# CAR project: computation of the AUC based on 3 sampling points

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## 1 Background

Cortisol awakening response (CAR) describes the period of sharp increase in cortisol secretion in the first 60 min after awakening. It is used in various clinical studies, including studies on the serotonin transporter or on serotonin 4 receptors.

CAR is usually estimated using saliva samples obtained immediately upon awakening, and at 15, 30, 45, and 60 minutes after awakening. First, the concentration in cortisol in each saliva sample is measured. The five measurements are then used to represent the temporal evolution of the cortisol concentration (see Figure 1).

The CAR curve is then summarized either into the area under the curve with respect to increase  $(AUC_I)$  or the area under the curve  $(AUC_G)$ .  $AUC_G$  corresponds to the average concentration value multiplied by the duration of the experiment (here 60 minutes) while  $AUC_I$ , as defined by Fekedulegn et al. (2007), can be computed as  $AUC_I = AUC_G - AUC_B$  where  $AUC_B$  is the baseline cortisol value times the follow-up time (here 60 min). We note that since  $AUC_B$  is estimated in the same way with 3 or 5 samples, the properties of  $AUC_I$  can be deduced from the one of  $AUC_G$ . This is why we will focus on the estimation of  $AUC_G$  in the aim and method sections. Nevertheless we will report results for the estimation of the  $AUC_I$ .

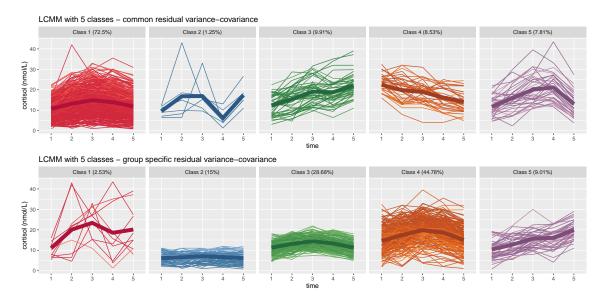


Figure 1: Trajectories of the cortisol concentration over time in healthy individuals with 5 measurement and a  $AUC_G$  below 2000. Trajectories were divided into 5 classes according to two different latent class linear mixed models (row 1 and row 2). The brightness of the color reflects the membership probability to the class.

## 2 Aim

The project's aim is to assess the reliability of an estimator of the CAR based on only 3-samples (instead of the usual 5). Three aspects should be discussed:

- Parameter of interest: the parameter of interest are the  $AUC_I$  and  $AUC_G$  which seems also to be commonly used in the litterature.

  However their value depends on the duration of the cortisol measurements which can be problematic:
  - (i) when subjects do not followed the scheduled measurement times, e.g. subject 10834 has samples at time 9h16, 9h30, 9h45, 10h00, 10h15, i.e. was 1 minute too early at his second measurement so his  $AUC_G$  which will be biased toward 0 compared to what we would have computed has the subject followed the schedule.
  - (ii) when changing the sampling strategy, e.g. only using measurements up to 30 min (instead of 60 min) will lead to a systematically lower  $AUC_G$ .

A "good" parameter of interest should be independent of the study design (i.e. sampling strategy). A possible remedie would be to consider the  $AUC_I$  or  $AUC_G$  per hour.

• Estimators of the  $AUC_G$ : currently the method used to estimate the  $AUC_G$  is the trapezoidal rule, i.e., using a weighted sum of the cortisol measurements where the weights are a function of the measurement times (see appendix B for an example).

One could also try a more data driven method, i.e. learn on a dataset what

are the optimal weights to match the 5-samples AUC value. This approach is especially relevant for correcting the shorter observation time: we can for instance weight more each measurement when using only the 0, 15, and 30 minute samples and get a 3-sample estimator of the  $AUC_G$  that is no more downward biased <sup>1</sup>.

• Assessment: Ideally we would like to assess both the accuracy and the precision of our new estimators of the  $AUC_G$ . For instance, consider indivividuals with the same CAR but different trajectories, we would like to know whether in average we estimate the right value (accuracy) and how by how much our estimates fluctuates over individuals (precision). To do so we should compare our estimates to the true value and thus obtain residuals. The accuracy can quantified based on the mean (or median) of the residuals and the precision based on the variance (or quantiles) of the residuals. Sometime we don't require to estimate the right value, but only that up to a (possibly unknwon) transformation, we estimate the right value  $^2$ . In that case, correlation coefficients can be of interest. We will report the Pearson's correlation coefficient which corresponds to a linear transformation.

Unfortunately we don't have access to a "truth" for the  $AUC_G$  values. Instead we will use the  $AUC_G$  estimated using 5-measurements as a proxy for the "truth".

## 3 Method

## 3.1 Training data

The full dataset contains 984 series of cortisol measurements both from healthy individuals and patients. The following exclusion criteria were applied:

- (i) wake-up time posterior to the time of first sample or time of first sample later than 15 minutes after wake-up time (16 individuals).
- (ii) time of first sample posterior to the time of second sample or time of second sample later than 20 minutes after time of first sample (8 individuals). Same for third (20 individuals), fourth (23 individuals), and fifth (23 individuals) sample.
- (iii) at least one missing cortisol measurement (86 individuals)
- (iv) at least one missing measurement time (21 individuals)

<sup>&</sup>lt;sup>1</sup>More complex learning strategies could be used to better handle various types of trajectories. For instance, if the cortisol concentration is always decreasing over time, weighting more each measurement will not be a valid solution when using only the 0, 15, and 30 minutes samples. But to keep things simple, we will not look into that.

<sup>&</sup>lt;sup>2</sup>e.g. the correlation/covariance between  $AUC_G$  and PET values would be insensitive to linear transformations of the  $AUC_G$ .

Note that the same individual may appear in several exclusion criteria; see appendix A for details. In total, it remains 815 trajectories belonging to 540 distinct individuals, 470 trajectores originating from 325 healthy individuals and 345 trajectories originating from 215 patients. In what follows we will not take into account that some series originates from the same patient and call a serie of 5 cortisol measurements a trajectory.

The calculation of the  $AUC_G$  was performed based on the trapezoidal rule (R function pracma::trapz) and matched the  $AUC_G$  values present in the datatest. There was also very close aggreement between the  $AUC_I$  computed in R and from the database. However there were significant discripancy in  $AUC_B$  (see appendix B for detail) but since they are not used later on this is not considered an issue.

For the exploratory analysis and for training the statistical models, we will only consider the healthy controls with no missing values (i.e. all 5 samples). As shown in Figure 2 there are some clear outliers. To simplify visualization and modeling, they were excluded by removing all trajectories having a  $AUC_g$  above 2000. When using the cases as testing set, individuals with large  $AUC_g$  were also excluded (here  $AUC_g > 5000$ ). In both the training and test set individuals with delayed measurements (first sample more than 15 min after wake up, or more than 5 minutes delay in following measurements) were also excluded.

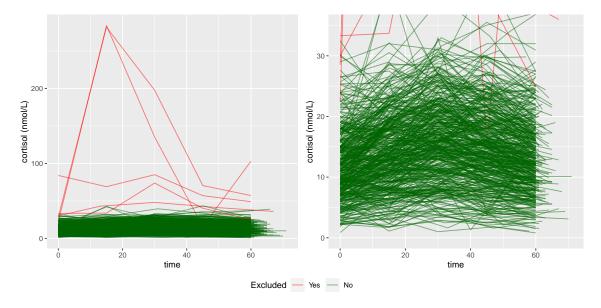


Figure 2: Individual cortisol trajectories in the healthy controls. The colors indicate whether a trajectory was used in the exploratory analysis and training of the statistical model.

## 3.2 Statistical analysis

**Exploratory**: Identifing typical shapes of trajectories can help to decide which three samples to use. For instance if two trajectories start the same but differ at latter timepoints, it may not be possible to get an accurate AUC based only on the first

measurements (e.g. consider class 2 and 3 in row 1 of Figure 1). Latent class linear mixed models (LCMM) were used to try to identify these typical trajectories and estimate the percentage of observations associated to each typical trajectory. The number of classes (i.e. typical trajectories) was varied from 1 to 6. A different mean parameter was estimated for each class and timepoint. An unstructured covariance matrix was used to model the covariance between the residuals (within trajectory). Two types of LCMM were fitted: one where the covariance matrix is assumed to be the same for all classes and another where it is class specific.

WARNING: to save computation time each model was run using a single initialization. One would need to compare several initializations to check the stability of the results.

Evaluation of the estimators: The  $AUC_G$  for with 5-samples was computed using the trapezoidal rule and used as a gold standard. The 3-samples  $AUC_G$  was computed either using the trapezoidal rule or using the linear predictor of a linear regression. The linear regression was fitted using the 5-sample  $AUC_G$  as an outcome, the  $AUC_G$  estimated by the trapezoidal rule on 3-samples as an offset, and the 3 cortisol values multiplied by the time intervals as regressors (see appendix C for details). We always used the first sample (0 minute) and two of the four following samples (15, 30, 45, or 60 minutes). This gives rise to 2\*6 estimators.

These estimators were evaluated on the healthy control dataset (when using the linear regression, a 10-fold cross validation was used) and on the patient dataset.

Note that, because  $AUC_B$  does not vary over estimators, the estimation error for the  $AUC_I$  will be the same as for the  $AUC_G$ . The correlation between the 3 and 5-sample estimators may differ though. We won't report relative error because it is not well defined as it requires to divide by  $AUC_I$  (which may be null).

## 4 Results

## 4.1 Exploratory analysis

As shown in Table 1, all LCMM but one converged (common variance, 6 classes). Visual inspection of the class trajectories suggested to retain the 5 class model <sup>3</sup>. Figure 1 shows the typical trajectories estimated for each class along with the observed trajectories belonging to that class. Some patterns were identified:

- inverse V shape trajectory: increase then decrease. About about 8% of the trajectories according the LCMM with common variance (row 1 Class 5).
- monotone trajectory: increase or decrease. About 9% of the trajectories (row 1 Class 3 and 4 and row 2 class 5).
- stable trajectory. About 15% of the trajectories were rather constant, fluctuating only between rather low values (row 2 Class 2).

<sup>&</sup>lt;sup>3</sup>this is a bit arbitrary.

• very variable trajectory. A few percents (row 1 Class 2 and row 2 Class 1).

Unfortunately for still a rather large proportion of trajectories (70%, row 1 Class 1 or row 2 Class 3 and 4), no clear pattern was identified. This show the limits of this "generic" LCMM approach. Better shape identification might be possible with an model specifically design for this problem (but this would require much more work!). For the previous types, one would expect that using 3-samples at time 0, 30, and 60 to give a reasonnable approximation - with the exception of the few very variable trajectory. Considering only early (0, 15, and 30 minutes) or only late (30, 45, and 60 minutes) is unlikely to be satisfying since one would not be able to distinguish between monotonic and inverse V shape trajectories. This is problematic since these represent a non-neglectable proportion of the sample.

## 4.2 Evaluation of the estimators: 3 vs. 5-sample $AUC_G$

From the estimated coefficients of the linear regression (Table 2), it appears that the trapezoidal rule tends to underestimate the  $AUC_G$  (positive intercept in all models). In models not including the 60 minute sample, the last sample was given additional weight compared to the trapezoidal rule to further correct the downward bias. The weights of the other samples were essentially unchanged.

The performance of the estimators are displayed in Figure 3 and summarized in Table 3. Performance between the training (i.e. healthy controls) and test set (i.e. patients) were very similar. While all estimators showed high correlation with the 5-sample  $AUC_G$  (see Figure 4 for a visual representation of the impact of the estimator on the correlation), they greatly differ in term of accuracy and precision.

When using the trapezoidal rule, as expected, all estimators not including the 60 minute sample were downward biased. Moreover the 0-15-30 was vary variable. Overall using the samples 0, 30 minutes, and 60 minutes lead to the least bias (about -10 nmol.h/L or -1%) and least variation (about 65 nmol.h/L or 8%). The other estimators showed much higher bias and/or variability and are not recommanded.

The linear regression had very little impact on the 0-15-30 estimator (as shown in Table 2). For all other estimators, it corrected most of the bias and greatly reduced their variability. With this approach the 0-15-45 and 0-30-45 estimators become an option with a bias of about +/-5 nmol.h/L (0.5%) and fluactuation of about 60 nmol.h/L (7%). Figure 4 can also be used to see the accuracy and precision along the  $AUC_G$  value. They don't seem to vary much for the recommanded estimators -compare to the estimator trapezoidal rule 0-15-30 whose precision decreases (i.e. the variance increases) when looking at higher  $AUC_G$  values. This may be easier to see when considering the relative error along the AUCg values (Figure 5).

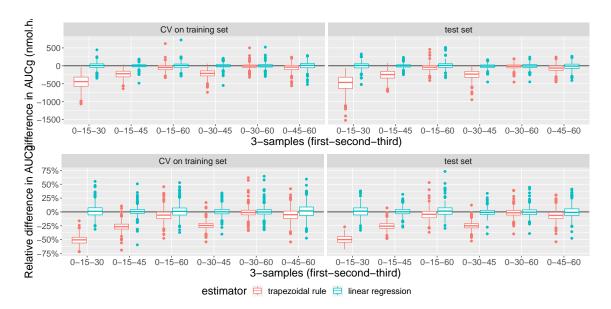


Figure 3: Boxplot of the difference between the estimated 5-sample  $AUC_G$  and the estimated 3-sample  $AUC_G$ . The closer to 0 the better. The first row displays the difference in unit of cortisol concentration (summed over an hour) while the second row display the relative difference (unitless), i.e. the difference divided by the estimated 5-sample  $AUC_G$ .

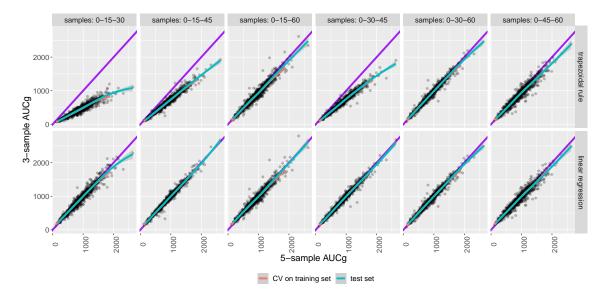


Figure 4: Correlation between the estimated 5-sample  $AUC_G$  and the estimated 3-sample  $AUC_G$ . The estimates for both the healthy individuals and the patients are displayed (black points). The colored lines show the trend separately for the healthy individuals and the patients (not always visible because they are essential the same). The purple line is the identity line (i.e. no bias).

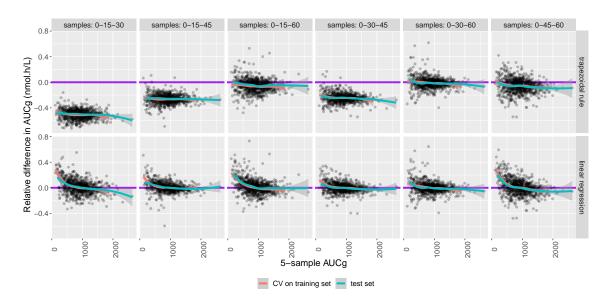


Figure 5: Relative error as a function of the estimated 5-sample  $AUC_G$ . The estimates for both the healthy individuals and the patients are displayed (black points). The colored lines show the trend separately for the healthy individuals and the patients (not always visible because they are essential the same). The purple line corresponds to no bias.

## 4.3 Evaluation of the estimators: 3 vs. 5-sample $AUC_I$

Results for the  $AUC_I$  are rather similar to the  $AUC_G$ , e.g. see Figure 6, Figure 7 and Table 4. The main difference is that the correlation was a bit lower. This can be easily explained: the error was the same as for the  $AUC_G$ , so since the  $AUC_G$  is larger (in absolute value) compared to the  $AUC_I$ , the variability was higher.

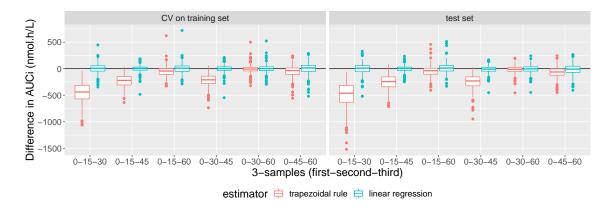


Figure 6: Boxplot of the difference between the estimated 5-sample  $AUC_I$  and the estimated 3-sample  $AUC_I$ . The closer to 0 the better.

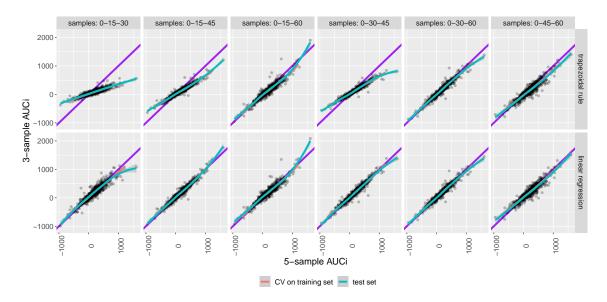


Figure 7: Correlation between the estimated 5-sample  $AUC_I$  and the estimated 3-sample  $AUC_I$ . The estimates for both the healthy individuals and the patients are displayed (black points). The colored lines show the trend separately for the healthy individuals and the patients (not always visible because they are essential the same). The purple line is the identity line (i.e. no bias).

## 5 Application of the 3-sample AUC

### 5.1 Re-analysis of (Jakobsen et al., 2016)

We will now replicate the study of Jakobsen et al (2016).

**Data management**: 1 subject (50678) had missing wake-up time and another (50524) had missing time for sample. Both were assigned the most likely time with respect to how the other sample were taken. It turns out that the other samples were all on schedule (e.g. 15 minutes between sample 4 and 5) so the assigned values lead to perfect adherence to planned schedule. See Figure 8 for a graphical display of the data.

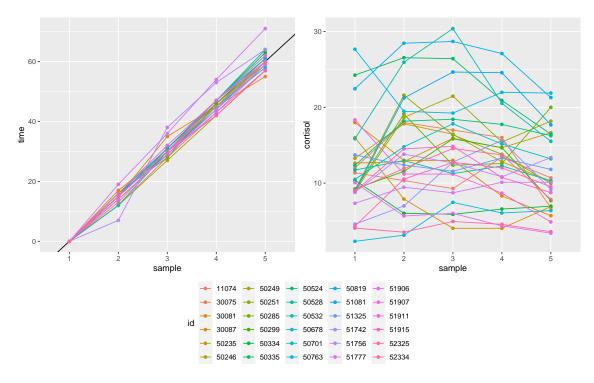


Figure 8: Left panel: time at which the sample were taken. Right panel: cortisol values per individual.

**AUC** calculation (5 samples): the AUCg and AUCi computed in R exactly matched the one from the database.

**AUC** calculation (3 samples): We focused on the 3-sample AUC with the sample taken at 0, 30, and 60 minutes. The discrepancy with the 5-sample AUC is shown on Figure 9. For the AUCg the error varied -66.35 to +139.53. Relatively to the 5-sample AUC value, it varied between -13.61% and +17.96%. There was a tendency for a too low estimated value when using the 3-sample approach (-20.983, p=0.0339). There was no evidence that the error was AUC dependent for the AUCg (p=0.276) while there was rather strong evidence in favor of a linear trend for the AUCi (slope=0.1, p=0.002).

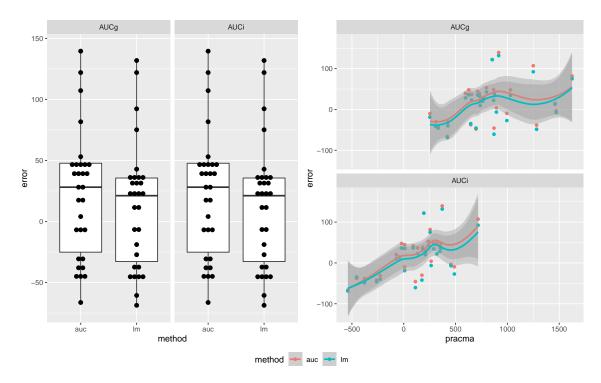


Figure 9: First two panels: boxplot of discrepancy between 3- and 5-sample AUC by estimator. Last two panels: discrepancy between 3- and 5-sample AUC along the 5-sample AUC value.

Estimation of the association binding-cortisol: Table 5 shows the estimated effect when using 3- or 5- samples to compute the AUC. The effect seems a little bit attenuated and its estimation a bit less uncertain. Overall the p-values are very similar.

## 5.2 Re-analysis of Frokjaer et al 2014

We will now replicate the analysis of Frojkaer et al (2014).

**Data management**: 2 subject had missing cortisol level at one timepoint. Subject 11083 (Case) was missing the 4th value and subject 11101 was missing the 5th value. See Figure 10 for a graphical display of the data:

**AUC** calculation (5 samples): the AUCi computed in R excactly matched the one from the database.

**AUC** calculation (3 samples): We focused on the 3-sample AUC with the sample taken at 0, 30, and 60 minutes. The 1m could not estimate the AUC for the individual missing the 5th cortisol measurement. The discrepancy with the 5-sample AUC is shown on Figure 11. For the AUCg the error varied -501.0 to +322.4, which relatively to the 5-sample AUC value, corresponds to -38.21 and +54.97%. 4 observations were driving the error; for the rest of the observations the error varied between -141 and +123.75 (-24.32% and 51.07%). There was no evidence for a biased estimate when using the 3-sample approach (e.g. AUCi p=0.304, AUCg p=0.419 with the trapezoidal rule).

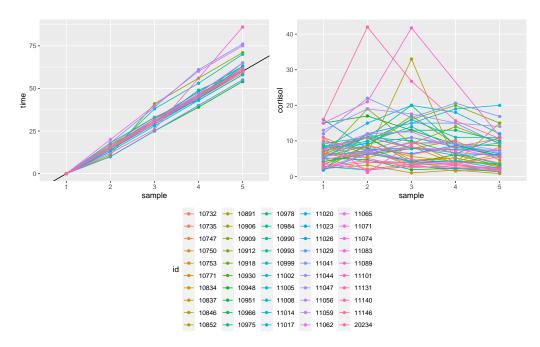


Figure 10: Left panel: time at which the sample were taken. Right panel: cortisol values per individual.

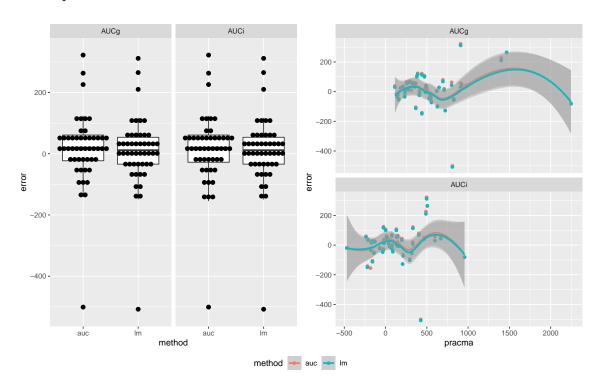


Figure 11: First two panels: boxplot of discrepancy between 3- and 5-sample AUC by estimator. Last two panels: discrepancy between 3- and 5-sample AUC along the 5-sample AUC value.

Estimation of the association binding-cortisol: Table 6 shows the estimated effect when using 3- or 5- samples to compute the AUC. The effect seems rather similar but with larger standard error leading to larger p-values.

## 6 Conclusion

We have shown that the best estimators of the  $AUC_G$  are:

- the 0-30-60 with the trapezoidal rule
- the 0-15-45 or 0-30-45 with the linear regression

They exhibit a bias close to 0 and a typical fluctuation in  $AUC_G$  of 60-80 nmol.h/L (about 7-9%) when compared to the 5-sample  $AUC_G$ . The same error 60-80 nmol.h/L was observed for the  $AUC_I$  which means that in relative terms (i.e. %) the 3-samples was less precise for the  $AUC_I$  than for the  $AUC_G^4$ .

The "best" estimator may also depend on other considerations:

- which sampling scheme is the most convenient. In particular is it convenient to avoid the 60 minutes and have instead to do a 45 minutes measurement.
- whether one is willing to use a data-driven approach (linear regression) instead of the well established trapezoidal rule.

However we must be aware that so far we used the 5-sample  $AUC_G$  as a reference, which may not give a perfect picture of the true  $AUC_G$ . Therefore we can only claim that (i) the recommanded 3-sample estimators are not more biased than 5-sample estimators and (ii) derive an upper bound for the loss in precision (here 60-80 nmol.h/L, 7-9%). It is also important to realize that these results may be very specific to the AUC-statistic. Other summary statistics, such as peak value may be much more affected by the reduction of the number of samples.

Finally so far we haven't used any covariate such as age, gender, .... They could for instance be used to see whether they explain the heterogeneity in cortisol values or in the shape of the cortisol trajectory (increasing, decreasing, V-shape).

<sup>&</sup>lt;sup>4</sup>it is important to keep in mind that an error of 60 may be small if the true value is 600 but may be large if the true value is 100.

## 7 Tables

Common residual variance-covariance								
nb. classes	loglik	cv	nb. parameters	AIC	BIC	SABIC	entropy	
1.00	-6635.30	1.00	21.00	13312.61	13399.59	13332.94	1.00	
2.00	-6586.74	1.00	27.00	13227.47	13339.31	13253.62	0.91	
3.00	-6587.36	1.00	33.00	13240.73	13377.42	13272.68	0.70	
4.00	-6512.69	1.00	39.00	13103.38	13264.92	13141.14	0.88	
5.00	-6515.22	1.00	45.00	13120.43	13306.82	13164.00	0.87	
6.00	-6456.58	1.00	51.00	13015.16	13226.40	13064.54	0.85	
Group spec	ific residua	l varia	nce-covariance					
nb. classes	loglik	cv	nb. parameters	AIC	BIC	SABIC	entropy	
1.00	-6635.30	1.00	21.00	13312.61	13399.59	13332.94	1.00	
2.00	-6505.25	1.00	28.00	13066.50	13182.48	13093.62	0.58	
3.00	-6435.97	1.00	35.00	12941.95	13086.92	12975.84	0.79	
4.00	-6409.37	1.00	42.00	12902.74	13076.71	12943.41	0.79	
5.00	-6389.42	1.00	49.00	12876.84	13079.80	12924.28	0.71	
6.00	-6393.03	1.00	56.00	12898.06	13130.01	12952.28	0.75	

Table 1: Convergence (column cv, 0 indicates convergence issue) and information criteria for the two LCMM. For AIC, BIC, SABI the lower the better while for entropy the higher the better.

Samples	(Intercept)	sample 1	sample 2	sample 3
0-15-30	48.96 [26.91;71]	0.01 [-0.26;0.28]	0.07 [-0.09;0.23]	3.14 [2.89;3.38]
0 - 15 - 45	30.43 [15.74;45.12]	0.04 [-0.13; 0.22]	-0.02 [-0.08;0.04]	$0.91 \ [0.84; 0.98]$
0-15-60	41.37 [19.43;63.32]	-0.02 [-0.29;0.24]	-0.08 [-0.14;-0.01]	0.17 [0.1; 0.23]
0-30-45	18.67 [2.95;34.39]	-0.05 [-0.13;0.03]	0.07 [0; 0.14]	1.6 [1.4; 1.79]
0-30-60	9.28 [-7.97;26.53]	-0.05 [-0.13;0.04]	-0.02 [-0.07;0.03]	0.09 [0; 0.19]
0-45-60	42.74 [18.14;67.34]	-0.05 [-0.13;0.03]	0.02 [-0.07; 0.1]	$0.15 \left[-0.21;0.5\right]$

Table 2: Coefficients of the linear regression for correcting the trapezoidal rule.

dataset	method		median	q. 2.5%	q. 97.5%	IQR	cor.
training	auc	0-15-30	-440 (-50.5%)	-847 (-65.7%)	-114 (-37.2%)	256 (10.3%)	0.94
(with CV)		0 - 15 - 45	$-221 \ (-26.8\%)$	$-456 \ (-39.5\%)$	-46 (-13%)	$156 \ (8.7\%)$	0.97
		0-15-60	$-45 \ (-5.8\%)$	$-241 \ (-24.7\%)$	$92\ (15.7\%)$	$105 \ (11.7\%)$	0.97
		0-30-45	$-210 \ (-24.5\%)$	$-451 \ (-38.3\%)$	-33 (-8%)	$138 \ (7.5\%)$	0.97
		0-30-60	-8 (-1.1%)	-139 (-18.1%)	$107 \ (17.2\%)$	65 (8.3%)	0.98
		0 - 45 - 60	$-36 \ (-4.9\%)$	-248 (-28.4%)	$105 \ (17.2\%)$	$118 \ (13.4\%)$	0.96
	lm	0-15-30	8 (1%)	-199 (-20.1%)	$173\ (25.8\%)$	99 (12.8%)	0.97
		0 - 15 - 45	4~(0.5%)	-118 (-12%)	$111 \ (16.9\%)$	57 (7%)	0.98
		0 - 15 - 60	9 (1%)	-185 (-17.9%)	$151\ (28.7\%)$	$101\ (12.7\%)$	0.97
		0-30-45	2(0.2%)	-119 (-14%)	$119 \ (19.5\%)$	64 (8.1%)	0.98
		0-30-60	0 (0%)	-131 (-16.9%)	$122 \ (18.1\%)$	68 (8%)	0.98
		0-45-60	$14 \ (1.7\%)$	$-185 \ (-20.8\%)$	156 (30.2%)	$116 \ (15\%)$	0.96
test set	auc	0-15-30	-463 (-50%)	-1092 (-65%)	-119 (-36.9%)	314 (10.1%)	0.94
		0 - 15 - 45	-244 (-25.8%)	-536 (-39.4%)	-55 (-11.7%)	$186 \ (8.2\%)$	0.98
		0 - 15 - 60	-38 (-4.3%)	-248 (-22.7%)	$107 \ (14.2\%)$	$113 \ (11.5\%)$	0.97
		0 - 30 - 45	$-231 \ (-25.1\%)$	-528 (-38.9%)	-44 (-10.5%)	$167 \ (7.5\%)$	0.98
		0-30-60	-12 (-1.5%)	-182 (-18.6%)	97 (15.1%)	$78 \ (8.3\%)$	0.99
		0-45-60	-62 (-6.3%)	-299 (-28.2%)	$119 \ (17.2\%)$	118 (11.2%)	0.97
	lm	0-15-30	$10 \ (1.3\%)$	-232 (-18.8%)	$143 \ (21.9\%)$	$113 \ (12.7\%)$	0.97
		0-15-45	3(0.3%)	-115 (-11.5%)	$116 \ (17.6\%)$	61 (8%)	0.99
		0-15-60	$11 \ (1.5\%)$	-186 (-16.7%)	160~(26.6%)	$101 \ (11.5\%)$	0.97
		0-30-45	-8 (-0.7%)	-149 (-13.4%)	103~(12.6%)	$71 \ (7.5\%)$	0.99
		0-30-60	-3 (-0.4%)	-166 (-17.2%)	$105 \ (16.5\%)$	79~(8.6%)	0.99
		0-45-60	-8 (-0.8%)	-241 (-20.9%)	177 (28.8%)	116 (12%)	0.97

Table 3: Discrepancy of the proposed 3-sample estimators with the 5-sample  $AUC_G$  estimated with the trapezoidal rule. q. 2.5% and q. 97.5% stand for 2.5 and 97.5 quantile, IQR for interquartile range, cor. for correlation, auc for  $AUC_G$  estimated with the trapezoidal rule, Im for  $AUC_G$  estimated using a linear regression. The column median indicates the median bias (the closer to 0 the higher the accuracy). The column IQR reflect the precision of the estimator (the lower the better).

dataset	method	timepoint	median	q. 2.5%	q. 97.5%	IQR	cor
training	auc	0-15-30	-440.00	-847.00	-114.00	256.00	0.90
(with CV)		0-15-45	-221.00	-456.00	-46.00	156.00	0.96
		0-15-60	-45.00	-241.00	92.00	105.00	0.94
		0-30-45	-210.00	-451.00	-33.00	138.00	0.97
		0-30-60	-8.00	-139.00	107.00	65.00	0.97
		0-45-60	-36.00	-248.00	105.00	118.00	0.93
	lm	0 - 15 - 30	8.00	-199.00	173.00	99.00	0.94
		0 - 15 - 45	4.00	-118.00	111.00	57.00	0.97
		0-15-60	9.00	-185.00	151.00	101.00	0.94
		0-30-45	2.00	-119.00	119.00	64.00	0.97
		0-30-60	-0.00	-131.00	122.00	68.00	0.97
		0 - 45 - 60	14.00	-185.00	156.00	116.00	0.93
test set	auc	0-15-30	-463.00	-1092.00	-119.00	314.00	0.92
		0-15-45	-244.00	-536.00	-55.00	186.00	0.97
		0-15-60	-38.00	-248.00	107.00	113.00	0.96
		0 - 30 - 45	-231.00	-528.00	-44.00	167.00	0.97
		0-30-60	-12.00	-182.00	97.00	78.00	0.98
		0-45-60	-62.00	-299.00	119.00	118.00	0.95
	lm	0-15-30	10.00	-232.00	143.00	113.00	0.94
		0 - 15 - 45	3.00	-115.00	116.00	61.00	0.98
		0-15-60	11.00	-186.00	160.00	101.00	0.96
		0 - 30 - 45	-8.00	-149.00	103.00	71.00	0.98
		0-30-60	-3.00	-166.00	105.00	79.00	0.98
		0-45-60	-8.00	-241.00	177.00	116.00	0.95

Table 4: Discrepancy of the proposed 3-sample estimators with the 5-sample  $AUC_I$  estimated with the trapezoidal rule. IQR stands for interquartile range, auc for  $AUC_I$  estimated with the trapezoidal rule, lm for  $AUC_I$  estimated using a linear regression. The column median indicates the median bias (the closer to 0 the higher the accuracy). The column IQR reflect the precision of the estimator (the lower the better).

	Pallidostriatum									
	i miidosullaudili									
AUC estimator	effect	se	p-value	lower	upper					
AUC with 5 samples	-328.241	123.285	0.013	-581.657	-74.825					
ACC with 5 samples	-328.241	125.265	0.015	-361.037	-14.625					
AUC with 3 samples	-284.250	108.123	0.014	-506.501	-62.000					
LM with 3 samples	-289.480	108.821	0.013	-513.165	-65.795					
Hippocampus										
AUC estimator	effect	se	p-value	lower	upper					
AUC with 5 samples	-334.606	411.014	0.423	-1179.457	510.245					
AUC with 3 samples	-315.322	358.762	0.387	-1052.767	422.124					
LM with 3 samples	-334.732	361.406	0.363	-1077.612	408.149					

Table 5: Estimate association between the AUCi and the binding potential adjusted for age and gene (LA.LA).

AUC estimator	$\operatorname{effect}$	se	p-value	lower	upper
AUC with 5 samples	1715.996	594.288	0.006	519.755	2912.237
AUC with 3 samples	1676.618	646.631	0.013	375.019	2978.218
LM with 3 samples	1716.492	656.861	0.012	393.506	3039.478

Table 6: Estimate association between the AUCi and DASB adjusted for age and MDMA.

## 8 References

- Fekedulegn, D. B., Andrew, M. E., Burchfiel, C. M., Violanti, J. M., Hartley, T. A., Charles, L. E., and Miller, D. B. (2007). Area under the curve and other summary indicators of repeated waking cortisol measurements. *Psychosomatic medicine*, 69(7):651–659.
- Jakobsen, G. R., Fisher, P. M., Dyssegaard, A., McMahon, B., Holst, K. K., Lehel, S., Svarer, C., Jensen, P. S., Knudsen, G. M., and Frokjaer, V. G. (2016). Brain serotonin 4 receptor binding is associated with the cortisol awakening response. *Psychoneuroendocrinology*, 67:124–132.

## Appendix A Appendix: Excluded subjects

#### Id's of the excluded individual

```
id.rm

$interval.awaket0
```

```
[1] "50473"
               "50542"
                          "52514_I1" "11128"
                                                "50219"
 [7] "50753"
              "51738_I2" "51995_I1" "52168_I2" "52463_I3" "52645_I2"
[13] "52687_I1" "52698_I1" "53566"
                                     "55815"
$interval.t0t15
[1] "52514_I1" "53100_I1" "52184"
                                    "52391_I2" "52594"
                                                          "52690_I2" "53809"
[8] "55059"
$interval.t15t30
 [1] "52185_I1" "52391_I2" "10909"
                                     "10999"
                                                         "30048"
                                                "11041"
              "50127_I1" "50276"
 [7] "30156"
                                     "50682"
                                                "51756_I1" "52115_I1"
[13] "52495_I1" "52594"
                          "53010_I1" "53350"
                                                "53619"
                                                           "53882"
[19] "53888_I2" "55796_I2"
$interval.t30t45
 [1] "50798_I2" "55264"
                           "11041"
                                     "11092"
                                                "11140_I3" "30156"
 [7] "50217" "50276"
                          "51411_I1" "51745"
                                                "51918 I2" "52235 I2"
[13] "52470_I2" "52579_I1" "52661_I2" "52687_I2" "53882"
                                                           "55777 I1"
$interval.t45t60
 [1] "50752_I2" "53062_I2" "53639"
                                                "11083"
                                      "10960"
                                                           "30156"
 [7] "50276"
                                      "50705_I1" "51749_I1" "52104_I1"
              "50327"
                          "50682"
                          "52690_I1" "52704_I1" "52711"
                                                           "53103_I3"
[13] "52151_I2" "52621"
[19] "53122_I3" "53595"
                          "53882"
                                     "55121"
                                                "55264"
$na.cortisol
 [1] "10987"
               "11077"
                          "11080"
                                     "11083"
                                                "11086"
                                                           "11092"
                                                "30054"
 [7] "11101"
               "11104"
                          "30003"
                                     "30006"
                                                           "30066"
               "50073_I2" "50219"
[13] "30141"
                                     "50228"
                                                "50288_I2" "50315"
[19] "50318"
               "50330"
                          "50336"
                                      "50462"
                                                "50489_I1" "50516_I1"
[25] "50670"
               "50681_I1" "50769"
                                      "50798 I1" "51745"
                                                           "51798 I2"
[31] "51995_I2" "52030_I1" "52085_I2" "52115_I2" "52145_I3" "52151_I2"
[37] "52190_I2" "52412_I3" "52435_I2" "52460"
                                                "52550"
                                                           "53103_I3"
                                                "53215_I3" "53215_I4"
[43] "53103_I4" "53127_I3" "53127_I4" "53206"
[49] "53217_I3" "53217_I4" "53259"
                                      "53304"
                                                "53305"
                                                           "53336"
[55] "53443"
               "53505"
                          "53512"
                                     "53532"
                                                "53545"
                                                           "53548"
[61] "53553"
                                                "53716" "53777"
               "53569"
                          "53704"
                                     "53705"
[67] "53814"
               "53888_I3" "55032"
                                     "55065"
                                                "55072_I2" "55142"
               "55738_I2" "55777_I1" "55792_I1" "55811" "55999_I2"
[73] "55184"
[79] "56008"
               "56046_I1" "56111_I1" "56137_I2" "56216_I1" "56220_I2"
```

```
[85] "56233_I2" "56288"

$na.time

[1] "50463" "50465" "50473" "50507_I1" "50507_I2" "50514_I3"

[7] "50743_I2" "50778_I1" "50822_I2" "51745" "51939_I2" "52046_I2"

[13] "52085_I1" "52085_I2" "52470_I2" "52523" "52579_I2" "52632_I3"

[19] "53100_I3" "53247" "56103_I1"
```

**Note**: for some patient the value of  $AUC_g$  is missing even though there are all cortisol measurements, e.g.:

```
date time_wake AUCg
        id2
1:
     50058 19/11/2008
                        9:30:00
                                   NA
2:
     50294 20/01/2010
                       7:15:00
                                   NA
     52041 11/01/2012 12:00:00
3:
                                   NA
4: 52690_I3 22/05/2013
                       6:40:00
                                   NA
5: 53009_I3 20/06/2013
                       8:00:00
                                   NA
6:
     56177 15/11/2018
                       7:15:00
                                   NA
        id2 time_t0 time_t15 time_t30 time_t45 time_t60
     50058 9:45:00 10:05:00 10:22:00 10:38:00 10:55:00
1:
2:
     50294 7:30:00 7:45:00 8:00:00 8:15:00 8:30:00
3:
      52041 12:15:00 12:30:00 12:45:00 13:00:00 13:15:00
4: 52690_I3 6:52:00 7:08:00 7:23:00 7:38:00 7:55:00
5: 53009_I3 8:15:00 8:30:00 8:45:00 9:00:00 9:15:00
6:
      56177 7:30:00 7:45:00 8:00:00 8:15:00 8:30:00
        id2 cortisol_t0 cortisol_t15 cortisol_t30 cortisol_t45 cortisol_t60
                                             3.04
1:
     50058
                   4.60
                                4.80
                                                          3.55
                                                                       3.11
2:
     50294
                   8.76
                                            24.92
                               18.38
                                                         27.09
                                                                      18.09
3:
     52041
                 11.08
                                            11.91
                                                         11.75
                                                                       9.34
                               11.60
4: 52690_I3
                                                                      22.79
                 17.66
                               24.80
                                            22.64
                                                         21.69
5: 53009<sub>I</sub>3
                                            11.78
                                                         16.48
                                                                       9.65
                  21.65
                               12.79
6:
      56177
                   5.55
                                4.73
                                            17.22
                                                         14.64
                                                                      13.52
```

Is that voluntary? Can I use the cortisol values?

## Appendix B Appendix: calculation of the CAR using the trapezoidal rule

#### B.1 AUCg

For subjects with regular measurement times, e.g.:

the  $AUC_g$  can be computed as a weighted average of the cortisol measurement with weights 7.5, 15, 15, 15, 7.5:

```
3.2 * 7.5 + 8.8 * 15 + 5.6 *15 + 4.2 * 15 + 3.3 * 7.5
```

#### [1] 327.75

We can check the result using the **trapz** function from the *pracma* package in R:

```
trapz(x = c(0,15,30,45,60), y = c(3.2,8.8,5.6,4.2,3.3))
```

#### [1] 327.75

For subjects with irregular measurement times, e.g.:

```
dtW.fulldata[1, .SD, .SDcols = keep.col]
```

the weights need to be adapted. The correct weights correspond to half of the time interval on each side of the measurement:

```
8.9 * (14/2) + 5.3 * (14+15)/2 + 8.4 * (15+15)/2 + 3.6 * (15+15)/2 + 6.3 * 15/2
```

```
[1] 366.4
```

```
trapz(x = c(0,14,29,44,59), y = c(8.9, 5.3, 8.4, 3.6, 6.3))
```

#### [1] 366.4

Thus over all patients we get the same AUCg as the one of the database

```
range(dtLR.HC$AUCg-dtLR.HC$AUCg.pracma, na.rm=TRUE)
```

```
[1] -1.023182e-12 1.023182e-12
```

#### B.2 AUCb

Consider the individual:

```
id cortisol_t0 time_t0 time_t15 time_t30 time_t45 time_t60 AUCb
1: 10837 3.2 7:10:00 7:25:00 7:40:00 7:55:00 8:10:00 135.75
```

that has had taken cortisol measurements during 1h. His area under the curve with respect to the baseline should therefore be:

```
3.2*60
```

#### [1] 192

The database value is difference, 135.75 because it is treated as special case since the CAR measurement are not monotonically increasing over time. This however somehow does not impact the AUCi:

```
range(dtLR.HC$AUCi-dtLR.HC$AUCi.pracma, na.rm=TRUE)
```

```
[1] -1.023182e-12 1.023182e-12
```

## Appendix C Appendix: bias-correction using the linear regression

### C.1 Example

We start with an example. Consider the following individual:

```
dtW.HC[id2=="11008"]
```

```
id id2 AUCg AUCg.pracma c0 c15 c30 c45 c60
1: 11008 11008 141.75 141.75 2.8 1.8 2.9 2.1 2.5
```

who perfectly followed the measurement schedule. His  $AUC_g$  with respect to the ground is:

```
GS <- 2.8 * 7.5 + 1.8 * 15 + 2.9 * 15 + 2.1 * 15 + 2.5 * 7.5
GS
```

#### [1] 141.75

But if we would take only the first three samples we would get:

```
estimate <- 2.8 * 7.5 + 1.8 * 15 + 2.9 * 7.5 estimate
```

#### [1] 69.75

which is way too low. Fortunately we can use the correction proposed in Table 2:

```
estimate + 48.96 + 0.01 * 2.8 * 7.5 + 0.07 * 1.8 * 15 + 3.14 * 2.9 * 7.5
```

#### [1] 189.105

While not perfect, the is much closer to the value obtained with 5 samples.

## C.2 Theory

Consider:

- 3 cortisol measurements  $X_1$ ,  $X_2$ ,  $X_3$ , at time 0,  $t_1$ , and  $t_2$ .
- the 5-sample  $AUC_G$ .
- weights corresponding to the time intervals, i.e.  $w_1 = \frac{t_1}{2}$ ,  $w_1 = \frac{t_2}{2}$ , and  $w_3 = \frac{t_2-t_1}{2}$ .

The  $AUC_G$  can be computed as:

$$\widetilde{AUC}_G = w_1 * X_1 + w_2 * X_2 + w_3 * X_3$$

A more flexible approach would be to estimate it as:

$$\widehat{AUC}_G = \alpha + \beta_1 * w_1 * X_1 + \beta_2 * w_2 * X_2 + \beta_3 * w_3 * X_3$$

where  $\alpha$ ,  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$  are estimated based on the data to minimize the average squared difference between the 5-sample AUC and the estimated one.

For instance imagine that the cortisol value is constant over time. Then the area below the curve from 0 to 30 is half of the area below the curve from 0 to 60. Choosing  $\alpha = 0$  and  $\beta_1 = \beta_2 = \beta_3$  leads to:

$$\widehat{AUC}_G = 2 * \widehat{AUC}_G$$

which fixes the problem.