

DM Assignment 1

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1. The optimal price for selling car seats in a “good” location at a cost \$55 to make is \$163.63.
2. The optimal price for selling car seats in a “bad” location at a cost \$55 to make is \$135.07.

3. Good Location

##	Cost	Optimal Price
## A	40.00	156.13
## B	45.00	158.63
## C	50.00	161.13
## D	55.00	163.63
## E	60.00	166.13
## F	65.00	168.63
## G	70.00	171.13
## H	75.00	173.63
## I	80.00	176.13
## J	85.00	178.63

Bad Location

4.	Cost	Optimal Price
## A	40.00	127.57
## B	45.00	130.07
## C	50.00	132.57
## D	55.00	135.07
## E	60.00	137.57
## F	65.00	140.07
## G	70.00	142.57
## H	75.00	145.07
## I	80.00	147.57
## J	85.00	150.07

Uploading dataset

```
library(ISLR)
SafeBabies <- Carseats[,c(1,6,7)]
```

Split the data by Shelf Location

```
SafeBabies_Split <- split(SafeBabies, SafeBabies$ShelveLoc)
SafeBabies_Bad <- SafeBabies_Split$Bad
SafeBabies_Good <- SafeBabies_Split$Good
```

Creating best fit line

```
ols_bad <- lm(Sales ~ Price, data = SafeBabies_Bad)
ols_good <- lm(Sales ~ Price, data = SafeBabies_Good)
ols_bad

##
## Call:
## lm(formula = Sales ~ Price, data = SafeBabies_Bad)
##
## Coefficients:
## (Intercept)      Price
##    11.83298    -0.05522

ols_good

##
## Call:
## lm(formula = Sales ~ Price, data = SafeBabies_Good)
##
## Coefficients:
## (Intercept)      Price
##    17.96886    -0.06578
```

Plot Bad Location Regression Model

```
plot (SafeBabies_Bad$Sales ~ SafeBabies_Bad$Price,
      main = "Bad Location Regression Model",
      xlab = "Price",
      ylab = "Sales",
      pch = 18,
      col = "red" )

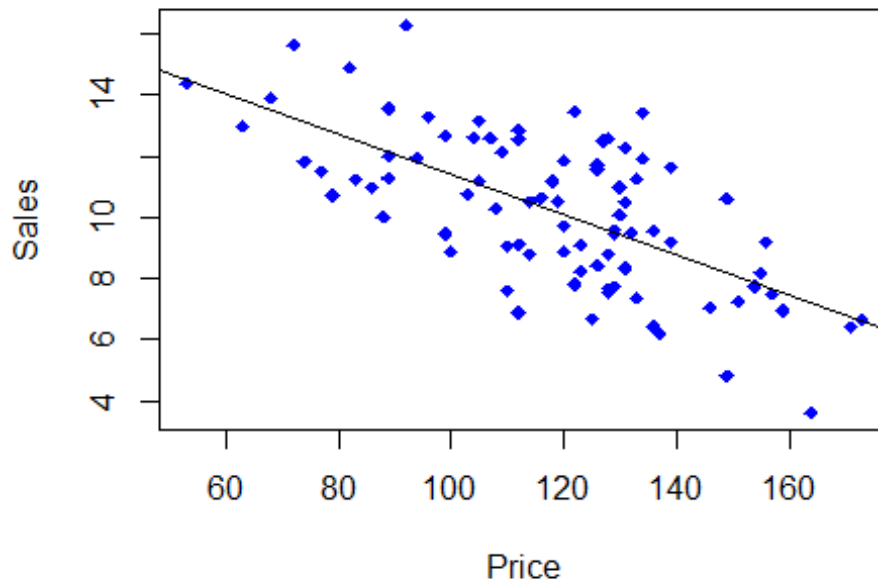
abline(ols_bad)
```



Plot Good Location Regression Model

```
plot (SafeBabies_Good$Sales ~ SafeBabies_Good$Price,  
      main = "Good Location Regression Model",  
      xlab = "Price",  
      ylab = "Sales",  
      pch = 18,  
      col = "blue" )  
  
abline(ols_good)
```

Good Location Regression Model



Optimal Prices for Bad Location Car Seats

```

optimal_bad_prices <- matrix(c(40,127.57,45,130.07,50,132.57,55,135.07,60,137.57,65,140.07,70,142.57,75,145.07,80,147.57,85,150.07),ncol=2,byrow=TRUE)

bad_location_cost <- c(40,45,50,55,60,65,70,75,80,85)
bad_location_prices <- c(127.57,130.07,132.57,135.07,137.57,140.07,142.57,145.07,147.57,150.07)
ols_bad_optimal <- lm( bad_location_cost ~ bad_location_prices )

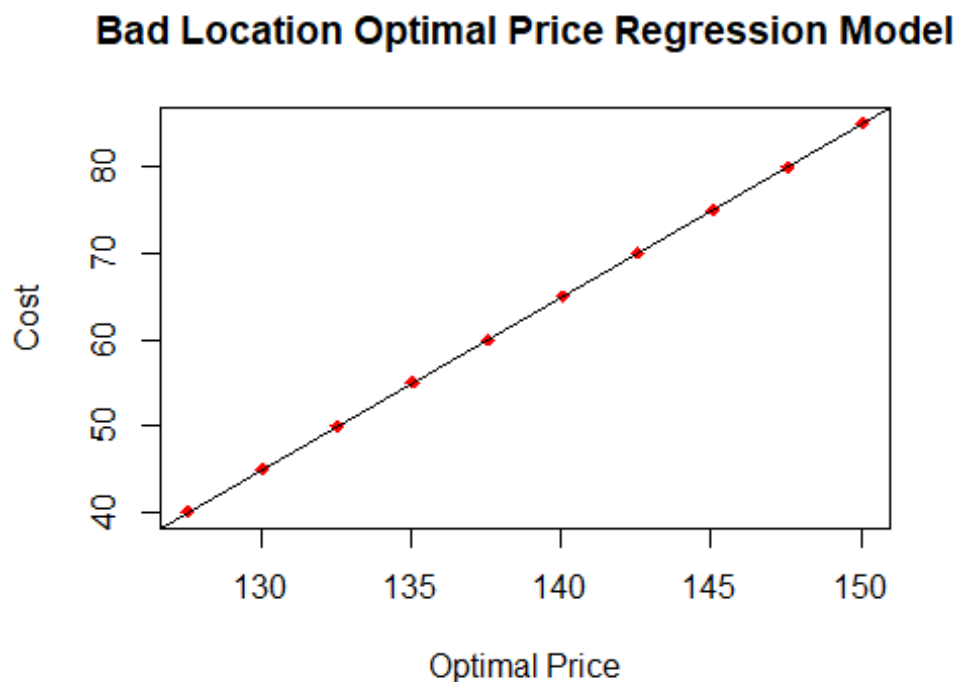
colnames(optimal_bad_prices) <- c("Cost","Optimal Price")

optimal_bad_prices<- as.table(optimal_bad_prices)
optimal_bad_prices
##      Cost Optimal Price
## A  40.00      127.57
## B  45.00      130.07
## C  50.00      132.57
## D  55.00      135.07
## E  60.00      137.57
## F  65.00      140.07
## G  70.00      142.57
## H  75.00      145.07
## I  80.00      147.57
## J  85.00      150.07

```

Plot Optimal Price Bad Location Regression Model

```
plot (bad_location_cost ~ bad_location_prices,  
      main = "Bad Location Optimal Price Regression Model",  
      xlab = "Optimal Price",  
      ylab = "Cost",  
      pch = 18,  
      col = "red" )  
  
abline(ols_bad_optimal)
```



Optimal Prices for Good Location Car Seats

```
optimal_good_prices <- matrix(c(40,156.13,45,158.63,50,161.13,55,163.63,60,166.13,65,168.63,70,171.13,75,173.63,80,176.13,85,178.63),ncol=2,byrow=TRUE)  
  
good_location_cost <- c(40,45,50,55,60,65,70,75,80,85)  
good_location_prices <- c(156.13,158.63,161.13,163.63,166.13,168.63,171.13,173.63,176.13,178.63)  
ols_good_optimal <- lm( good_location_cost ~ good_location_prices )  
  
colnames(optimal_good_prices) <- c("Cost","Optimal Price")  
  
optimal_good_prices<- as.table(optimal_good_prices)  
optimal_good_prices
```

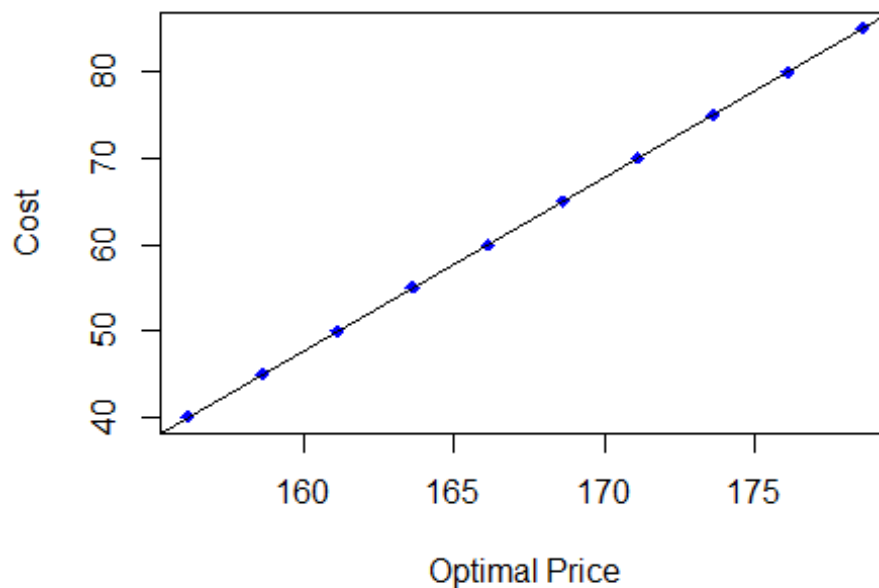
```
##      Cost Optimal Price
## A   40.00      156.13
## B   45.00      158.63
## C   50.00      161.13
## D   55.00      163.63
## E   60.00      166.13
## F   65.00      168.63
## G   70.00      171.13
## H   75.00      173.63
## I   80.00      176.13
## J   85.00      178.63
```

Plot Optimal Price Bad Location Regression Model

```
plot (good_location_cost ~ good_location_prices,
      main = "Good Location Optimal Price Regression Model",
      xlab = "Optimal Price",
      ylab = "Cost",
      pch = 18,
      col = "blue" )

abline(ols_good_optimal)
```

Good Location Optimal Price Regression Model



Calculations for optimal prices for both good and bad locations

Bad Location

$$\begin{aligned} b_0 &= 11.833 & 1. & \quad b_1 x^2 + b_0 x - (b_1)(\text{cost})x - (b_0)(\text{cost}) \\ b_1 &= -0.055 & f(x) &= -0.055x^2 + 11.833x - (-2.475x) - 532.485 \\ \text{Cost} &= 45 & f(x) &= -0.055x^2 + 14.308x - 532.485 \end{aligned}$$

$$f'(x) = -0.11x + 14.308$$

$$0 = -0.11x + 14.308$$

$$-14.308 = -0.11x$$

$$x = 130.07$$

$$\begin{aligned} \text{Cost} &= 50 & 2. & \quad f(x) = -0.055x^2 + 11.833x - (-0.055)(50)x - (11.833)(50) \\ & & & \quad -0.055x^2 + 11.833x - (-2.75x) - 591.65 \\ & & f(x) &= -0.055x^2 + 14.583x - 591.65 \end{aligned}$$

$$f'(x) = -0.11x + 14.583$$

$$0 = -0.11x + 14.583$$

$$0.11x = 14.583$$

$$x = 132.57$$

$$\begin{aligned} \text{Cost} &= 55 & 3. & \quad f(x) = -0.055x^2 + 11.833x - (-0.055)(55)x - (11.833)(55) \\ & & & \quad -0.055x^2 + 11.833x - (-3.025x) - 650.815 \\ & & f(x) &= -0.055x^2 + 14.858x - 650.815 \end{aligned}$$

$$f'(x) = -0.11x + 14.858$$

$$0 = -0.11x + 14.858$$

$$0.11x = 14.858$$

$$x = 135.07$$

Bad Location

$$b_0 = 11.833$$

$$b_1 = -0.055$$

$$\text{Cost} = 60$$

$$4. f(x) = -0.055x^2 + 11.833x - (-0.055)(60)x - (11.833)(60)$$

$$-0.055x^2 + 11.833x - (-3.3x) - 709.98$$

$$f(x) = -0.055x^2 + 15.133x - 709.98$$

$$f'(x) = -0.11x + 15.133$$

$$0 = -0.11x + 15.133$$

$$0.11x = 15.133$$

$$x = 137.57$$

$$\text{Cost} = 65$$

$$5. f(x) = -0.055x^2 + 11.833x - (-0.055)(65)x - (11.833)(65)$$

$$-0.055x^2 + 11.833x - (-3.575x) - 769.145$$

$$f(x) = -0.055x^2 + 15.408x - 769.145$$

$$f'(x) = -0.11x + 15.408$$

$$0 = -0.11x + 15.408$$

$$0.11x = 15.408$$

$$x = 140.07$$

$$\text{Cost} = 70$$

$$6. f(x) = -0.055x^2 + 11.833x - (-0.055)(70)x - (11.833)(70)$$

$$-0.055x^2 + 11.833x - (-3.85x) - 828.31$$

$$f(x) = -0.055x^2 + 15.683x - 828.31$$

$$f'(x) = -0.11x + 15.683$$

$$0 = -0.11x + 15.683$$

$$0.11x = 15.683$$

$$x = 142.57$$

Bad Location

$$b_0 = 11.833$$

$$b_1 = -0.055$$

$$\text{Cost} = 75$$

$$7. f(x) = -0.055x^2 + 11.833x - (-0.055)(75)x - (11.833)(75)$$

$$-0.055x^2 + 11.833x - (-4.125x) - 887.475$$

$$f(x) = -0.055x^2 + 15.958x - 887.475$$

$$f'(x) = -0.11x + 15.958$$

$$0 = -0.11x + 15.958$$

$$0.11x = 15.958$$

$$x = 145.07$$

$$\text{Cost} = 80$$

$$8. f(x) = -0.055x^2 + 11.833x - (-0.055)(80)x - (11.833)(80)$$

$$-0.055x^2 + 11.833x - (-4.4x) - 946.64$$

$$f(x) = -0.055x^2 + 16.233x - 946.64$$

$$f'(x) = -0.11x + 16.233$$

$$0 = -0.11x + 16.233$$

$$0.11x = 16.233$$

$$x = 147.57$$

$$\text{Cost} = 85$$

$$9. f(x) = -0.055x^2 + 11.833x - (-0.055)(85)x - (11.833)(85)$$

$$-0.055x^2 + 11.833x - (-4.675x) - 1,005.805$$

$$f(x) = -0.055x^2 + 16.508x - 1,005.805$$

$$f'(x) = -0.11x + 16.508$$

$$0 = -0.11x + 16.508$$

$$0.11x = 16.508$$

$$x = 150.07$$

Bad Location

$$b_0 = 11.833$$

$$b_1 = -0.055$$

$$\text{Cost} = 40$$

$$10. f(x) = -0.055x^2 + 11.833x - (-0.055)(40)x - (11.833)(40)$$

$$= -0.055x^2 + 11.833x - (-2.2x) - 473.32$$

$$f(x) = -0.055x^2 + 14.033x - 473.32$$

$$f'(x) = -0.11x + 14.033$$

$$0 = -0.11x + 14.033$$

$$0.11x = 14.033$$

$$x = 127.57$$

Good Location

$$b_0 = 17.969$$

$$b_1 = -0.066$$

$$\text{Cost} = 40$$

$$1. f(x) = -0.066x^2 + 17.969x - (-0.066)(40)x - (17.969)(40)$$

$$= -0.066x^2 + 17.969x - (-2.64x) - 718.76$$

$$f(x) = -0.066x^2 + 20.609x - 718.76$$

$$f'(x) = -0.132x + 20.609$$

$$0 = -0.132x + 20.609$$

$$0.132x = 20.609$$

$$x = 156.13$$

$$\text{Cost} = 45 \quad 2. f(x) = -0.066x^2 + 17.969x - (-0.066)(45)x - (17.969)(45)$$

$$= -0.066x^2 + 17.969x - (-2.97x) - 808.605$$

$$f(x) = -0.066x^2 + 20.939x - 808.605$$

$$f'(x) = -0.132x + 20.939$$

$$0 = -0.132x + 20.939$$

$$0.132x = 20.939$$

$$x = 158.63$$

Good Location

$$b_0 = 17.969$$

$$b_1 = -0.066$$

$$\text{Cost} = 50$$

$$3. f(x) = -0.066x^2 + 17.969x - (-0.066)(50)x - (17.969)(50)$$

$$-0.066x^2 + 17.969x - (-3.3x) - 898.45$$

$$f(x) = -0.066x^2 + 21.269x - 898.45$$

$$f'(x) = -0.132x + 21.269$$

$$0 = -0.132x + 21.269$$

$$0.132x = 21.269$$

$$x = 161.13$$

$$\text{Cost} = 55$$

$$4. f(x) = -0.066x^2 + 17.969x - (-0.066)(55)x - (17.969)(55)$$

$$-0.066x^2 + 17.969x - (-3.63)x - 988.295$$

$$f(x) = -0.066x^2 + 21.599x - 988.295$$

$$f'(x) = -0.132x + 21.599$$

$$0 = -0.132x + 21.599$$

$$0.132x = 21.599$$

$$x = 163.63$$

$$\text{Cost} = 60$$

$$5. f(x) = -0.066x^2 + 17.969x - (-0.066)(60)x - (17.969)(60)$$

$$-0.066x^2 + 17.969x - (-3.96x) - 1,078.14$$

$$f(x) = -0.066x^2 + 21.929x - 1,078.14$$

$$f'(x) = -0.132x + 21.929$$

$$0 = -0.132x + 21.929$$

$$0.132x = 21.929$$

$$x = 166.13$$

Good Location

$$b_0 = 17.969$$

$$b_1 = -0.066$$

$$\text{Cost} = 65$$

$$6. f(x) = -0.066x^2 + 17.969x - (-0.066)(65)x - (17.969)(65)$$

$$-0.066x^2 + 17.969x - (-4.29x) - 1,167.985$$

$$f(x) = -0.066x^2 + 22.259x - 1,167.985$$

$$f'(x) = -0.132x + 22.259$$

$$0 = -0.132x + 22.259$$

$$0.132x = 22.259$$

$$x = 168.63$$

$$\text{Cost} = 70$$

$$7. f(x) = -0.066x^2 + 17.969x - (-0.066)(70)x - (17.969)(70)$$

$$-0.066x^2 + 17.969x - (-4.62x) - 1,257.83$$

$$f(x) = -0.066x^2 + 22.589x - 1,257.83$$

$$f'(x) = -0.132x + 22.589$$

$$0 = -0.132x + 22.589$$

$$0.132x = 22.589$$

$$x = 171.13$$

$$\text{Cost} = 75$$

$$8. f(x) = -0.066x^2 + 17.969x - (-0.066)(75)x - (17.969)(75)$$

$$-0.066x^2 + 17.969x - (-4.95x) - 1,347.675$$

$$f(x) = -0.066x^2 + 22.919x - 1,347.675$$

$$f'(x) = -0.132x + 22.919$$

$$0 = -0.132x + 22.919$$

$$0.132x = 22.919$$

$$x = 173.63$$

Good Location

$$\text{Cost} = 80$$

$$b_0 = 17.969$$

$$b_1 = -0.066$$

$$9. f(x) = -0.066x^2 + 17.969x - (-0.066)(80)x - (17.969)(80)$$
$$-0.066x^2 + 17.969x - (-5.28x) - 1,437.52$$

$$f(x) = -0.066x^2 + 23.249x - 1,437.52$$

$$f'(x) = -0.132x + 23.249$$

$$0 = -0.132x + 23.249$$

$$0.132x = 23.249$$

$$x = 176.13$$

$$\text{Cost} = 85$$

$$10. f(x) = -0.066x^2 + 17.969x - (-0.066)(85)x - (17.969)(85)$$
$$-0.066x^2 + 17.969x - (-5.61x) - 1,527.365$$

$$f(x) = -0.066x^2 + 23.579x - 1,527.365$$

$$f'(x) = -0.132x + 23.579$$

$$0 = -0.132x + 23.579$$

$$0.132x = 23.579$$

$$x = 178.63$$