

Inherited Sequences

The purpose of this program is to apply the computing principles of

- inheritance
- class design
- polymorphism

Write a program called `SequenceGenerator.java`. In this program, you will write several classes that model different types of sequences. All of these classes will be written in the file `SequenceGenerator.java`. If you need help writing multiple classes in the same file, refer to the video in Blackboard.

Recall that

- An arithmetic sequence is a sequence that has a constant difference between terms. If you know the first term in the sequence and the constant difference, you can find any term in the sequence. The following arithmetic sequence has a first term of 0 and a common difference of 0.5:

0, 0.5, 1.0, 1.5, 2.0, ...

- A geometric sequence is a sequence that has a constant ratio between terms. If you know the first term in the sequence and the constant ratio, you can find any term in the sequence. The following geometric sequence has a first term of 1 and a common ratio of -2:

1, -2, 4, -8, 16, ...

- The Fibonacci sequence is a sequence where each term in the sequence is the sum of the two terms that precede it. The first two terms in the Fibonacci sequence are 0 and 1. For this exercise, we will allow the user to define the first 2 terms, and subsequent terms will be determined by adding the 2 preceding terms. The following "Fibonacci-like" sequence as a first term of 1 and a second term of 0.5:

1, 0.5, 1.5, 2.0, 3.5, 5.5, 9.0, ...

Your assignment:

1. Write an *abstract class* called `Sequence`. This class defines properties and methods that all sequences will have. This class should include the following:
 - a. A `PRIVATE` field for the firstTerm in the sequence (a double)
 - b. A no-arg constructor that sets the firstTerm to 1
 - c. A constructor that sets the firstTerm using a parameter value
 - d. A method that returns the first term in the sequence
 - e. A `toString` method that you will define later, after all other classes have been written
 - f. An abstract method, `getNthTerm`, that takes an integer argument specifying the desired term
 - g. A `getNthSum` method that takes an integer argument specifying the number of terms to sum. This method calculates and returns the sum of the desired number of terms.
2. Write an `ArithmeticSequence` class that extends the `Sequence` class. This class should include the following:
 - a. A `PRIVATE` field for the common difference
 - b. A no-arg constructor that initializes the first term to 1 and the common difference to 0
 - c. A constructor that uses parameters to initialize the first term and common difference
 - d. An implementation for the abstract method defined in the `Sequence` class.
3. Write a `GeometricSequence` class that extends the `Sequence` class. This class should include the following:
 - a. A `PRIVATE` field for the ratio
 - b. A no-arg constructor that initializes the first term to 1 and the ratio to 1.
 - c. A constructor that uses parameters to initialize the ratio and the first term.
 - d. An implementation for the abstract method defined in the `Sequence` class.

4. Write a FibonacciSequence class that extends the Sequence class. This class should include the following:
 - a. A PRIVATE field for the second term in the sequence
 - b. A no-arg constructor that initializes the first term to 1 and the second term to 1
 - c. A constructor that uses parameters to initialize the first and second terms
 - d. An implementation for the abstract method defined in the Sequence class.
5. Add a toString method in the Sequence class. This method should display the first 10 terms in a sequence in a comma delimited list.
6. Write a main method that does the following:
 - a. Creates a SEQUENCE reference variable
 - b. Reads from the input file SEQ.in, which is organized as follows:
 - i. The first entry on a line is a letter that represents the type of sequence
 - ii. The second entry on a line is a numeric value that represents the first term in the sequence
 - iii. The third entry on a line is a numeric value that represents either the common difference, ratio or second term, depending upon the type of sequence.
 - c. Use toString and other methods to produce output in the following format. This output was produced using a file with this data:


```
A 3 5
G 1 2
F 0 4
```

The first 10 terms in the sequence are:

```
3.0, 8.0, 13.0, 18.0, 23.0, 28.0, 33.0, 38.0, 43.0, 48.0
sum of the first 5 terms = 65.0
```

The first 10 terms in the sequence are:

```
1.0, 2.0, 4.0, 8.0, 16.0, 32.0, 64.0, 128.0, 256.0, 512.0
sum of the first 5 terms = 31.0
```

The first 10 terms in the sequence are:

```
0.0, 4.0, 4.0, 8.0, 12.0, 20.0, 32.0, 52.0, 84.0, 136.0
sum of the first 5 terms = 28.0
```

Caveats

- You must declare a Sequence reference variable in the main method. No Arithmetic, Geometric, or Fibonacci reference variables allowed.
- Statements that output the terms and the sum of terms occur only once in your main method
- Your toString returns a String that contains the first 10 terms in the sequence and nothing else.
- You may not implement the Fibonacci getNthTerm recursively. Doing so will cost you 10 points.