

CS2403 Programming Languages

Syntax and Semantic



Chung-Ta King
Department of Computer Science
National Tsing Hua University

(Slides are adopted from *Concepts of Programming Languages*, R.W. Sebesta)

Roadmap

Ch. 1

Classification of languages
What make a “good” language?

Ch. 2

Evolution of languages

Ch. 3

How to define languages?

Ch. 4

How to compile and translate programs?

Ch. 5

Variables in languages

Ch. 7

Statements and program constructs in languages

Ch. 15

Functional and logic languages

Outline

- ◆ Introduction (Sec. 3.1)
- ◆ The General Problem of Describing Syntax (Sec. 3.2)
- ◆ Formal Methods of Describing Syntax (Sec. 3.3)
- ◆ Attribute Grammars (Sec. 3.4)
- ◆ Describing the Meanings of Programs:
Dynamic Semantics (Sec. 3.5)

Description of a Language

- ◆ **Syntax:** the form or structure of the expressions, statements, and program units
- ◆ **Semantics:** the meaning of the expressions, statements, and program units
 - What programs do, their behavior and meaning
- ◆ So, when we say one's English grammar is wrong, we actually mean _____ error?

What Kind of Errors They Have?

กิน ข้าว คน (syntax error)

คน กิน ข้าว

ข้าว กิน คน (sematic error)

Syntax and Semantics in PL

Ex:

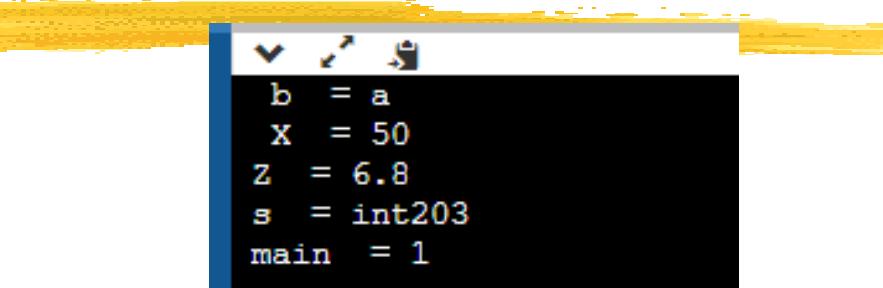
```
int x = 10;  
int y = x + u;
```

Valid Syntax : int x = 100;
 int y = x + u;

Invalid semantics : u undefined

Terminology :

```
9 #include <iostream>
10
11 using namespace std;
12
13 int main( )
14 {
15     char b = 'a';
16     int X = 50;
17     float Z=6.8;
18     char s[20] = "int203";
19     int main = 1;
20     cout << " b = " << b << '\n';
21     cout << " X = " << X << '\n';
22     cout << " Z = " << Z << '\n';
23     cout << " s = " << s << '\n';
24     cout << " main = " << main << '\n';
25
26 }
```



```
b = a
X = 50
Z = 6.8
s = int203
main = 1
```

Terminology

```
9 #include <iostream>
10
11 using namespace std;
12
13 int main( )
14 {
15     char b = 'a';
16     int X = 50;
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18     char s[20] = "int203";
19     int main = 1;
20     cout << " b = " << b << '\n';
21     cout << " X = " << X << '\n';
22     cout << " Z = " << Z << '\n';
23     cout << " s = " << s << '\n';
24     cout << " main = " << main << '\n';
25     return 0 ;
26 }
```

Reserved word : int,float,char,return
Operator (special character) : (,) , = , ;
Character constant : 'a'
Floating point constant : 6.8
Integer constant : 50
String constant : "int203"
Identifier : b,X,Z s , u ,cont
Keyword : main
Statement/sentence : char b = 'a';

Keywords are ‘predefined identifier that can be used as identifiers again

Outline

- ◆ Introduction (Sec. 3.1)
- ◆ The General Problem of Describing Syntax (Sec. 3.2)
- ◆ **Formal Methods of Describing Syntax (Sec. 3.3)**
 - Issues in Grammar Definitions: Ambiguity, Precedence, Associativity, ...
- ◆ Attribute Grammars (Sec. 3.4)
- ◆ Describing the Meanings of Programs: Dynamic Semantics (Sec. 3.5)

Type - 3 Grammar

Type-3 grammars generate regular languages. Type-3 grammars must have a single non-terminal on the left-hand side and a right-hand side consisting of a single terminal or single terminal followed by a single non-terminal.

The productions must be in the form $X \rightarrow a$ or $X \rightarrow aY$

where $X, Y \in N$ (Non terminal)

and $a \in T$ (Terminal)

The rule $S \rightarrow \epsilon$ is allowed if S does not appear on the right side of any rule.

Example

$$\begin{aligned} X &\rightarrow \epsilon \\ X &\rightarrow a \mid aY \\ Y &\rightarrow b \end{aligned}$$

Type - 2 Grammar

Type-2 grammars generate context-free languages.

The productions must be in the form $A \rightarrow \gamma$

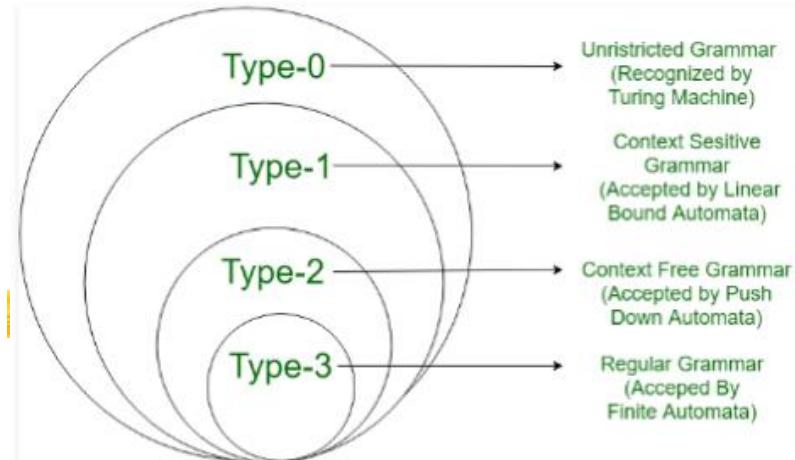
where $A \in N$ (Non terminal)

and $\gamma \in (T \cup N)^*$ (String of terminals and non-terminals).

These languages generated by these grammars are recognized by a non-deterministic pushdown automaton.

Example

$$\begin{aligned} S &\rightarrow X \ a \\ X &\rightarrow a \\ X &\rightarrow aX \\ X &\rightarrow abc \\ X &\rightarrow \epsilon \end{aligned}$$



Type - 1 Grammar

Type-1 grammars generate context-sensitive languages. The productions must be in the form

$$\alpha A \beta \rightarrow \alpha \gamma \beta$$

where $A \in N$ (Non-terminal)

and $\alpha, \beta, \gamma \in (T \cup N)^*$ (Strings of terminals and non-terminals)

The strings α and β may be empty, but γ must be non-empty.

The rule $S \rightarrow \epsilon$ is allowed if S does not appear on the right side of any rule. The languages generated by these grammars are recognized by a linear bounded automaton.

Example

$$\begin{aligned} AB &\rightarrow AbBc \\ A &\rightarrow bcA \\ B &\rightarrow b \end{aligned}$$

Type - 0 Grammar

Type-0 grammars generate recursively enumerable languages. The productions have no restrictions.

They are any phrase structure grammar including all formal grammars.

They generate the languages that are recognized by a Turing machine.

The productions can be in the form of $\alpha \rightarrow \beta$ where α is a string of terminals and nonterminals with at least one non-terminal and α cannot be null. β is a string of terminals and non-terminals.

Example

$$\begin{aligned} S &\rightarrow ACaB \\ Bc &\rightarrow acB \\ CB &\rightarrow DB \\ aD &\rightarrow Db \end{aligned}$$

ตัวอย่าง 1.1

ไวยากรณ์ $G_0 = (\{S, A, B\}, \{a, b\}, S, \{S \rightarrow ABB, AB \rightarrow b, A \rightarrow \epsilon, bB \rightarrow cA, B \rightarrow a\})$

ไวยากรณ์ $G_1 = (\{S, A, B\}, \{a, b\}, S, \{S \rightarrow ABA, BA \rightarrow bB, bB \rightarrow \epsilon, A \rightarrow a, B \rightarrow b\})$

ไวยากรณ์ $G_2 = (\{S, A, B\}, \{a, b\}, S, \{S \rightarrow AB, A \rightarrow bB, A \rightarrow a, B \rightarrow \epsilon, B \rightarrow b\})$

ไวยากรณ์ $G_3 = (\{S, A, B\}, \{a, b\}, S, \{S \rightarrow aA, A \rightarrow bB, A \rightarrow a, A \rightarrow \epsilon, B \rightarrow b\})$

ไวยากรณ์ $G_4 = (\{S, A, B\}, \{a, b\}, S, \{S \rightarrow Aa, A \rightarrow Bb, A \rightarrow a, A \rightarrow \epsilon, B \rightarrow b\})$

กำหนดให้ไวยากรณ์ G_{1_1} ประกอบด้วย

ไวยากรณ์ $G_{1_1} : (\{S, B, C\}, \{a, b, c\}, S, P)$  Formal language.

โดย $P = \{S \rightarrow aSBC, S \rightarrow abC, bB \rightarrow bb, bC \rightarrow bc, CB \rightarrow BC, cC \rightarrow cc\}$

จงพิสูจน์ว่า $a^2b^2c^2$ เป็นประโยคที่อยู่ในภาษา $L(G_{1_1})$ หรือไม่

$S \Rightarrow aSBC$ แทนคุ้วย $S \rightarrow aSBC$

$\Rightarrow aabCBC$ แทนคุ้วย $S \rightarrow abC$

$\Rightarrow aabBCC$ แทนคุ้วย $CB \rightarrow BC$

$\Rightarrow aabbCC$ แทนคุ้วย $bB \rightarrow bb$

$\Rightarrow aabbcC$ แทนคุ้วย $bC \rightarrow bc$

$\Rightarrow aabbcc$ แทนคุ้วย $cC \rightarrow cc$



Formal Description of Syntax

Most widely known methods for describing syntax:

- ◆ Formal form (Context-Free Grammars)
 - Developed by Noam Chomsky in the mid-1950s
 - Define a class of languages: **context-free languages**

- ◆ Backus-Naur Form (1959)
 - Invented by John Backus to describe ALGOL 58
 - Equivalent to context-free grammars

Lexeme & token

"if",a,c,f -> terminal(lexeme)

S -> aBcAf ("if ",reserved word) ->token

S -> "if" B "{"
 A

("{",operator) ->token

"}"
("}",operator) ->token

in PL , **terminal symbols**, "a" or "if" , and called as "*lexeme*".
and its category of lexemes is called "*token*"

BNF (it 's equivalent to "CFG")

- ◆ A BNF grammar consists of four parts:
 - The set of *tokens* and *lexemes* (*terminals*)
 - The set of *non-terminals*, e.g., <sentence>, <verb>
 - The *start* symbol, e.g., <sentence>
 - The set of *production rules*, e.g.,

<sentence> → <noun> <verb> <preposition> <noun>

<noun> → *place*

<verb> → “is” | “belongs” <preposition> → “in” | “to”

The *start* symbol is the particular non-terminal that forms the starting point of generating a sentence of the language
ie. <sentence> .

An Example Grammar

```
<program> → <stmts>
<stmts> → <stmt> | <stmt> ; <stmts>
<stmt> → <var> = <expr>
<var> → a | b | c | d
<expr> → <term> + <term> | <term> - <term>
<term> → <var> | const
```

<program> is the start symbol

a, b, c, const, +, -, ;, = are the terminals (*lexemes*)

Derivation

- ◆ A *derivation* is a repeated application of rules, starting with the start symbol and ending with a sentence (all terminal symbols), e.g.,

```
<program> => <stmts>
              => <stmt>
              => <var> = <expr>
              => a = <expr>
              => a = <term> + <term>
              => a = <var> + <term>
              => a = b + <term>
              => a = b + const
```

Derivation Leftmost & rightmost

$$S \rightarrow aABb$$

$$A \rightarrow aA \mid a$$

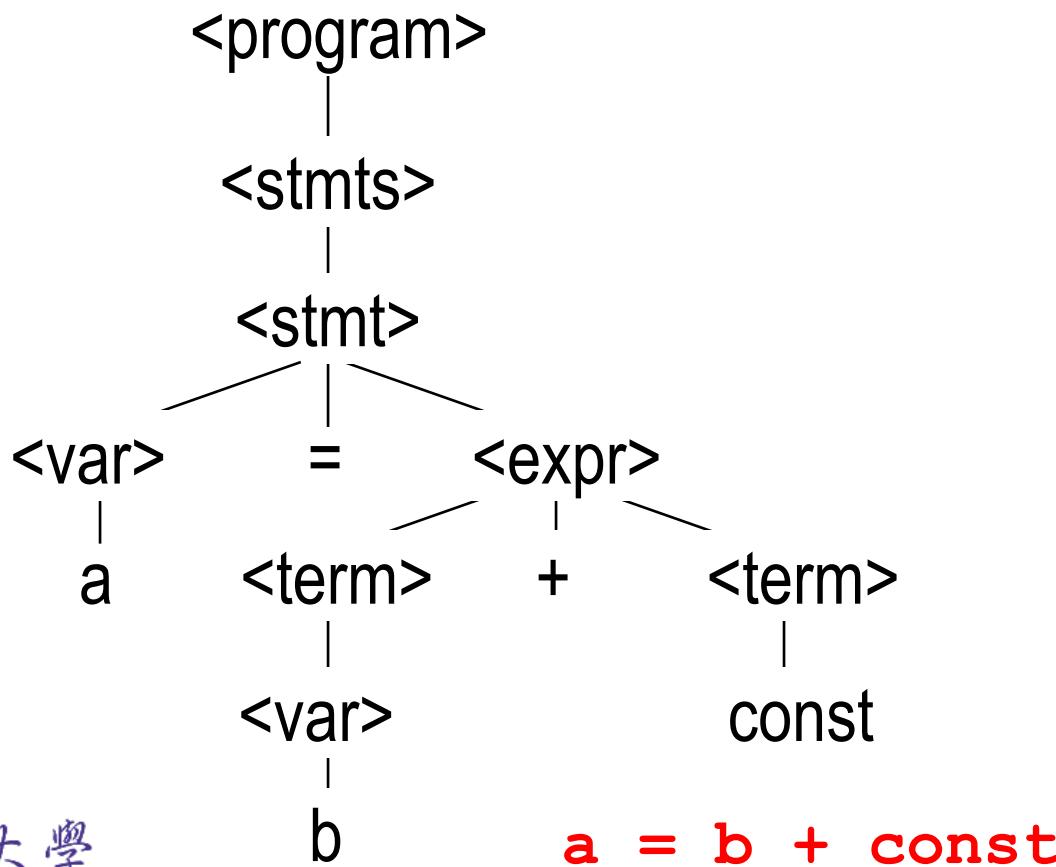
$$B \rightarrow bB \mid b$$

Derivations for a string "aaabb".

- **Leftmost:** $S \Rightarrow a\underline{AB}b \Rightarrow aa\underline{AB}b \Rightarrow aaa\underline{B}b \Rightarrow aaabb$
- **Rightmost:** $S \Rightarrow a\underline{AB}b \Rightarrow a\underline{A}bb \Rightarrow aa\underline{Ab}b \Rightarrow aaabb$

Parse Tree

- ◆ A hierarchical representation of a derivation



Ambiguity in Grammars

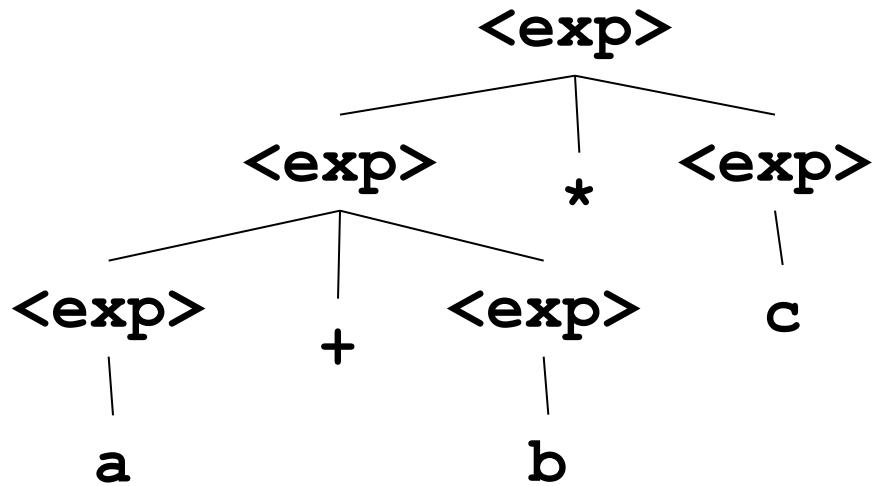
- ♦ If a sentential form can be generated by two or more distinct parse trees, the grammar is said to be *ambiguous*, because it has two or more different meanings
- ♦ Problem with ambiguity:
 - Consider the following grammar and the sentence $a+b*c$

$$\begin{aligned}\langle \text{exp} \rangle &\rightarrow \langle \text{exp} \rangle + \langle \text{exp} \rangle \mid \\ &\quad \langle \text{exp} \rangle * \langle \text{exp} \rangle \mid \\ &\quad (\langle \text{exp} \rangle) \mid \\ &\quad a \mid b \mid c\end{aligned}$$

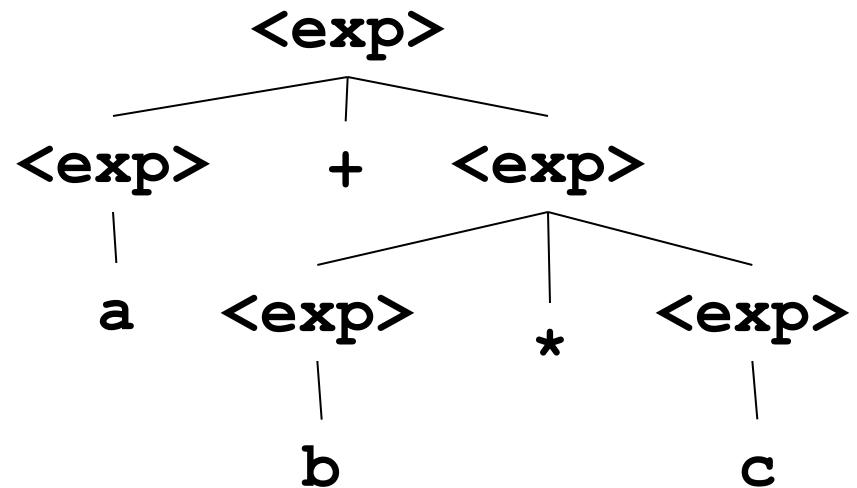
An Ambiguous Grammar

```
<exp> → <exp> + <exp> |  
          <exp> * <exp> |  
          (<exp>) |  
          a | b | c
```

- ◆ Two different parse trees for $a+b*c$



Means $(a+b)^*c$



Means $a+(b*c)$

Three “Equivalent” Grammars

G1 : $\langle subexp \rangle \rightarrow a \mid b \mid c \mid \langle subexp \rangle - \langle subexp \rangle$

G2 : $\langle subexp \rangle \rightarrow \langle var \rangle - \langle subexp \rangle \mid \langle var \rangle$
 $\langle var \rangle \rightarrow a \mid b \mid c$

G3 : $\langle subexp \rangle \rightarrow \langle subexp \rangle - \langle var \rangle \mid \langle var \rangle$
 $\langle var \rangle \rightarrow a \mid b \mid c$

These grammars all define the same language: the language of strings that contain one or more **a**s, **b**s or **c**s separated by minus signs, e.g., **a-b-c**. But...

Extended BNF

- ◆ Optional parts are placed in brackets []
 $\langle \text{proc_call} \rangle \rightarrow \text{ident} [(\langle \text{expr_list} \rangle)]$
- ◆ Alternative parts of RHSs are placed inside parentheses and separated via vertical bars
 $\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle \ (+ | -) \ \text{const}$
- ◆ Repetitions (0 or more) are placed inside braces { }
 $\langle \text{ident} \rangle \rightarrow \text{letter} \ \{ \text{letter} | \text{digit} \}$

BNF and EBNF

◆ BNF

```
<expr> → <expr> + <term>
         | <expr> - <term>
         | <term>

<term> → <term> * <factor>
         | <term> / <factor>
         | <factor>
```

◆ EBNF

```
<expr> → <term> { (+ | -) <term> }
<term> → <factor> { (* | /) <factor> }
```