

4th Aug, 2025

Information and Network Security

Cryptography and Network security

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• plain text $\xrightarrow{\text{encryption}}$ cipher text

→ Error control: Data Link layer, Transport layer

→ Confidentiality: No data breach, no unauthorized access

→ Integrity: Data should reach in entirety + no alteration midway

→ Availability: Availability of data at the time it is required

→ Authentication: Digital signature

→ Non-Reputation: Trusted 3rd party presides over data transfer

① SSL, Secure socket layer: placed b/w Application and Transport layer.

↳ protocol used to connect web browser and web server → connection oriented protocol

→ placed b/w Application & Transport layer as headers are added at Transport, Network & DLL (port no., IP Address, MAC Address) → so SSL should not encrypt these addresses.

Cryptography

public

Asymmetric

priv.

Symmetric

(same key is used for encryption & decryption)

Each user has a pair of keys

- public key: can be known to other users as well. Both sender & receiver are aware of each other's public key.
- Sender encrypts plain text into cipher with its private key. Receiver deciphers using his sender's public key. → used in digital signature { not secure, as public key may also be known to other users }



7/8/24

INSModular Arithmetic

- In modular arithmetic, both c/p & o/p belong to same set $(0 \text{ to } n-1)$ for \mathbb{Z}_n
- w/ Additive Inverse : mod - 0
- multiplicative Inverse : mod - 1
- Residue : Result obtained after modulo op.

for any matrix A to become a key \rightarrow it's multiplicative inverse must exist \Rightarrow its $\det(A) \neq 0$ & $\det(A) \& n$ must be co-prime,
i.e.

$$\gcd(\det(A), n) = 1 \quad \text{where } n = \text{no. of symbols}$$

cipher Text = $AB \rightarrow$ Key

→ All the ops. involved are modular $\Rightarrow (a+b) \% n$

Ciphers

→ Stream : char by char

→ Block : e.g. modular {a block of chars.}

A key

Monalph

(1) Additive
each
a key
sub.

eg:

C
R
Y
P
T
E
C

32

Substitution cipher

Page No. _____

Date _____

→ monalphabetic → polyalphabetic

* Substitution: char replaced by symbol that may or may not be present in plain text

— monalphabetic: ONE TO ONE mapping. + char. only replaced by 1 particular same char.

— polyalphabetic: ONE TO MANY.

multiple chars. can be used to replace a char.
A key stream is generated.

Monalphabetic ciphers

(1) Additive cipher: eg. caesar cipher ($K=3$)

each symbol in plain text is converted to int;
a key is agreed upon → added during encryption,
subt. during decryption. It is a stream cipher

eg. key = 15, data = cryptography.

$$C \rightarrow (2+15) \mod 26 = 17 \rightarrow R$$

$$R \rightarrow (17+15) \mod 26 = 6 \rightarrow G$$

$$Y \rightarrow (24+15) \mod 26 = 13 \rightarrow N$$

$$P \rightarrow (15+15) \mod 26 = 4 \rightarrow E$$

$$T \rightarrow (19+15) \mod 26 = 8 \rightarrow I$$

$$O \rightarrow (14+15) \mod 26 = 3 \rightarrow D$$

$$G \rightarrow (6+15) \mod 26 = 21 \rightarrow V$$

$$R \rightarrow (17+15) \mod 26 = 6 \rightarrow G$$

$$A \rightarrow (0+15) \mod 26 = 15 \rightarrow P$$

$$P \rightarrow (15+15) \mod 26 = 4 \rightarrow E$$

$$H \rightarrow (7+15) \mod 26 = 22 \rightarrow W$$

$$Y \rightarrow (24+15) \mod 26 = 13 \rightarrow N$$

39

34

32

39

- NO. of keys possible in \mathbb{Z}_{26} = 0 to $n-1$
 $0 \text{ to } 25 = 26 \text{ keys}$
- key domain = 26 (NO. of keys) \mathbb{Z}_n

(2) Multiplicative Inv cipher

Let $K=7 \rightarrow$ as $\gcd(7, 26) = 1$ ✓ eligible key

For decryption key $(7 \times x) \% 26 = 1$
 \downarrow
 15

$$7x15 = 105 \% 26 = 1 \checkmark$$

→ eligible keys in \mathbb{Z}_{26} (key domain)
key inverse

0 → 7x	15 → 7
1 → 7x	16 x
2 → 7x	17 → 23
3 → 7x	18 x
4 → 7x	19 → 11
5 → 7x	20 x
6 → 7x	21 → 5
7 → 7x	22 x
8 → 7x	23 → 9
9 → 7x	24 → x
10 → 7x	25 → 25
11 → 7x	26 → x
12 → 7x	
13 → 7x	
14 → 7x	

→ Find multiples of n (=26)
 → check if key can be multiplied with a no. in range [0 to $n-1$] to obtain (multiple (26) + 1)

\times as key domain of Additive \rightarrow Multiplicative \rightarrow Additive cipher is stronger.

(3) Affine cipher: combination of Additive + multiplicative ciphers.

$$T \leftarrow P \times K_1$$

$$C \leftarrow T + K_2$$

L

$$P \leftarrow T \times K_1^{-1}$$

$$T \leftarrow C - K_2$$

↑

key domain = 26×12 (strongest among 3)

→ bias cannot be controlled by increasing dataset.

Regularization

- penalize large coeff. values

$$\tilde{E}(w) = \frac{1}{2} \sum_{n=1}^N \{y(x_n, w) - t_n\}^2 + \frac{\lambda}{2} \|w\|^2$$

magnitude of vector

↑

→ To achieve better fitting

vector of coeffs w_0, w_1, w_2, \dots

1/8/25

INS

* transposition cipher → permutation / arrangement of char. change.

(i) monoalphabetic substitution cipher → Each char. is to be replaced by a fixed char.

A B → . Z

↓
26 × 25 × ... → 1

⇒ 26!

key domain
(strongest)

Polyalphabetic substitution ciphers (ONE to MANY)
depends on ① plain text char. ② position of char.

(i) Auto key cipher

- 1st subkey → the one agreed upon by sender & receiver (predetermined)
- 2nd subkey → table int corresponding to first char of plain text.
- 3rd subkey → int corresponding to 2nd char of plain text

pre-determined by sender & receiver

Page No. _____

Date _____

Plain Text → INFORMATION

keys →
$$\begin{array}{r} 8 \ 13 \\ + \ + \\ 3 \ 8 \\ \hline 1 \ 13 \end{array}$$

cipher →
$$\begin{array}{r} 11 \ 21 \\ \hline (L \ 2 \ V \ \dots) \end{array}$$

(iii) Playfair cipher

→ Key is predecided by sender & receiver in form of 5×5 matrix (I & J share same cell.)

U	T	F	C	A	Any random combination
V	S	E	D	B	
W	P	O	Q	G	H
X	Q	M	L	I	J
Y	R	N	K	Z	

- If there are any 2 consecutive same chars. → Insert a bogus char. in b/w
- Finally length must be even → if not then add a bogus char. at end.
- Process the text in pairs.
- For each pair of chars in Plain Text:
 - ① They may be in same row in matrx → Then they are replaced by next char. in that row (circular)
 - ② They may be in same column → Replaced by 1 char. down in same column
 - ③ They are in diff row & col → Each char. replaced by char lying on intersection of these chars. & in same row as char. to be replaced.

eg. G H → H W
S Q → P R
A D → L S

(iii) vignere cipher

Sender & Receiver agree upon a subkey word

→ Does not depend upon position of char.

INFORMATION
 subkey ← H E L L O H E L L O H

(iv) hill cipher

→ Block cipher

→ Key used → A square matrix, having an inverse
 of size $m \times m$

size of block to be encrypted

→ Plain Text taken in a matrix of size $l \times m$

$$\begin{bmatrix} \text{plain Text} \\ l \times m \end{bmatrix} \times \begin{bmatrix} \text{key} \\ m \times m \end{bmatrix} = \begin{bmatrix} \text{cipher Text} \\ l \times m \end{bmatrix}$$

NO. of
blocks in
plain
Text

→ find determinant of key matrix → If its
 multiplicative inverse exists in \mathbb{Z}_{26} → it
 is a valid key

1B/8/25

Transposition cipher

key ① Railfence Technique : Arrange alternate chars. in zigzag manner & then write row by row.

e.g. INFORMATION

① → I F R A T I N
② → N O M A T O N

⇒ IFRAINNOMTO

key
w/ ②

Columnar Technique : Fix no. of columns & place text row by row, e.g. let no. of columns (pre-agreed) = 4

↓ ↓ ↓ ↓

I N F O
R M A T
I O N

⇒ IRINMOFANT

1st col

* key → an element getting used at both ends to cipher / decipher.

12
64/800
6/1000

~~use key~~

1	2	3	4	5
3	2	1	5	4

Encryption

Decryption

- (3) A Block size chosen & their internal permutation is pre-agreed. (if no. of cols < slot size → Add padding/extral bogus char)

- (2) NO. of columns fixed → Text written row-wise and then during encryption → ~~permutation~~ order of columns decided by key.
(Key size = NO. of columns)

Modern Ciphers

- Bit oriented instead of char oriented
- Block ciphers

n-bit plain Text

n-bit plain Text

↓
Encryption Algo

K bits
key

→ Decryption Algo

↓
n-bit cipher Text → n-bit cipher

Soln: Total no. of char to be encrypted = 100 & using ASCII coding of size 8 & block size = 64 Bits, calculate no. of padding chars.

→ No. of bits for each char = 8

$$\text{Total Bits} = 8 \times 100 = 800$$

$$\text{No. of padding} = 800 \mod 64 = 32$$

$$\text{Total no. of Bits} = 800 + 32 = \underline{\underline{832}}$$

No. of times iteration need =

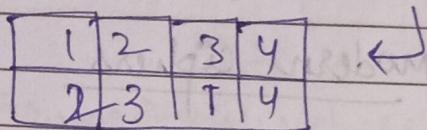
$$832 / 64 = 13 \text{ (approx)} \rightarrow \text{on one side}$$

→ In Bit oriented transposition ciphers → no. of 0's & 1's remain same → Helps adversary in brute force attack.

Components of modern cipher

(i) Permutation Boxes (P Boxes)

- ← ⁱ⁾ straight P-Box → Invertible
- same no. of i/p & o/p lines
- Interconnections are interwoven in hardware



✓ → In software : Take an array of size n and directly write core i/p chars. as per pre-decided combination.

$\begin{bmatrix} 2 & 3 & 1 & 1 & 4 \end{bmatrix} \Rightarrow \begin{bmatrix} 0 & u & f & t & 4 \end{bmatrix}$ Text = four
1 2 3 4

(ii) Expansion P-Box → Non-invertible (when

No. of o/p chars > i/p chars. i/p lines ≠ o/p lines

(iii) compression P-Box (8x4) (Non invertible)

o/p chars ← i/p chars
values in Box → i/p chars
position values in Box → o/p chars.

INS

- DES: Data Encryption Standard
- 64 rounds of Algos are used performed on DES
- Data itself can never be encrypted by any non-invertible component
- Non-invertible components are used for key generation
- Symmetric Block cipher

Components of modern cipher

(2) S-BOX Substitution Boxi) Invertible \Rightarrow Non-invertible

→ No. of input bits are made to multiples of 3 bits

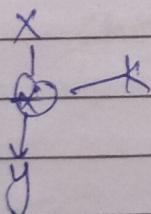
eg. $\underline{1} \underline{0} \underline{1} \underline{0} \underline{1} \underline{1} \underline{0} \underline{0} \underline{0}$ padding

Now in 3 bit NO.

row $\overbrace{\quad\quad}$
all $\overbrace{\quad\quad}$

	00	01	10	11
0	01	00	10	11
1	11	01	00	10

ROT

eg. $101 \rightarrow \underline{1} \underline{0} \underline{1} \Rightarrow 01$ $011 \rightarrow \underline{0} \underline{1} \underline{1} \Rightarrow 11$ $000 \rightarrow \underline{0} \underline{0} \underline{0} \Rightarrow 01$ Hence, $101011000 \Rightarrow \underline{011101}$ (3) X-OR \rightarrow InvertibleNow,

$$y \oplus k \Rightarrow x$$

~~PROOF~~ $y = x \wedge k$
 $y \wedge k = x \wedge k \wedge k$

$y \wedge k = x \wedge 0$

$x = y \wedge k$

(4) circular shift

Left shift / Right shift
 $x \ll k$

$k \in [0, n-1]$

To make it invertible, just shift k times in decrypting algo.

- (5) complement
- (6) split & combine

(7) Swapper

- circular shift where $k = n/2$
- can be used if no. of bits are even
- divides bits into 2 & swaps

product cipher

Feistal Non-feistal

diffusion: Extent of complexity shown by \rightarrow the relation b/w plain text & cipher text.

confusion: Relation b/w cipher text & encryption key

→ product ciphers are block ciphers wherein multiple algo / components used for encryption

→ feistal: Both types of components (invertible & non-invertible) \rightarrow eg. DES

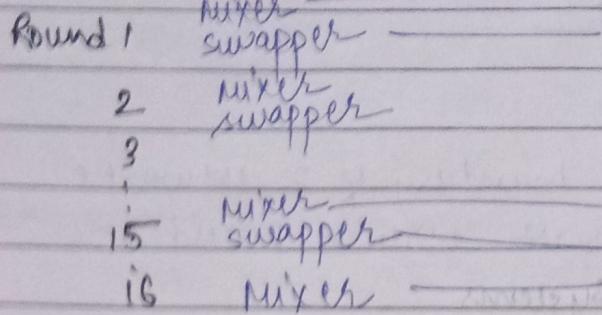
→ non-feistal: only invertible components used
eg. AES

→ blocking system call on a thread does NOT block entire process (other threads can execute parallelly)

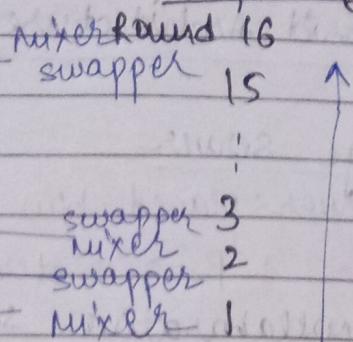
INS

- * Data Encryption Standard (DES)
 - each round composed of swapper & mixer
 - 16 rounds for encryption + 16 decryption
 - uses 56 bit symmetric key initially → each round has different sub key
 - size of sub key = 48 bits (generated by key generator)
 - size of block = 64 Bits

Ciphering

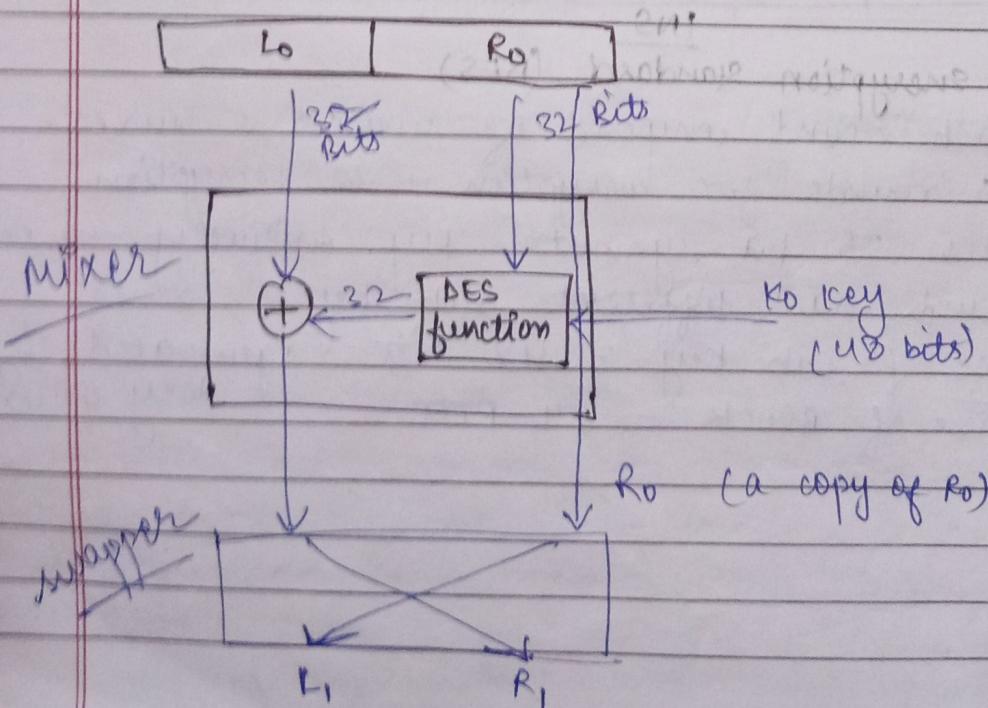


Deciphering



→ Not rounds, but sections of rounds (mixer - swapper, swapper - swapper) are aligned.

- Plain text is divided into Block sizes of 64 bits
- straight P-Boxes are used in initial permutation & final permutation
- size of straight p-Box used = 8×8
 ~ 64 bits (1 to 64)
- swapper: we have 64 bits. Divide into 2 equal halves & swap.
- mixer → DES function
whitener (X-OR)



→ swapper : Invertible
→ mixer : self invertible (eff of non-invertible components gets cancelled)
Page No. _____
Date _____

① DES Function

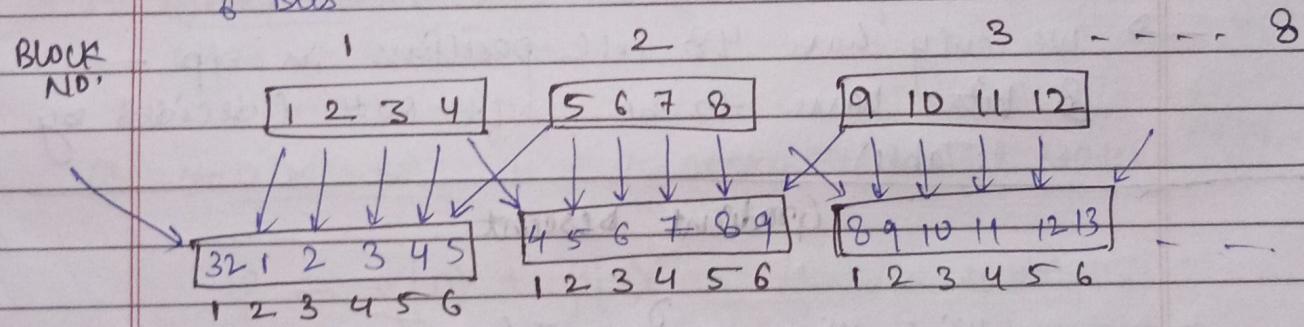
Inputs : ① 32 bits R₀ + ② 48 bit key

4 operations:

- ① Expansion Key Box
- ② XOR operation
- ③ S-Box
- ④ straight P Box

① Expansion Key Box : converts 32 bits R₀ to 48 bit size = 32×48 , with a pre-determined logic (repeat certain I/P lines)

→ Divide 32 bits into 8 sub-sections of 4 bits each. Each 4 bit block will return 8 bits



② XOR: XOR of 48 bits of expansion p-box o/p and 48 bit subkey

③ S-Box: Divide 48 bits into 8 blocks of 6 bits each.

Non-invertible → DES uses 8 S-Box tables, one for each block (4x16 size each)

→ First & last bit will combine to form row no. 2 b/w 4 Bits = col no.

Assignment : AES
Advanced Encryption

12/16

Page No.		
Date		

each block has its own P-S-Box Table (S-Box
Table 1, 2, ...)

→ only sender & receiver are aware of 56 bit
key

* Key Generation → Generate 16 subkeys of 48 bits each

- (1) split key into 28 bits each ($28 + 28 = 56$)
- (2) Apply circular shift (left) op on both parts

for rounds 1, 2, 9, 16
left circular shift by
1 place

remaining
left circular shift
by 2 places

3) combine 2 halves

4) apply compression p-Box (56×48)

→ we only have 48 cell positions in opp →
8 bits have to be left out (decided by
Table)

Gradient Descent

$$w_j = w_j - \alpha \frac{\partial}{\partial w} J(w_0, w_1)$$

To compute follow of symbols

Rule 1: $\text{follow}(S) = \{ \$ \}$, if S is start symbol

Rule 2: if there is a production rule of form

$A \rightarrow \alpha B \beta$, where $\beta \neq \epsilon$

then

$\text{follow}(B) = \{ \text{first}(\beta) \}$

$= \{ \text{first}(\beta) - \epsilon \}$

$\text{first}(\beta) \neq$

everything included in
 $\text{first}(\beta)$ except ϵ

Rule 3: for prodⁿ full of form

$A \rightarrow \alpha B$ or $A \rightarrow \alpha B \beta$, when $\text{first}(\beta)$ contains ϵ , then

$\text{follow}(B) = \{ \text{follow}(A) \}$

INS

- RSA: Rivest Shamir Adleman. → Asymmetric cipher
 - used for all authentication, non-repudiation, confidentiality.
 - 2 different keys used for encryption/decryption
 - Receiver always initiates communication → by sending its public key & a number n.
 - sender then encrypts the text using public key of receiver & number n.
 - Encrypted text is sent to Receiver, which decrypts it using its own private key
- for a system of n nodes → there are total $2n$ keys
- It is difficult to factorize product of 2 large prime no.

Let $P = 7$ & $Q = 17$

$$N = P \times Q = 119$$

$$(P-1) \times (Q-1) = 6 \times 16 = 96$$

KAR

* eqⁿ to be followed

$$(D \times E) \bmod (P-1)(Q-1) = 1$$

→ choose E such that factor of E & $(P-1)(Q-1)$
do not have any factor in common

encryption key

→ factors of $(P-1)(Q-1) = 96 = 1 \times 2 \times 3 \times 4 \times 6 \times 8 \times 12 \times 24 \times 48 \times 96$

Let, $\boxed{E = 5}$

$(D \times 5) \bmod 96 = 1$ → multiples of 96
as $384 + 1 = 385$ (a multiple of 5) - 96, 192, 288
 $D \times 5 = 385 \rightarrow \boxed{D = 77}$ 384...
Now we need +1 for remainder = 1

$E \rightarrow$ public key

$D \rightarrow$ private key

→ Receiver sends E and $N = P \times Q$ to sender

→ cipher text

$$\boxed{CT = (PT)^E \bmod N}$$

→ plain Text

→ plain text

$$\boxed{PT = (CT)^D \bmod N}$$

* Digital signature

→ Sender initiates the communication

→ used for authentication of sender

→ created using private key of sender & decrypted

by receiver using public key of sender.

- ④ when both confidentiality & authentication needed
 - use digital signature over cipher Text.
 - Receiver then deciphers using public key of sender & further decrypts using its own symmetric / asymmetric key.

5/3
Date: 10/06
1526

26/8/25

INS

① Integrity: content of msg. should remain intact, no modification.

→ In MD5 → NO 2 diff. messages can have same msg. digest.

→ proposed by Rivest; version 5 in use
message digest: It is a fingerprint of plain Text

→ block size used in MD5 = 512 bits

→ output generated by MD5 = 128 bits (size of message digest)
→ Total size (NOT per block)

Inputs:

① ABCD Register: 4 registers of 32 bits each
Total = 128 bits

→ 4 registers are initialized with some values
→ These contain 128 bit output (Message Digest)

② T-Array : Array of 64 elements having pre-determined values. Each element → 32 Bits
 $t[1], \dots, t[64]$

→ Block size of 512 bits is divided into 16 blocks of 32 bits each. Each block to be processed in 4 rounds. Total rounds = $4 \times 16 = 64$ rounds; Each round requires 1 element of T-array.

Algorithm

→ NO. of 1's in 64 bits less than multiple of 512

→ Add padding bits to satisfy the condⁿ

- Add length of original msg. in remaining
 64 bits
 → M.

① Processing of 1 Block

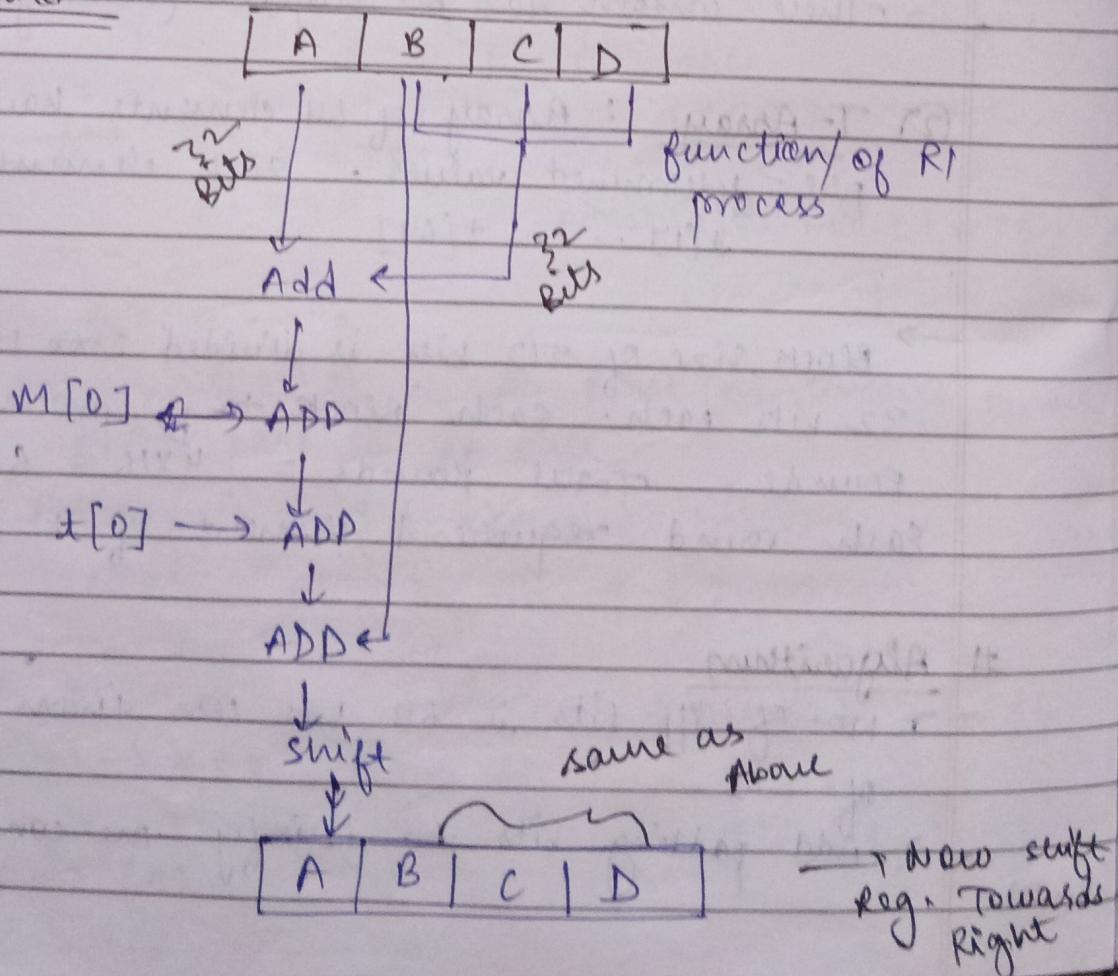
$\begin{array}{c} \diagup \diagdown \\ M[0] \dots M[15] \end{array}$ 16 sub-blocks of 32 bits

- All 16 sub-blocks passed via R1, R2, R3, R4 sequentially → 64 Iterations Total.

Initialization of ABCD

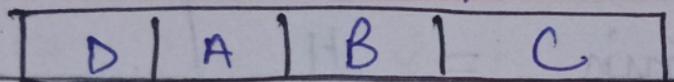
A	01	23	45	67
B	89	AB	CD	EF
C	FE	DC	BA	98
D	76	54	32	10

Round 1



→ Message digest is one way entity → can't decipher to obtain plain Text back.

Page No.		
Date		



→ ABCD register for
2nd iteration

→ Now for each ~~block~~ sub-block $M[1] \dots M[15]$ perform R1.

→ Then at 17th iteration, → 2nd Round of $M[0]$

33rd → Round 3

49th → Round 4

27/8/25

ITC

28/8/25

INS

- MAC: Message Authentication Code
- same key is used at both ends → shared symmetric key
- objective is to generate a hash (MAC) → Not to decrypt → used to check integrity
- MAC generated at both ends & then compared.
- As shared symmetric key is used → MAC
- can be also used for
 - ① Authentication
 - ② Non-repudiation
- Exchanging shared symmetric key on an insecure channel is an issue.
- key size (bits) not fixed → decided by sender & receiver
- Inputs:

K : Bits of key

L : No. of blocks

b : Bits in each block

ipad : 86 bits

opad : 56 bits

→ NO. of bits in key = NO. of bits in block

→ Algo makes bits in key same as NO. of bits in block, if not already not equal.

① If $K < b$ → Add padding bits (0) to left of key.

② If $K > b$ → Trim NO. of bits in K using message digest

Step 2 Apply XOR b/w ipad bits and key K.

$$\text{XOR}(H1 \cdot K) = \text{XOR}(\text{ipad } K) = S1$$

(3) $S1 + M \rightarrow$ append original msg.

(4) \rightarrow Apply message digest, on off of step 3 & call it $H1$

(5) XOR opad bits and key K

$$\text{XOR}(\text{opad } K) = S2$$

(6) $S2 + H1 \rightarrow$ append $H1$ to $S2$

(7) Apply message digest to generate $H2$

\Rightarrow No. of times MD algo is applied: 2 (in Algo) + 1 (for trimming K)
plain text

\rightarrow Message is sent along with $H2$ to receiver.
Receiver finds MAC from same Algo (same values of ipad, opad, key K) \rightarrow & then compare. If MAC's are same \rightarrow data is intact.

problems:

(1) sharing secret key

(2) multiple receivers \rightarrow key has to be shared with all

(3) Non-repudiation in case of multiple receivers \rightarrow How to identify msg. came from sender & not other receiver \rightarrow as they also have same key.