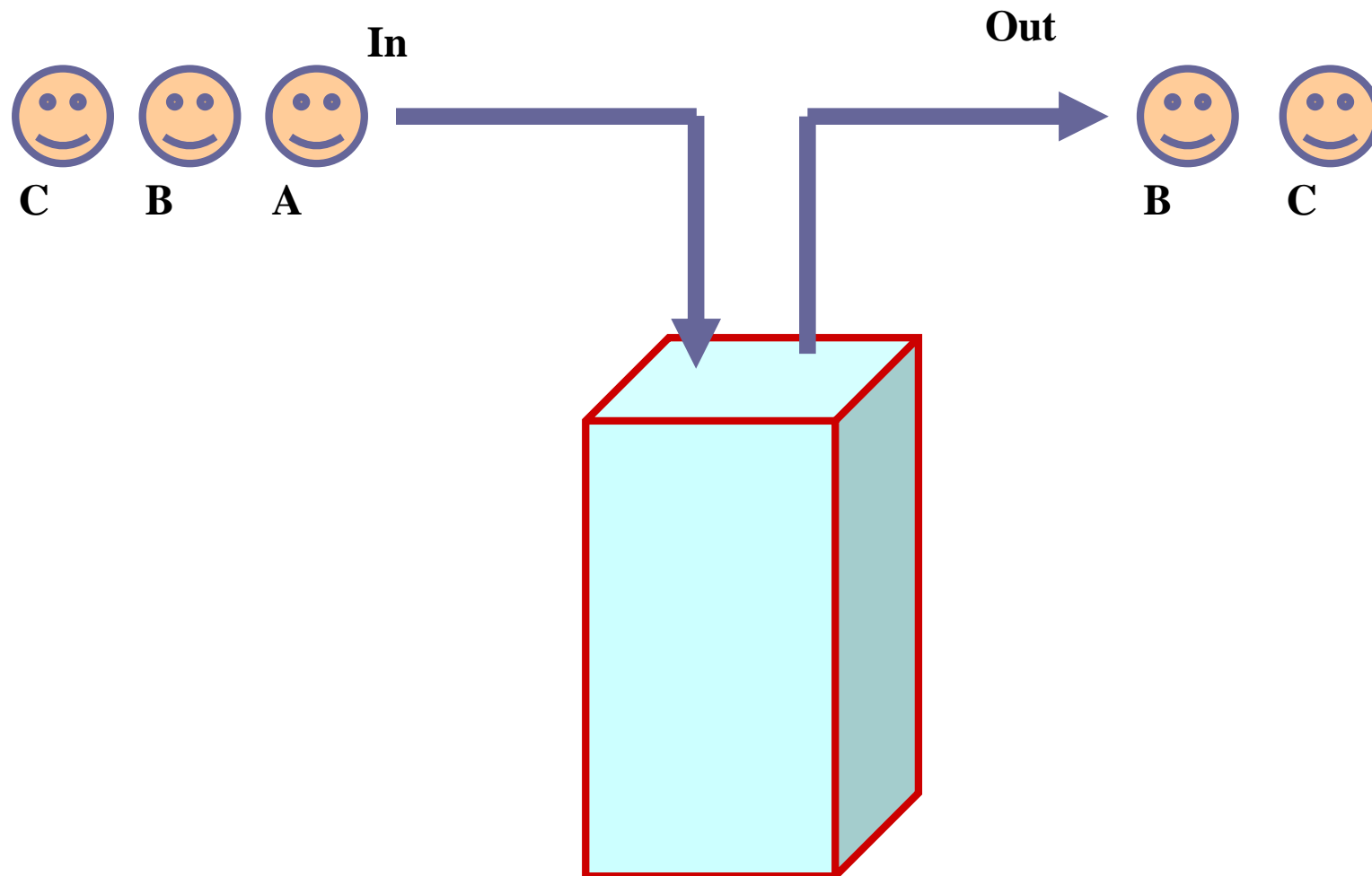




Stack and Queue

Stack

Data structure with **Last-In First-Out (LIFO)** behavior



Typical Operations on Stack

isempty: determines if the stack has no elements

isfull: determines if the stack is full in case of a bounded sized stack

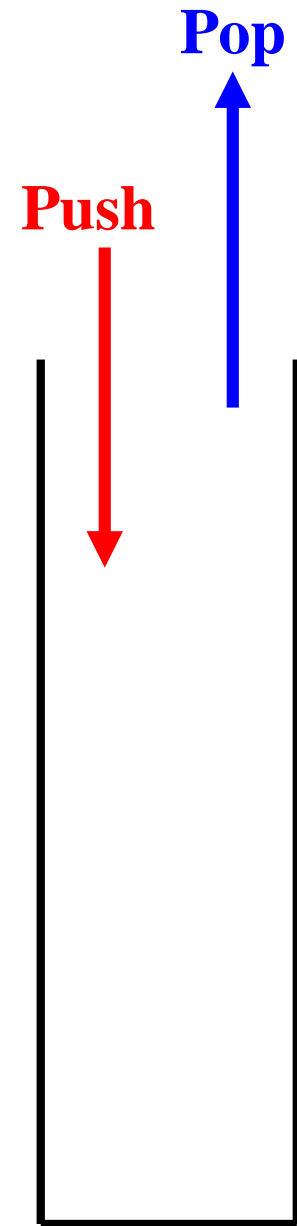
top: returns the top element in the stack

push: inserts an element into the stack

pop: removes the top element from the stack

push is like inserting at the front of the list

pop is like deleting from the front of the list



Creating and Initializing a Stack

Declaration

```
#define MAX_STACK_SIZE 100
typedef struct {
    int key; /* just an example, can have
              any type of fields depending
              on what is to be stored */
} element;
typedef struct {
    element list[MAX_STACK_SIZE];
    int top; /* index of the topmost element */
} stack;
```

Create and Initialize

```
stack Z;
Z.top = -1;
```

Operations

```
int isfull (stack *s)
{
    if (s->top >=
        MAX_STACK_SIZE - 1)
        return 1;
    return 0;
}
```

```
int isempty (stack *s)
{
    if (s->top == -1)
        return 1;
    return 0;
}
```

Operations

```
element top( stack *s )  
{  
    return s->list[s->top];  
}
```

```
void push( stack *s, element e )  
{  
    (s->top)++;  
    s->list[s->top] = e;  
}
```

```
void pop( stack *s )  
{  
    (s->top)--;  
}
```

Application: Parenthesis Matching

- Given a parenthesized expression, test whether the expression is properly parenthesized

□ Examples:

`()({ } [({ } { } ())])` is proper

`() { []` is not proper

`({) }` is not proper

`)([]` is not proper

`([]))` is not proper



■ Approach:

- Whenever a left parenthesis is encountered, it is pushed in the stack
- Whenever a right parenthesis is encountered, pop from stack and check if the parentheses match
- Works for multiple types of parentheses
(), { }, []

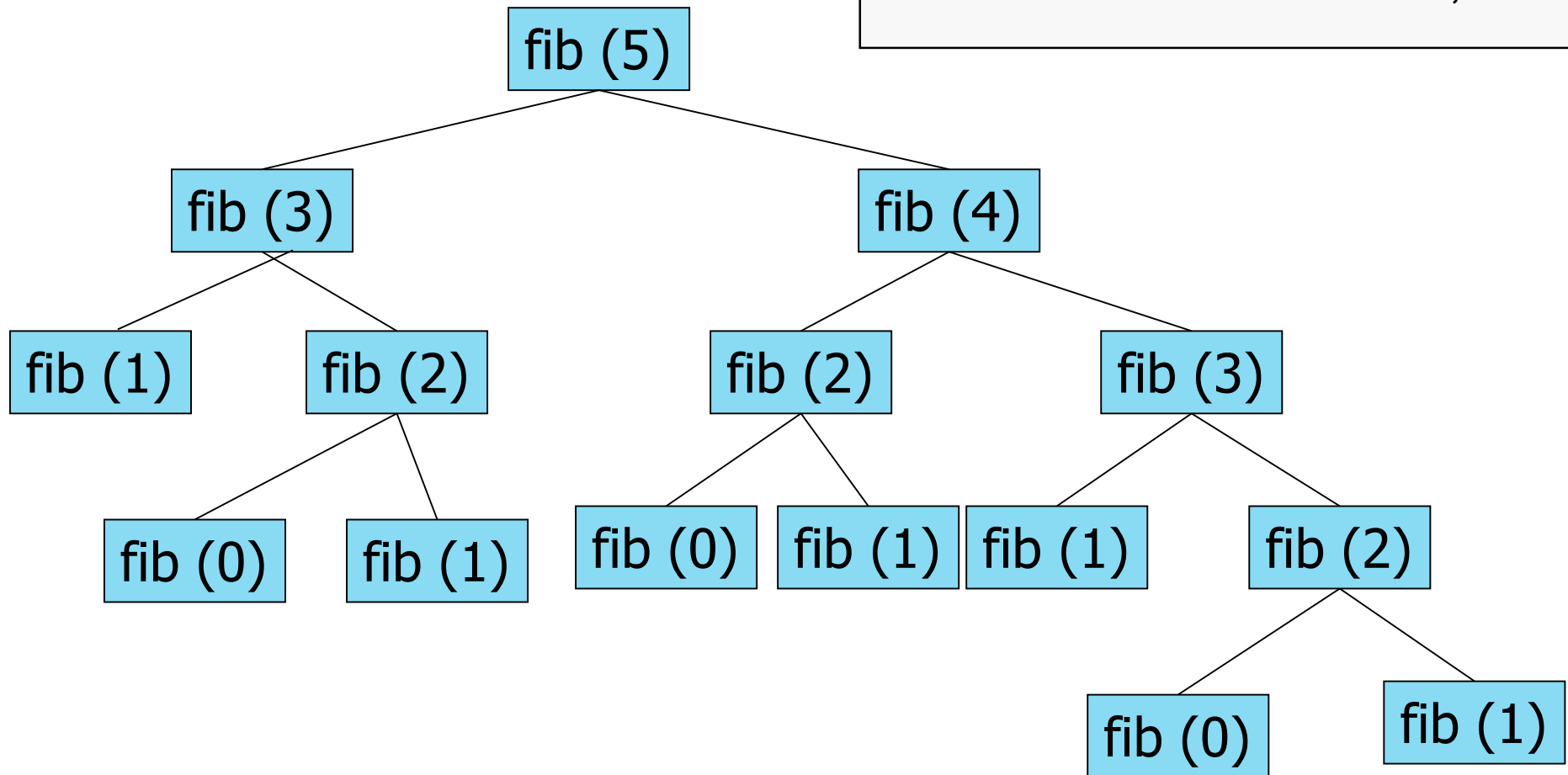
Parenthesis matching

```
while (not end of string) do
{
    a = get_next_token();
    if (a is '(' or '{' or '[') push (a);
    if (a is ')' or '}' or ']')
    {
        if (is_stack_empty( ))
            { print ("Not well formed"); exit(); }
        x = top();
        pop();
        if (a and x do not match)
            { print ("Not well formed"); exit(); }
    }
}
if (not is_stack_empty( )) print ("Not well formed");
```

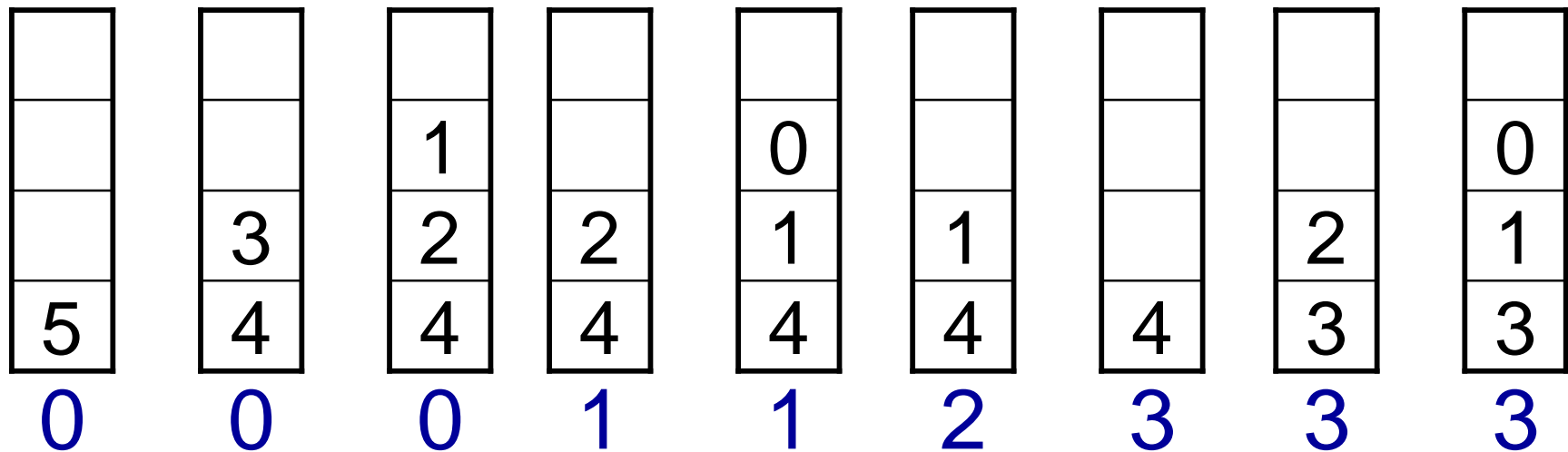
Recursion can be implemented as a stack

Fibonacci recurrence:

$\text{fib}(n) = 1$ if $n = 0$ or 1 ;
 $= \text{fib}(n - 2) + \text{fib}(n - 1)$
otherwise;



Fibonacci Recursion Stack



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