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diagonals: Fat Diagonals in R

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Abstract

The abstract of the article.

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1. Introduction

Diagonals are an important matrix manipulation. We present the diagonals R package, which implements functions for dealing with **fat diagonals**. Fat diagonals are block matrix-diagonals that occur when two or more dimensions are mapped along a single edge of a matrix. For an asymmetric network graph (e.g. a dyadic social network) to be mapped to a matrix, we would need each node along each edge of matrix, however we would also need to map the direction of the tie, which is an additional dimension. Typically these would be represented as higher-order arrays (i.e. >= 3). In order to effectively visualise such arrays, it can be helpful to do so in a matrix. This could for instance be represented as in the following matrix (where the i and o suffices represent incoming and outgoing receptively).

	Αi	Αo	Βi	Во	Ci	Со	Di	Do
Α	1	1	0	0	1	0	1	0
В	0	1	1	1	0	1	0	1
С	1	0	0	0	1	1	0	0
D	1	0	1	0	1	1	1	1

Sometimes the ties of a node to itself are not particularly meaningful (e.g. feeling of amiability towards oneself) and can be removed. For a symmetric network this can simply be done using the function diag() in R's base package, e.g.

```
sm <- matrix(1, nrow=4, ncol=4)</pre>
```

```
diag(sm) <- NA
```

	[,1]	[,2]	[,3]	[,4]
[1,]	NA	1	1	1
[2,]	1	NA	1	1
[3,]	1	1	NA	1
[4,]	1	1	1	NA

However, for higher-order matrices this does not work well.

```
diag(m) <- NA
m
  Ai Ao Bi Bo Ci Co Di Do
            0
  O NA
         1
            1
                0
                   1
                      0
                         1
      O NA
            0
                1
                   1
                      0
                         0
      0
         1 NA
               1
                      1
```

In comes the diagonals package and its workhorse fatdiag() function. The function is designed to mimic the behaviour of the diag() as closely as possible, but with then for fat diagonals.

```
library(diagonals)
```

0

0

0 1 0

O NA NA

```
# the matrix m was restored to its original state
fatdiag(m, steps=4) <- NA</pre>
m
  Ai Ao Bi Bo Ci Co Di Do
A NA NA
         0
            0
      1 NA NA O 1
```

0 1 1 NA NA

Note that the steps argument defines the number of steps on the diagonal ladder. Alternatively we could set the size of the step, more on this later.

2. Design

The implementation of fat diagonals in the diagonals package is intended to be as close as possible to the functions dealing with diagonals included in the base package. As such, the package includes two functions.

• fatdiag()

• fatdiag()<-

These functions offer a very similar syntax to the base functions:

- diag()
- diag()<-

With the exception that the fat diagonal functions generally need more information in terms of the number of steps on the diagonal ladder, or the size of these steps.

The function fatdiag<- like its base package equivalent replaces the (fat) diagonal of its first argument x with the right side argument value. The value argument can either be a scalar, in which case it is recycled for the length of the diagonal, or it can be vector. For the base package function diag()<- this vector has be of the same length as the diagonal (here, the shortest dimension of the matrix), however, the fatdiag()<- function will accept any vector that is of a length that is an integer divisor of the length of the diagonal. For example, if the length of the diagonal is 12, then the follow lengths for the replacement vector are accepted: 1, 2, 3, 4, and 6.

The fatdiag function act similar to the diag() function. Both these functions have two main applications. The first application is (fat) diagonal extraction, is the first argument x is a matrix, i.e. length(dim(x)) == 2, then the function extracts the diagonal matrix and returns it as a vector.

The second application is (fat) diagonal matrix creation. This can be done in two ways, using a scalar, or using a vector. If a scalar is used for x, the diag() function returns an identity matrix Ix, i.e. a matrix of dimensions x times x is returned, with 1 on the diagonal positions and 0 elsewhere. The fatdiag() function supports the creation of non-square matrices (e.g. using size = c(3,2)) and therefore uses x as the longest dimension of the matrix, where the other dimension is determined automatically using the size argument.

3. Usage

In the introduction we briefly demonstrate the usage of the fatdiag() function for assigning a new value to the fat diagonal. Here we take a closer look at some of the additional functionality that is implemented.

```
fatdiag(m, size=c(1,2) ) <- 881:888 m
```

```
Ci
                             Со
    Αi
         Αo
              Βi
                   Во
                                  Dί
                                       Dο
A 881 882
               0
                    0
                         1
                              0
                                   1
                                         0
В
          1 883 884
                         0
                                   0
                                         1
С
                                        0
     1
               0
                    0 885 886
                                   0
D
     1
          0
               1
                    0
                         1
                              1 887 888
```

So far we have been using the set fatdiag(), i.e. fatdiag()<-. However, we can also use the fatdiag() function either for diagonal extraction, or diagonal matrix creation.

fatdiag(m, steps = 4)

[1] 881 882 883 884 885 886 887 888

Fat diagonal matrices can be created using a scalar:

fatdiag(9, steps=3)

	[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]	[,9]
[1,]	1	1	1	0	0	0	0	0	0
[2,]	1	1	1	0	0	0	0	0	0
[3,]	1	1	1	0	0	0	0	0	0
[4,]	0	0	0	1	1	1	0	0	0
[5,]	0	0	0	1	1	1	0	0	0
[6,]	0	0	0	1	1	1	0	0	0
[7,]	0	0	0	0	0	0	1	1	1
[8,]	0	0	0	0	0	0	1	1	1
[9,]	0	0	0	0	0	0	1	1	1

or using a vector:

fatdiag(1:27, steps=3)

	[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]	[,9]
[1,]	1	4	7	0	0	0	0	0	0
[2,]	2	5	8	0	0	0	0	0	0
[3,]	3	6	9	0	0	0	0	0	0
[4,]	0	0	0	10	13	16	0	0	0
[5,]	0	0	0	11	14	17	0	0	0
[6,]	0	0	0	12	15	18	0	0	0
[7,]	0	0	0	0	0	0	19	22	25
[8,]	0	0	0	0	0	0	20	23	26
[9,]	0	0	0	0	0	0	21	24	27

We can extract a fat diagonal and diagonalise it again.

m <- matrix(801:881, nrow=9, ncol=9)
fatdiag(fatdiag(m, steps=3), steps=3)</pre>

	[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]	[,9]
[1,]	801	810	819	0	0	0	0	0	0
[2,]	802	811	820	0	0	0	0	0	0
[3,]	803	812	821	0	0	0	0	0	0
[4,]	0	0	0	831	840	849	0	0	0
[5,]	0	0	0	832	841	850	0	0	0
[6,]	0	0	0	833	842	851	0	0	0
[7,]	0	0	0	0	0	0	861	870	879
[8,]	0	0	0	0	0	0	862	871	880
[9,]	0	0	0	0	0	0	863	872	881

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4. Conclusion

Higher-order arrays can sometimes be mapped to a matrix, which enables us to visualise these arrays in a intuitive manner. However, the standard matrix manipulations relating to diagonals become more complex when we do so. The diagonals package provides the fatdiag() function family, which enables the manipulation of fat diagonals in R, using a syntax that is very close to the diag() function family from Rs base package.

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