

CS2403 Programming Languages

Syntax and Semantic



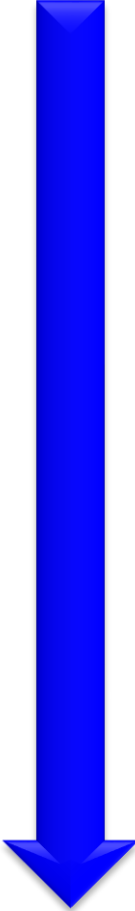
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(Slides are adopted from *Concepts of Programming Languages*, R.W. Sebesta)

Roadmap



Ch. 1	Classification of languages What make a “good” language?
Ch. 2	Evolution of languages
Ch. 3	How to define languages?
Ch. 4	How to compile and translate programs?
Ch. 5	Variables in languages
Ch. 7	Statements and program constructs in languages
Ch. 15	Functional and logic languages

Outline

- ◆ Introduction (Sec. 3.1)
- ◆ The General Problem of Describing Syntax (Sec. 3.2)
- ◆ Formal Methods of Describing Syntax (Sec. 3.3)
- ◆ Attribute Grammars (Sec. 3.4)
- ◆ Describing the Meanings of Programs: Dynamic Semantics (Sec. 3.5)

Description of a Language

- ◆ **Syntax:** the form or structure of the expressions, statements, and program units
- ◆ **Semantics:** the meaning of the expressions, statements, and program units
 - What programs do, their behavior and meaning
- ◆ So, when we say one's English grammar is wrong, we actually mean _____ error?

What Kind of Errors They Have?

กิน ข้าว คน (syntax error)

คน กิน ข้าว

ข้าว กิน คน (semantic error)

Syntax and Semantics in PL

Ex:

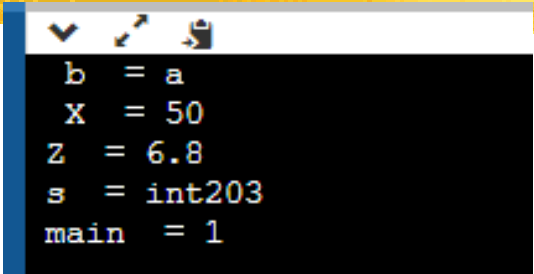
```
int x = 10;  
int y = x + u;
```

Valid Syntax : int x = 100;
 int y = x + u;

Invalid semantics : **u undefined**

Terminology :

```
9  #include <iostream>
10
11  using namespace std;
12
13  int main( )
14  {
15      char b = 'a';
16      int X = 50;
17      float Z=6.8;
18      char s[20] = "int203";
19      int main = 1;
20      cout << "  b  = " << b << '\n';
21      cout << "  X  = " << X << '\n';
22      cout << "  Z  = " << Z << '\n';
23      cout << "  s  = " << s << '\n';
24      cout << " main = " << main << '\n';
25      return 0 ;
26  }
```



A screenshot of a debugger's 'Variables' window. It shows a list of variables and their current values: 'b' is 'a', 'X' is 50, 'Z' is 6.8, 's' is 'int203', and 'main' is 1. The window has a dark background and a light blue header bar with icons for expand, edit, and delete.

```
b  = a
X  = 50
Z  = 6.8
s  = int203
main = 1
```

Terminology

```
#include <iostream>

using namespace std;

int main( )
{
    char b = 'a';
    int X = 50;
    float Z=6.8;
    char s[20] = "int203";
    int main = 1;
    cout << " b = " << b << '\n';
    cout << " X = " << X << '\n';
    cout << " Z = " << Z << '\n';
    cout << " s = " << s << '\n';
    cout << " main = " << main << '\n';
    return 0 ;
}
```

Reserved word : `int, float, char, return`

Operator (Special character) : `(,) , = , ;`

Character constant : `'a'`

Floating point constant : `6.8`

Integer constant : `50`

String constant : `"int203"`

Identifier : `b, X, Z s , u , cont`

Keyword : `main`

Statement/sentence : `char b = 'a';`

Keywords are 'predefined identifier that can be used as identifiers again

Outline

- ◆ Introduction (Sec. 3.1)
- ◆ The General Problem of Describing Syntax (Sec. 3.2)
- ◆ **Formal Methods of Describing Syntax (Sec. 3.3)**
 - Issues in Grammar Definitions: Ambiguity, Precedence, Associativity, ...
- ◆ Attribute Grammars (Sec. 3.4)
- ◆ Describing the Meanings of Programs: Dynamic Semantics (Sec. 3.5)

Type - 3 Grammar

Type-3 grammars generate regular languages. Type-3 grammars must have a single non-terminal on the left-hand side and a right-hand side consisting of a single terminal or single terminal followed by a single non-terminal.

The productions must be in the form $X \rightarrow a$ or $X \rightarrow aY$

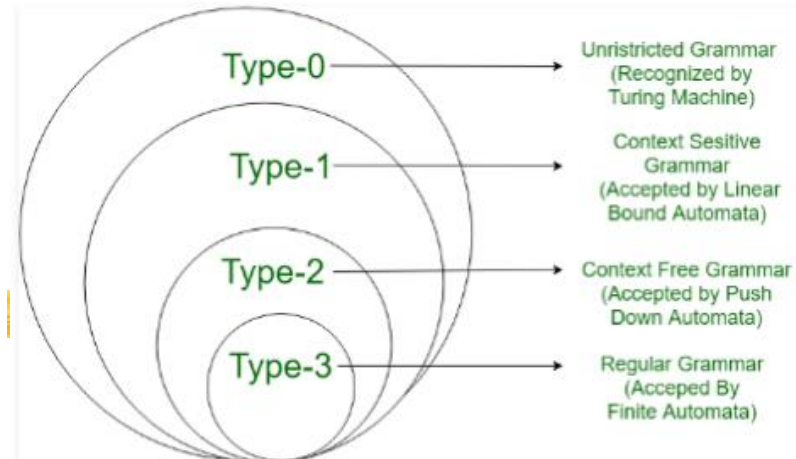
where $X, Y \in N$ (Non terminal)

and $a \in T$ (Terminal)

The rule $S \rightarrow \epsilon$ is allowed if S does not appear on the right side of any rule.

Example

```
X → ε
X → a | aY
Y → b
```



Type - 1 Grammar

Type-1 grammars generate context-sensitive languages. The productions must be in the form

$$\alpha A \beta \rightarrow \alpha \gamma \beta$$

where $A \in N$ (Non-terminal)

and $\alpha, \beta, \gamma \in (T \cup N)^*$ (Strings of terminals and non-terminals)

The strings α and β may be empty, but γ must be non-empty.

The rule $S \rightarrow \epsilon$ is allowed if S does not appear on the right side of any rule. The languages generated by these grammars are recognized by a linear bounded automaton.

Example

```
AB → AbBc
A → bcA
B → b
```

Type - 2 Grammar

Type-2 grammars generate context-free languages.

The productions must be in the form $A \rightarrow \gamma$

where $A \in N$ (Non terminal)

and $\gamma \in (T \cup N)^*$ (String of terminals and non-terminals).

These languages generated by these grammars are recognized by a non-deterministic pushdown automaton.

Example

```
S → X a
X → a
X → aX
X → abc
X → ε
```

Type - 0 Grammar

Type-0 grammars generate recursively enumerable languages. The productions have no restrictions. They are any phase structure grammar including all formal grammars.

They generate the languages that are recognized by a Turing machine.

The productions can be in the form of $\alpha \rightarrow \beta$ where α is a string of terminals and nonterminals with at least one non-terminal and α cannot be null. β is a string of terminals and non-terminals.

Example

```
S → ACaB
Bc → acB
CB → DB
aD → Db
```

ตัวอย่าง 1.1

ไวยากรณ์ $G_0 = (\{S, A, B\}, \{a, b\}, S, \{ S \rightarrow ABB, AB \rightarrow b, A \rightarrow \epsilon, bB \rightarrow cA, B \rightarrow a \})$

ไวยากรณ์ $G_1 = (\{S, A, B\}, \{a, b\}, S, \{ S \rightarrow ABA, BA \rightarrow bB, bB \rightarrow \epsilon, A \rightarrow a, B \rightarrow b \})$

ไวยากรณ์ $G_2 = (\{S, A, B\}, \{a, b\}, S, \{ S \rightarrow AB, A \rightarrow bB, A \rightarrow a, B \rightarrow \epsilon, B \rightarrow b \})$

ไวยากรณ์ $G_3 = (\{S, A, B\}, \{a, b\}, S, \{ S \rightarrow aA, A \rightarrow bB, A \rightarrow a, A \rightarrow \epsilon, B \rightarrow b \})$

ไวยากรณ์ $G_4 = (\{S, A, B\}, \{a, b\}, S, \{ S \rightarrow Aa, A \rightarrow Bb, A \rightarrow a, A \rightarrow \epsilon, B \rightarrow b \})$

กำหนดให้ไวยากรณ์ G_{1_1} ประกอบด้วย

ไวยากรณ์ $G_{1_1} : (\{S, B, C\}, \{a, b, c\}, S, P)$  Formal language.

โดย $P = \{ S \rightarrow aSBC, S \rightarrow abC, bB \rightarrow bb, bC \rightarrow bc, CB \rightarrow BC, cC \rightarrow cc \}$

จงพิสูจน์ว่า $a^2b^2c^2$ เป็นประโยคที่อยู่ในภาษา $L(G_{1_1})$ หรือไม่

$S \Rightarrow aSBC$ แทนด้วย $S \rightarrow aSBC$

$\Rightarrow aabCBC$ แทนด้วย $S \rightarrow abC$

$\Rightarrow aabBCC$ แทนด้วย $CB \rightarrow BC$

$\Rightarrow aabbCC$ แทนด้วย $bB \rightarrow bb$

$\Rightarrow aabb cC$ แทนด้วย $bC \rightarrow bc$

$\Rightarrow aabbcc$ แทนด้วย $cC \rightarrow cc$



Formal Description of Syntax

Most widely known methods for describing syntax:

- ◆ Formal form (Context-Free Grammars)
 - Developed by Noam Chomsky in the mid-1950s
 - Define a class of languages: **context-free languages**
- ◆ Backus-Naur Form (1959)
 - Invented by John Backus to describe ALGOL 58
 - Equivalent to context-free grammars

Lexeme & token

S -> aBcAf

S -> "if" B "{"
A
"}"

"if",a,c,f -> terminal(lexeme)

("if " ,reserved word) ->token

("{" ,operator) ->token

("}" ,operator) ->token

in PL , **terminal symbols**, "a" or "if" , and called as *"lexeme"*.
and its category of lexemes is called *"token"*

BNF (it 's equivalent to "CFG")

- ◆ A BNF grammar consists of four parts:
 - The set of *tokens* and *lexemes* (*terminals*)
 - The set of *non-terminals*, e.g., *<sentence>*, *<verb>*
 - The *start* symbol, e.g., *<sentence>*
 - The set of *production rules*, e.g.,

<sentence> → *<noun>* *<verb>* *<preposition>* *<noun>*

<noun> → *place*

<verb> → "is" | "belongs" *<preposition>* → "in" | "to"

The *start* symbol is the particular non-terminal that forms the starting point of generating a sentence of the language

ie. *<sentence>* .

An Example Grammar

$\langle \text{program} \rangle \rightarrow \langle \text{stmts} \rangle$

$\langle \text{stmts} \rangle \rightarrow \langle \text{stmt} \rangle \mid \langle \text{stmt} \rangle ; \langle \text{stmts} \rangle$

$\langle \text{stmt} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

$\langle \text{var} \rangle \rightarrow a \mid b \mid c \mid d$

$\langle \text{expr} \rangle \rightarrow \langle \text{term} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle - \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{var} \rangle \mid \text{const}$

$\langle \text{program} \rangle$ is the start symbol

$a, b, c, \text{const}, +, -, ;, =$ are the terminals (*lexemes*)

Derivation

- ◆ A *derivation* is a repeated application of rules, starting with the start symbol and ending with a sentence (all terminal symbols), e.g.,

```
<program> => <stmts>
           => <stmt>
           => <var> = <expr>
           => a = <expr>
           => a = <term> + <term>
           => a = <var> + <term>
           => a = b + <term>
           => a = b + const
```


Derivation Leftmost & rightmost

$S \rightarrow aABb$

$A \rightarrow aA \mid a$

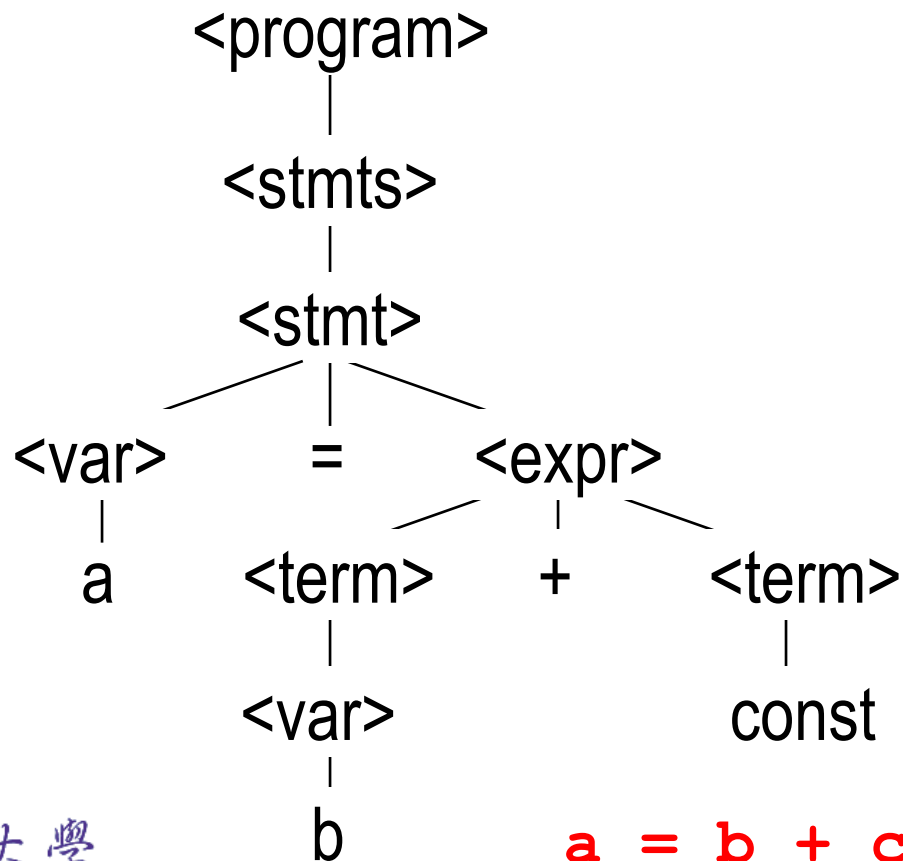
$B \rightarrow bB \mid b$

Derivations for a string "aaabb".

- **Leftmost:** $S \Rightarrow a\underline{A}Bb \Rightarrow aa\underline{A}Bb \Rightarrow aaa\underline{B}b \Rightarrow aaabb$
- **Rightmost:** $S \Rightarrow aA\underline{B}b \Rightarrow aA\underline{b}b \Rightarrow aa\underline{A}bb \Rightarrow aaabb$

Parse Tree

- ◆ A hierarchical representation of a derivation



Ambiguity in Grammars

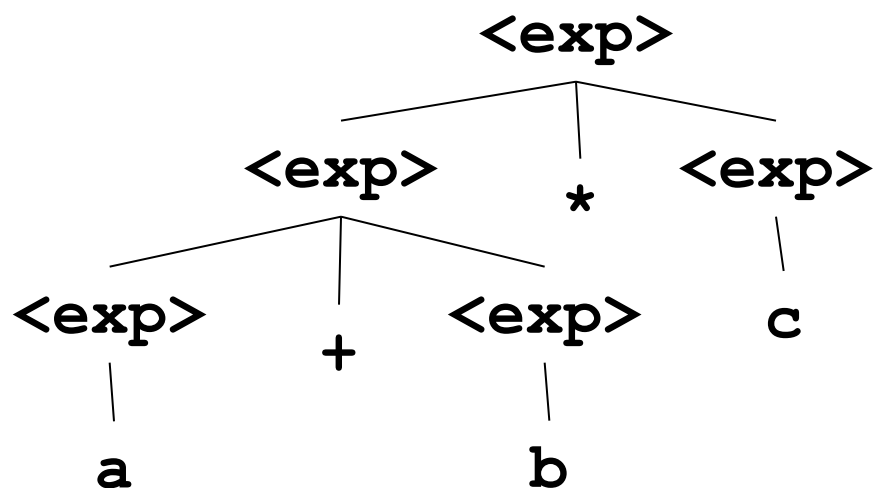
- ◆ If a sentential form can be generated by two or more distinct parse trees, the grammar is said to be *ambiguous*, because it has two or more different meanings
- ◆ Problem with ambiguity:
 - Consider the following grammar and the sentence $a+b*c$

$$\begin{aligned} \langle \text{exp} \rangle &\rightarrow \langle \text{exp} \rangle + \langle \text{exp} \rangle \mid \\ &\quad \langle \text{exp} \rangle * \langle \text{exp} \rangle \mid \\ &\quad (\langle \text{exp} \rangle) \mid \\ &\quad a \mid b \mid c \end{aligned}$$

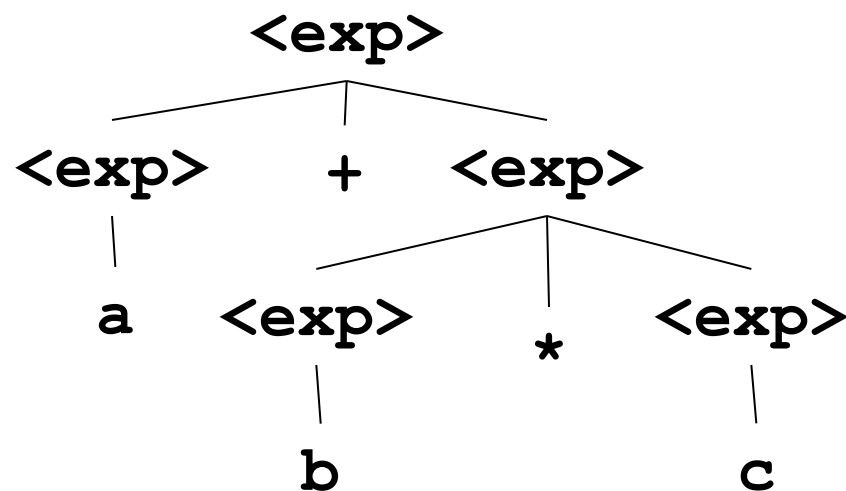
An Ambiguous Grammar

$$\begin{aligned} \langle \text{exp} \rangle \rightarrow & \langle \text{exp} \rangle + \langle \text{exp} \rangle \mid \\ & \langle \text{exp} \rangle * \langle \text{exp} \rangle \mid \\ & (\langle \text{exp} \rangle) \mid \\ & a \mid b \mid c \end{aligned}$$

- ◆ Two different parse trees for $a+b*c$



Means $(a+b)*c$



Means $a+(b*c)$

Three “Equivalent” Grammars

G1: $\langle \text{subexp} \rangle \rightarrow \mathbf{a} \mid \mathbf{b} \mid \mathbf{c} \mid \langle \text{subexp} \rangle - \langle \text{subexp} \rangle$

G2: $\langle \text{subexp} \rangle \rightarrow \langle \text{var} \rangle - \langle \text{subexp} \rangle \mid \langle \text{var} \rangle$
 $\langle \text{var} \rangle \rightarrow \mathbf{a} \mid \mathbf{b} \mid \mathbf{c}$

G3: $\langle \text{subexp} \rangle \rightarrow \langle \text{subexp} \rangle - \langle \text{var} \rangle \mid \langle \text{var} \rangle$
 $\langle \text{var} \rangle \rightarrow \mathbf{a} \mid \mathbf{b} \mid \mathbf{c}$

These grammars all define the same language: the language of strings that contain one or more **as**, **bs** or **cs** separated by minus signs, e.g., **a-b-c**. But...

Extended BNF

- ◆ Optional parts are placed in brackets []
`<proc_call> → ident [(<expr_list>)]`
- ◆ Alternative parts of RHSs are placed inside parentheses and separated via vertical bars
`<term> → <term> (+|-) const`
- ◆ Repetitions (0 or more) are placed inside braces { }
`<ident> → letter {letter|digit}`

BNF and EBNF

◆ BNF

$$\begin{aligned}\langle \text{expr} \rangle &\rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \\ &\quad | \langle \text{expr} \rangle - \langle \text{term} \rangle \\ &\quad | \langle \text{term} \rangle \\ \langle \text{term} \rangle &\rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \\ &\quad | \langle \text{term} \rangle / \langle \text{factor} \rangle \\ &\quad | \langle \text{factor} \rangle\end{aligned}$$

◆ EBNF

$$\begin{aligned}\langle \text{expr} \rangle &\rightarrow \langle \text{term} \rangle \{ (+ \mid -) \langle \text{term} \rangle \} \\ \langle \text{term} \rangle &\rightarrow \langle \text{factor} \rangle \{ (* \mid /) \langle \text{factor} \rangle \}\end{aligned}$$