

3. (45 points) Language **L** is simplified propositional logic for the purpose of writing logical formulas as programs. In this question you will design an LL parser for it.

It has two connectives  $\Rightarrow$ ,  $\neg$  (implication and negation), to build complex logical formulas. Both connectives are right-associative.

Proposition names are single letters (proposition letters).

1 (true) and 0 (false) are constant formulas of **L**.

Negation has higher precedence than implication. Formulas can be parenthesized, which has the highest precedence.

An **L** program is a sequence of definitions in the form of

```
x = formula
```

followed by a single `formula`, which is executed.

`x` is a name standing for the entire formula on the right hand side, and `formula` is a propositional formula.

The use of a propositional letter on the right side of a definition is meant to be substituted with its definition during execution. For example

```
x = 0 => 1
y = x => 1
¬y => x => 1
```

executes the propositional formula  $\neg((0 \Rightarrow 1) \Rightarrow 1) \Rightarrow ((0 \Rightarrow 1) \Rightarrow 1)$  as a program.

**i)** Show your FIRST and FOLLOW sets for the grammar you designed for **L**.

**ii)** Design an LL parsing table for **L**, with one-symbol lookahead. Assume that a tokenizer returns atomic tokens.

[hint: 4 grammar variables (yes, four) are enough to describe a grammar of **L**.]

**iii)** Show the sequential derivation of the example above using your LL table.