

# Problem Set 5

Bhavna Phogaat  
ECON833: Computational Methods for Economists  
Fall 2021

## Data Description

1. The data are in the CSV file `radio_merger_data.csv`.
2. There are 2 independent markets representing mergers in 2007 and 2008.
3. There are 45 mergers in 2007 and 54 in 2008.
4. A unique id is assigned to each buyer and target.
5. The variable names should be mostly obvious.
6. Prices are in constant dollars, population in number of people

## Objective

### Model 1

Consider a model of a one-to-one matching market representing radio station mergers. Each year there is a national market where radio station owners target new stations. In particular, the payoff to the merger between radio station buyer  $b$  and target  $t$  in market  $m$  is given by:

$$f_m(b, t) = x_{1bm}y_{1tm} + \alpha x_{2bm}y_{1tm} + \beta \text{distance}_{btm} + \epsilon_{btm} \quad (1)$$

where

1.  $x_{1bm}$  is the number of stations owned by the parent company of the buyer

2.  $y_{1tm}$  is the population in range of the target in market  $m$
3.  $x_{2bm}$  is an indicator for corporate ownership
4.  $distance_{btm}$  is the distance (in miles) between the buyer and target
5. The match-specific error term, is independent across matches

**The maximum score objective function is:**

$$Q(\alpha, \beta) = \sum_{m \in M} \sum_{i \in U_m} \sum_{j \in U_m \setminus i} 1[(f_{\alpha, \beta}(i, i) + f_{\alpha, \beta}(j, j) > f_{\alpha, \beta}(i, j) + f_{\alpha, \beta}(j, i))] \quad (2)$$

## Figures

```

Model1 Without Transfer:
Optimal value of alpha : 0.434999999999999894
Optimal value of beta : -0.6500000000000001
Maximum socre: 2286

```

Figure 1: Model 1

### Model 2

Estimate the version of model1 with transfers (the prices pay to acquire the target station). Here, use the data of the merger and a different inequality in the score function. In this case, let the payoff function also include target characteristics:

$$f_m(b, t) = \delta x_{1bm} y_{1tm} + \alpha x_{2bm} y_{1tm} + \gamma HHI_{tm} + \beta distance_{btm} + \epsilon_{btm} \quad (3)$$

where  $HHI_{tm}$  is the Hindahl-Hirschman Index measuring market concentration (a higher index means a more concentrated market) in the location of the target in market  $m$ .

**The maximum score objective function is:**

$$Q(\delta, \alpha, \gamma, \beta) = \sum_{m \in M} \sum_{i \in U_m} \sum_{j \in U_m \setminus i} 1[(f_{\delta, \alpha, \gamma, \beta}(i, i) + f_{\delta, \alpha, \gamma, \beta}(j, j) > f_{\delta, \alpha, \gamma, \beta}(i, j) + f_{\delta, \alpha, \gamma, \beta}(j, i))] \quad (4)$$

## Figures

```
Model2 With Transfer
Optimal value of delta: 0.1
Optimal value of alpha: -0.2
Optimal value of gamma: 0.21000000000000002
Optimal value of beta: -0.1
Maximum score: 2285
```

Figure 2: Model 2