(의જ/OI/케)

 $\mathbf{K}^{\mathbf{X}} = \mathcal{O}_{\mathbf{A}}^{\mathbf{X}}$

Exposé Groupe de travail Déformations

Alo il niga pos d'obehnets à les das. $G = (XT,X)^{H}$

[KOD, SPEN] COROLLAIRE GÉNÉRAL:

Le théorème de Bogomolov-Tian-Todorov

M= Xdiff ral. Co sour-jacost

$$X_{\ell} = (X, \mathcal{I}_{\ell}) \longrightarrow [\mathcal{J}_{\ell}] = [s_{\ell}] \qquad S_{\ell} \in \Gamma(X, T_{k}^{*} \circ \Omega_{k}^{*})$$

$$A^{s,t}(X) \stackrel{\sim}{=} A^{t,t}(X) \stackrel{\sim}{=} X \stackrel{\sim}{=} X \stackrel{\sim}{=} X$$

Idde, motivation

Soit
$$s_i \in H'(X_i TX)$$
 on veut $s(t) = \sum_{i > 0} s_i t^i \in DF(X)$

$$d_{\underline{o}} = s_i = \dot{s}(0) \quad dow \quad Def(X) \quad |_{T \in Def(X)} = H(TX)$$

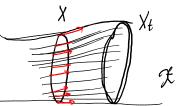
On va donoir resouche

$$\overline{\partial}$$
s(t) + $\frac{1}{2}$ [s(t), s(t)] = 0

EO de Maurier-Gartan

$$\Rightarrow \begin{cases} \overline{\partial} S_1 = 0 \\ \overline{\partial} S_2 + [S_1, S_1] = 0 \end{cases}$$

<u> III)</u>のBSTRUCTION



$$0 \rightarrow TX_0 \rightarrow T\mathcal{L}|_{X_0} \rightarrow N_{X_0/X_0} \rightarrow 0$$

$$H^{\circ}(T\mathcal{H}_{X_0}) \rightarrow T_0 S \rightarrow H(X_0, TX_0)$$

Ala en intigant a chap directa or a w boiholo Xo 1:1 Xt donc Xt n'est pas me vici défendais de X

H'(X,TX) = Obstruction à ce qu'en teoure un tel champ de vecteurle by de X = Obsteuetin à ce que 26 -> S soit loc. terrial. = Obstruction à ce qu'il n'y ail pes diffornite

H2(X,TX) = "Obstanction à l'obstanction" = Obskucto à la desenation

Quard or constait s

$$z = 3^{1} + 3^{2} + \cdots$$

$$2s^{2} + \frac{1}{2} [s^{1} s^{2}] = 0$$

$$2s^{2} + \frac{1}{2} [s^{2} s^{2}] = 0$$

Il faut done [s,,s,] Doract pour un box choix de s,

Rg [5,5] = 2[55,5] = 0 done [5,51] donne u ell de H2 Si en avoit charsit s' = s, + Do $\begin{bmatrix} S'_1, S'_1 \end{bmatrix} = \begin{bmatrix} S_1, S_1 \end{bmatrix} + \overline{\partial} \left(\begin{bmatrix} \sigma, S_1 \end{bmatrix} + \begin{bmatrix} \sigma, \overline{\partial} \sigma \end{bmatrix} \right) = \begin{bmatrix} S_1, S_1 \end{bmatrix}$ old \mathcal{H}^2

Con [S1, S1] ∈ H2(X,TX): dostent à ce que 52 exist

ZTVEHEZČISZÍRFTE (I)

$$X$$
 Var. Unalytique complexe. (X,Q_X) espace anohytique.
 (X,Q_X) espace anohytique. (X,Q_X) in (P^*,Q_X) in (P^*,Q_X)

induit may be
$$D = \frac{1}{2} = \frac{1}{2} = \frac{1}{2} = \frac{1}{2}$$
 de Eustonmer.

Que peut-12 se theser
$$\rightarrow$$
 184 LISSE A. (C[x,y])(xy))

A. This irreductive $X = Spac$ (C[x]/(xy))

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A. This is separated a space (C[x]/(xy))

$$qor for f both $f'(X_t) = f'(X_t) = f'(X_t)$$$

Xs/A, send "C.Y. S.L. AL"

$$(X_s) \simeq H'(X, T_{\kappa/kn})$$

$$O_s \qquad X_{s/kn} \text{ deforme!" (patt) de } X/kn$$

$$O_s \qquad O_s \qquad (X_s/x_n) \hookrightarrow O_s$$

, YAPPEC :

$$(A, \Omega, X) \rightarrow A, + \omega \rightarrow A, (A, \Omega, X) \rightarrow A, (A, \Omega, X)$$

$$d_{\Delta X} = \dim_{\Delta X} H'(X, \Delta X) = \dim_{\Delta X} H'(X, \Delta X) = \dim_{\Delta X} H'(X, \Delta X) = \lim_{N \to \infty} H^{N-1,1}(X_{A})$$

\mathbb{I}) Preuve

On real mortion que
$$\forall n \geq 1$$
 $\left(\begin{array}{c} D_{X}(A_{n+1}) \longrightarrow D_{X}(A_{n}) \\ S = \sum_{i=1}^{n} S_{i}t^{i} & \longmapsto \sum_{i=1}^{n} S_{i}t^{i} = \underline{S} \end{array}\right)$ surjeuline

$$T'(X_s) = \begin{cases} s + \varepsilon s' \mid s' \in T'(M, T'' \circ \Omega^{o_{1}}) \otimes A_s & \text{et } \overline{\partial}(s + \varepsilon s') + \frac{1}{2}[s + \varepsilon s', s + \varepsilon s'] = 0 \end{cases}$$

$$\varepsilon^{2} = 0 = \begin{cases} s + \varepsilon s' \mid \frac{1}{2} \left(s + \varepsilon s' + \frac{1}{2} \left($$

Lemme
$$T^d$$
-Lifting [Ren]
$$S: \varphi_n : T^l(X_S/A_n) \longrightarrow T^l(X_S/A_{n-1}) \quad \text{surj.} \quad \forall s \in D_k(A_n)$$

$$Alon \quad D_X(A_n) \longrightarrow D_k(A_n) \quad \text{surj.}$$

$$S = \sum_{i>0}^n S_i t^i \quad \underline{s} = \sum_{i>0}^{n-1} S_i t^i$$

$$T^l(X_S/A_n) \longrightarrow T^l(X_S/A_{n-1}) \quad D_k(A_n) \longrightarrow D_k(A_n)$$

$$S + \varepsilon S' \longmapsto \underline{s} + \varepsilon S' \qquad \underline{\sigma}$$

$$Soil \quad s \in D_X(A_n) \qquad S = \sum_{i=1}^n S_i t^i$$

$$casicl \quad \sum_{i=1}^{n-1} S_i t^i + \sum_{i=1}^n S_i t^{i-1} \varepsilon \quad C \quad T^l(X_S/A_n) \qquad \text{for } s \in D_k(A_n)$$

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$$\mathcal{R}_{\underline{Son}}$$
 $\hat{\mathbf{S}} = \mathbf{S} + \frac{G_n}{n+1} \mathbf{t}^{n+1} \in \Gamma(M, T^{1/2} \otimes \Omega^{2/4}) \otimes M_{\underline{An+1}}$

EILE VERIFIE (MC) à L'OEDRE 1,2,...n

-, il suffit qu'elle le ventre à l'orde n+1

$$\frac{1}{n+1} \overline{\partial s_n} + \frac{1}{2} \sum_{i=1}^{n} [S_i, S_{n+1,i}] = 0 \quad \text{sk} \quad \stackrel{?}{\text{s}} \in \mathbb{D}_{\lambda}(A_{nH})$$