

Project Report

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Problem Statement 1

Given a positive integer n , we have to calculate the sum of the series $1^1 + 2^2 + 3^3 + \dots + n^n$

Algorithm:

Lets say $\text{func}(n)$ is a recursive function which calculates the sum of the series

Recursive function :

```
func(1)=1;      // base case
func(n)=func(n-1)+n^n;
```

MIPS implementation:

- We prompt user to input n and store n in $\$a0$
- Then we will call the function `Find_sum` by passing the parameter $\$a0$, and storing $\$a0$ in $\$s0$
- Then we will call the function `power_n` which will calculate the value of n^n and stores it in $\$t2$
- We use $\$v0$ to store and update sum of series in each step as, $\$v0 = \$v0 + \$t2$
- The final value stored in $\$v0$ after the function ends will be returned

Example:

Input: $n = 2$

Output: 5

```
Find_sum(2)
$t2=1
while($t2<n)
    $t2=power_n(n)
    $v0=$v0+$t2
$v==5
Hence the final answer is 5
```

Problem Statement 2

Given a positive integer N , we define the Collatz sequence corresponding to N as the numbers formed by the following operations:

If N is even, $N \leftarrow N/2$ and if N is odd, $N \leftarrow 3N + 1$.

We have to find the number of steps required to reach 1 from N in the Collatz sequence corresponding to N .

Algorithm

```
func(n)=(n/2)+1 ; if(n%2==0)
func(3*n+1) +1 ; if(n%2==1)
```

MIPS implementation:

- We prompt user to input n and store n in $\$a0$
- Then we will call the function Collatz_Conjecture: by passing the parameter $\$a0$, and storing $\$a0$ in $\$s0$
- We will check if n is even or odd, if n is even we will call the function even: which will calculate $f(n/2)+1$ and if n is odd, we will call the function odd: which will calculate $f(3*n+1)+1$
- Function Collatz_Conjecture: will return 0 when $n=1$ (base case)
- The final value returned by Collatz_Conjecture: will be printed

Example:

Input: $n=10$

Output :6

How the recursion works for : $f(10)$

```
10 is even ,  $f(10)=f(5)+1$ ;  
5 is odd ,  $f(5)=f(16)+1$ ;  
16 is even,  $f(16)=f(8)+1$ ;  
8 is even ,  $f(8)=f(4)+1$ ;  
4 is even ,  $f(4)=f(2)+1$ ;  
2 is even ,  $f(2)=f(1)+1$ ;  
 $f(1)=0$ ; //base case
```

Hence $f(10)=1+1+1+1+1+1=6$