Supplementary Materials for Planning PEV Fast-Charging Stations Using Data-Driven Distributionally Robust Optimization Approach Based on ϕ -divergence

Abstract

The parameters of transportation network and distribution network are presented. The first two sections present the parameters of transportation network, the last section presents the parameters of distribution network.

I. THE PARAMETERS OF TRANSPORTATION NETWORK

The parameters of transportation network are generated by employing the data presented in [1].

TABLE I LINK DISTANCES FOR SIOUX FALLS NETWORK.

| Link | Length (km) | Link | Length (km) |
|-------------------|-------------|-------------------|-------------|
| (1,2)/(2,1) | 60 | (1,3)/(3,1) | 40 |
| (3,4)/(4,3) | 40 | (4,5)/(5,4) | 20 |
| (4,11)/(11,4) | 60 | (5,6)/(6,5) | 40 |
| (6,8)/(8,6) | 20 | (7,8)/(8,7) | 30 |
| (8,9)/(9,8) | 100 | (8, 16)/(16, 8) | 50 |
| (10, 11)/(11, 10) | 50 | (10, 15)/(10, 15) | 60 |
| (10, 17)/(17, 10) | 60 | (11, 12)/(12, 11) | 60 |
| (12, 13)/(13, 12) | 30 | (13, 24)/(24, 13) | 40 |
| (14, 23)/(23, 14) | 40 | (15, 19)/(19, 15) | 30 |
| (16, 17)/(17, 16) | 20 | (16, 18)/(18, 16) | 30 |
| (18, 20)/(20, 18) | 40 | (19, 20)/(19, 20) | 40 |
| (20, 22)/(22, 20) | 50 | (21, 22)/(22, 21) | 30 |
| (22, 23)/(23, 22) | 40 | (23, 24)/(24, 23) | 20 |
| (2,6)/(6,2) | 60 | (4,5)/(5,4) | 20 |
| (5,9)/(9,5) | 50 | (7, 18)/(18, 7) | 20 |
| (9,10)/(10,9) | 30 | (10, 16)/(16, 10) | 40 |
| (11, 14)/(14, 11) | 40 | (14, 15)/(15, 14) | 50 |
| (15, 22)/(22, 15) | 30 | (17, 19)/(19, 17) | 20 |
| (20, 21)/(21, 20) | 60 | (21, 24)/(24, 21) | 30 |
| (23, 24)/(24, 23) | 20 | | |

II. PEV flows over entire TN

 $\begin{tabular}{ll} TABLE \ II \\ Type \ 1 \ PEV \ flows \ between \ O-D \ pairs \ over \ 34 \ minutes. \end{tabular}$

| O-D pairs | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
|-----------|-----------|---------|---------|-----------|----------|----------|-----------|-----------|-----------|------------|------------|------------|------------|------------|------------|-----------|-----------|----------|-----------|------------|------------|------------|-----|----------|
| 1 | 0 | 25 | 25 | 125 | 50 | 75 | 125 | 200 | 125 | 325 | 125 | 50 | 125 | 75 | 0 | 125 | 100 | 25 | 75 | 75 | 25 | 100 | 75 | 25 |
| 2 | 25 | 0 | 25 | 50 | 25 | 100 | 50 | 100 | 50 | 150 | 50 | 25 | 75 | 25 | 25 | 100 | 50 | 0 | 25 | 25 | 0 | 25 | 0 | 0 |
| 3 | 25 | 25 | 0 | 50 | 25 | 75 | 25 | 50 | 25 | 75 | 75 | 50 | 25 | 25 | 25 | 50 | 25 | 0 | 0 | 0 | 0 | 25 | 25 | 0 |
| 4 | 125 | 50 | 50 | 0 | 125 | 100 | 100 | 175 | 175 | 300 | 375 | 150 | 150 | 125 | 125 | 200 | 125 | 25 | 50 | 75 | 50 | 100 | 125 | 50 |
| 5 | 50 | 25 | 25 | 125 | 0 | 50 | 50 | 125 | 200 | 250 | 125 | 50 | 50 | 25 | 50 | 125 | 50 | 0 | 25 | 25 | 25 | 50 | 25 | 0 |
| 6 | 75 | 100 | 75 | 100 | 50 | 0 | 100 | 200 | 100 | 200 | 100 | 50 | 50 | 25 | 50 | 225 | 125 | 25 | 50 | 75 | 25 | 50 | 25 | 25 |
| 7 | 125 | 50 | 25 | 100 | 50 | 100 | 0 | 250 | 150 | 475 | 125 | 175 | 100 | 50 | 125 | 100 | 250 | 50 | 100 | 125 | 50 | 125 | 50 | 25 |
| 8 | 200 | 100 | 50 | 175 | 125 | 200 | 250 | 0 | 200 | 400 | 200 | 150 | 150 | 100 | 150 | 550 | 350 | 75 | 175 | 225 | 100 | 125 | 75 | 50 |
| 9 | 125 | 50 | 25 | 175 | 200 | 100 | 150 | 200 | 0 | 700 | 350 | 150 | 150 | 150 | 250 | 350 | 225 | 50 | 100 | 150 | 75 | 175 | 125 | 50 |
| 10 | 325 | 150 | 75 | 300 | 250 | 200 | 475 | 400 | 700 | 0 | 975 | 500 | 475 | 525 | 1000 | 1100 | 975 | 175 | 450 | 625 | 300 | 650 | 450 | 200 |
| 11 | 125 | 50 | 75 | 350 | 125 | 100 | 125 | 200 | 350 | 1000 | 0 | 350 | 250 | 400 | 350 | 350 | 250 | 50 | 100 | 150 | 100 | 275 | 325 | 150 |
| 12 | 50 | 25 | 50 | 150 | 50 | 50 | 175 | 150 | 150 | 500 | 350 | 0 | 325 | 175 | 175 | 175 | 150 | 50 | 75 | 125 | 75 | 175 | 175 | 125 |
| 13 | 125 | 75 | 25 | 150 | 50 | 50 | 100 | 150 | 150 | 475 | 250 | 325 | 0 | 150 | 175 | 150 | 125 | 25 | 75 | 150 | 150 | 325 | 200 | 175 |
| 14 | 75 | 25 | 25 | 125 | 25 | 25 | 50 | 100 | 150 | 525 | 400 | 175 | 150 | 0 | 325 | 175 | 175 | 25 | 75 | 125 | 100 | 300 | 275 | 100 |
| 15 | 0 | 25 | 25 | 125 | 50 | 50 | 125 | 150 | 225 | 1000 | 350 | 175 | 175 | 325 | 0 | 300 | 375 | 50 | 200 | 275 | 200 | 650 | 250 | 100 |
| 16 | 125 | 100 | 50 | 200 | 125 | 225 | 350 | 550 | 350 | 1100 | 350 | 175 | 150 | 175 | 300 | 0 | 700 | 125 | 325 | 400 | 150 | 300 | 125 | 75 |
| 17 | 100 | 50 | 25 | 125 | 50 | 125 | 250 | 350 | 225 | 975 | 250 | 150 | 125 | 175 | 375 | 700 | 0 | 150 | 425 | 425 | 150 | 425 | 150 | 75 |
| 18 | 25 | 0 | 0 | 25 | 0 | 25 | 50 | 75 175 | 50 | 175 | 25 | 50 | 25 | 25 | 50 | 125 | 150 | 0 | 75 | 100 | 25 | 75 | 25 | 0 |
| 19 | 75 75 | 25 | 0 | 50 | 25 | 50 | 100 | 175 | 100 | 175 | 100 | 75 | 75 | 75 | 200 | 325 | 425 | 75 | 0 | 300 | 100 | 300 | 75 | 25 |
| 20 | 75 25 | 25 | 0 | 75 50 | 25 | 75 25 | 125 | 225 | 150 | 625 | 150 | 100 | 150 | 125 | 275 | 400 | 425 | 100 | 300 | 0 | 300 | 600 | 175 | 100 |
| 21 | 25 | 0 25 | 0 25 | 50 100 | 25 50 | 25 50 | 50 | 100 | 75 175 | 300 | 100 | 75 175 | 150 | 100 | 200 | 150 | 150 | 25 | 100 | 300 | 0 | 450 | 175 | 125 |
| 22 23 | 100 75 | 0 | 25 | 125 | 25 | 25 | 125 50 | 125 75 | 175 | 650 450 | 275 | 175 | 325 200 | 300 275 | 650 | 300 | 425 | 75 25 | 300 75 | 600 175 | 450 175 | 0 | 525 | 275 |
| 23 24 | 25 | 0 | 0 | 50 | 0 | 25 25 | 25 | 50 | 125 50 | 200 | 325 150 | 175 125 | 200 | 100 | 250 100 | 125 75 | 150 75 | 25 0 | 25 | 100 | 175 | 525 275 | 175 | 175 0 |

| O-D pairs | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
|-----------|-----------|-----|---------|------------|---------|----------|-----------|------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|-----|-----------|------------|------------|------|------|-----|
| 1 | 0 | 50 | 50 | 250 | 100 | 150 | 250 | 400 | 250 | 650 | 250 | 100 | 250 | 150 | 0 | 250 | 200 | 50 | 150 | 150 | 50 | 200 | 150 | 50 |
| 2 | 50 | 0 | 50 | 100 | 50 | 200 | 100 | 200 | 100 | 300 | 100 | 50 | 150 | 50 | 50 | 200 | 100 | 0 | 50 | 50 | 0 | 50 | 0 | 0 |
| 3 | 50 | 50 | 0 | 100 | 50 | 150 | 50 | 100 | 50 | 150 | 150 | 100 | 50 | 50 | 50 | 100 | 50 | 0 | 0 | 0 | 0 | 50 | 50 | 0 |
| 4 | 250 | 100 | 100 | 0 | 250 | 200 | 200 | 350 | 350 | 600 | 750 | 300 | 300 | 250 | 250 | 400 | 250 | 50 | 100 | 150 | 100 | 200 | 250 | 100 |
| 5 | 100 | 50 | 50 | 250 | 0 | 100 | 100 | 250 | 400 | 500 | 250 | 100 | 100 | 50 | 100 | 250 | 100 | 0 | 50 | 50 | 50 | 100 | 50 | 0 |
| 6 | 150 | 200 | 150 | 200 | 100 | 0 | 200 | 400 | 200 | 400 | 200 | 100 | 100 | 50 | 100 | 450 | 250 | 50 | 100 | 150 | 50 | 100 | 50 | 50 |
| 7 | 250 | 100 | 50 | 200 | 100 | 200 | 0 | 500 | 300 | 950 | 250 | 50 | 200 | 100 | 250 | 200 | 500 | 100 | 200 | 250 | 100 | 250 | 100 | 50 |
| 8 | 400 | 200 | 100 | 350 | 250 | 400 | 500 | 0 | 400 | 800 | 400 | 300 | 300 | 200 | 300 | 1100 | 700 | 150 | 350 | 450 | 200 | 250 | 150 | 100 |
| 9 | 250 | 100 | 50 | 350 | 400 | 200 | 300 | 400 | 0 | 1400 | 700 | 300 | 300 | 300 | 500 | 700 | 450 | 100 | 200 | 300 | 150 | 350 | 250 | 100 |
| 10 | 650 | 300 | 150 | 600 | 500 | 400 | 950 | 800 | 1400 | 0 | 1950 | 1000 | 950 | 1050 | 2000 | 2200 | 1950 | 350 | 900 | 1250 | 600 | 1300 | 900 | 400 |
| 11 | 250 | 100 | 150 | 700 | 250 | 200 | 250 | 400 | 700 | 2000 | 0 | 700 | 500 | 800 | 700 | 700 | 500 | 100 | 200 | 300 | 200 | 550 | 650 | 300 |
| 12 | 100 | 50 | 100 | 300 | 100 | 100 | 50 | 300 | 300 | 1000 | 700 | 0 | 650 | 350 | 350 | 350 | 300 | 100 | 150 | 250 | 150 | 350 | 350 | 250 |
| 13 | 250 | 150 | 50 | 300 | 100 | 100 | 200 | 300 | 300 | 950 | 500 | 650 | 0 | 300 | 350 | 300 | 250 | 50 | 150 | 300 | 300 | 650 | 400 | 350 |
| 14 | 150 | 50 | 50 | 250 | 50 | 50 | 100 | 200 | 300 | 1050 | 800 | 350 | 300 | 0 | 650 | 350 | 350 | 50 | 150 | 250 | 200 | 600 | 550 | 200 |
| 15 | 250 | 50 | 50 | 250 | 100 | 100 | 250 | 300 | 450 | 2000 | 700 | 350 | 350 | 650 | 0 | 600 | 750 | 100 | 400 | 550 | 400 | 1300 | 500 | 200 |
| 16 | 250 | 200 | 100 | 400 | 250 | 450 | 700 | 1100 | 700 | 2200 | 700 | 350 | 300 | 350 | 600 | 0 | 1400 | 250 | 650 | 800 | 300 | 600 | 250 | 150 |
| 17 | 200 | 100 | 50 | 250 | 100 | 250 | 500 | 700 | 450 | 1950 | 500 | 300 | 250 | 350 | 750 | 1400 | 0 | 300 | 850 | 850 | 300 | 850 | 300 | 150 |
| 18 | 50 | 0 | 0 | 50 | 0 | 50 | 100 | 150 | 100 | 350 | 50 | 100 | 50 | 50 | 100 | 250 | 300 | 0 | 150 | 200 | 50 | 150 | 50 | 0 |
| 19 | 150 | 50 | 0 | 100 | 50 | 100 | 200 | 350 | 200 | 350 | 200 | 150 | 150 | 150 | 400 | 650 | 850 | 150 | 0 | 600 | 200 | 600 | 150 | 50 |
| 20 | 150 | 50 | 0 | 150 | 50 | 150 | 250 | 450 | 300 | 1250 | 300 | 200 | 300 | 250 | 550 | 800 | 850 | 200 | 600 | 0 | 600 | 1200 | 350 | 200 |
| 21 | 50 | 0 | 0 | 100 | 50 | 50 | 100 | 200 | 150 | 600 | 200 | 150 | 300 | 200 | 400 | 300 | 300 | 50 | 200 | 600 | 0 | 900 | 350 | 250 |
| 22 | 200 | 50 | 50 | 200 | 100 | 100 | 250 | 250 | 350 | 1300 | 550 | 350 | 650 | 600 | 1300 | 600 | 850 | 150 | 600 | 1200 | 900 | 0 | 1050 | 550 |
| 23 24 | 150 50 | 0 | 50 0 | 250 100 | 50 0 | 50 50 | 100 50 | 150 100 | 250 100 | 900 400 | 650 300 | 350 250 | 400 400 | 550 200 | 500 200 | 250 150 | 300 150 | 50 | 150 50 | 350 200 | 350 250 | 1050 | 250 | 350 |
| 24 | 50 | 0 | U | 100 | U | 50 | 50 | 100 | 100 | 400 | 300 | 230 | 400 | 200 | 200 | 130 | 130 | 0 | 50 | 200 | 230 | 550 | 350 | 0 |

| O-D pairs | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
|-----------|-----|----|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 1 | 0 | 15 | 15 | 75 | 30 | 45 | 75 | 120 | 75 | 195 | 75 | 30 | 75 | 45 | 0 | 75 | 60 | 15 | 45 | 45 | 15 | 60 | 45 | 15 |
| 2 | 15 | 0 | 15 | 30 | 15 | 60 | 30 | 60 | 30 | 90 | 30 | 15 | 45 | 15 | 15 | 60 | 30 | 0 | 15 | 15 | 0 | 15 | 0 | 0 |
| 3 | 15 | 15 | 0 | 30 | 15 | 45 | 15 | 30 | 15 | 45 | 45 | 30 | 15 | 15 | 15 | 30 | 15 | 0 | 0 | 0 | 0 | 15 | 15 | 0 |
| 4 | 75 | 30 | 30 | 0 | 75 | 60 | 60 | 105 | 105 | 180 | 225 | 90 | 90 | 75 | 75 | 120 | 75 | 15 | 30 | 45 | 30 | 60 | 75 | 30 |
| 5 | 30 | 15 | 15 | 75 | 0 | 30 | 30 | 75 | 120 | 150 | 75 | 30 | 30 | 15 | 30 | 75 | 30 | 0 | 15 | 15 | 15 | 30 | 15 | 0 |
| 6 | 45 | 60 | 45 | 60 | 30 | 0 | 60 | 120 | 60 | 120 | 60 | 30 | 30 | 15 | 30 | 135 | 75 | 15 | 30 | 45 | 15 | 30 | 15 | 15 |
| 7 | 75 | 30 | 15 | 60 | 30 | 60 | 0 | 150 | 90 | 285 | 75 | 105 | 60 | 30 | 75 | 60 | 150 | 30 | 60 | 75 | 30 | 75 | 30 | 15 |
| 8 | 120 | 60 | 30 | 105 | 75 | 120 | 150 | 0 | 120 | 240 | 120 | 90 | 90 | 60 | 90 | 330 | 210 | 45 | 105 | 135 | 60 | 75 | 45 | 30 |
| 9 | 75 | 30 | 15 | 105 | 120 | 60 | 90 | 120 | 0 | 420 | 210 | 90 | 90 | 90 | 150 | 210 | 135 | 30 | 60 | 90 | 45 | 105 | 75 | 30 |
| 10 | 195 | 90 | 45 | 180 | 150 | 120 | 285 | 240 | 420 | 0 | 585 | 300 | 285 | 315 | 600 | 660 | 585 | 105 | 270 | 375 | 180 | 390 | 270 | 120 |
| 11 | 75 | 30 | 45 | 210 | 75 | 60 | 75 | 120 | 210 | 600 | 0 | 210 | 150 | 240 | 210 | 210 | 150 | 30 | 60 | 90 | 60 | 165 | 195 | 90 |
| 12 | 30 | 15 | 30 | 90 | 30 | 30 | 105 | 90 | 90 | 300 | 210 | 0 | 195 | 105 | 105 | 105 | 90 | 30 | 45 | 75 | 45 | 105 | 105 | 75 |
| 13 | 75 | 45 | 15 | 90 | 30 | 30 | 60 | 90 | 90 | 285 | 150 | 195 | 0 | 90 | 105 | 90 | 75 | 15 | 45 | 90 | 90 | 195 | 120 | 105 |
| 14 | 45 | 15 | 15 | 75 | 15 | 15 | 30 | 60 | 90 | 315 | 240 | 105 | 90 | 0 | 195 | 105 | 105 | 15 | 45 | 75 | 60 | 180 | 165 | 60 |
| 15 | 0 | 15 | 15 | 75 | 30 | 30 | 75 | 90 | 135 | 600 | 210 | 105 | 105 | 195 | 0 | 180 | 225 | 30 | 120 | 165 | 120 | 390 | 150 | 60 |
| 16 | 75 | 60 | 30 | 120 | 75 | 135 | 210 | 330 | 210 | 660 | 210 | 105 | 90 | 105 | 180 | 0 | 420 | 75 | 195 | 240 | 90 | 180 | 75 | 45 |
| 17 | 60 | 30 | 15 | 75 | 30 | 75 | 150 | 210 | 135 | 585 | 150 | 90 | 75 | 105 | 225 | 420 | 0 | 90 | 255 | 255 | 90 | 255 | 90 | 45 |
| 18 | 15 | 0 | 0 | 15 | 0 | 15 | 30 | 45 | 30 | 105 | 15 | 30 | 15 | 15 | 30 | 75 | 90 | 0 | 45 | 60 | 15 | 45 | 15 | 0 |
| 19 | 45 | 15 | 0 | 30 | 15 | 30 | 60 | 105 | 60 | 105 | 60 | 45 | 45 | 45 | 120 | 195 | 255 | 45 | 0 | 180 | 60 | 180 | 45 | 15 |
| 20 | 45 | 15 | 0 | 45 | 15 | 45 | 75 | 135 | 90 | 375 | 90 | 60 | 90 | 75 | 165 | 240 | 255 | 60 | 180 | 0 | 180 | 360 | 105 | 60 |
| 21 | 15 | 0 | 0 | 30 | 15 | 15 | 30 | 60 | 45 | 180 | 60 | 45 | 90 | 60 | 120 | 90 | 90 | 15 | 60 | 180 | 0 | 270 | 105 | 75 |
| 22 | 60 | 15 | 15 | 60 | 30 | 30 | 75 | 75 | 105 | 390 | 165 | 105 | 195 | 180 | 390 | 180 | 255 | 45 | 180 | 360 | 270 | 0 | 315 | 165 |
| 23 | 45 | 0 | 15 | 75 | 15 | 15 | 30 | 45 | 75 | 270 | 195 | 105 | 120 | 165 | 150 | 75 | 90 | 15 | 45 | 105 | 105 | 315 | 0 | 105 |
| 24 | 15 | 0 | 0 | 30 | 0 | 15 | 15 | 30 | 30 | 120 | 90 | 75 | 120 | 60 | 60 | 45 | 45 | 0 | 15 | 60 | 75 | 165 | 105 | 0 |

 $\label{table V} TABLE\ V$ Type 4 PEV flows between O-D pairs over 46 minutes.

| O-D pairs | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
|-----------|-----|----|----|-----|-----|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|----|-----|-----|-----|-----|-----|-----|
| 1 | 0 | 10 | 10 | 50 | 20 | 30 | 50 | 80 | 50 | 130 | 50 | 20 | 50 | 30 | 0 | 50 | 40 | 10 | 30 | 30 | 10 | 40 | 30 | 10 |
| 2 | 10 | 0 | 10 | 20 | 10 | 40 | 20 | 40 | 20 | 60 | 20 | 10 | 30 | 10 | 10 | 40 | 20 | 0 | 10 | 10 | 0 | 10 | 0 | 0 |
| 3 | 10 | 10 | 0 | 20 | 10 | 30 | 10 | 20 | 10 | 30 | 30 | 20 | 10 | 10 | 10 | 20 | 10 | 0 | 0 | 0 | 0 | 10 | 10 | 0 |
| 4 | 50 | 20 | 20 | 0 | 50 | 40 | 40 | 70 | 70 | 120 | 150 | 60 | 60 | 50 | 50 | 80 | 50 | 10 | 20 | 30 | 20 | 40 | 50 | 20 |
| 5 | 20 | 10 | 10 | 50 | 0 | 20 | 20 | 50 | 80 | 100 | 50 | 20 | 20 | 10 | 20 | 50 | 20 | 0 | 10 | 10 | 10 | 20 | 10 | 0 |
| 6 | 30 | 40 | 30 | 40 | 20 | 0 | 40 | 80 | 40 | 80 | 40 | 20 | 20 | 10 | 20 | 90 | 50 | 10 | 20 | 30 | 10 | 20 | 10 | 10 |
| 7 | 50 | 20 | 10 | 40 | 20 | 40 | 0 | 100 | 60 | 190 | 50 | 70 | 40 | 20 | 50 | 40 | 100 | 20 | 40 | 50 | 20 | 50 | 20 | 10 |
| 8 | 80 | 40 | 20 | 70 | 50 | 80 | 100 | 0 | 80 | 160 | 80 | 60 | 60 | 40 | 60 | 220 | 140 | 30 | 70 | 90 | 40 | 50 | 30 | 20 |
| 9 | 50 | 20 | 10 | 70 | 80 | 40 | 60 | 80 | 0 | 280 | 140 | 60 | 60 | 60 | 100 | 140 | 90 | 20 | 40 | 60 | 30 | 70 | 50 | 20 |
| 10 | 130 | 60 | 30 | 120 | 100 | 80 | 190 | 160 | 280 | 0 | 390 | 200 | 190 | 210 | 400 | 440 | 390 | 70 | 180 | 250 | 120 | 260 | 180 | 80 |
| 11 | 50 | 20 | 30 | 140 | 50 | 40 | 50 | 80 | 140 | 400 | 0 | 140 | 100 | 160 | 140 | 140 | 100 | 20 | 40 | 60 | 40 | 110 | 130 | 60 |
| 12 | 20 | 10 | 20 | 60 | 20 | 20 | 70 | 60 | 60 | 200 | 140 | 0 | 130 | 70 | 70 | 70 | 60 | 20 | 30 | 50 | 30 | 70 | 70 | 50 |
| 13 | 50 | 30 | 10 | 60 | 20 | 20 | 40 | 60 | 60 | 190 | 100 | 130 | 0 | 60 | 70 | 60 | 50 | 10 | 30 | 60 | 60 | 130 | 80 | 70 |
| 14 | 30 | 10 | 10 | 50 | 10 | 10 | 20 | 40 | 60 | 210 | 160 | 70 | 60 | 0 | 130 | 70 | 70 | 10 | 30 | 50 | 40 | 120 | 110 | 40 |
| 15 | 0 | 10 | 10 | 50 | 20 | 20 | 50 | 60 | 90 | 400 | 140 | 70 | 70 | 130 | 0 | 120 | 150 | 20 | 80 | 110 | 80 | 260 | 100 | 40 |
| 16 | 50 | 40 | 20 | 80 | 50 | 90 | 140 | 220 | 140 | 440 | 140 | 70 | 60 | 70 | 120 | 0 | 280 | 50 | 130 | 160 | 60 | 120 | 50 | 30 |
| 17 | 40 | 20 | 10 | 50 | 20 | 50 | 100 | 140 | 90 | 390 | 100 | 60 | 50 | 70 | 150 | 280 | 0 | 60 | 170 | 170 | 60 | 170 | 60 | 30 |
| 18 | 10 | 0 | 0 | 10 | 0 | 10 | 20 | 30 | 20 | 70 | 10 | 20 | 10 | 10 | 20 | 50 | 60 | 0 | 30 | 40 | 10 | 30 | 10 | 0 |
| 19 | 30 | 10 | 0 | 20 | 10 | 20 | 40 | 70 | 40 | 70 | 40 | 30 | 30 | 30 | 80 | 130 | 170 | 30 | 0 | 120 | 40 | 120 | 30 | 10 |
| 20 | 30 | 10 | 0 | 30 | 10 | 30 | 50 | 90 | 60 | 250 | 60 | 40 | 60 | 50 | 110 | 160 | 170 | 40 | 120 | 0 | 120 | 240 | 70 | 40 |
| 21 | 10 | 0 | 0 | 20 | 10 | 10 | 20 | 40 | 30 | 120 | 40 | 30 | 60 | 40 | 80 | 60 | 60 | 10 | 40 | 120 | 0 | 180 | 70 | 50 |
| 22 | 40 | 10 | 10 | 40 | 20 | 20 | 50 | 50 | 70 | 260 | 110 | 70 | 130 | 120 | 260 | 120 | 170 | 30 | 120 | 240 | 180 | 0 | 210 | 110 |
| 23 | 30 | 0 | 10 | 50 | 10 | 10 | 20 | 30 | 50 | 180 | 130 | 70 | 80 | 110 | 100 | 50 | 60 | 10 | 30 | 70 | 70 | 210 | 0 | 70 |
| 24 | 10 | 0 | 0 | 20 | 0 | 10 | 10 | 20 | 20 | 80 | 60 | 50 | 80 | 40 | 40 | 30 | 30 | 0 | 10 | 40 | 50 | 110 | 70 | 0 |

III. THE PARAMETERS OF DISTRIBUTION NETWORK

The PG&E static residential and commercial profiles [2] are employed to generate 24 representative scenarios, that is, annual weekdays and weekends of two types of load profiles, which are shown in Figure 1 and Figure 2.

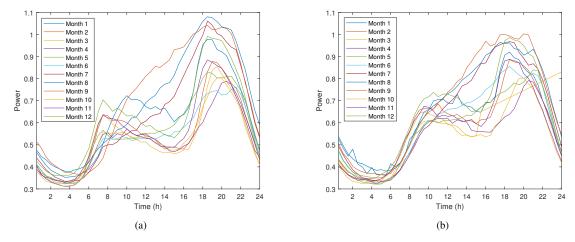
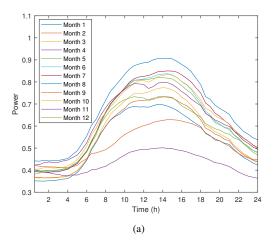


Fig. 1. Resident load profiles. (a). Weekday load profiles. (b). Weekend load profiles.



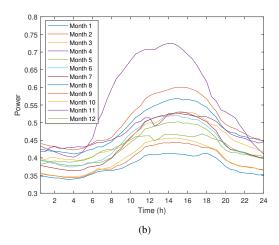


Fig. 2. Commercial load profiles. (a). Weekday load profiles. (b). Weekend load profiles.

Then the DN load at each bus i can be calculated as follows:

$$L_i(\omega,t) = \bar{L}_i \times \left(\alpha_i^{Res} \times L_i^{Res}(\omega,t) + \alpha_i^{Com} \times L_i^{Com}(\omega,t)\right),$$

where, \bar{L}_i is the summation of active load, reactive load and compensation given in Table 4, which is the peak load in a day. α_i^{Res} and α_i^{Com} are representatively the load component ratio of residential and commercial loads given in Table 4. $L_i^{Res}(\omega,t)$ and $L_i^{Com}(\omega,t)$ are respectively the corresponding per-unit load profiles of each scenario.

 $TABLE\ VI \\ Branch parameters of the distribution network.$

| Branch ID | From Bus | To Bus | Length (km) | R (p.u.) | X (p.u.) | Capacity (MVA) |
|-----------|----------|--------|-------------|----------|----------|----------------|
| 1 | 1 | 2 | 30 | 0.0317 | 0.0760 | 200.0 |
| 2 | 1 | 3 | 70 | 0.0739 | 0.1774 | 200.0 |
| 3 | 1 | 4 | 20 | 0.0211 | 0.0507 | 200.0 |
| 4 | 2 | 5 | 110 | 0.1793 | 0.2870 | 108.0 |
| 5 | 2 | 6 | 70 | 0.1952 | 0.1913 | 101.2 |
| 6 | 5 | 7 | 60 | 0.1674 | 0.1640 | 101.2 |
| 7 | 3 | 8 | 50 | 0.0815 | 0.1305 | 108.0 |
| 8 | 8 | 9 | 30 | 0.0837 | 0.0820 | 101.2 |
| 9 | 8 | 10 | 40 | 0.1116 | 0.1093 | 101.2 |
| 10 | 3 | 11 | 60 | 0.1674 | 0.1640 | 101.2 |
| 11 | 4 | 12 | 40 | 0.1116 | 0.1093 | 101.2 |
| 12 | 4 | 13 | 80 | 0.1304 | 0.2088 | 108 |
| 13 | 13 | 14 | 60 | 0.1674 | 0.1640 | 101.2 |
| | | | | | | |

TABLE VII

LOAD DATA OF THE DISTRIBUTION NETWORK.

| Bus ID | Active load | Reactive load | Reactive compensation | Load component (%) | | | | | |
|--------|-------------|---------------|-----------------------|--------------------|------------|--|--|--|--|
| Bus ID | (MW) | (MVAR) | (MVAR) | Residential | Commercial | | | | |
| 1 | 0 | 0 | 0 | 0 | 0 | | | | |
| 2 | 50.0000 | 16.8200 | 0 | 40 | 60 | | | | |
| 3 | 21.0000 | 12.7067 | 0 | 40 | 60 | | | | |
| 4 | 37.8750 | 15.6875 | 0 | 40 | 60 | | | | |
| 5 | 23.0000 | 13.5000 | 0.4688 | 40 | 60 | | | | |
| 6 | 33.0000 | 9.8125 | 0.9900 | 50 | 50 | | | | |
| 7 | 25.1205 | 7.2500 | 0 | 50 | 50 | | | | |
| 8 | 26.3750 | 9.6250 | 2.2500 | 60 | 40 | | | | |
| 9 | 28.4375 | 5.7500 | 6.3750 | 60 | 40 | | | | |
| 10 | 24.1250 | 6.1875 | 1.1250 | 60 | 40 | | | | |
| 11 | 23.8750 | 12.6875 | 3.3750 | 70 | 30 | | | | |
| 12 | 50.8750 | 11.3125 | 0 | 70 | 30 | | | | |
| 13 | 28.8750 | 10.6875 | 0 | 30 | 70 | | | | |
| 14 | 46.9375 | 10.8750 | 3.3750 | 30 | 70 | | | | |

References

^[1] H. Bar-Gera, "Transportation Networks for Research". [Online]. Available: https://github.com/bstabler/TransportationNetworks, accessed Nov. 14, 2018.

^[2] PG&E. "2000 static load profiles", [Online]. Available: https://www.pge.com/nots/rates/2000_static.shtml, accessed December 5, 2019.