                 1.0000000
                                       0 0.0000000 0.000000000
                 0.5808172
                                       0 0.4092908 0.009892024
     2:
             1
     3:
                 0.5416667
                                       0 0.3583333 0.100000000
     4:
                 1.0000000
                                       0 0.0000000 0.000000000
              1
     5:
                 0.5947180
                                       0 0.3940119 0.011270046
    ___
249996:
                 0.000000
                                       0 1.0000000 0.000000000
             1
249997:
                                       0 0.0000000 0.000000000
             1
                 1.0000000
249998:
                                       0 0.0000000 0.000000000
             1
                 1.0000000
249999:
                 1.0000000
                                       0 0.0000000 0.000000000
             1
                                       0 0.2000000 0.300000000
250000:
                 0.5000000
```

We see that the first pair, composed of observations 1 and 501, is classified as favorable. If we look closer at these two observations:

```
dt.CR[c(1,501),]
```

The treatment patient of the pair experienced the competing event while the control patient experienced the event of interest. In the GPC method it is considered that a patient experiencing the competing event will never experience the event of interest at a later time, and his time to the event of interest is thus considered infinite. In the present case, the treatment patient will never experience the event of interest and his time to the event of interest is thus considered infinite. The pair is therefore classified as favorable as the treatment patient has a longer time to the event of interest than the control patient. Similarly, pairs with the control patient having the competing event and the treatment patient having the event of interest are classified as unfavorable. Finally, pairs with two competing events are classified as neutral as both patients have an infinite time to the event of interest.

In this example, the net benefit is estimated to 0.1408. This positive value indicates that the probability to have a larger time to death due to cancer with the treatment compared to the control is larger than the probability to have a larger time to death due to cancer with the control compared to the treatment. This therefore suggests a beneficial effect of the treatment compared to the control regarding the event of interest.

What about the competing event?

The net benefit focuses on the time to the event of interest of the patients of the two treatment groups. The time to the competing event in both groups should therefore be analyzed too, to avoid missing important information about the experimental treatment and its effect on the competing event. This can be done by performing a log-rank test to determine whether there is a significant difference between the cause-specific hazards of the competing event in the two groups.

What about censoring?

As in the absence of competing risks, censoring can be handled in several ways. The first one consists in applying the Peron scoring rule instead of the Gehan scoring rule in order to use the cumulative incidence functions estimate to compute the pairs' score (see above example). Other ways are the use of a correction, either the IPCW correction or the correction at the pair level, to remove completely the uninformative pairs:

Generalized pairwise comparisons with 1 endpoint

```
> statistic
                  : net benefit (delta: endpoint specific, Delta: global)
> null hypothesis : Delta == 0
> treatment groups: C (control) vs. T (treatment)
> censored pairs : use Kaplan Meier survival curves to compute the score
> uninformative pairs: score equals the averaged score of all informative pairs
> results
 endpoint threshold total favorable unfavorable neutral uninf
eventtime
                  1
                      100
                              32.93
                                          18.74
                                                   48.33
                                                             0 0.1419
Delta
0.1419
```

Note that in this particular example, the effect of the correction at the pair level is really moderate as the original proportion of uninformative pairs was small.