$$\theta = \frac{\pi}{6}, \ w = 2R\sin\frac{\pi}{12}$$