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# PyTimeVar

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The PyTimeVar package offers state-of-the-art estimation and statistical inference methods for time series regression models with flexible trends and/or time-varying coefficients.

The Overview section provides details on the installation and usage of the package.



**README FILE**





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## PYTIMEVAR: A PYTHON PACKAGE FOR TRENDING TIME-VARYING TIME SERIES MODELS

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Discussion paper titled “PyTimeVar: A Python Package for Trending Time-Varying Time Series Models” is available at <https://tinbergen.nl/discussion-paper/6365/24-060-iii-pytimevar-a-python-package-for-trending-time-varying-time-series-models>.

### 2.1 Purpose of the package

The PyTimeVar package offers state-of-the-art estimation and statistical inference methods for time series regression models with flexible trends and/or time-varying coefficients. The package implements nonparametric estimation along with multiple recently proposed bootstrap-assisted inference methods. Pointwise confidence intervals and simultaneous bands of parameter curves via bootstrap can be easily obtained using user-friendly commands. The package also includes four commonly used methods for modeling trends and time-varying relationships: boosted Hodrick-Prescott filter, power-law trend models, state-space models, and score-driven models. This allows users to compare different approaches within a unified environment.

The package is built upon several papers and books. We list the key references below.

#### 2.1.1 Local linear kernel estimation and bootstrap inference

Friedrich and Lin (2024) (doi: <https://doi.org/10.1016/j.jeconom.2022.09.004>); Lin et al. (2025) (doi: <https://doi.org/10.1080/10618600.2024.2403705>); Friedrich et al. (2020) (doi: <https://doi.org/10.1016/j.jeconom.2019.05.006>); Smeeke and Urbain (2014) (doi: <https://doi.org/10.26481/umagsb.2014008>); Zhou and Wu (2010) (doi: <https://doi.org/10.1111/j.1467-9868.2010.00743.x>); Buhlmann (1998) (doi: <https://doi.org/10.1214/aos/1030563978>);

### 2.1.2 Boosted HP filter

Mei et al. (2024) (doi: <https://doi.org/10.1002/jae.3086>); Biswas et al. (2024) (doi: <https://doi.org/10.1080/07474938.2024.2380704>); Phillips and Shi (2021) (doi: <https://doi.org/10.1111/iere.12495>);

### 2.1.3 Power-law trend models

Lin and Reuvers (2025) (doi: <https://doi.org/10.1111/jtsa.12805>); Robinson (2012) (doi: <https://doi.org/10.3150/10-BEJ349>);

### 2.1.4 State-space models

Durbin and Koopman (2012) (doi: <https://doi.org/10.1093/acprof:oso/9780199641178.001.0001>);

### 2.1.5 Score-driven models

Creal et al. (2013) (doi: <https://doi.org/10.1002/jae.1279>); Harvey (2013) (doi: <https://doi.org/10.1017/CBO9781139540933>); Harvey and Luati (2014) (doi: <https://doi.org/10.1080/01621459.2014.887011>) Blasques et al. (2016) (doi: <https://doi.org/10.1016/j.ijforecast.2015.11.018>);

## 2.2 Features

- Nonparametric estimation of time-varying time series models, along with various bootstrap-assisted methods for inference, including local blockwise wild bootstrap, wild bootstrap, sieve bootstrap, sieve wild bootstrap, autoregressive wild bootstrap.
- Alternative estimation methods for modeling trend and time-varying relationships, including boosted HP filter, power-law trend models, state-space, and score-driven models. The package includes inference methods for power-law trend models, state-space models, and score-driven models.
- Unified framework for comparison of methods.
- Multiple datasets for illustration.

## 2.3 Getting started

The PyTimeVar can implemented as a PyPI package. To download the package in your Python environment, use the following command:

```
pip install PyTimeVar
```

## 2.4 Support

The documentation of the package can be found at the GitHub repository <https://github.com/bpvand/PyTimeVar>, and ReadTheDocs <https://pytimevar.readthedocs.io/en/latest/>.

For any questions or feedback regarding the PyTimeVar package, please feel free to contact the authors via email: [m3.song@student.vu.nl](mailto:m3.song@student.vu.nl); [vandersluis@ese.eur.nl](mailto:vandersluis@ese.eur.nl); [yc.lin@vu.nl](mailto:yc.lin@vu.nl).



## PYTIMEVAR

### 3.1 PyTimeVar package

#### 3.1.1 Subpackages

##### PyTimeVar.bhpfiler package

##### Submodules

##### PyTimeVar.bhpfiler.bHP module

**class** PyTimeVar.bhpfiler.bHP.**BoostedHP**(*vY*, *dLambda*=1600, *iMaxIter*=100)

Bases: object

Class for performing the boosted HP filter

##### Parameters

- **vY** (*np.ndarray*) – The dependent variable (response) array.
- **dLambda** (*float*) – The smoothing parameter.
- **iMaxIter** (*int*) – The maximum number of iterations for the boosting algorithm.

##### **vY**

The input time series data.

##### Type

array-like

##### **dLambda**

The smoothing parameter.

##### Type

float

##### **iMaxIter**

The maximum number of iterations for the boosting algorithm.

##### Type

int

##### **results**

A tuple containing the results of the Boosted HP filter.

**Type**  
tuple

**dAlpha**

The significance level for the stopping criterion 'adf'.

**Type**  
float

**stop**

Stopping criterion ('adf', 'bic', 'aic', 'hq').

**Type**  
string

**results**

Contains the trends per iteration, the current residuals, the information criteria values, the number of iterations, and the estimated trend.

**Type**  
tuple

**fit**(*boost=True, stop='adf', dAlpha=0.05, verbose=False*)

Fits the Boosted HP filter to the data.

**Parameters**

- **boost** (*bool*) – If True, boosting is used.
- **stop** (*str*) – Stopping criterion ('adf', 'bic', 'aic', 'hq').
- **dAlpha** (*float*) – The significance level for the stopping criterion 'adf'.
- **verbose** (*bool*) – If True, a progress bar is displayed.

**Returns**

- **vbHP** (*np.ndarray*) – The estimated trend.
- **vCurrentRes** (*np.ndarray*) – The residuals after iMaxIter iterations.

**plot**(*tau=None*)

Plots the true data against estimated trend

**Parameters**

**tau** (*list, optional*) – The list looks the following: tau = [start,end]. The function will plot all data and estimates between start and end.

**Raises**

**ValueError** – No valid tau is provided.

**summary**()

Prints a summary of the results.

## Module contents

### PyTimeVar.datasets package

#### Subpackages

### PyTimeVar.datasets.co2 package

#### Submodules

### PyTimeVar.datasets.co2.data module

`PyTimeVar.datasets.co2.data.load(start_date=None, end_date=None, regions=None)`

Load the CO2 emissions dataset and optionally filter by date range and/or countries. This dataset contains the emissions data from 1900 to 2017, for a range of countries.

#### Parameters

- **start\_date** (*str*, *optional*) – The start year to filter the data. Format ‘YYYY’. Minimum start year is 1900.
- **end\_date** (*str*, *optional*) – The end year to filter the data. Format ‘YYYY’. Maximum end year is 2017.
- **regions** (*list*, *optional*) – Regions to be selected from data. Available options are:  
 AUSTRALIA, AUSTRIA, BELGIUM, CANADA, DENMARK, FINLAND, FRANCE, GERMANY, ITALY, JAPAN, NETHERLANDS, NEW ZEALAND, NORWAY, PORTUGAL, SPAIN, SWEDEN, SWITZERLAND, UNITED KINGDOM, UNITED STATES, CHILE, SRI LANKA, URUGUAY, BRAZIL, GREECE, PERU, VENEZUELA, COLOMBIA, ECUADOR, INDIA, MEXICO

#### Returns

DataFrame containing the filtered data with columns ‘Date’ and regions.

#### Return type

pandas.DataFrame

#### Warning

Prints warnings if any provided regions are not found in the dataset. Prints warnings if the start year is earlier than the minimum year in the data or the end year is later than the maximum year in the data.

## Module contents

### PyTimeVar.datasets.herding package

#### Submodules

### PyTimeVar.datasets.herding.data module

`PyTimeVar.datasets.herdling.data.load(start_date=None, end_date=None, data_replication=False)`

Load the Herding dataset and optionally filter by date range. This dataset contains the herding data from Jan 5 2015 to Apr 29 2022.

#### Parameters

- **start\_date** (*str, optional*) – The start date to filter the data. Format ‘YYYY-MM-DD’. Minimum start date is 2015-01-05.
- **end\_date** (*str, optional*) – The end date to filter the data. Format ‘YYYY-MM-DD’. Maximum end date is 2022-04-29.
- **data\_replication** (*bool, optional*) – If True, the data is returned to replicate the output in Section 4.2 of the reference paper Song et al. (2024).

#### Returns

DataFrame containing the filtered data with columns ‘Date’ and regressors.

#### Return type

pandas.DataFrame

#### Warning

Prints warnings if the start\_date is earlier than the minimum date in the data or the end\_date is later than the maximum date in the data.

## Module contents

### PyTimeVar.datasets.temperature package

#### Submodules

### PyTimeVar.datasets.temperature.data module

`PyTimeVar.datasets.temperature.data.load(start_date=None, end_date=None, regions=None)`

Load the temperature dataset and optionally filter by by date range and/or regions. This dataset contains the average yearly temperature change in degrees Celsius for different regions of the world from 1961 to 2023.

#### Parameters

- **start\_date** (*str, optional*) – The start year to filter the data. Format ‘YYYY’. Minimum start year is 1961.
- **end\_date** (*str, optional*) – The end year to filter the data. Format ‘YYYY’. Maximum end year is 2023.
- **regions** (*list, optional*) –

**List of regions to filter the dataset by. Available options are:**

World, Africa, Asia, Europe, North America, Oceania, South America

#### Returns

DataFrame containing the filtered data with columns ‘Date’ and regions.

#### Return type

pandas.DataFrame



**Warning**

Prints warnings if any provided regions are not found in the dataset. Prints warnings if the `start_date` is earlier than the minimum year in the data or the `end_date` is later than the maximum year in the data.

**Module contents****PyTimeVar.datasets.usd package****Submodules****PyTimeVar.datasets.usd.data module**

`PyTimeVar.datasets.usd.data.load(start_date=None, end_date=None, type='Open')`

Load the USD index dataset and optionally filter by date range. This dataset contains the USD index data from 1961 to 2023.

**Parameters**

- **start\_date** (*str, optional*) – The start date to filter the data. Format ‘YYYY-MM-DD’. Minimum start date is 2015-01-20.
- **end\_date** (*str, optional*) – The end date to filter the data. Format ‘YYYY-MM-DD’. Maximum end date is 2024-09-06.
- **type** (*str, optional*) – The type of data to load. Available options are: [‘Open’, ‘High’, ‘Low’, ‘Close’]

**Returns**

DataFrame containing the filtered data.

**Return type**

pandas.DataFrame

**Warning**

Prints warnings if any provided currencies are not found in the dataset. Prints warnings if the `start_date` is earlier than the minimum date in the data or the `end_date` is later than the maximum date in the data.

**Module contents****PyTimeVar.datasets.inflation package****Submodules****PyTimeVar.datasets.inflation.data module**

`PyTimeVar.datasets.inflation.data.load(start_date=None, end_date=None)`

Load the inflation dataset, construct inflation rate dataset and optionally filter by date range. This dataset contains the inflation rate data from 1947 to 2024.

### Parameters

- **start\_date** (*str, optional*) – The start year-month to filter the data. Format ‘YYYY-MM’. Minimum start year-month is 1947-02.
- **end\_date** (*str, optional*) – The end year-month to filter the data. Format ‘YYYY’. Maximum end year is 2024-08.

### Returns

- *pandas.DataFrame* – DataFrame containing the filtered data with columns ‘Date’ and CPI-AUCSI.
- *Warnings*
- *Prints warnings if the start year is earlier than the minimum year in the data or the end year is later than the maximum year in the data.*

## Module contents

### Submodules

#### PyTimeVar.datasets.utils module

`PyTimeVar.datasets.utils.load_csv(base_file, csv_name, sep=',', convert_float=False)`

Standard simple csv loader

## Module contents

Dataset module for PyTimeVar package.

### PyTimeVar.gas package

#### Submodules

#### PyTimeVar.gas.GAS module

`class PyTimeVar.gas.GAS.GAS(vY, mX, method='none', vgamma0=None, bounds=None, options=None, niter=None, if_hetero=False)`

Bases: `object`

Class for performing score-driven (GAS) filtering.

### Parameters

- **vY** (*np.ndarray*) – The dependent variable (response) array.
- **mX** (*np.ndarray*) – The independent variable (predictor) matrix.
- **method** (*string*) – Method to estimate GAS model. Choose between ‘gaussian’ or ‘student’.
- **vgamma0** (*np.ndarray*) – Initial parameter vector.
- **bounds** (*list*) – List to define parameter space.
- **options** (*dict*) – Stopping criteria for optimization.

- **niter** (*int*) – The number of optimization iterations, for `scipy.optimize.basinhopping()`
- **if\_hetero** (*bool*) – If True, a heteroskedastic specification is assumed. Filter additionally returns the estimated path of time-varying variance.

**vY**

The dependent variable (response) array.

**Type**

`np.ndarray`

**mX**

The independent variable (predictor) matrix.

**Type**

`np.ndarray`

**n**

The length of vY.

**Type**

`int`

**n\_est**

The number of coefficients.

**Type**

`int`

**method**

Method to estimate GAS model.

**Type**

`string`

**vgamma0**

The initial parameter vector.

**Type**

`np.ndarray`

**bounds**

List to define parameter space.

**Type**

`list`

**options**

Stopping criteria for optimization.

**Type**

`dict`

**niter**

The number of optimization iterations, for `scipy.optimize.basinhopping()`

**Type**

`int`

**if\_hetero**

If True, a heteroskedastic specification is assumed. Filter additionally returns the estimated path of time-varying variance.

**Type**

bool

**success**

If True, optimization was successful.

**Type**

bool

**betas**

The estimated coefficients.

**Type**

np.ndarray

**params**

The estimated GAS parameters.

**Type**

np.ndarray

**sigma2\_t**

The estimated path of time-varying variance. None for a homoskedastic specification.

**Type**

np.ndarray

**inv\_hessian**

The inverse Hessian after optimization.

**Type**

np.ndarray

**Raises**

**ValueError** – No valid number of initial parameters is provided.

**Parameters**

- **vY** (*ndarray*)
- **mX** (*ndarray*)
- **method** (*str*)
- **vgamma0** (*ndarray*)
- **bounds** (*list*)
- **options** (*dict*)
- **niter** (*int*)
- **if\_hetero** (*bool*)

**fit()**

Fit score-driven model, according to the specified method ('gaussian' or 'student')

**Returns**

- **mBetaHat** (*np.ndarray*) – The estimated coefficients.
- **vparaHat** (*np.ndarray*) – The estimated GAS parameters.
- **sigma2\_hat** (*np.ndarray*) – The path of estimated time-varying variance. Only returned if `hetero = True`.

**plot**(*tau=None, confidence\_intervals=False, alpha=0.05, iM=1000*)

Plot the beta coefficients over a normalized x-axis from 0 to 1.

#### Parameters

- **tau** (*list, optional*) – The list looks the following: `tau = [start,end]`. The function will plot all data and estimates between start and end.
- **confidence\_intervals** (*bool, optional*) – If True, simulation-based confidence intervals will be plotted around the estimates.
- **alpha** (*float*) – Significance level for confidence intervals.
- **iM** (*int*) – The number of simulations for simulation-based confidence intervals.

#### Raises

**ValueError** – No valid tau is provided.

## Module contents

### PyTimeVar.kalman package

#### Submodules

### PyTimeVar.kalman.kalman module

**class** PyTimeVar.kalman.kalman.**Kalman**(*vY=None, T=None, R=None, Q=None, sigma\_u=None, b\_1=None, P\_1=None, mX=None*)

Bases: object

Class for performing Kalman filtering and smoothing.

#### Parameters

- **vY** (*np.ndarray*) – The dependent variable (response) array.
- **T** (*np.ndarray, optional*) – The transition matrix of the state space model.
- **R** (*np.ndarray, optional*) – The transition correlation matrix of the state space model.
- **Q** (*np.ndarray, optional*) – The transition covariance matrix of the state space model.
- **sigma\_u** (*np.ndarray, optional*) – The observation noise variance of the state space model.
- **b\_1** (*np.ndarray, optional*) – The initial mean of the state space model.
- **P\_1** (*np.ndarray, optional*) – The initial covariance matrix of the state space model.
- **mX** (*np.ndarray, optional*) – The regressors to use in the model. If provided, the model will be a linear regression model.

**vY**

The dependent variable (response) array.

**Type**

np.ndarray

**n**

The length of vY.

**Type**

int

**isReg**

If True, regressors are provided by the user.

**Type**

bool

**T**

The transition matrix of the state space model.

**Type**

np.ndarray

**Z**

Auxiliary (1,1)-vector of a scalar 1. This is used in case there are no regressors.

**Type**

np.ndarray

**R**

The transition correlation matrix of the state space model.

**Type**

np.ndarray

**Q**

The transition covariance matrix of the state space model.

**Type**

np.ndarray

**H**

The observation noise variances of the state space model. Each entry corresponds to the observation noise variance at a time point.

**Type**

np.ndarray

**a\_1**

The initial mean of the state space model.

**Type**

np.ndarray, optional

**P\_1**

The initial covariance matrix of the state space model.

**Type**

np.ndarray

**mX**

The regressors to use in the model. If provided, the model will be a linear regression model.

**Type**

np.ndarray

**Z\_reg**

The regressors matrix in correct format to use in filtering.

**Type**

np.ndarray

**p\_dim**

The number of coefficients.

**Type**

int

**m\_dim**

The number of response variables. This is always 1.

**Type**

int

**filt**

The filtered coefficients.

**Type**

np.ndarray

**pred**

The predicted coefficients.

**Type**

np.ndarray

**smooth**

The smoothed coefficients.

**P\_filt**

The filtered state variances.

**Type**

np.ndarray

**P**

The predicted state variances.

**Type**

np.ndarray

**V**

The smoothed state variances.

**Type**

np.ndarray

**fit(option='filter')**

Computes the Kalman filtered states, one-step ahead predicted states or smoothed states for the data.

**Parameters**

**option** (*string*) – Denotes the fitted trend: filter, predictor, smoother, or all.

**Raises**

**ValueError** – No valid option is provided.

**Returns**

Estimated trend. If option='all', a list of trends is returned:

[filter, predictor, smoother]

**Return type**

np.ndarray

**plot**(*individual=False, tau=None, confidence\_intervals=False, alpha=0.05*)

Plot the estimated beta coefficients over a normalized x-axis from 0 to 1 or over a date range.

**Parameters**

- **individual** (*bool, optional*) – If True, the filtered states, the predictions, and smoothed states are shown in separate figures.
- **tau** (*list, optional*) – The list looks the following: tau = [start,end]. The function will plot all data and estimates between start and end.
- **confidence\_intervals** (*bool, optional*) – If True, the confidence intervals will be plotted around the filtered states, the predictions, and smoothed states. The confidence intervals are plotted for individual plots only, not for joint plots.
- **alpha** (*float*) – Significance level for confidence intervals.

**Raises**

**ValueError** – No valid tau is provided.

**summary**()

Prints a summary of the state-space model specification.

## Module contents

### PyTimeVar.locallinear package

#### Submodules

#### PyTimeVar.locallinear.LLR module

**class** PyTimeVar.locallinear.LLR.**LocalLinear**(*vY, mX, h=0, bw\_selection=None, kernel='epanechnikov', LB\_bw=None, UB\_bw=None*)

Bases: object

Class for performing local linear regression (LLR).

Local linear regression is a non-parametric regression method that fits linear models to localized subsets of the data to form a regression function. The code is based on the code provided by Lin et al. [1].

**Parameters**

- **vY** (*np.ndarray*) – The dependent variable (response) array.
- **mX** (*np.ndarray*) – The independent variable (predictor) matrix.
- **h** (*float*) – The bandwidth parameter controlling the size of the local neighborhood. If not provided, it is estimated as the average of all methods in the package.



- **bw\_selection** (*string*) – The name of the bandwidth selection method to be used. Choice between ‘aic’, ‘gcv’, ‘lmcv-l’ with  $l=0,2,4,6$ , etc., or ‘all’. If not provided, it is set to ‘all’.
- **kernel** (*string*) – The name of the kernel function used for estimation. If not provided, it is set to ‘epanechnikov’ for the Epanechnikov kernel.
- **LB\_bw** (*float*) – The lower bound for the bandwidth selection. If not provided, it is set to 0.06.
- **UB\_bw** (*float*) – The upper bound for the bandwidth selection. If not provided, it is set to 0.2 for LMCV-l and to 0.7 for AIC and GCV.

**vY**

The response variable array.

**Type**

np.ndarray

**mX**

The predictor matrix.

**Type**

np.ndarray

**n**

The length of vY.

**Type**

int

**times**

Linearly spaced time points for the local regression.

**Type**

np.ndarray

**tau**

Points at which the regression is evaluated.

**Type**

np.ndarray

**tau\_bw\_selection**

Points at which the cross-validation is evaluated.

**Type**

np.ndarray

**n\_est**

The number of coefficients.

**Type**

int

**kernel**

The name of the kernel function.

**Type**

string

**bw\_selection**

The name of the bandwidth selection.

**Type**

string

**lmcv\_type**

If LMCV is used for bandwidth selection, this attribute denotes the  $l$  in leave- $2 \cdot l + 1$ -out.

**Type**

int

**dict\_bw**

The dictionary that contains the optimal bandwidth values for each individual method.

**Type**

dict

**h**

The bandwidth used for local linear regression.

**Type**

float

**h\_gcv**

The optimal bandwidth value according to Generalized CV method.

**Type**

string

**betahat**

The estimated coefficients.

**Type**

np.ndarray

**predicted\_y**

The fitted values for the response variable.

**Type**

np.ndarray

**residuals**

The residuals resulting from the local linear regression.

**Type**

np.ndarray

**Raises**

**ValueError** – No valid bandwidth selection procedure is provided.

**Parameters**

- **vY** (ndarray)
- **mX** (ndarray)
- **h** (float)
- **bw\_selection** (str)
- **kernel** (str)

- **LB\_bw** (*float*)
- **UB\_bw** (*float*)

## Notes

The local linear regression is computed at each point specified in *tau*. The bandwidth *h* controls the degree of smoothing.

## References

[1] Lin, Y., Song, M., & van der Sluis, B. (2025).

Bootstrap inference for linear time-varying coefficient models in locally stationary time series. *Journal of Computational and Graphical Statistics*, 34(2), 654-667.

**confidence\_bands**(*bootstrap\_type*='LBWB', *alpha*=None, *gamma*=None, *ic*=None, *Gsubs*=None, *Chtilde*=2, *B*=1299, *plots*=False)

Compute and plot confidence bands.

### Parameters

- **bootstrap\_type** (*str*) – Type of bootstrap to use ('SB', 'WB', 'SWB', 'MB', 'LBWB', 'AWB').
- **alpha** (*float*) – Significance level for quantiles.
- **gamma** (*float*) – Parameter value for Autoregressive Wild Bootstrap.
- **ic** (*str*) – Type of information criterion to use for Sieve and Sieve Wild Bootstrap. Possible values are: 'aic', 'hqic', 'bic'
- **Gsubs** (*list of tuples*) – List of sub-ranges for G. Each sub-range is a tuple (start\_index, end\_index). Default is None, which uses the full range (0, T).
- **Chtilde** (*float*) – Multiplication constant to determine size of oversmoothing bandwidth htilde. Default is 2, if none or negative is specified.
- **B** (*int*) – The number of bootstrap samples. Default is 1299, if not provided by the user.
- **plots** (*bool*) – If True, plots are shown of the estimated coefficients and corresponding confidence bands.
- **bootstrap\_type** (*str*)

### Returns

- **S\_LB** (*np.ndarray*) – The lower simultaneous confidence bands.
- **S\_UB** (*np.ndarray*) – The upper simultaneous confidence bands.
- **P\_LB** (*np.ndarray*) – The lower pointwise confidence intervals.
- **P\_UB** (*np.ndarray*) – The upper pointwise confidence intervals.

## fit()

Fits the linear model by local linear regression to the data.

### Returns

**self.betahat** – The estimated coefficients.

### Return type

*np.ndarray*

**plot\_betas**(*tau=None*)

Plot the beta coefficients over a normalized x-axis from 0 to 1.

**Parameters**

**tau** (*list*, *optional*) – The list looks the following: tau = [start,end]. The function will plot all data and estimates between start and end.

**Raises**

**ValueError** – No valid tau is provided.

**plot\_predicted**(*tau=None*)

Plot the actual values of Y against the predicted values of Y over a normalized x-axis from 0 to 1.

**Parameters**

**tau** (*list*, *optional*) – The list looks the following: tau = [start,end]. The function will plot all data and estimates between start and end.

**Raises**

**ValueError** – No valid tau is provided.

**plot\_residuals**(*tau=None*)

Plot the residuals over a normalized x-axis from 0 to 1.

**Parameters**

**tau** (*list*, *optional*) – The list looks the following: tau = [start,end]. The function will plot all data and estimates between start and end.

**Raises**

**ValueError** – No valid tau is provided.

**Returns**

**self.residuals** – Array of residuals.

**Return type**

np.ndarray

**summary**()

Print a summary of the regression results.

## Module contents

### PyTimeVar.powerlaw package

#### Submodules

#### PyTimeVar.powerlaw.pwr module

**class** PyTimeVar.powerlaw.pwr.**PowerLaw**(*vY*, *n\_powers=None*, *vgamma0=None*, *bounds=None*, *options=None*)

Bases: object

Class for implementing the Power-Law method.

**Parameters**

- **vY** (*np.ndarray*) – The dependent variable (response) array.
- **n\_powers** (*int*) – The number of powers.

- **vgamma0** (*np.ndarray*) – The initial parameter vector.
- **bounds** (*tuple*) – Tuple to define parameter space.
- **options** (*dict*) – Stopping criteria for optimization.

**vY**

The dependent variable (response) array.

**Type**

*np.ndarray*

**n**

The length of vY.

**Type**

*int*

**p**

The number of powers. Default is set to 2.

**Type**

*int*

**vgamma0**

The initial parameter vector.

**Type**

*np.ndarray*

**bounds**

Tuple to define parameter space.

**Type**

*tuple*

**cons**

Dictionary that defines the constraints.

**Type**

*dict*

**trendHat**

The estimated trend.

**Type**

*np.ndarray*

**gammaHat**

The estimated power parameters.

**Type**

*np.ndarray*

**coeffHat**

The estimated coefficients.

**Type**

*np.ndarray*

**C\_LB\_trend**

The lower bounds of the pointwise confidence intervals for the trend.

**Type**

np.ndarray

**C\_UB\_trend ; np.ndarray**

The upper bound of the pointwise confidence intervals for the trend.

**alpha**

The significance level for the confidence intervals.

**Type**

float

**Raises**

**ValueError** – No valid bounds are provided.

**Parameters**

- **vY** (ndarray)
- **n\_powers** (float)
- **vgamma0** (ndarray)
- **bounds** (tuple)
- **options** (dict)

**confidence\_intervals**(*bootstraptype*, *alpha=None*, *gamma=None*, *ic=None*, *B=1299*, *block\_constant=2*, *verbose=True*)

Construct confidence intervals using bootstrap methods.

**Parameters**

- **bootstraptype** (*str*) – Type of bootstrap to use ('SB', 'WB', 'SWB', 'MB', 'LBWB', 'AWB').
- **alpha** (*float*) – Significance level for quantiles.
- **gamma** (*float*) – Parameter value for Autoregressive Wild Bootstrap.
- **ic** (*str*) – Type of information criterion to use for Sieve and Sieve Wild Bootstrap. Possible values are: 'aic', 'hqic', 'bic'
- **B** (*int*) – The number of bootstrap samples. Deafult is 1299, if not provided by the user.
- **block\_constant** (*float*) – The constant to determine the window length for blocks bootstraps. Default is 2.
- **verbose** (*bool*) – If True, a progress bar is displayed.

**Raises**

**ValueError** – No valid bootstrap type is provided.

**Returns**

The pointwise lower and upper confidence intervals for the coefficients, powers, and trend, respectively.

**Return type**

list of tuples

**fit()**

Fits the Power-Law model to the data.

**Returns**

- **self.trendHat** (*np.ndarray*) – The estimated trend.
- **self.gammaHat** (*np.ndarray*) – The estimated power parameters.

**plot**(*tau=None, confidence\_intervals=True*)

Plots the original series and the trend component.

**Parameters**

- **tau** (*list, optional*) – The list looks the following: tau = [start,end]. The function will plot all data and estimates between start and end.
- **confidence\_intervals** (*bool*) – If True, the estimated confidence intervals are displayed as well. If the confidence intervals are not computed yet, no confidence intervals are displayed.

**Raises**

**ValueError** – No valid tau is provided.

**summary()**

Print the mathematical equation for the fitted model

## Module contents

### 3.1.2 Module contents





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