

# Motor Trend - Bastiaan Quast

## Executive Summary

We look at estimate an OLS model, regressing mileage on an automatic/manual dummy. Find a significantly negative effect of automatic on mileage. We redo the estimation as TSLS, using weight as an instrument for automatic. These results are even more significant.

## Analysis

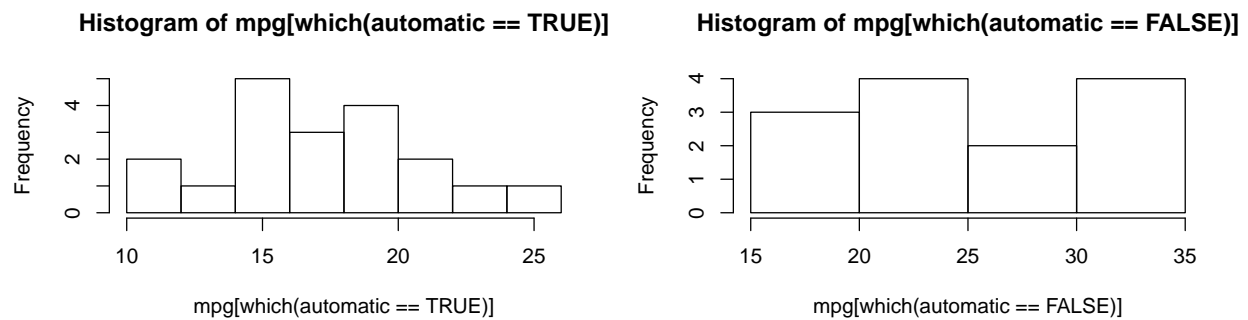
We start by loading the **mtcars** data frame and recode **am** to a logical **automatic** variable.

```
data( mtcars )
mtcars$automatic <- mtcars$am == 0
attach( mtcars )

## The following objects are masked from mtcars (position 3):
##
##      am, automatic, carb, cyl, disp, drat, gear, hp, mpg, qsec, vs,
##      wt
## The following objects are masked from mtcars (position 4):
##
##      am, automatic, carb, cyl, disp, drat, gear, hp, mpg, qsec, vs,
##      wt
## The following objects are masked from mtcars (position 6):
##
##      am, automatic, carb, cyl, disp, drat, gear, hp, mpg, qsec, vs,
##      wt
## The following objects are masked from mtcars (position 7):
##
##      am, automatic, carb, cyl, disp, drat, gear, hp, mpg, qsec, vs,
##      wt
```

We plot the milage for automatic and non-automatic cars.

```
par( mfrow=c(1,2) )
hist( mpg[which(automatic == TRUE)] )
hist( mpg[which(automatic == FALSE)] )
```



We estimate the Ordinary Least Squares (OLS) model.

```
ols <- lm( mpg ~ automatic, data=mtcars )
summary( ols )
```

```
##
## Call:
## lm(formula = mpg ~ automatic, data = mtcars)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.392 -3.092 -0.297  3.244  9.508
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      24.39         1.36   17.94 < 2e-16 ***
## automaticTRUE     -7.24         1.76   -4.11  0.00029 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.9 on 30 degrees of freedom
## Multiple R-squared:  0.36,    Adjusted R-squared:  0.338
## F-statistic: 16.9 on 1 and 30 DF,  p-value: 0.000285
```

There is a significant negative effect of automatic on milage. We redo the estimation using Two-Stage Least Squares (TSLS), using weight (**wt**) as an instrument for automatic.

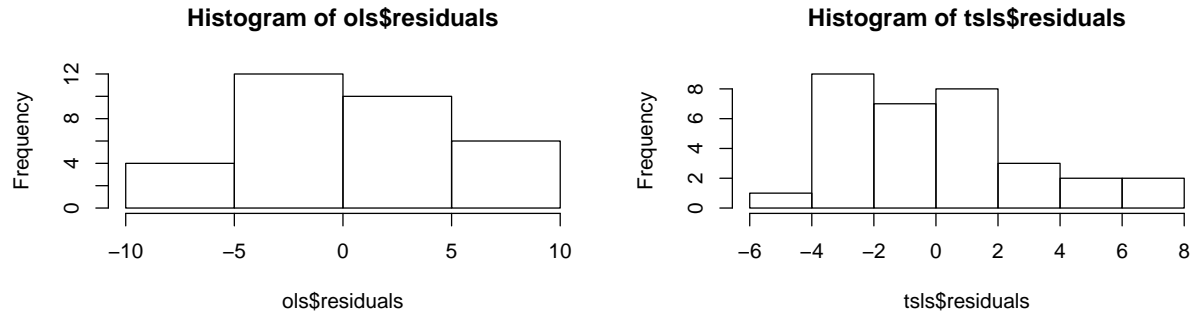
```
tsls.fs <- lm(automatic ~ wt)
tsls <- lm(mpg ~ tsls.fs$fitted.values)
summary(tsls)
```

```
##
## Call:
## lm(formula = mpg ~ tsls.fs$fitted.values)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.543 -2.365 -0.125  1.410  6.873
##
## Coefficients:
```

```
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)      29.08      1.08   26.84 < 2e-16 ***
## tsls.fs$fitted.values -15.13      1.58   -9.56 1.3e-10 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.05 on 30 degrees of freedom
## Multiple R-squared:  0.753, Adjusted R-squared:  0.745
## F-statistic: 91.4 on 1 and 30 DF, p-value: 1.29e-10
```

This coefficient is even more negative, and even more significant. We finally plot the residuals for both estimations.

```
par( mfrow=c(1,2) )
hist( ols$residuals )
hist( tsls$residuals )
```



The residuals of the OLS estimation appear to be normally distributed, the TSLS somewhat less, though  $n$  is too small to make any real claims.