

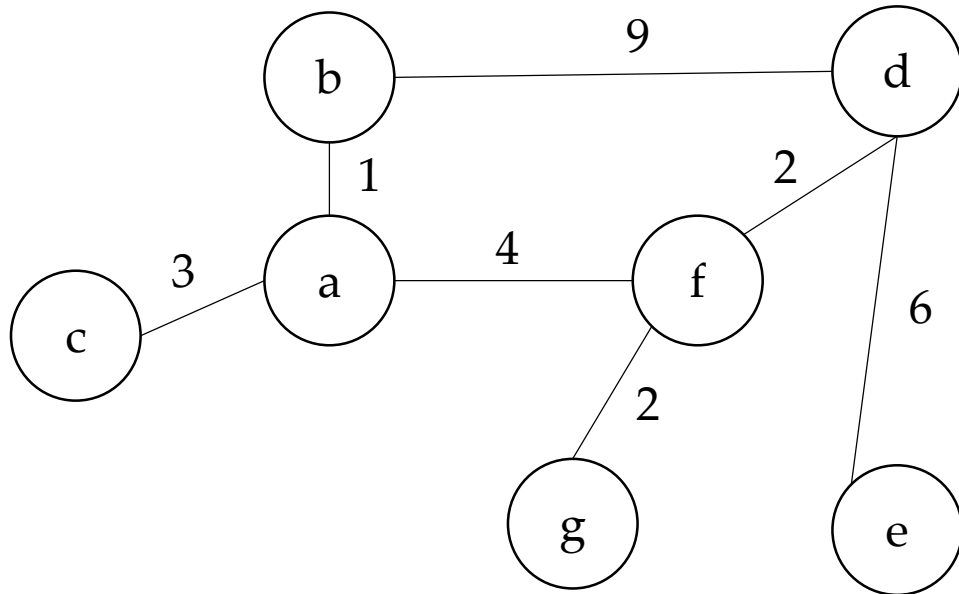
Check in First

Course Code: JI3NK

# Lab 09: Dijkstra's Algorithm and Kruskal's Minimum Spanning Tree

- For this lab, you will write two common graph algorithms: Dijkstra's Shortest path algorithm and Kruskal's Minimum Spanning Tree (MST) algorithm.
- You will read summary map information from a text file, like what you did in lab 05.

# Dijkstra's Shortest Path Algorithm



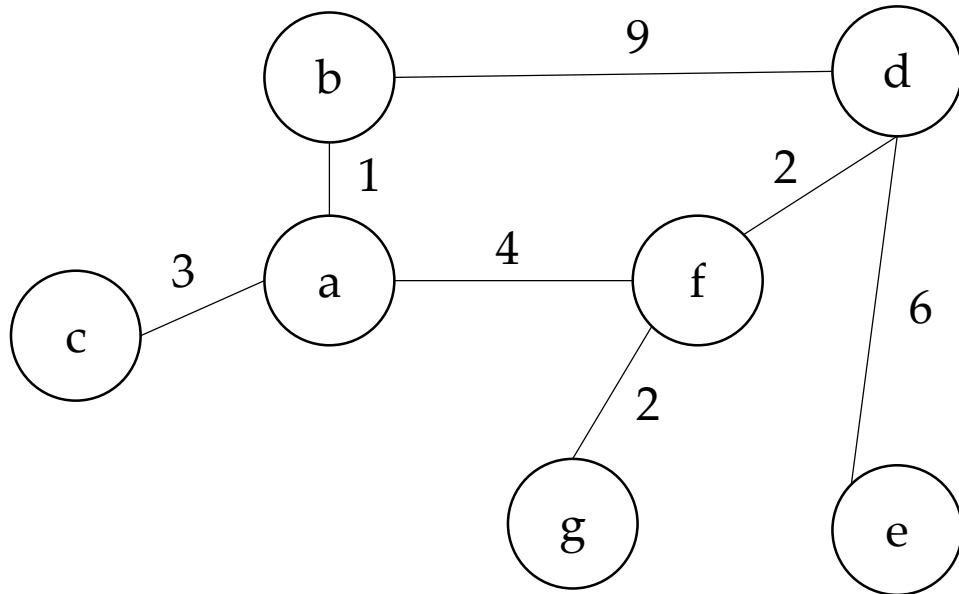
Distance Table

a
b
c
d
e
f
g

Visited Nodes:

Minimum Heap:

# Dijkstra's Shortest Path Algorithm



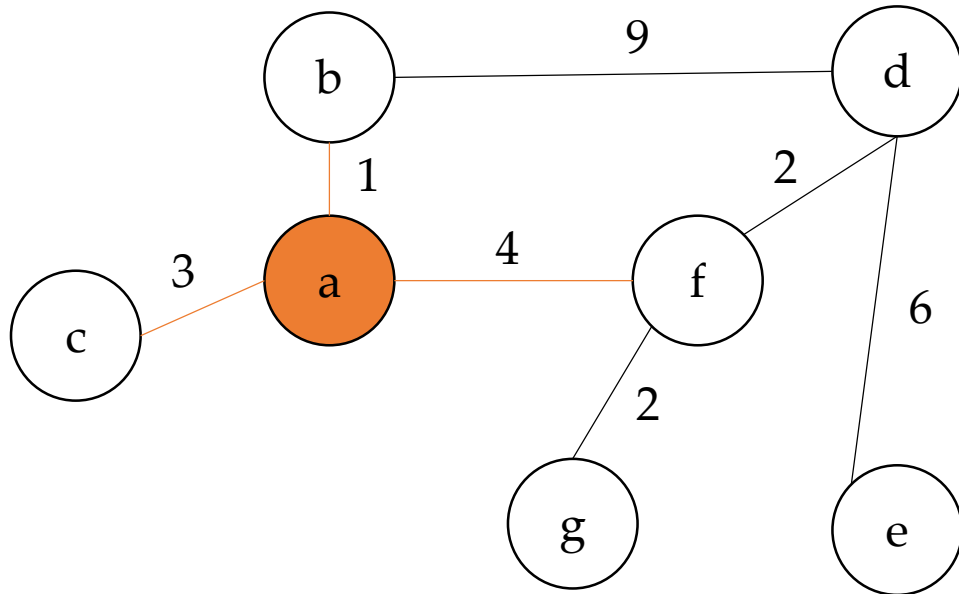
Start from **a**, initialize distance table.

Distance Table	
a	0
b	INF
c	INF
d	INF
e	INF
f	INF
g	INF

Visited Nodes:

Minimum Heap: (a, 0)

# Dijkstra's Shortest Path Algorithm



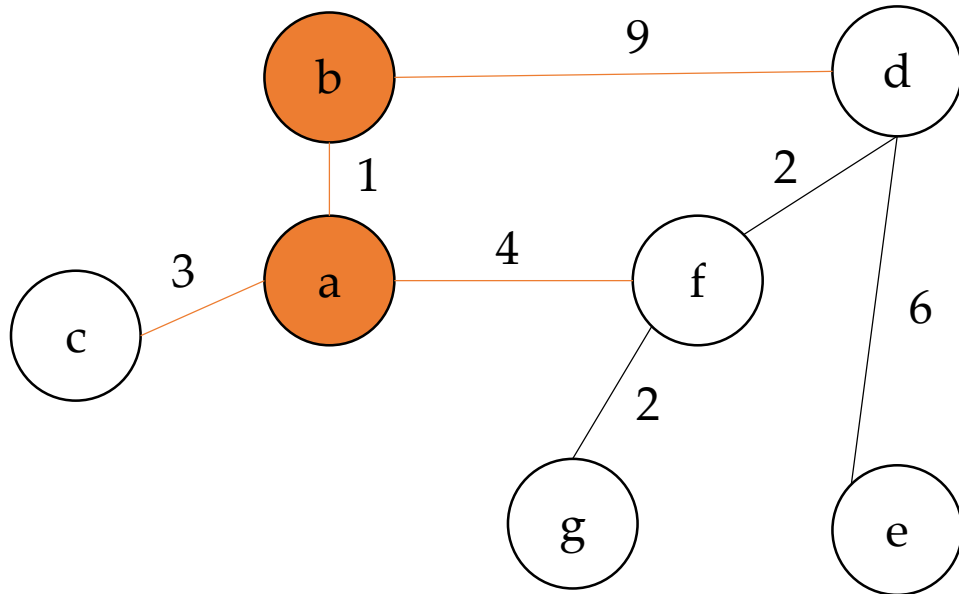
Distance Table

a	0
b	$0+1 < \text{INF? } 1$
c	$0+3 < \text{INF? } 3$
d	INF
e	INF
f	$0+4 < \text{INF? } 4$
g	INF

Visited Nodes: a

Minimum Heap: ~~(a, 0)~~ (b, 1), (c, 3), (f, 4)

# Dijkstra's Shortest Path Algorithm

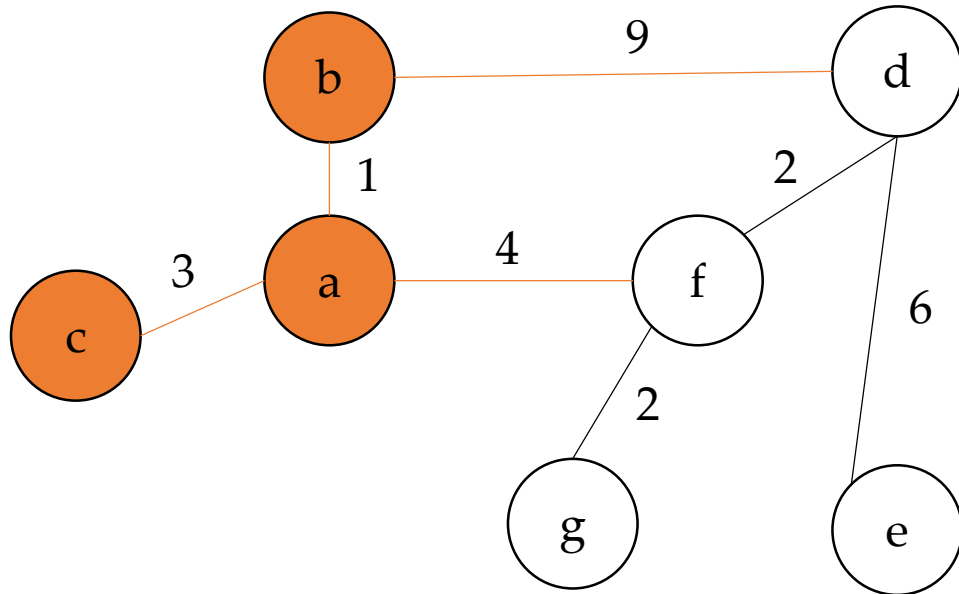


Distance Table	
a	0
b	1
c	3
d	1+9 < INF? 10
e	INF
f	4
g	INF

Visited Nodes: a, b

Minimum Heap: ~~(b, 1)~~ (c, 3), (f, 4), (d, 10)

# Dijkstra's Shortest Path Algorithm



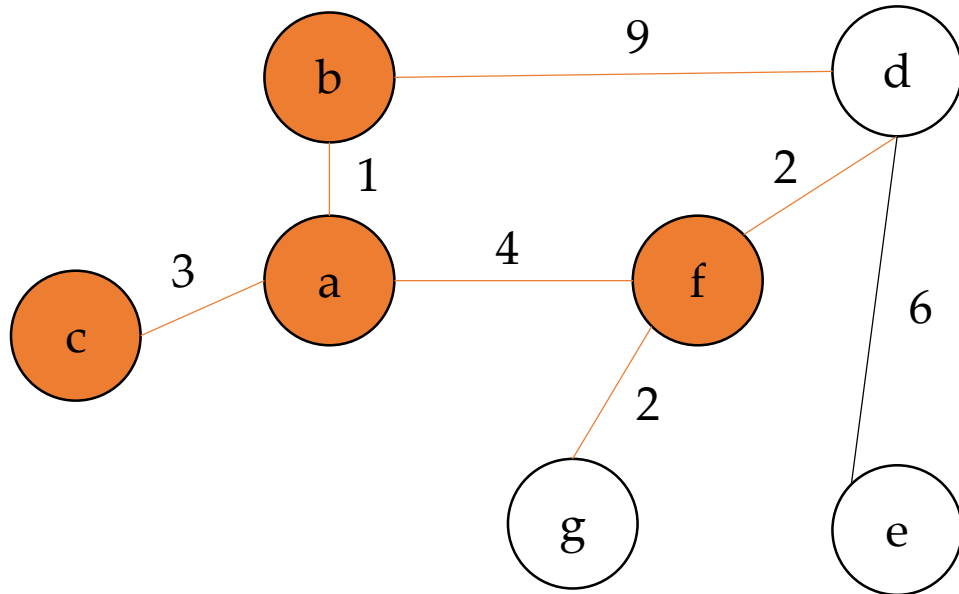
Distance Table

a	$3+3 < 0? 0$
b	1
c	3
d	10
e	INF
f	4
g	INF

Visited Nodes: a, b, c

Minimum Heap: ~~(c, 3)~~ (f, 4), (d, 10)

# Dijkstra's Shortest Path Algorithm



Distance Table

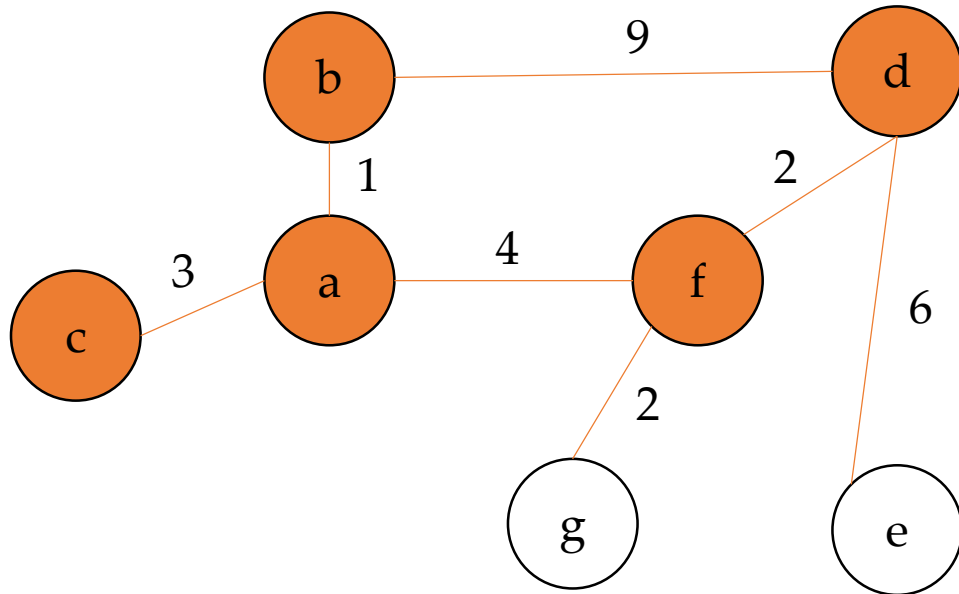
a	$4+4 < 0? 0$
b	1
c	3
d	$4+2 < 10? 6$
e	INF
f	4
g	$4+2 < \text{INF}? 6$

Visited Nodes: a, b, c, f

Minimum Heap: ~~(f, 4)~~ (d, 6), (g, 6), (d, 10)



# Dijkstra's Shortest Path Algorithm



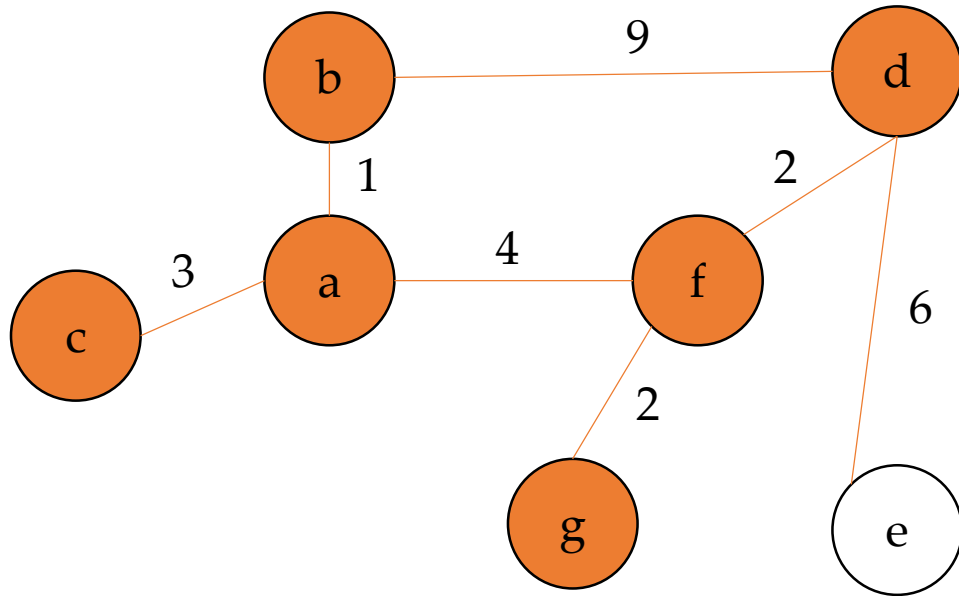
Distance Table

a	0
b	$6+9 < 1?$ 1
c	3
d	6
e	$6+6 < \text{INF}?$ 12
f	$6+2 < 4?$ 4
g	6

Visited Nodes: a, b, c, f, d

Minimum Heap: ~~(d, 6)~~ (g, 6), (d, 10), (e, 12)

# Dijkstra's Shortest Path Algorithm



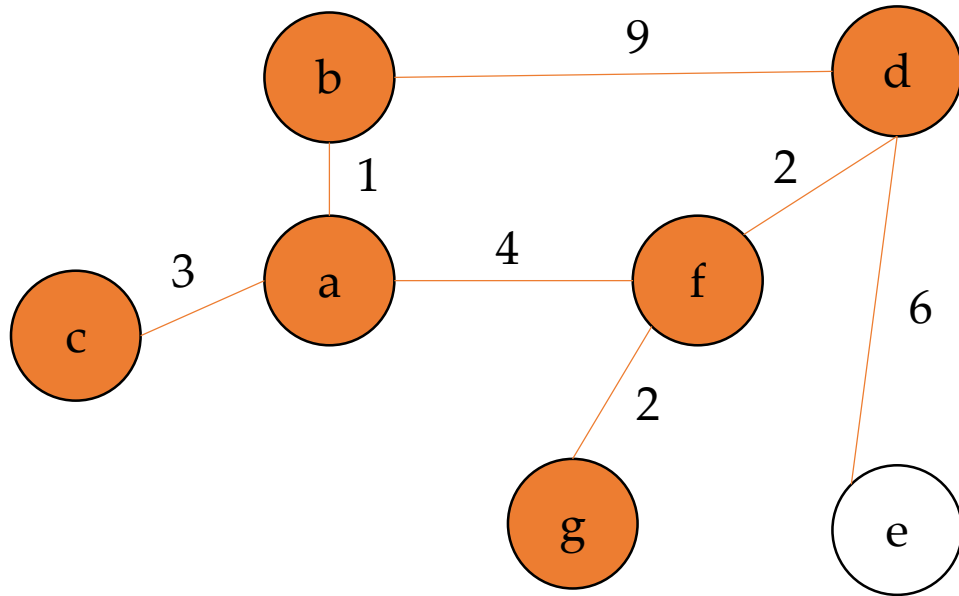
Distance Table

a	0
b	1
c	3
d	6
e	12
f	6+2 < 4? 4
g	6

Visited Nodes: a, b, c, f, d, g

Minimum Heap: ~~(g, 6)~~ (d, 10), (e, 12)

# Dijkstra's Shortest Path Algorithm



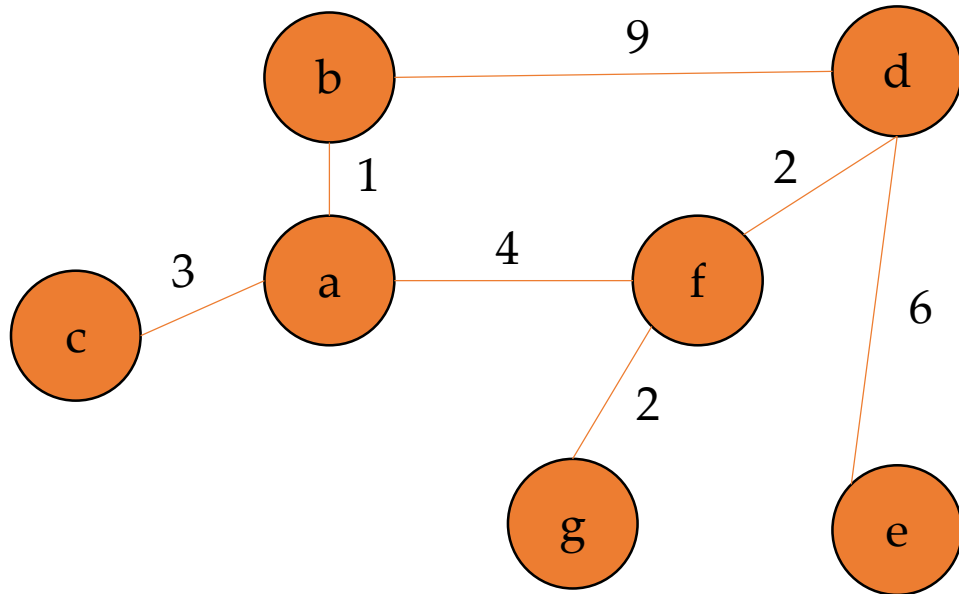
Distance Table

a	0
b	1
c	3
d	6
e	12
f	4
g	6

Visited Nodes: a, b, c, f, **d**, g

Minimum Heap: (~~d, 10~~) (e, 12)

# Dijkstra's Shortest Path Algorithm



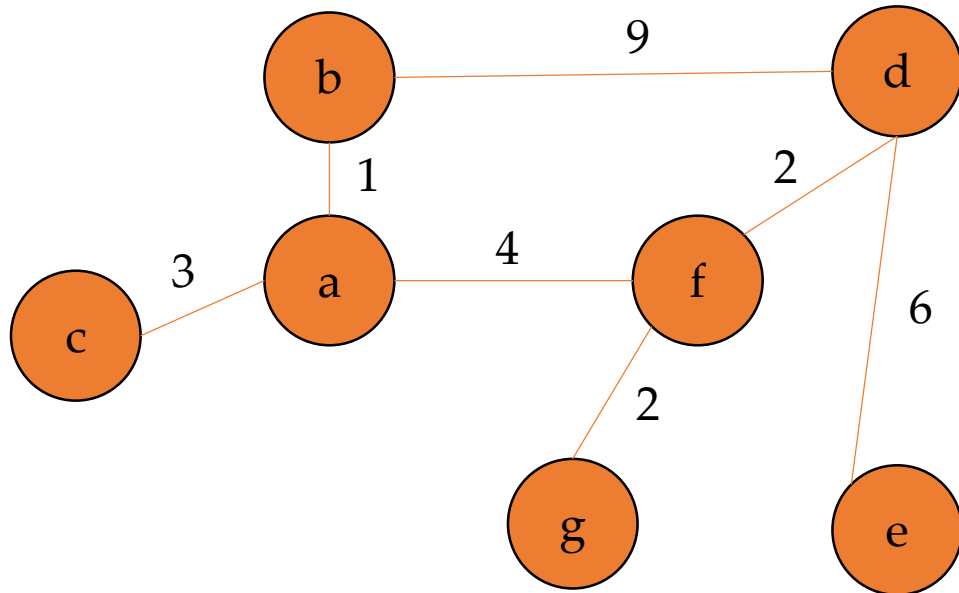
Distance Table

a	0
b	1
c	3
d	$12+6 < 6?$ 6
e	12
f	4
g	6

Visited Nodes: a, b, c, f, d, g, e

Minimum Heap: ~~(e, 12)~~

# Dijkstra's Shortest Path Algorithm



Distance Table

a	0
b	1
c	3
d	6
e	12
f	4
g	6

Visited Nodes: a, b, c, f, d, g, e

Minimum Heap:

# Pseudocode for Dijkstra's Algorithm

Create distance table, visited set, and minimum heap

Initialize distance table as [slide 5](#)

While the size of visited set  $\neq$  the size of the graph:

    get the front element of the heap

    if we have not visited this node:

        add it to the visited set

        for all its neighbors in the graph:

            new distance = heap distance + distance to its neighbors

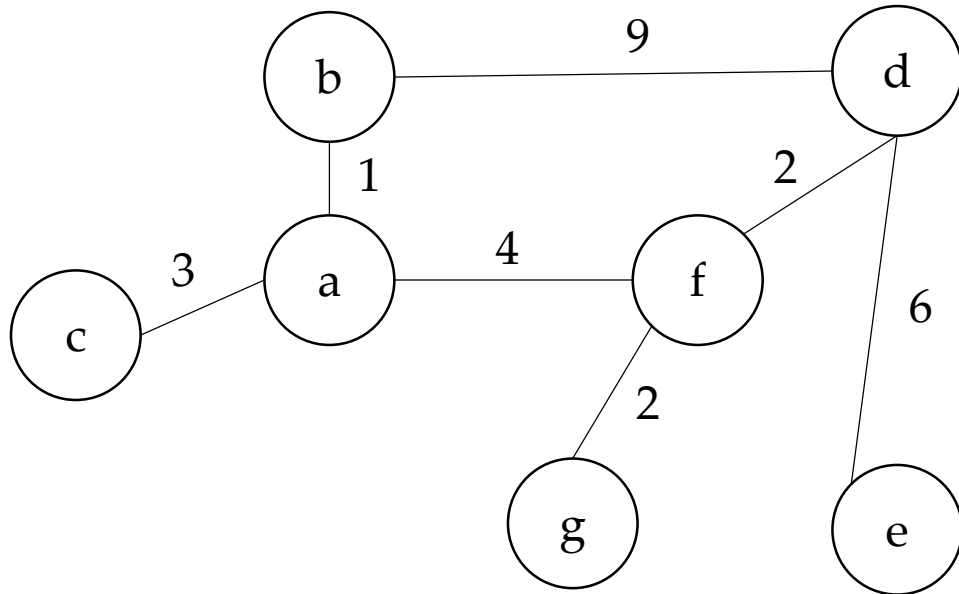
            if new distance < distance table[neighbor]:

                update distance table

                push the neighbor into the minimum heap

Print the distance table

# Kruskal's MST Algorithm



When we create the graph, we also create an edge list, and it should be sorted at the beginning of the algorithm.

Edge list:

(a, b, 1)

(f, g, 2)

(d, f, 2)

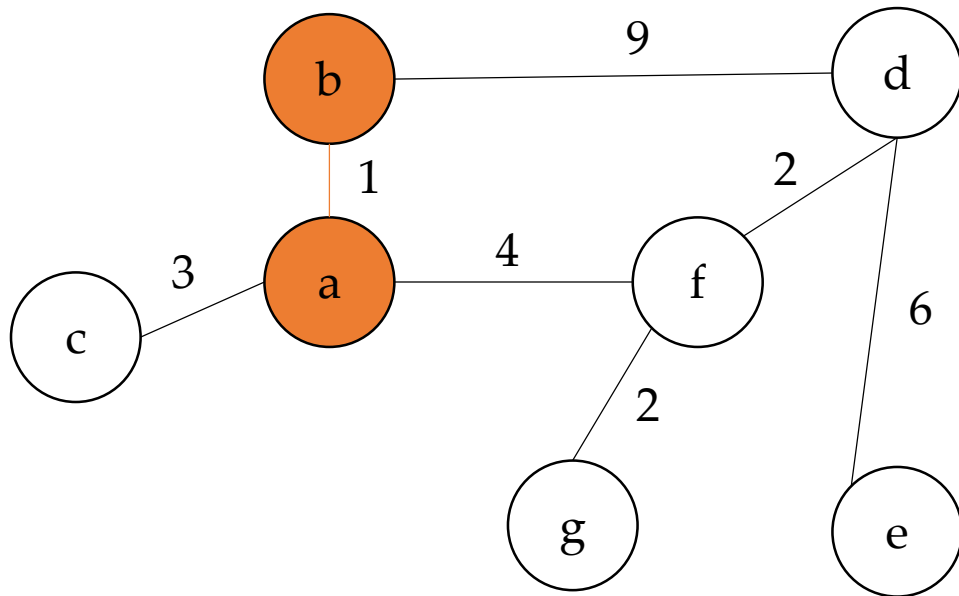
(a, c, 3)

(a, f, 4)

(d, e, 6)

(b, d, 9)

# Kruskal's MST Algorithm



Minimum spanning tree:  
(a, b, 1)

Edge list:

(a, b, 1)

(f, g, 2)

(d, f, 2)

(a, c, 3)

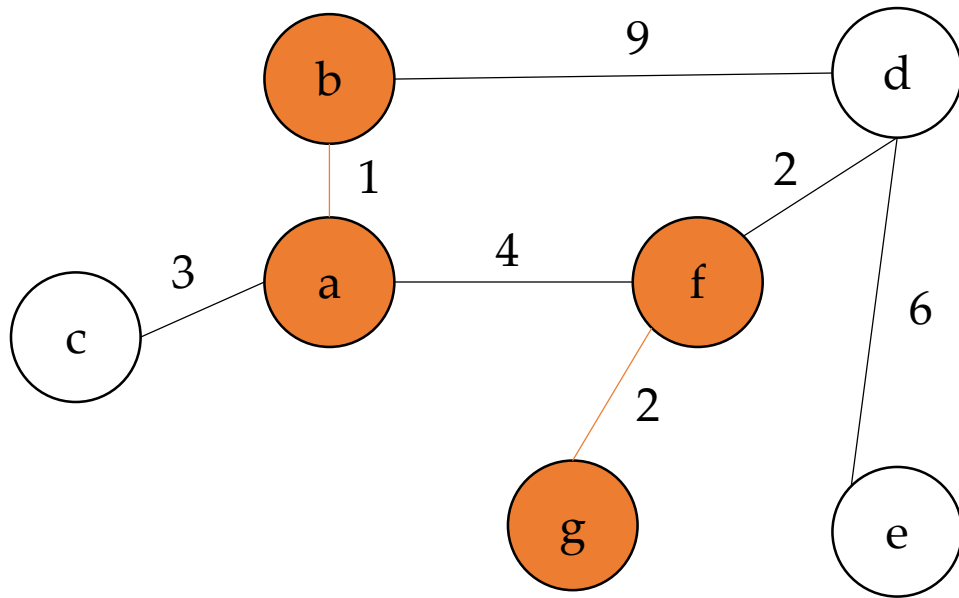
(a, f, 4)

(d, e, 6)

(b, d, 9)



# Kruskal's MST Algorithm



Minimum spanning tree:  
(a, b, 1), (f, g, 2)

Edge list:

(a, b, 1)

(f, g, 2)

(d, f, 2)

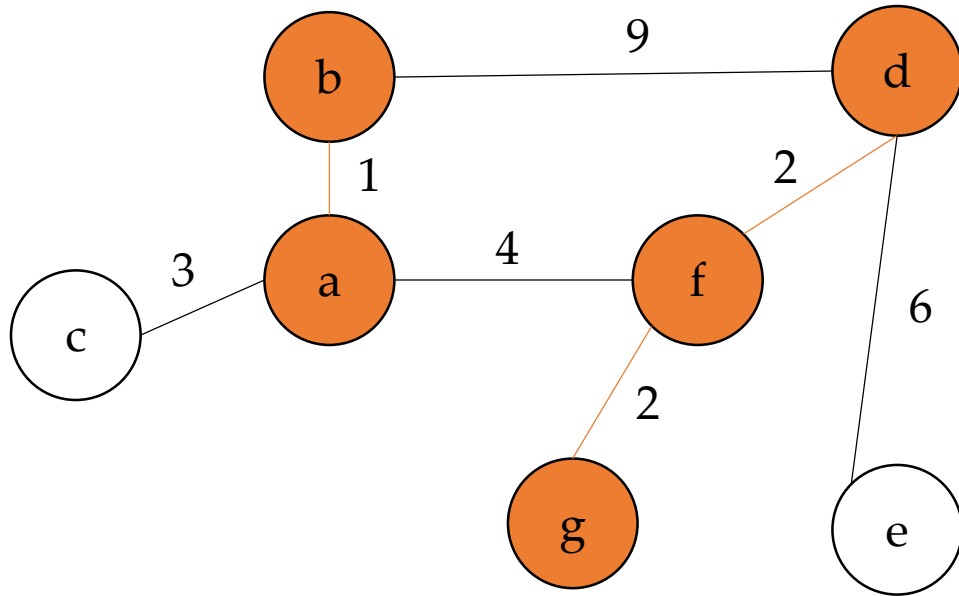
(a, c, 3)

(a, f, 4)

(d, e, 6)

(b, d, 9)

# Kruskal's MST Algorithm



Minimum spanning tree:  
(a, b, 1), (f, g, 2), (d, f, 2)

Edge list:

(a, b, 1)

(f, g, 2)

(d, f, 2)

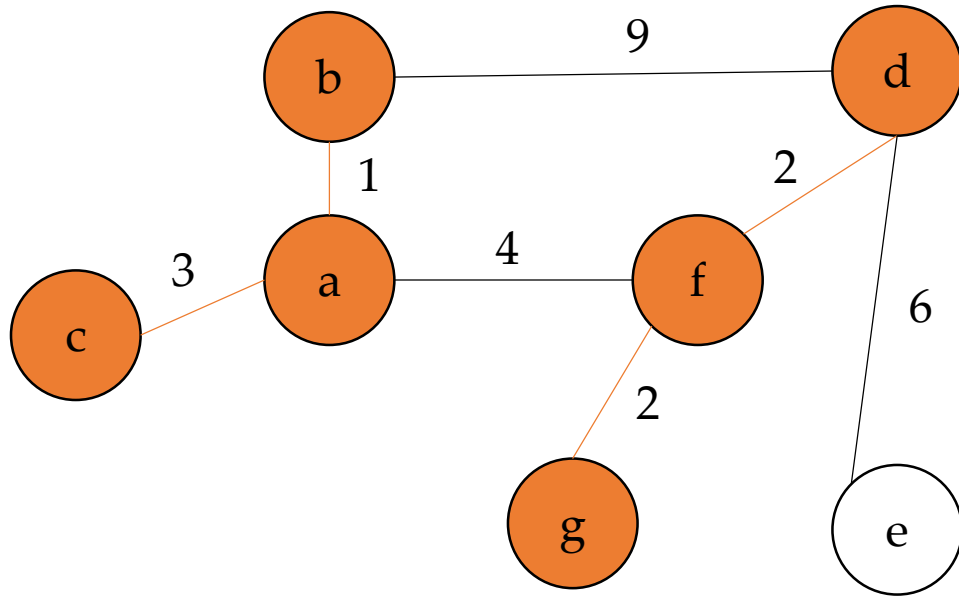
(a, c, 3)

(a, f, 4)

(d, e, 6)

(b, d, 9)

# Kruskal's MST Algorithm



Minimum spanning tree:

(a, b, 1), (f, g, 2), (d, f, 2), (a, c, 3)

Edge list:

(a, b, 1)

(f, g, 2)

(d, f, 2)

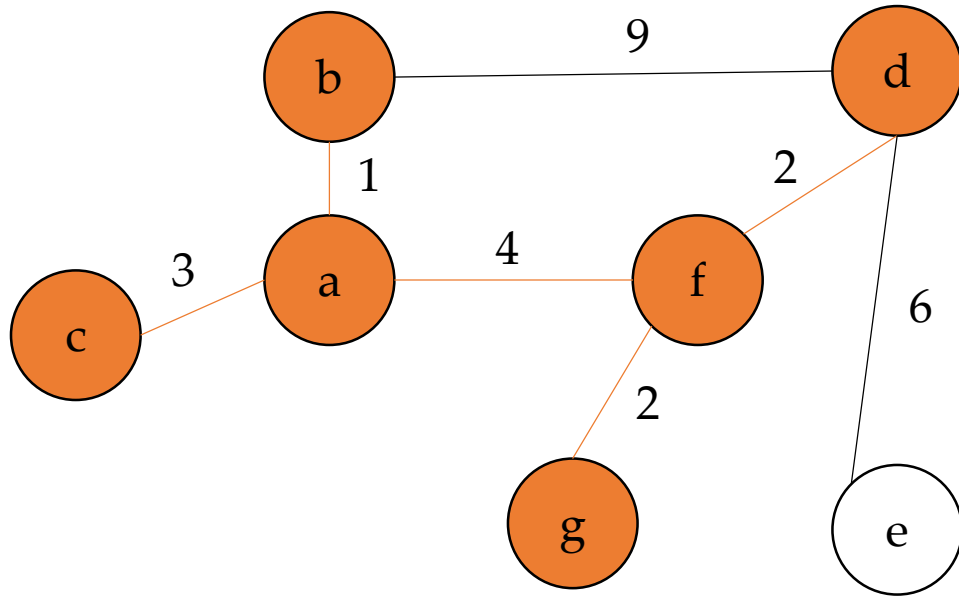
(a, c, 3)

(a, f, 4)

(d, e, 6)

(b, d, 9)

# Kruskal's MST Algorithm



Minimum spanning tree:

(a, b, 1), (f, g, 2), (d, f, 2), (a, c, 3), (a, f, 4)

Edge list:

(a, b, 1)

(f, g, 2)

(d, f, 2)

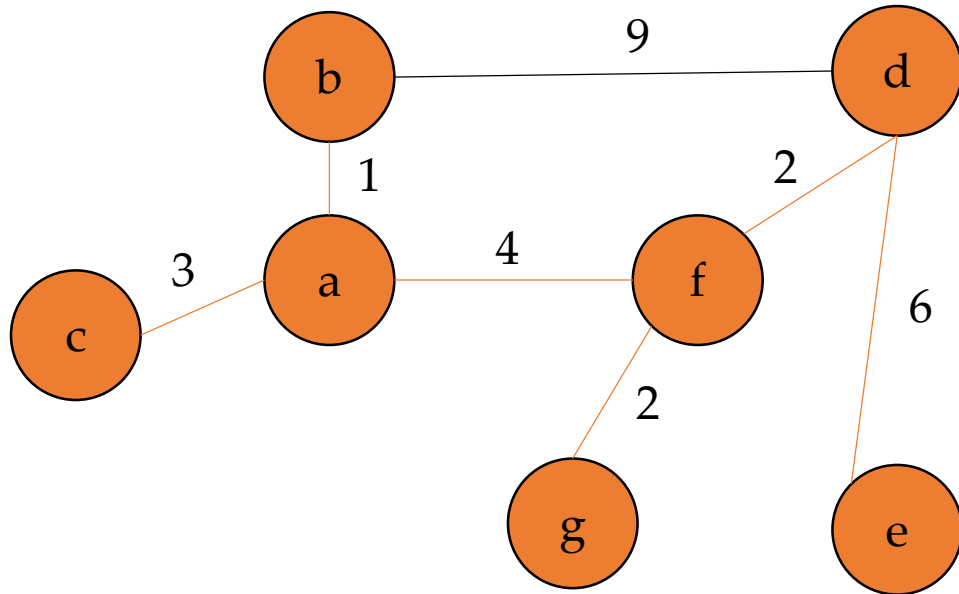
(a, c, 3)

(a, f, 4)

(d, e, 6)

(b, d, 9)

# Kruskal's MST Algorithm



Minimum spanning tree:

(a, b, 1), (f, g, 2), (d, f, 2), (a, c, 3), (a, f, 4), (d, e, 6)

Edge list:

(a, b, 1)

(f, g, 2)

(d, f, 2)

(a, c, 3)

(a, f, 4)

(d, e, 6)

(b, d, 9)

The program should stop here, but if we add b-d edge, we will have a **cycle** in the graph!

# Pseudocode for Kruskal's Algorithm

Create minSpanTreeGraph and minSpanTreeEdges

Sort the edge list (add edges in it in add\_edge() function)

Initialize i to 0

While the size of minSpanTreeEdges  $\neq$  the size of the graph - 1:

    get the i-th edge of the edge list

    add the edge into minSpanTreeGraph

    if minSpanTreeGraph contains a cycle:

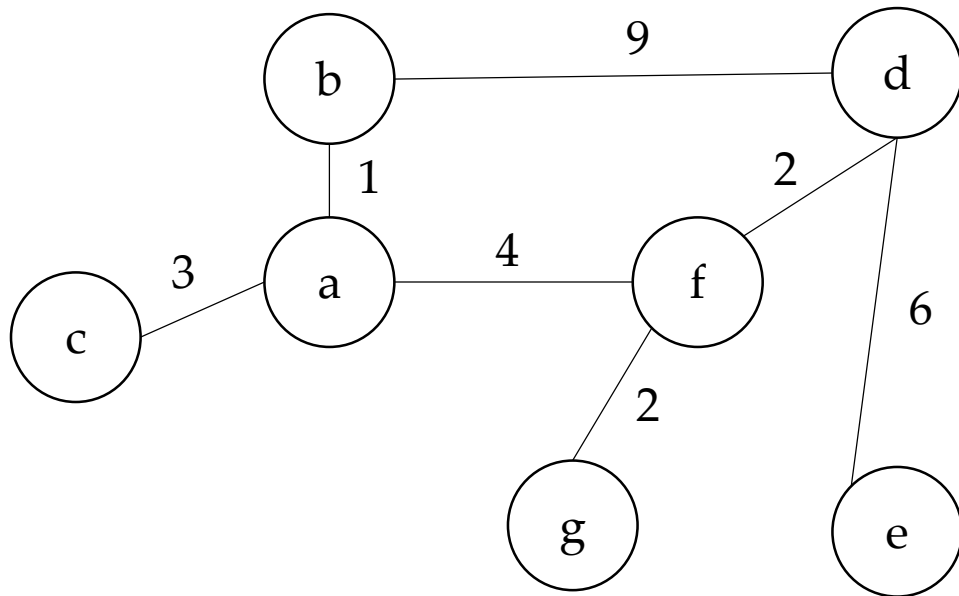
        remove the edges we just added

    else:

        add the edge into the minSpanTreeEdges

Print minSpanTreeEdges

# Decide a Cycle in an Undirected Graph



- You can use DFS to detect if there is a circle in the graph.
- Useful link:  
<https://www.geeksforgeeks.org/detect-cycle-undirected-graph/>

# Coding

- Remember we used `map<node, vector<pair<node, int> > >` in lab 05? However, we may not use it in this lab, because we need `sort (node, distance)` in the minimum heap. (I suggest that you create a new structure and write the operator function)
- Use `<climits>` library and `INT_MAX` to represent the infinite value.
- For Kruskal's algorithm, you need to create a structure (e.g. `edge`) that contains two nodes and the distance between them, and write operator `<` function so that you can use `sort()` in `<algorithm>` library.



# Submission

- Submit both source files (graphalgs.h) and at least three test cases (lab09.txt). Please keep the original test cases!
- Due date: **Next Friday 11:59 PM.**