## Inference for numerical data

#### North Carolina births

In 2004, the state of North Carolina released a large data set containing information on births recorded in this state. This data set is useful to researchers studying the relation between habits and practices of expectant mothers and the birth of their children. We will work with a random sample of observations from this data set.

#### Exploratory analysis

Load the nc data set into our workspace.

load("more/nc.RData")

We have observations on 13 different variables, some categorical and some numerical. The meaning of each variable is as follows.

variable	description
fage	father's age in years.
mage	mother's age in years.
mature	maturity status of mother.
weeks	length of pregnancy in weeks.
premie	whether the birth was classified as premature (premie) or full-term.
visits	number of hospital visits during
marital	pregnancy. whether mother is married or not married at birth.
gained	weight gained by mother during pregnancy in pounds.
weight	weight of the baby at birth in pounds.
lowbirthweight	whether baby was classified as low
	birthweight (low) or not (not low).
gender	gender of the baby, female or male.
habit	status of the mother as a nonsmoker or a smoker.
whitemom	whether mom is white or not white.

1. What are the cases in this data set? How many cases are there in our sample?

## The cases in this data set are individual births including data on the mother, father, child. There are 1000 cases in our sample.

As a first step in the analysis, we should consider summaries of the data. This can be done using the summary command:

#### summary(nc)

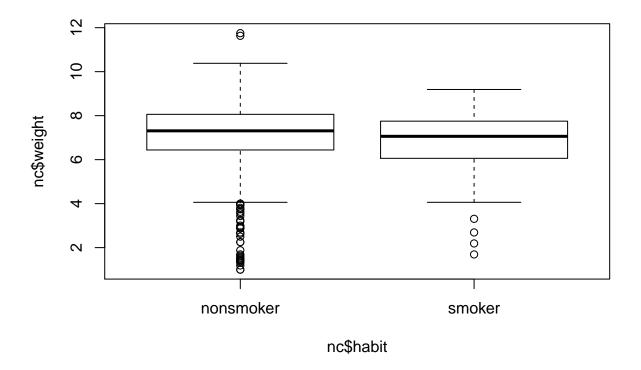
```
##
         fage
                                             mature
                                                            weeks
                           mage
##
    Min.
            :14.00
                                                        Min.
                                                                :20.00
                     Min.
                              :13
                                    mature mom :133
    1st Qu.:25.00
                     1st Qu.:22
                                    younger mom:867
                                                        1st Qu.:37.00
    Median :30.00
                                                        Median :39.00
##
                     Median:27
            :30.26
                              :27
                                                                :38.33
##
    Mean
                     Mean
                                                        Mean
##
    3rd Qu.:35.00
                     3rd Qu.:32
                                                        3rd Qu.:40.00
##
            :55.00
                     Max.
                              :50
                                                                :45.00
    Max.
                                                        Max.
    NA's
            :171
                                                        NA's
                                                                :2
##
##
          premie
                          visits
                                              marital
                                                              gained
##
    full term:846
                     Min.
                              : 0.0
                                      married
                                                  :386
                                                          Min.
                                                                  : 0.00
##
    premie
              :152
                      1st Qu.:10.0
                                      not married:613
                                                          1st Qu.:20.00
    NA's
                                                          Median :30.00
##
              : 2
                     Median:12.0
                                      NA's
                                                  : 1
##
                     Mean
                             :12.1
                                                          Mean
                                                                  :30.33
##
                     3rd Qu.:15.0
                                                          3rd Qu.:38.00
##
                     Max.
                             :30.0
                                                                  :85.00
                                                          Max.
##
                     NA's
                              :9
                                                          NA's
                                                                  :27
##
        weight
                       lowbirthweight
                                          gender
                                                            habit
##
            : 1.000
                       low
                               :111
                                       female:503
                                                      nonsmoker:873
    1st Qu.: 6.380
##
                       not low:889
                                       male :497
                                                      smoker
                                                                :126
##
    Median : 7.310
                                                      NA's
    Mean
##
            : 7.101
    3rd Qu.: 8.060
##
            :11.750
    Max.
##
##
         whitemom
    not white: 284
##
##
    white
              :714
##
    NA's
              : 2
##
##
##
##
```

As you review the variable summaries, consider which variables are categorical and which are numerical. For numerical variables, are there outliers? If you aren't sure or want to take a closer look at the data, make a graph.

Consider the possible relationship between a mother's smoking habit and the weight of her baby. Plotting the data is a useful first step because it helps us quickly visualize trends, identify strong associations, and develop research questions.

2. Make a side-by-side boxplot of habit and weight. What does the plot highlight about the relationship between these two variables?

```
boxplot(nc$weight ~ nc$habit)
```



## The plot highlights about the two variables that the birth weight tends to be lower for smokers than non-smokers.

The box plots show how the medians of the two distributions compare, but we can also compare the means of the distributions using the following function to split the weight variable into the habit groups, then take the mean of each using the mean function.

```
by(nc$weight, nc$habit, mean)

## nc$habit: nonsmoker

## [1] 7.144273

## ------
## nc$habit: smoker

## [1] 6.82873
```

There is an observed difference, but is this difference statistically significant? In order to answer this question we will conduct a hypothesis test .

#### Inference

3. Check if the conditions necessary for inference are satisfied. Note that you will need to obtain sample sizes to check the conditions. You can compute the group size using the same by command above but replacing mean with length.

```
by(nc$weight, nc$habit, length)

## nc$habit: nonsmoker

## [1] 873

## ------

## nc$habit: smoker

## [1] 126
```

We can assume independence since both are random samples and they are less than 10% of the population. The sample sizes are large enough to assume a normal distribution.

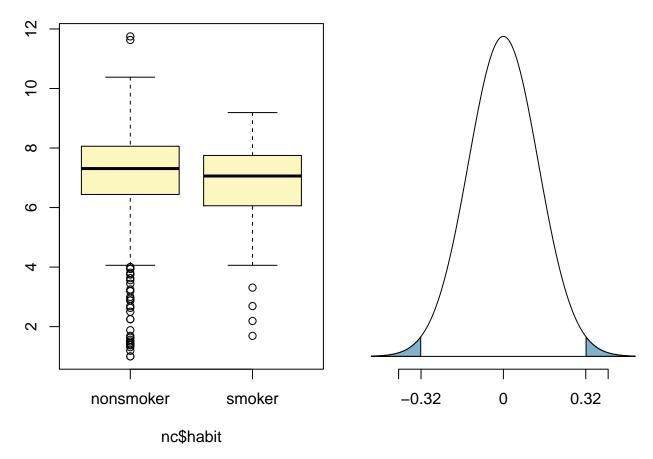
4. Write the hypotheses for testing if the average weights of babies born to smoking and non-smoking mothers are different.

H0: The average weights of babies born to smoking and non-smoking mothers are different. HA: The average weights of babies born to smoking and non-smoking mothers are the same.

Next, we introduce a new function, inference, that we will use for conducting hypothesis tests and constructing confidence intervals.

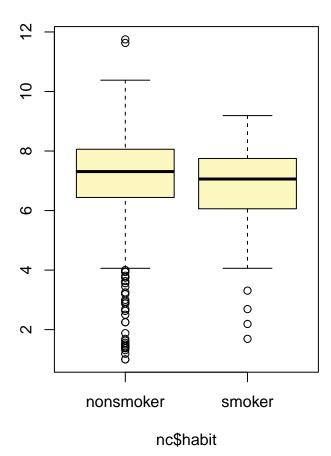
```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_nonsmoker = 873, mean_nonsmoker = 7.1443, sd_nonsmoker = 1.5187
## n_smoker = 126, mean_smoker = 6.8287, sd_smoker = 1.3862

## Observed difference between means (nonsmoker-smoker) = 0.3155
##
## HO: mu_nonsmoker - mu_smoker = 0
## HA: mu_nonsmoker - mu_smoker != 0
## Standard error = 0.134
## Test statistic: Z = 2.359
## p-value = 0.0184
```



Let's pause for a moment to go through the arguments of this custom function. The first argument is y, which is the response variable that we are interested in: nc\$weight. The second argument is the explanatory variable, x, which is the variable that splits the data into two groups, smokers and non-smokers: nc\$habit. The third argument, est, is the parameter we're interested in: "mean" (other options are "median", or "proportion".) Next we decide on the type of inference we want: a hypothesis test ("ht") or a confidence interval ("ci"). When performing a hypothesis test, we also need to supply the null value, which in this case is 0, since the null hypothesis sets the two population means equal to each other. The alternative hypothesis can be "less", "greater", or "twosided". Lastly, the method of inference can be "theoretical" or "simulation" based.

5. Change the type argument to "ci" to construct and record a confidence interval for the difference between the weights of babies born to smoking and non-smoking mothers.

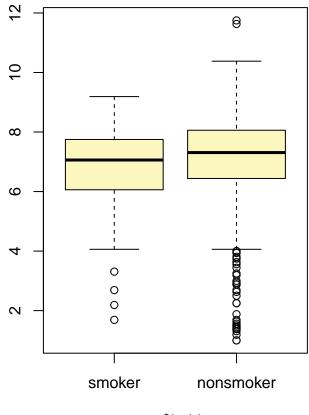


```
## Observed difference between means (nonsmoker-smoker) = 0.3155
##
## Standard error = 0.1338
## 95 % Confidence interval = ( 0.0534 , 0.5777 )
```

The confidence interval for the difference between the weights of babies born to smoking and non-smoking mothers is (0.0534, 0.5777).

By default the function reports an interval for  $(\mu_{nonsmoker} - \mu_{smoker})$ . We can easily change this order by using the order argument:

```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_smoker = 126, mean_smoker = 6.8287, sd_smoker = 1.3862
## n_nonsmoker = 873, mean_nonsmoker = 7.1443, sd_nonsmoker = 1.5187
```



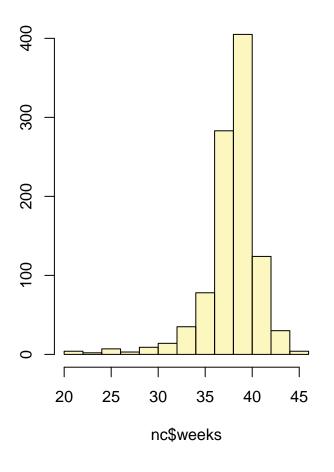
### nc\$habit

```
## Observed difference between means (smoker-nonsmoker) = -0.3155 ## ## Standard error = 0.1338 ## 95 % Confidence interval = (-0.5777, -0.0534)
```

### On your own

• Calculate a 95% confidence interval for the average length of pregnancies (weeks) and interpret it in context. Note that since you're doing inference on a single population parameter, there is no explanatory variable, so you can omit the x variable from the function.

```
## Single mean
## Summary statistics:
```

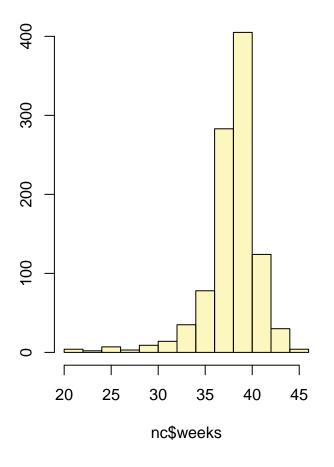


```
## mean = 38.3347; sd = 2.9316; n = 998 ## Standard error = 0.0928 ## 95 % Confidence interval = ( 38.1528 , 38.5165 )
```

# The 95% confidence interval for the average length of pregnancies is (38.1528, 38.5165).

• Calculate a new confidence interval for the same parameter at the 90% confidence level. You can change the confidence level by adding a new argument to the function: conflevel = 0.90.

## Single mean
## Summary statistics:

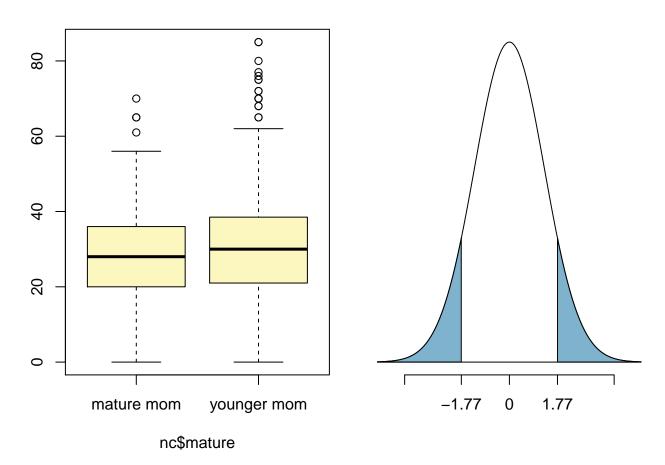


```
## mean = 38.3347 ; sd = 2.9316 ; n = 998
## Standard error = 0.0928
## 90 % Confidence interval = ( 38.182 , 38.4873 )
```

# The 90% confidence interval for the average length of pregnancies is (38.182, 38.4873).

• Conduct a hypothesis test evaluating whether the average weight gained by younger mothers is different than the average weight gained by mature mothers.

```
## Standard error = 1.286
## Test statistic: Z = -1.376
## p-value = 0.1686
```



P-value = 0.1686. If we assume a 95% confidence interval, since the p-value is greater than 0.05, we accept H0 that there is no difference in the average weight gained by young and mature mothers.

• Now, a non-inference task: Determine the age cutoff for younger and mature mothers. Use a method of your choice, and explain how your method works.

```
by(nc$mage, nc$mature, min)

## nc$mature: mature mom
## [1] 35
## ------
## nc$mature: younger mom
## [1] 13

by(nc$mage, nc$mature, max)
```

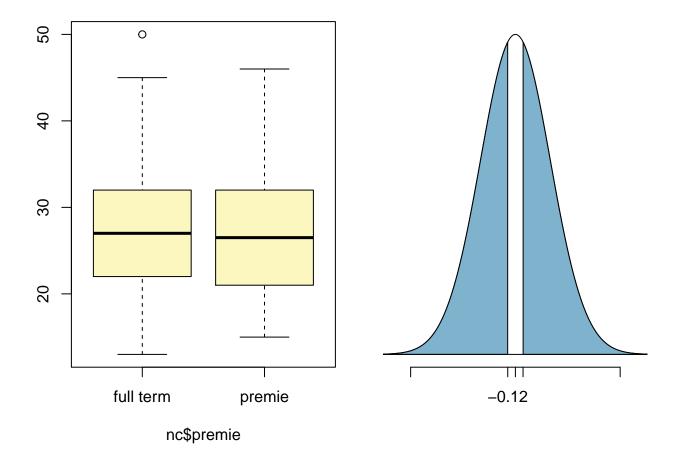
```
## nc$mature: mature mom
## [1] 50
## ------
## nc$mature: younger mom
## [1] 34
```

The age cutoff for younger and mature mothers is 35. The method I used involves using the by() function. I used two of them to show the min and max age for younger and mature mothers. We see for younger mothers the min is 13 ad the max is 34. For mature mothers the min is 35 and the max is 50. Since the max age for younger mothers is 34 and the min age for mature mothers is 35, that makes the age cutoff is 35.

• Pick a pair of numerical and categorical variables and come up with a research question evaluating the relationship between these variables. Formulate the question in a way that it can be answered using a hypothesis test and/or a confidence interval. Answer your question using the inference function, report the statistical results, and also provide an explanation in plain language.

The numerical variable I am choosing is the mother's age or mage. The categorical variable I am choosing is premature pregnancies or premie. Question: Is there a difference in the average age of mothers for premature pregnancies compared to full term pregnancies? H0: There is no difference in the average age of mothers for premature pregnancies compared to full term pregnancies. HA: There is a difference in the average age of mothers for premature pregnancies compared to full term pregnancies.

```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_full term = 846, mean_full term = 27, sd_full term = 6.1444
## n_premie = 152, mean_premie = 26.875, sd_premie = 6.533
## Observed difference between means (full term-premie) = 0.125
##
## HO: mu_full term - mu_premie = 0
## HA: mu_full term - mu_premie != 0
## Standard error = 0.57
## Test statistic: Z = 0.219
## p-value = 0.8266
```



P-value is 0.8266. Since the p-value is greater than 0.05 and if we assume a 95% confidence interval, we fail to reject H0.