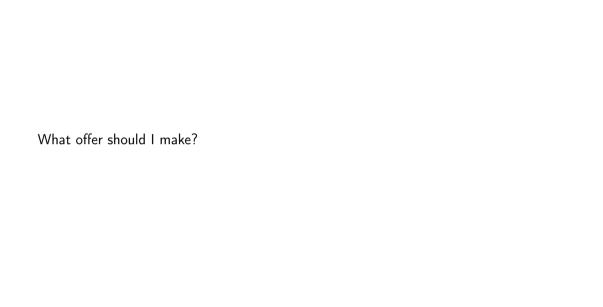
Optimal Bargaining on eBay Using Deep Reinforcement Learning

Etan Green¹ E. Barry Plunkett^{1,2}

¹University of Pennsylvania

²D. E. Shaw

November 2020





This project

For any listing and at any point in the offer history, what offer maximizes the eventual payoff? For the seller? For the buyer?

► Characterize optimal behavior in a way that humans can use.

Larger goal

Tutorial for solving real-world dynamic decision problems.

▶ Where experimentation is infeasible but data are plentiful.

And characterizing the solutions.

Reinforcement learning

In each state, find the policy that maximizes the eventual payoff.

$$\pi(s): s \to f(a)$$

Chess

► State: board position

► Action: allowable move

► Payoff: 1 for a win, 0 for a loss

Play randomly at first, reinforce actions that lead to higher payoffs.

Deep reinforcement learning

Approximates states from features.

$$\pi(\mathbf{x}): \mathbf{x} \to f(a)$$



"Best Offer" listings on eBay

- ► State: listing features + offer history
- ► Action: an offer
- ► Payoff: (tbd)

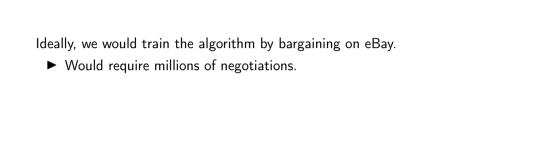
Can we train an algorithm to play optimally against human buyers and sellers on eBay?

"Best Offer" listings on eBay

- ► State: listing features + offer history
- Action: an offer
- ► Payoff: (tbd)

Can we train an algorithm to play optimally against human buyers and sellers on eBay?

► Optimal ≠ equilibrium



Ideally, we would train the algorithm by bargaining on eBay.

► Would require millions of negotiations.

Our approach:

- 1. Train neural nets to mimic human buyers and sellers.
- 2. Train reinforcement learning agents to play optimally against these simulated buyers and sellers.

Outline

- 1. Gameplay
- 2. Data
- 3. Simulator
- 4. Payoffs
- 5. RL seller

Outline

- 1. Gameplay
- 2. Data
- 3. Simulator
- 4. Payoffs
- 5. RL seller

Seller sets three prices

- 1. A list price, at which the item may be purchased immediately.
- 2. An optional **auto-accept price**, above which buyer offers are immediately accepted.
- 3. An optional auto-reject price, below which buyer offers are immediately rejected.

1. Buyer makes an offer.

- 1. Buyer makes an offer.
- 2. If offer is between the automatic thresholds, seller may accept, counter or reject.
 - ► If seller does not respond in 48 hours, offer is rejected.

- 1. Buyer makes an offer.
- 2. If offer is between the automatic thresholds, seller may accept, counter or reject.
 - ► If seller does not respond in 48 hours, offer is rejected.
- 3. If seller does not accept, buyer may accept, counter or walk.
 - ► If buyer does not respond in 48 hours, buyer walks.

- 1. Buyer makes an offer.
- 2. If offer is between the automatic thresholds, seller may accept, counter or reject.
 - ► If seller does not respond in 48 hours, offer is rejected.
- 3. If seller does not accept, buyer may accept, counter or walk.
 - ▶ If buyer does not respond in 48 hours, buyer walks.
- 4. Repeat (2) & (3) until buyer and seller have each had 3 turns.

- 1. Buyer makes an offer.
- 2. If offer is between the automatic thresholds, seller may accept, counter or reject.
 - ▶ If seller does not respond in 48 hours, offer is rejected.
- 3. If seller does not accept, buyer may accept, counter or walk.
 - ► If buyer does not respond in 48 hours, buyer walks.
- 4. Repeat (2) & (3) until buyer and seller have each had 3 turns.
- 5. After 3rd seller response, buyer faces take-it-or-leave-it offer.

A thread ends when...

- 1. An offer is accepted (on any thread).
- 2. The buyer walks (actively or passively).
- 3. The listing expires.

Outline

- 1. Gameplay
- 2. Data
- 3. Simulator
- 4. Payoffs
- 5. RL seller

Backus et al. (2020)

Universe of "Best Offer" listings on eBay from 2012-13.

► Complete offer histories for all negotiations.

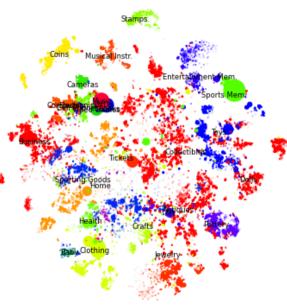
What else is in the data?

An incomplete list:

- ► List price and automatic thresholds.
- ► Category and subcategory.
- ► Listing start and end dates.
- ► Number of photos.
- ► Seller's rating.
- ► Offer timestamps.
- ► Whether a message is attached to the offer.

What's not in the data

- ► The photos themselves.
- ► The messages themselves.
- ► Item descriptions.



Original data: 98.3M listings.

1. Plausibly unique listings (unique title): 28.6M

- 1. Plausibly unique listings (unique title): 28.6M
- 2. and fixed list price: 18.6M

- 1. Plausibly unique listings (unique title): 28.6M
- 2. and fixed list price: 18.6M
- 3. and list price between \$9.95 and \$1000.00: 14.6M

- 1. Plausibly unique listings (unique title): 28.6M
- 2. and fixed list price: 18.6M
- 3. and list price between \$9.95 and \$1000.00: 14.6M
- 4. and no other funny stuff: 13.4M

Partitions

- 13.4M listings, from 771.6k sellers, split into 4 partitions:
 - 1. Simulator training: 75% of sellers
 - 2. RL training: 10%
 - 3. Validation: 5%
 - 4. Test: 10%

All results that follow are from validation partition.

Outline

- 1. Gameplay
- 2. Data
- 3. Simulator
- 4. Payoffs
- 5. RL seller

Example listing

- ► \$100 list price
- ► \$60 auto-reject price
- ► No auto-accept price

In the data, the item sells for the list price to the first buyer.

Example listing

- ► \$100 list price
- ► \$60 auto-reject price
- ► No auto-accept price

In the data, the item sells for the list price to the first buyer. Counterfactual:

- 1. Buyer 1 offers \$50.
- 2. Seller auto-rejects.
- 3. Buyer 1 offers \$75 of list price.
- 4. Buyer 2 purchases the item for the list price.

Overview

Simulate:

- 1. The arrival of buyers.
- 2. The offer path of each thread.

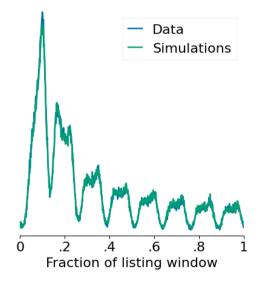
All features of the listing are held constant.

► e.g., list price and automatic thresholds

Listings expire after 1 week.

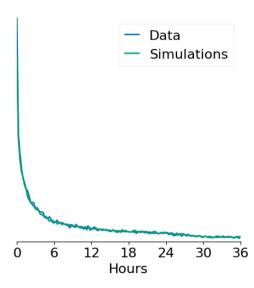
► Common listing duration in the data.

Arrival time of first buyer

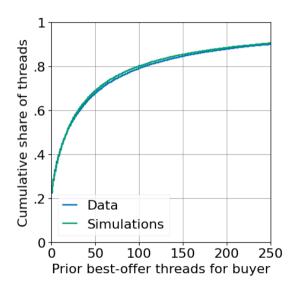


70% of listings expire without an arrival.

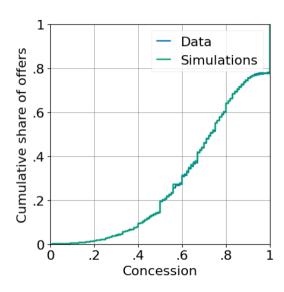
Interarrival time



Buyer experience



First buyer offer

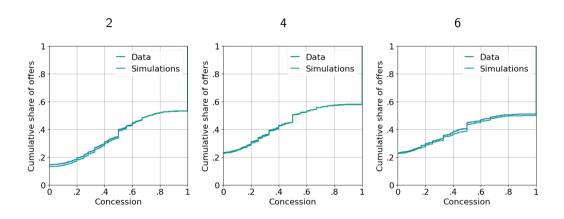


Offers as concessions

How much of the bargaining zone is conceded.

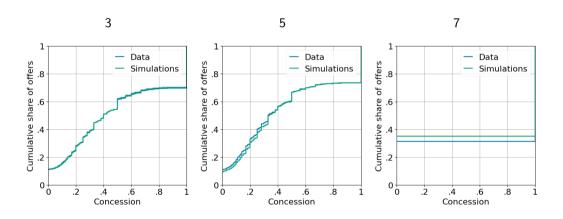
- e.g., buyer last offered \$50 and seller last offered \$100.
- ► \$60 buyer offer = 20% concession
- ▶ \$90 seller offer = 20% concession

Concessions: seller turns



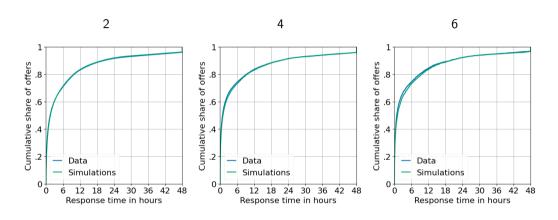
Note: excludes automatic offers and expirations.

Concessions: buyer turns



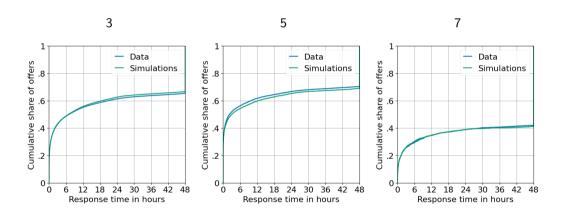
Note: excludes expirations.

Response time: seller turns

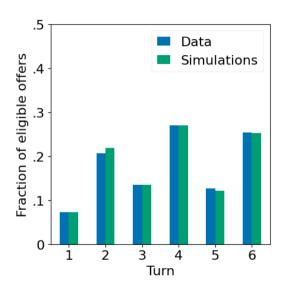


Note: excludes automatic offers.

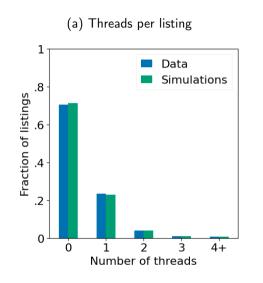
Response time: buyer turns

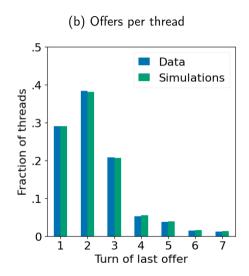


Message rates

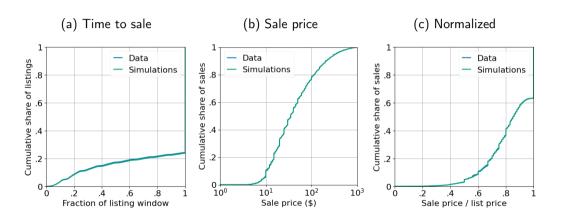


Summary statistics

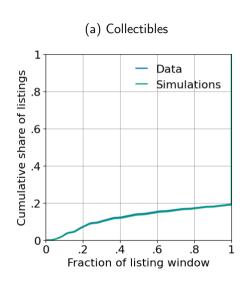


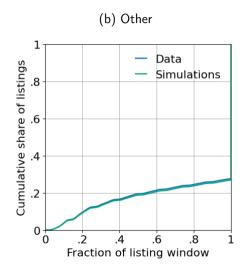


Sale time and price

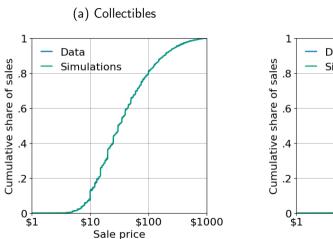


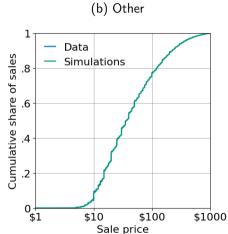
By category: time to sale



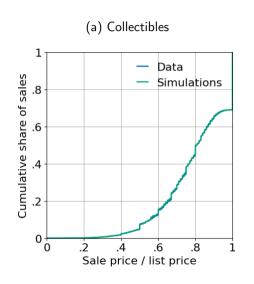


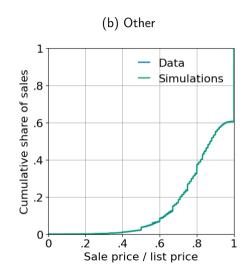
By category: sale price





By category: normalized sale price





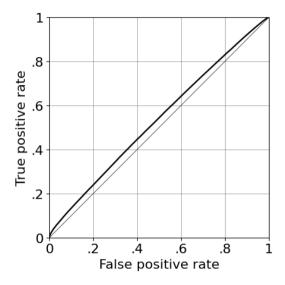
Discriminator

Observes a complete thread, either from data or simulations.

- ► Fixed listing features.
- ► Offer path.

Predicts the whether the thread is real or simulated.

Discriminator performance



AUC: 56%

Outline

- 1. Gameplay
- 2. Data
- 3. Simulator
- 4. Payoffs
- 5. RL seller

Payoffs

Buyer:

- ▶ item value less sale price, if buyer purchases item
- ► 0, otherwise

Payoffs

Buyer:

- ▶ item value less sale price, if buyer purchases item
- ▶ 0, otherwise

Seller:

- ► sale price, if item sells
- lacktriangle item value discounted by $\delta \in [0,1]$, otherwise

Payoffs

Buyer:

- ▶ item value less sale price, if buyer purchases item
- ▶ 0, otherwise

Seller:

- ► sale price, if item sells
- lacktriangle item value discounted by $\delta \in [0,1]$, otherwise

What is an item's value?

- ► Calculate a "market value" for each item.
- ► Characterize optimal behavior under these values.

$$v = P(\mathtt{sale}) \cdot \mathbb{E}[\mathtt{price}|\mathtt{sale}] + (1 - P(\mathtt{sale})) \cdot v$$

$$v = P(\mathtt{sale}) \cdot \mathbb{E}[\mathtt{price}|\mathtt{sale}] + \left(1 - P(\mathtt{sale})\right) \cdot \ v$$

$$extstyle v = rac{P(extst{sale}) \cdot \mathbb{E}[extstyle{ extstyle{price}| extstyle{sale}}]}{1 - \delta(1 - P(extstyle{sale}))}$$

$$v = P(\mathtt{sale}) \cdot \mathbb{E}[\mathtt{price}|\mathtt{sale}] + ig(1 - P(\mathtt{sale})ig) \cdot v$$

$$v = rac{P(\mathtt{sale}) \cdot \mathbb{E}[\mathtt{price} | \mathtt{sale}]}{1 - \delta(1 - P(\mathtt{sale}))}$$

- $\blacktriangleright \ \delta = 0 \to \mathtt{value} = P(\mathtt{sale}) \cdot \mathbb{E}[\mathtt{price} | \mathtt{sale}]$
- $lackbox{lack}\delta=1
 ightarrow extsf{value}=\mathbb{E}[extsf{price}| extsf{sale}]$

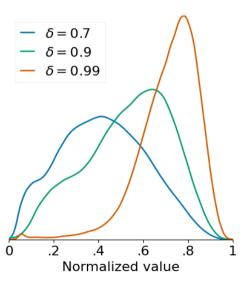
$$v = P(\mathtt{sale}) \cdot \mathbb{E}[\mathtt{price}|\mathtt{sale}] + \left(1 - P(\mathtt{sale})\right) \cdot \ v$$

$$v = rac{P(\mathtt{sale}) \cdot \mathbb{E}[\mathtt{price}|\mathtt{sale}]}{1 - \delta(1 - P(\mathtt{sale}))}$$

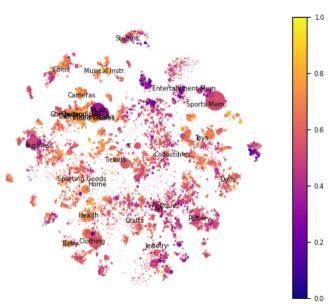
- $\blacktriangleright \ \delta = 0 \to \mathtt{value} = P(\mathtt{sale}) \cdot \mathbb{E}[\mathtt{price}|\mathtt{sale}]$
- $\blacktriangleright \ \delta = 1 \to \mathtt{value} = \mathbb{E}[\mathtt{price}|\mathtt{sale}]$

Simulate each listing to estimate P(sale) and $\mathbb{E}[price|sale]$.

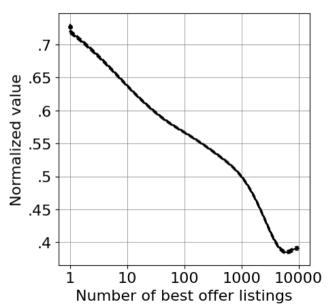
Normalized values



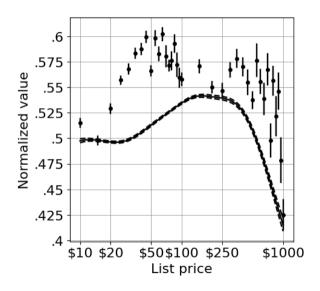
Category predicts value



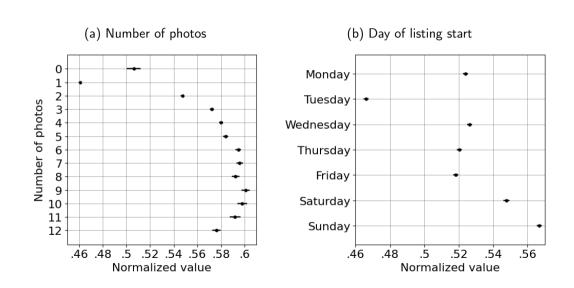
Seller experience predicts value



Round list prices have higher values



Some other predictors of value



Outline

- 1. Gameplay
- 2. Data
- 3. Simulator
- 4. Payoffs
- 5. RL seller

Training procedure

$$\pi(\mathbf{x}): \mathbf{x} \to f(a)$$

Initialize seller policy π .

- 1. Draw a listing from RL Training partition.
- 2. Simulate using π to draw seller offers.
- 3. If listing sells, payoff is sale price.
 - ightharpoonup Otherwise payoff is δv .
- 4. Update π .

Repeat until π converges to deterministic policy.

► Simulate each listing in holdout partition 10 times.

Seller offers

$$\pi(\mathbf{x}): \mathbf{x} \to f(a)$$

x : features that are observable to seller.

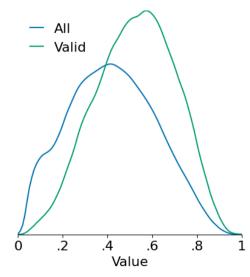
- e.g., features that summarize offers on other threads.
- ► Excludes item value.
- $a \in \{\text{expiration}, \text{reject}, .2, .25, .33, .4, .5, .6, .67, accept}\}$
 - ► Make offer when a human seller would.
 - Cannot send a message.

Valid listings

A listing is valid if agent seller makes ≥ 1 non-automatic offer.

- 1. i.e., a buyer arrives and
- 2. make an offer between the automatic thresholds and
- 3. seller has an opportunity to respond before listing ends.

Values ($\delta = 0.7$)



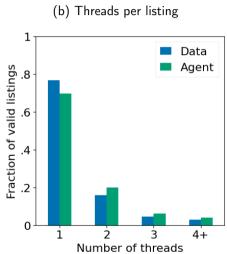
Sale prices ($\delta = 0.7$)



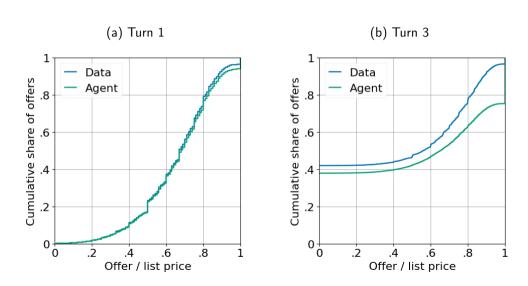
Avg normalized sale price (among sales): .76 in data / .83 for agent

Is the agent more patient than human sellers?

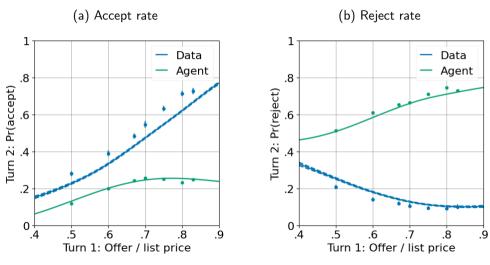




Agent seller induces full-price offers on turn 3

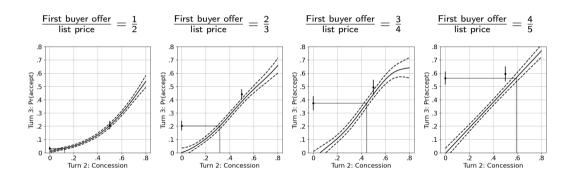


Humans and agent diverge in turn 2



Note: excludes auto-accepts and auto-rejects.

Turn 2 rejects induce accepts



Summary so far

Human sellers accept higher first offers at higher rates.

► Consistent with comparing offer to reservation value or goal.

Summary so far

Human sellers accept higher first offers at higher rates.

► Consistent with comparing offer to reservation value or goal.

The agent seller rejects higher first offers at higher rates.

► Consistent with inferring willingness to pay from offer.

Summary so far

Human sellers accept higher first offers at higher rates.

► Consistent with comparing offer to reservation value or goal.

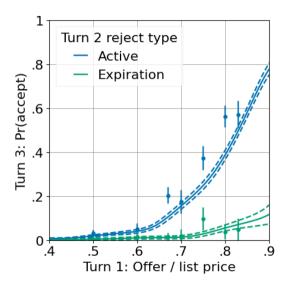
The agent seller rejects higher first offers at higher rates.

► Consistent with inferring willingness to pay from offer.

Rejections induce higher accept rates than small concessions.

► Consistent with a price integrity hypothesis.

Don't play hard to get

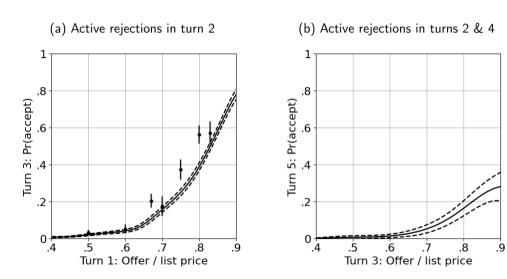


Reject rates

	Turn 2		Turn 4		Turn 6	
	Data	Agent	Data	Agent	Data	Agent
Expire	.04	-	.04	-	.03	-
Reject	.14	.63	.22	-	.22	-

Note: excludes auto-rejects.

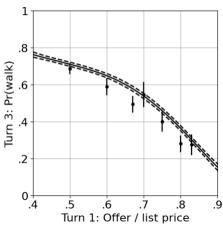
Active rejections don't have same effect in later turns



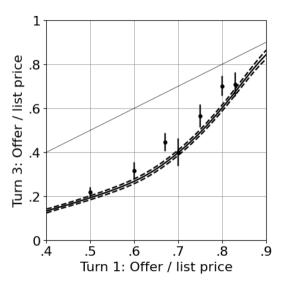
A more complete picture







A more complete picture



Bargaining is a dynamic problem

Goal is to maximize eventual payoff.

▶ Not to maximize counterparty's response in next turn.

Bargaining is a dynamic problem

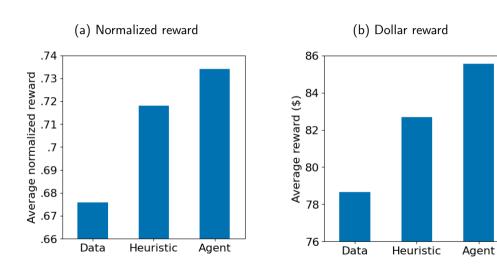
Goal is to maximize eventual payoff.

▶ Not to maximize counterparty's response in next turn.

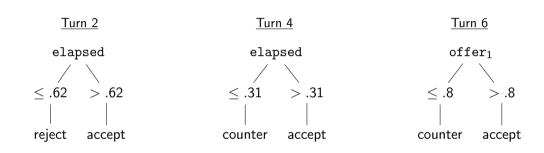
The payoff to the rejecting on turn 2 comes from:

- 1. Buyer acceptances on turn 3.
- 2. Agreements with the same buyer in a later turn.
- 3. An agreement with another buyer.

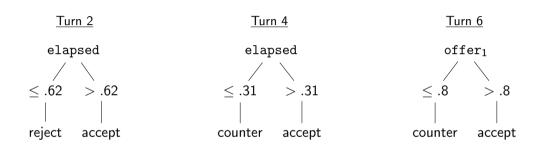
Is there a simple agent that does almost as well?



Heuristic agent

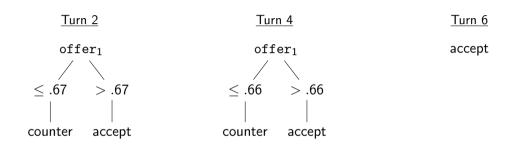


Heuristic agent

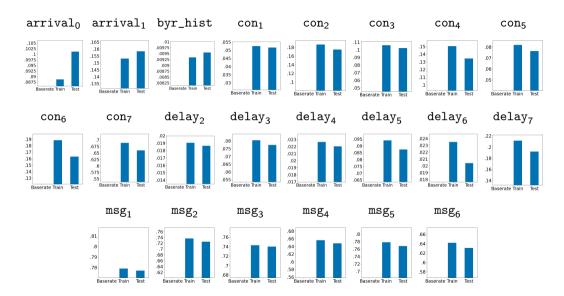


Reject early, concede later.

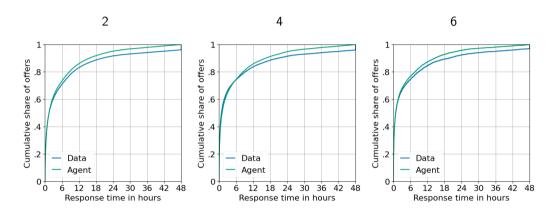
Heuristic human agent







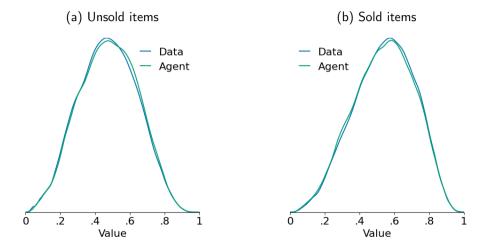
When does agent seller make offers?



Drawn from turn-specific distribution for simulated seller.

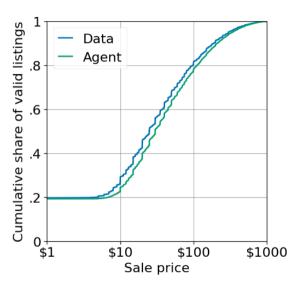
► Conditional on delay < 48 hours.

Values ($\delta = 0.7$)



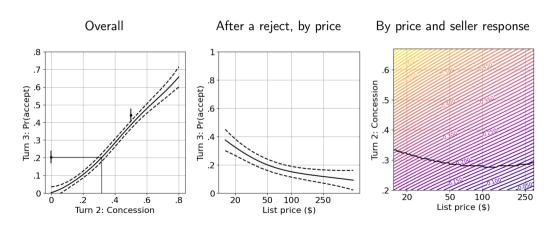
80.7% of valid listings sell in data vs. 80.3% for agent.

Sale prices



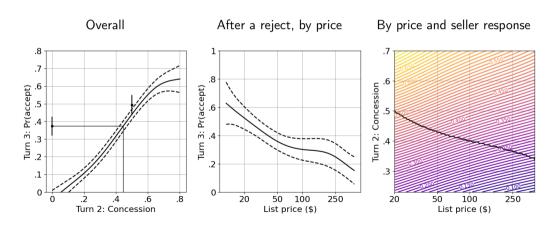
Turn 3 accept rates

$$\frac{\text{First buyer offer}}{\text{list price}} = \frac{2}{3}$$



Turn 3 accept rates

$$\frac{\text{First buyer offer}}{\text{list price}} = \frac{3}{4}$$



Turn 2 rejection rates

